

Velocity dispersion profiles

Galaxy orbits

Cluster mass estimate

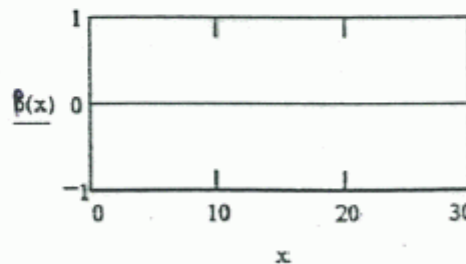
Simple models made with software.

Analytical models of clusters
based on the **JEANS EQUATION**: ^{e.g.} (Merritt 87)

same ϕ potential
same T kinetic energy

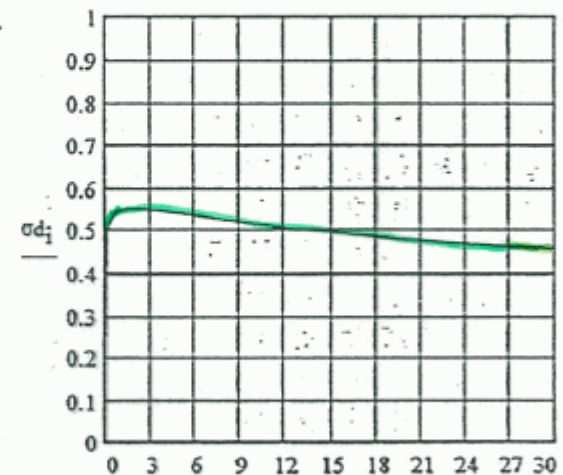
anisotropy
parameter

isotropic
case
 $\beta=0$



$$\beta(r) = \frac{r^2}{r^2 + r_0^2} \quad \begin{matrix} \text{velocity} \\ \text{anisotropy} \end{matrix}$$

$\sigma_{\text{obs}}(r_z)$ profile



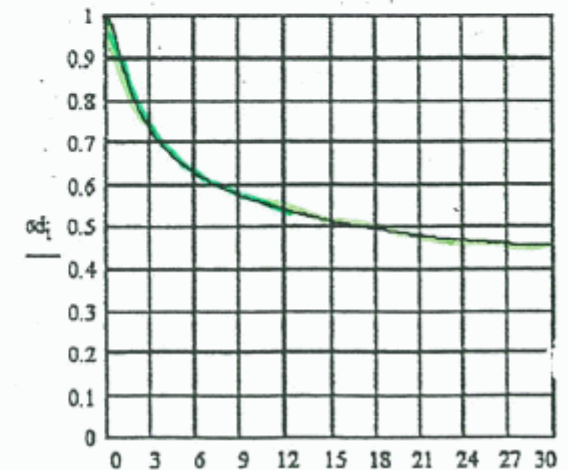
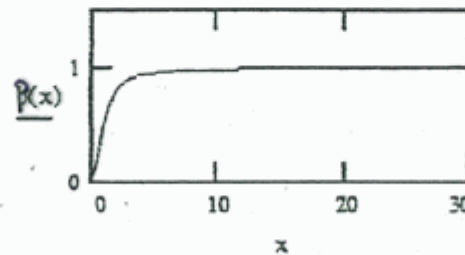
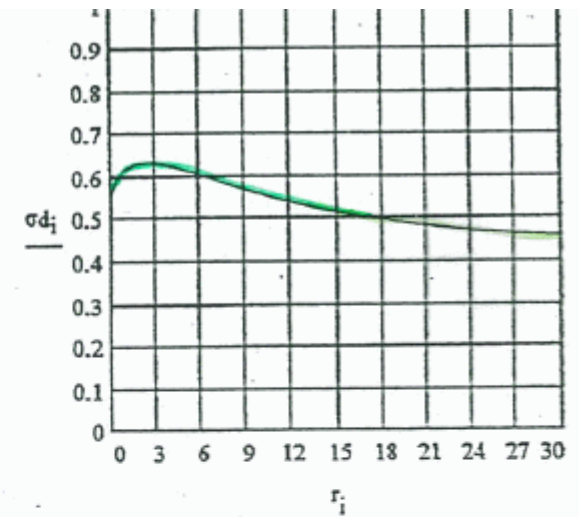
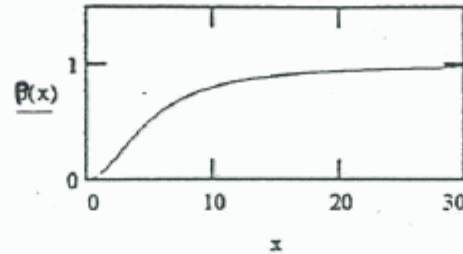
$$r_i = \frac{r}{r_c}$$

r_i (projected
distance)



external
radial orbits
 $\beta > 0$

$\beta = 1$
completely
radial



The only way to avoid the use of the unknown beta, it is to integrate in the whole cluster. The global value of velocity dispersion does not depend of the velocity anisotropies. This is an advantage of the virial theorem with respect to the Jeans equation.

