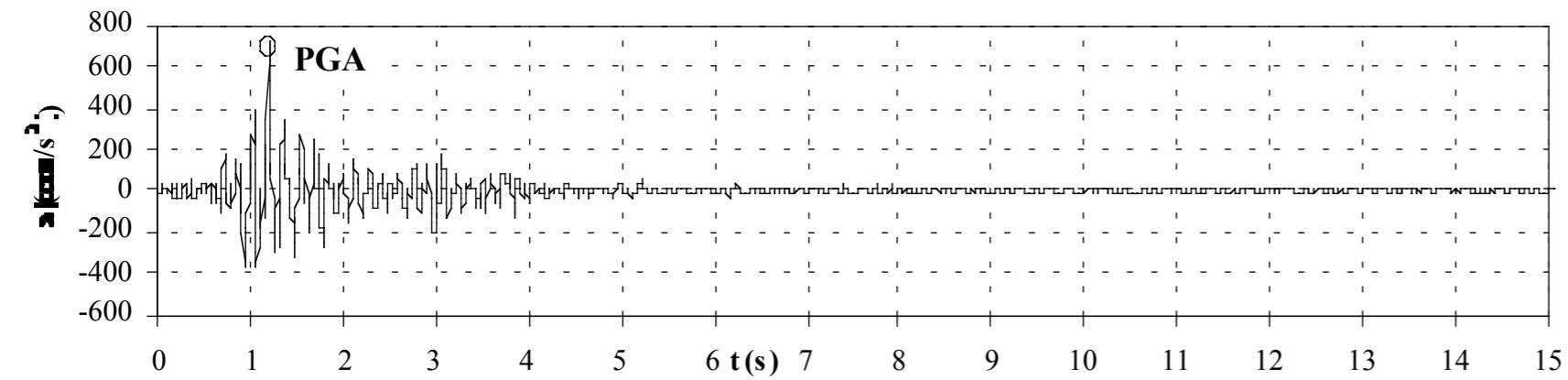
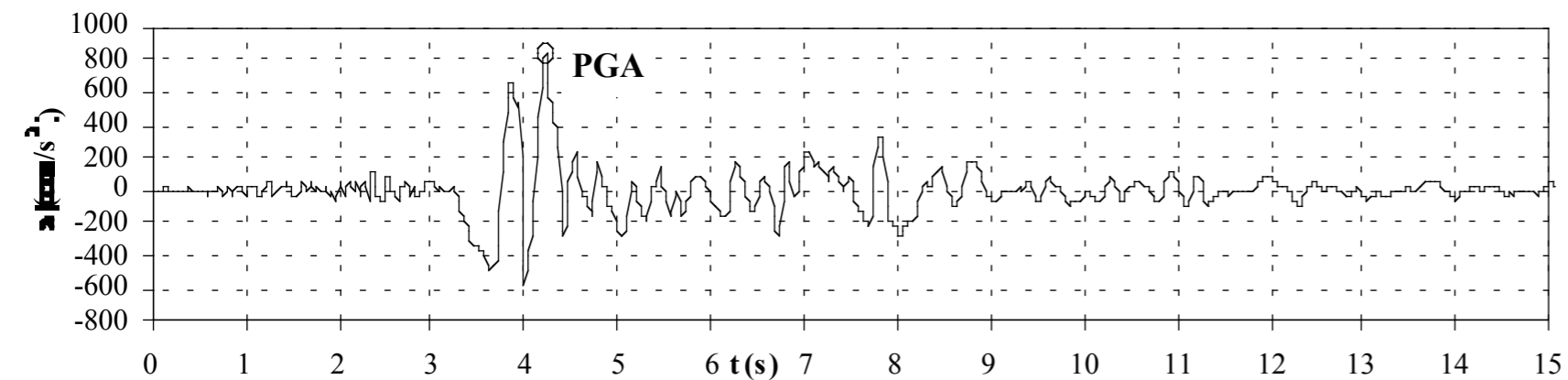


PARAMETERS CHARACTERIZING  
THE **SEISMIC DEMAND**  
FOR  
EARTHQUAKE DAMAGE SCENARIO  
EVALUATION

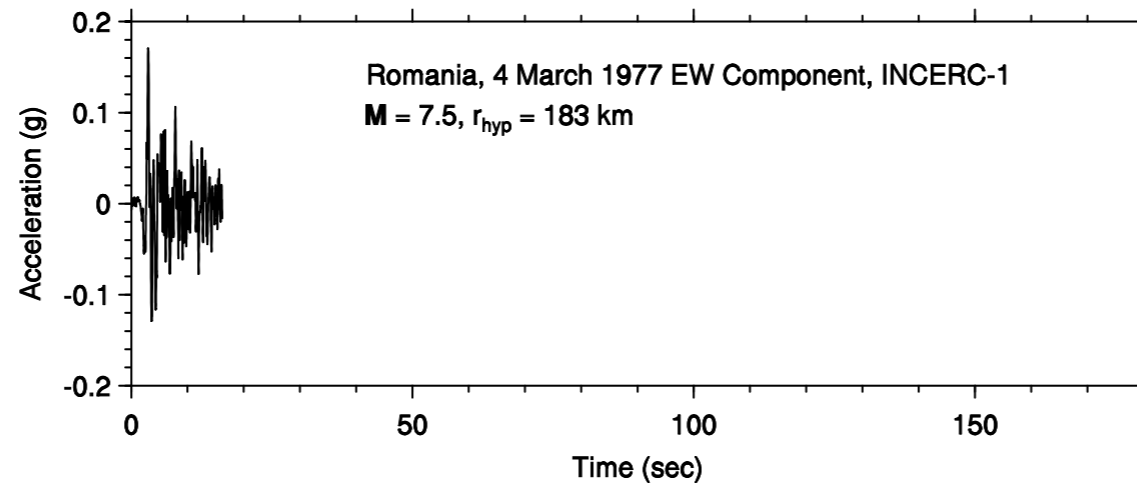