Velocity Dispersion Profiles and Velocity Anisotropies

MG et al. 98

Ensemble cluster built with gals of 160 nearby clusters \Rightarrow observational profile
Jeans eq. + mass distribution + assumption for v-anisotropy \Rightarrow theoretical profile.

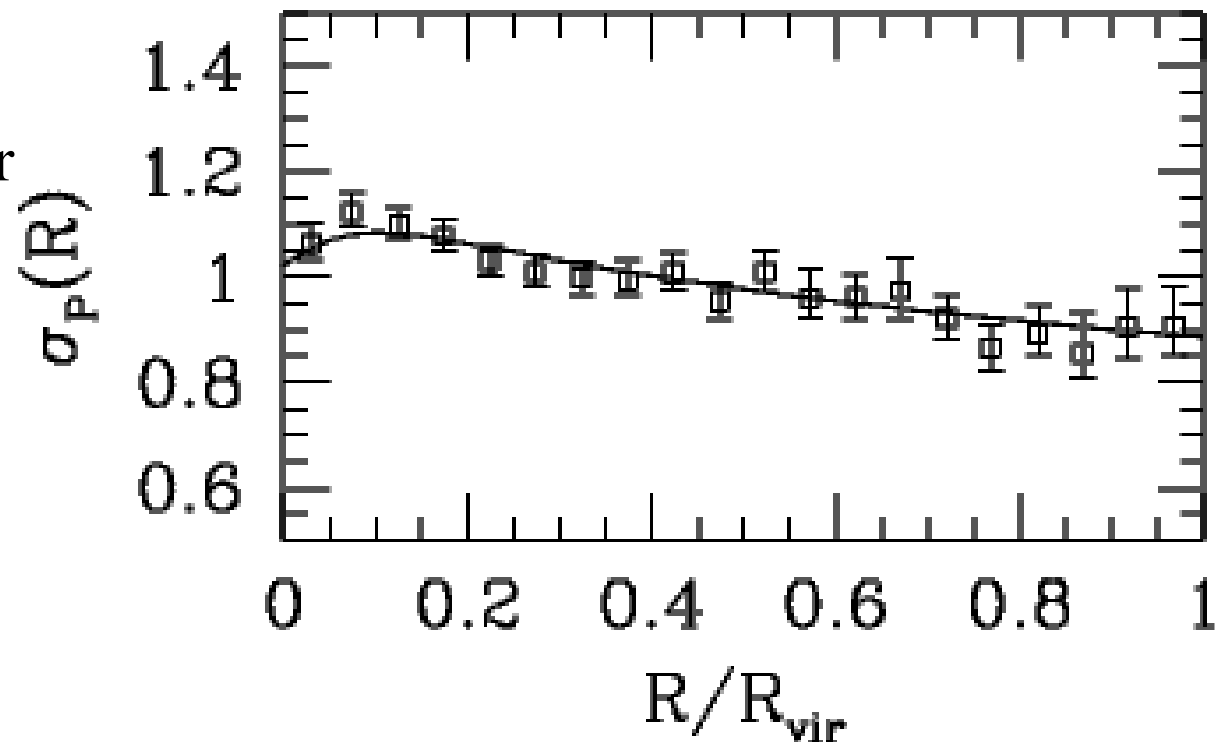
Mass-follows-light
assumption

Velocity anisotropy parameter

$$\beta(r) = 1 - \sigma_t(r)/\sigma_r(r) = 0:$$

χ^2 goodness of fit is 96%.

The "average" cluster
has isotropic velocities!



\Rightarrow Mean surface term correction to virial mass about 20%.

Velocity Dispersion Profiles and Velocity Anisotropies

MG et al. 98

3 families of clusters (for $\neq \sigma_v$ in central regions/ σ_{TOT}) \Rightarrow 3 ensemble clusters.

Jeans eq.+ mass distribution+assumption for anisotropy \Rightarrow theoretical profile

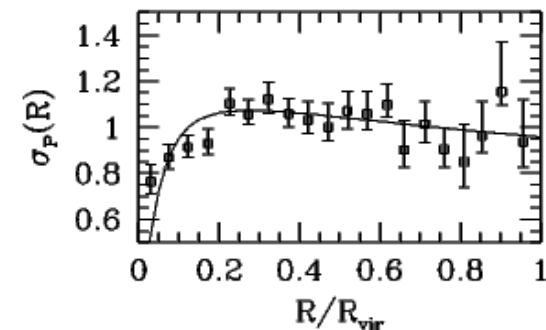
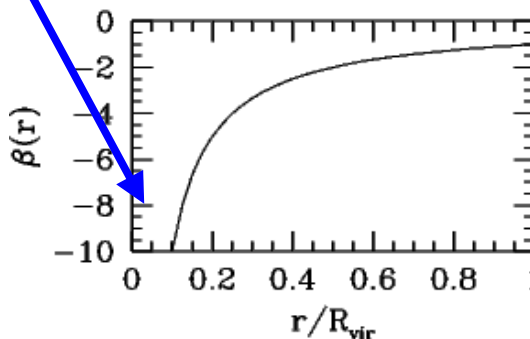
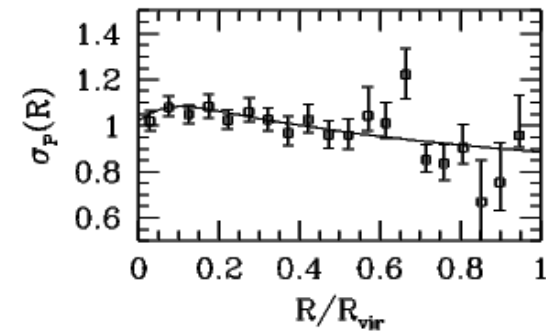
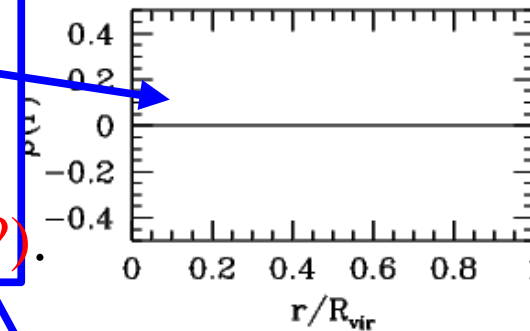
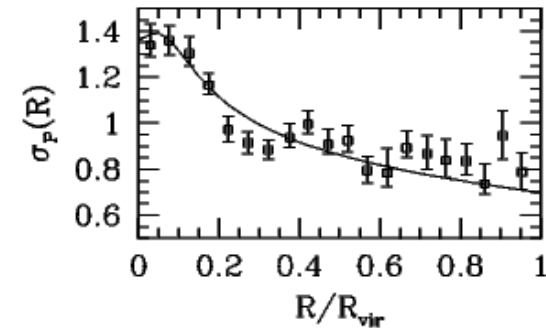
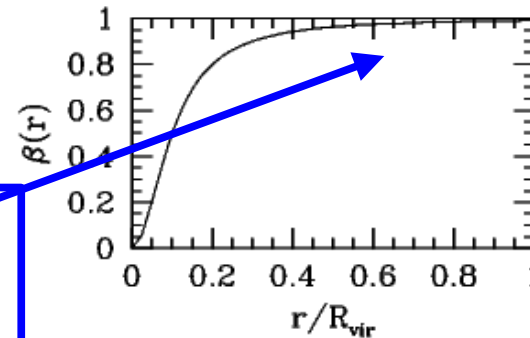
$$M \propto L$$

$$\beta(r) = 1 - \sigma_\tau(r) / \sigma_r(r)$$

Radial orbits in external regions
(infall of galaxies?);
isotropic orbits
(violent relaxation?);
circular orbits in internal regions
(secondary relaxation phenomena?).

\Rightarrow Surface term correction to virial mass about 18-40%.

Clusters may be characterized by different anisotropies...
different stages of evolution?



Biviano & Katgert 2004

Projected
velocity dispersion profiles

E bright: cannot be explained
by no velocity anisotropy →
The Jeans equation cannot be applied
→ may be due that E-bright
Produced by mergers.

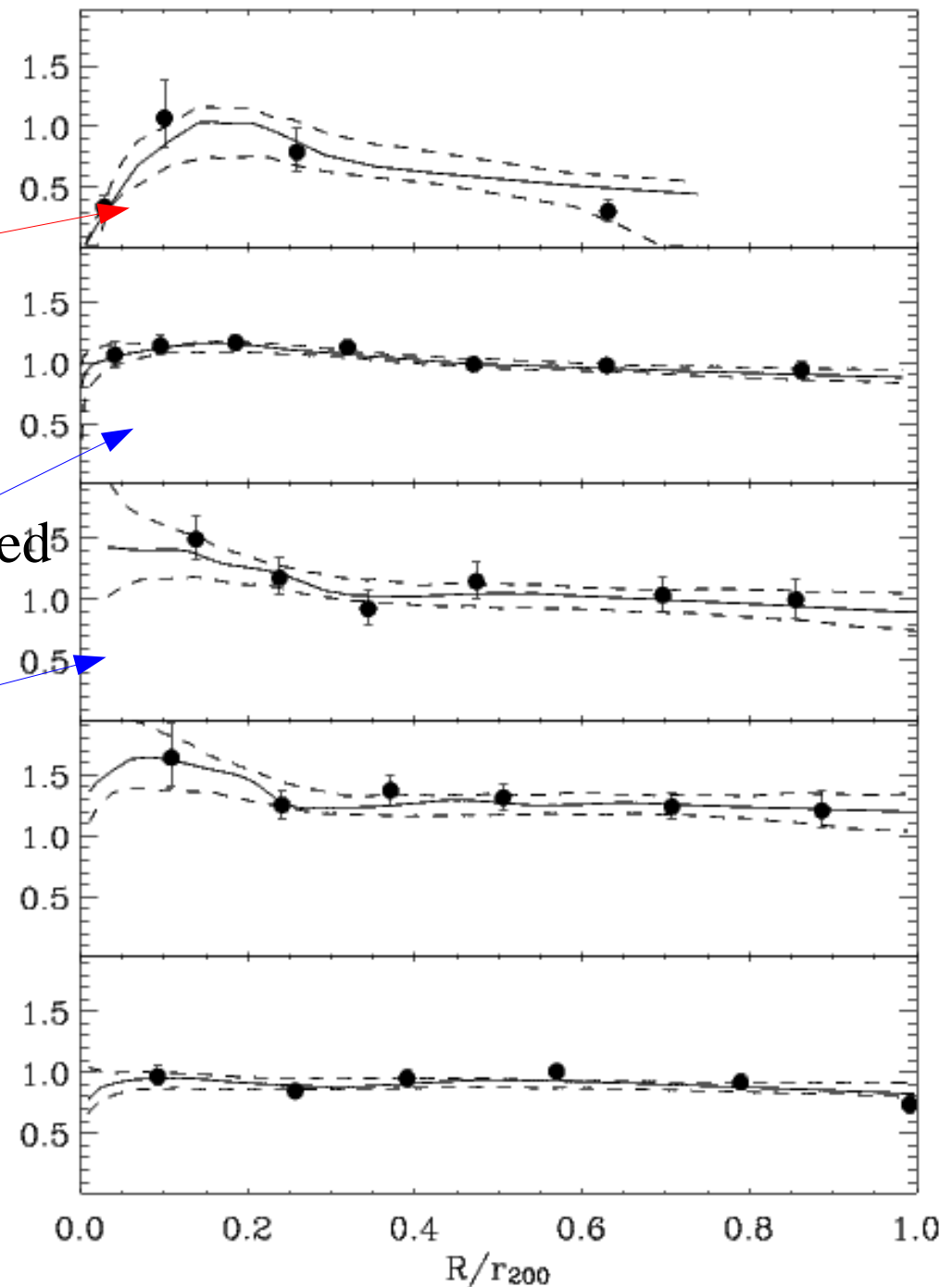
E-galaxies

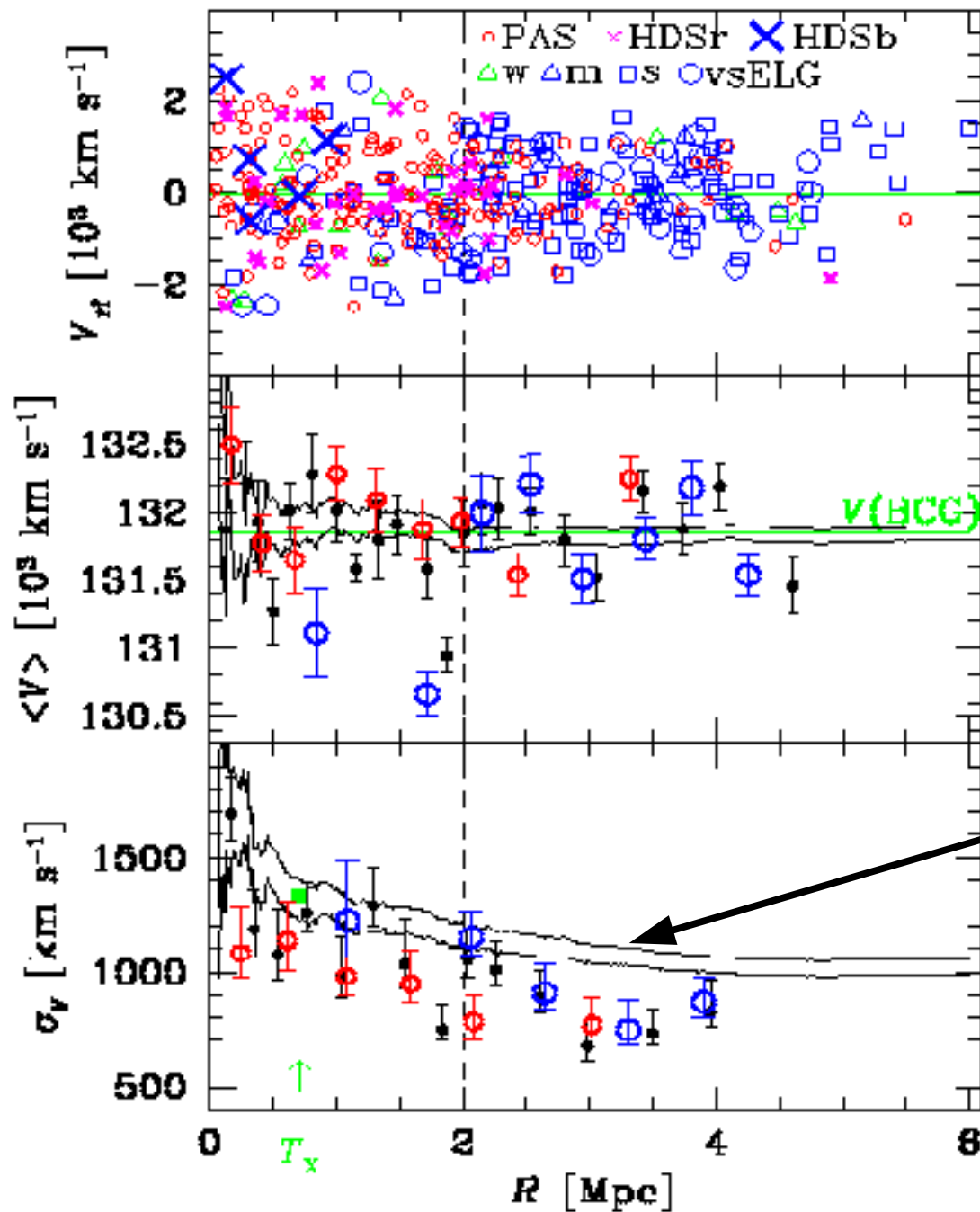
Spi-early

Spi-late

-

Spi populations have larger radial
Orbits than E-galaxies...
OK with recent infall of Spi

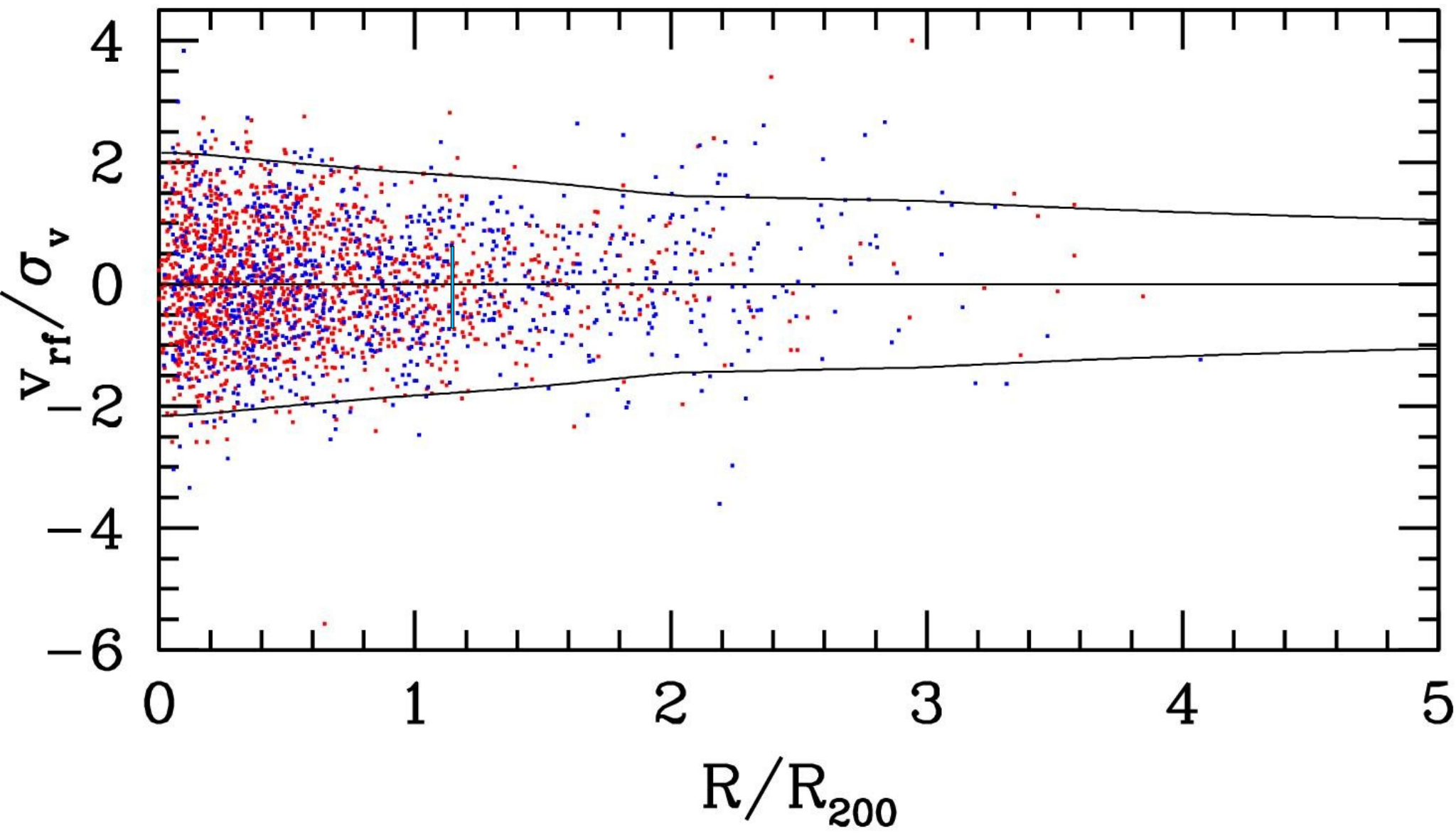




~500 gals per cluster
 MACS1206 at $z \sim 0.4$
 CLASH-VLT data
 Girardi et al. 2015

Passive and star
 forming galaxies have
 different velocity
 dispersion profiles
 (VDP).

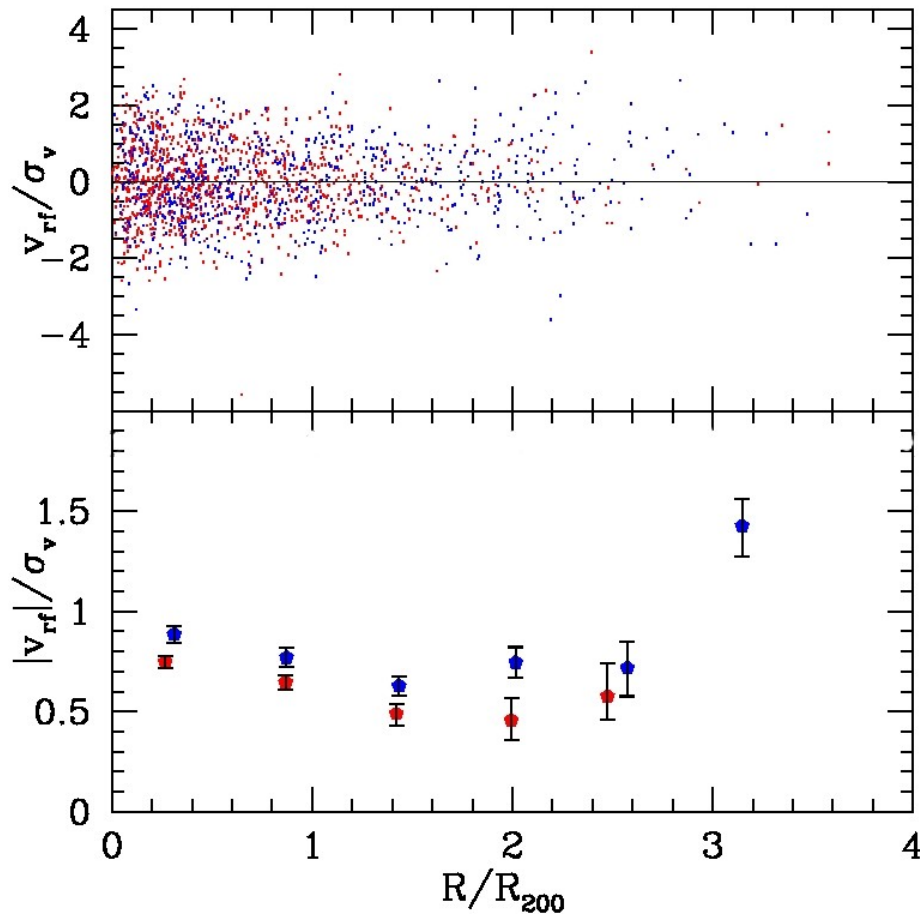
Barsanti's thesis (Barsanti et al. In prep.) ~50 clusters $0.8 < z < 1.4$
NWF profile \rightarrow Escape velocity curve to check
the member selection in the projected phase space.



Velocity Dispersion Profiles (Barsanti's thesis)

$0.4 < z < 0.8$

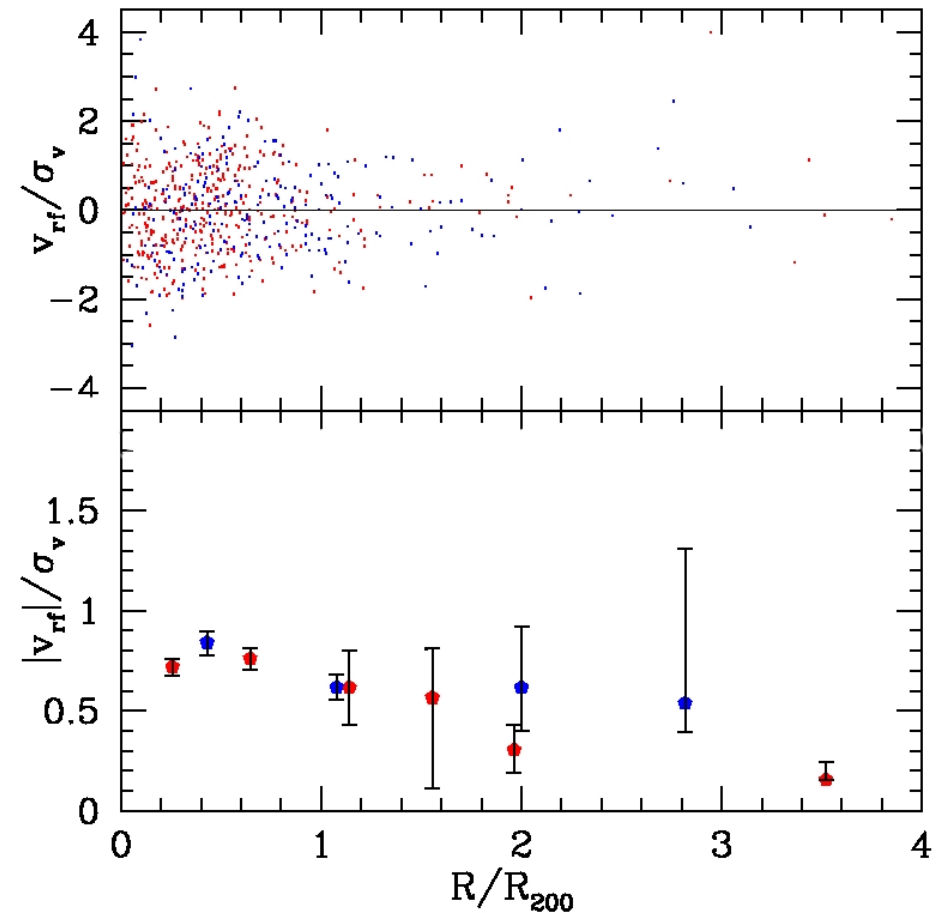
VDPs are different.

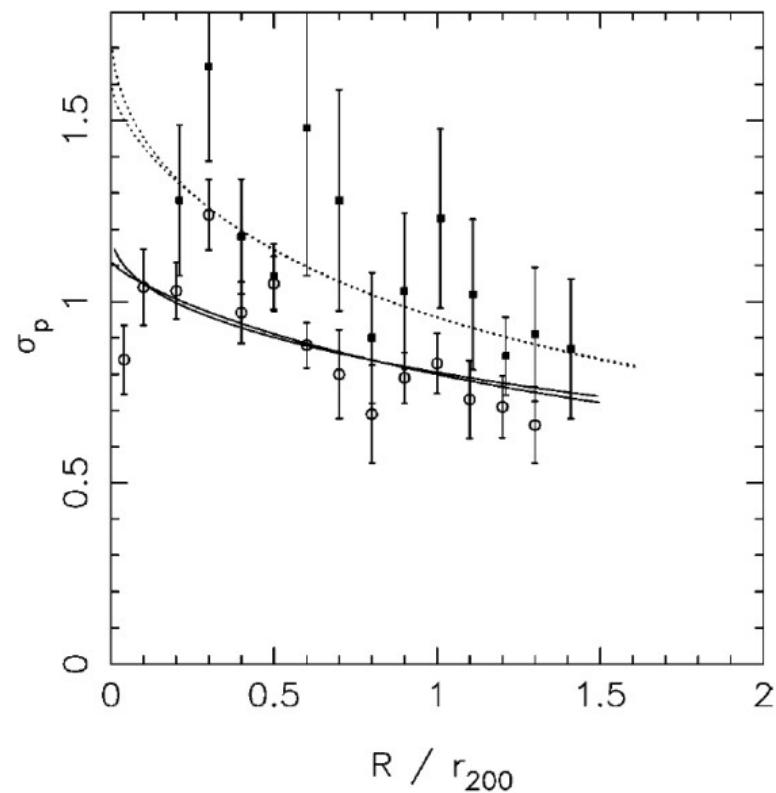
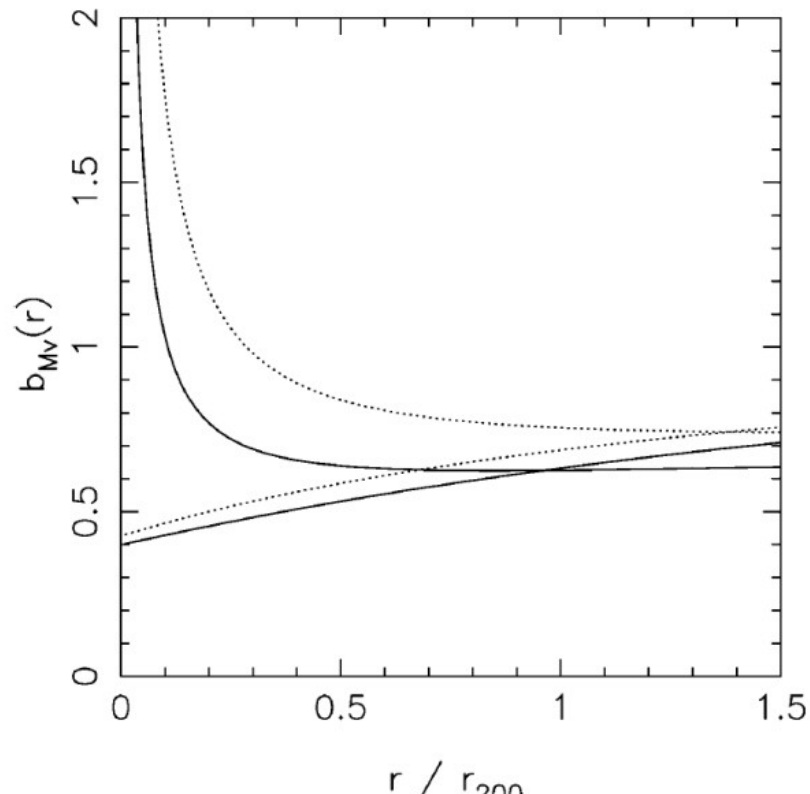
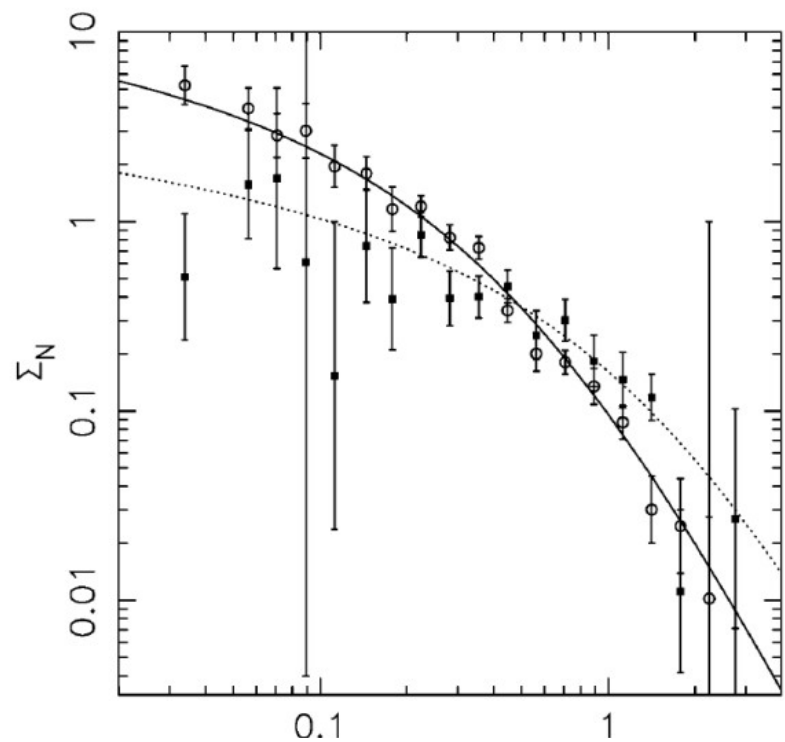


$0.8 < z < 1.4$

VDPs are not different!

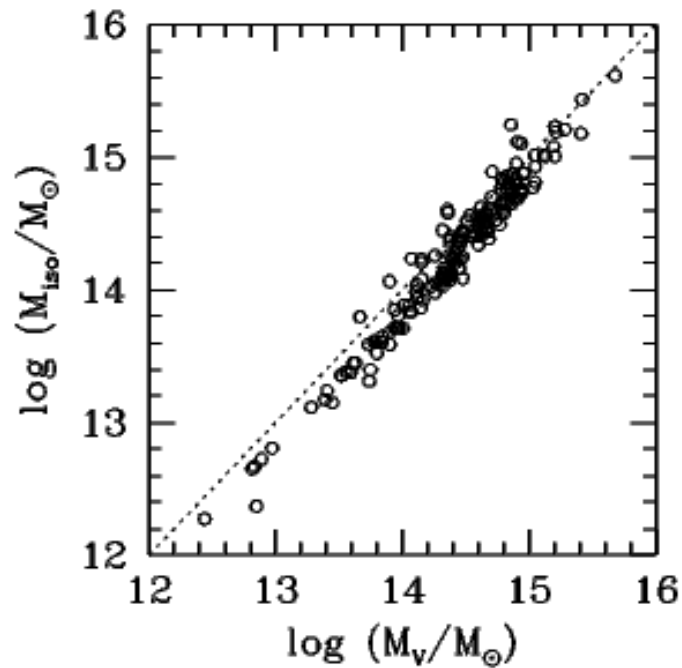
Connected to evolution of
Galaxies & clusters.





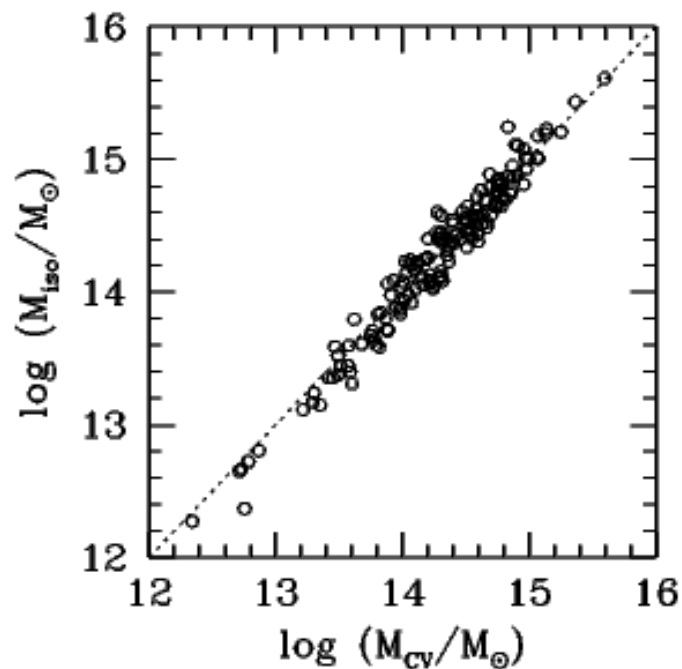
Carlberg et al. 1996 – CNOC clusters red and blue galaxies have different galaxy distribution and velocity dispersion profiles BUT they are both in dynamical equilibrium and can be used in the Jeans equation to give mass.

The difference between the mass from The Jeans eq. and the virial mass $b = M_{\text{Jeans}}(r) / L(r) * \langle L \rangle / M_{\text{vir}} < 1$. is due to the surface pressure correction.



$M_{\text{iso}} = M_{\text{Jeans}}$ i.e. mass from the Jeans eq.
 $M_v = \text{virial Mass}$, i.e. mass from the virial theorem.

The difference between M_{iso} and M_c is due to the surface pressure correction, that is to the fact that clusters are not sampled out to infinity and at the observed external radius, the radial velocity dispersion is still >0 .



M_{vcorr} virial Mass after the opportune correction.

Girardi et al. 1998

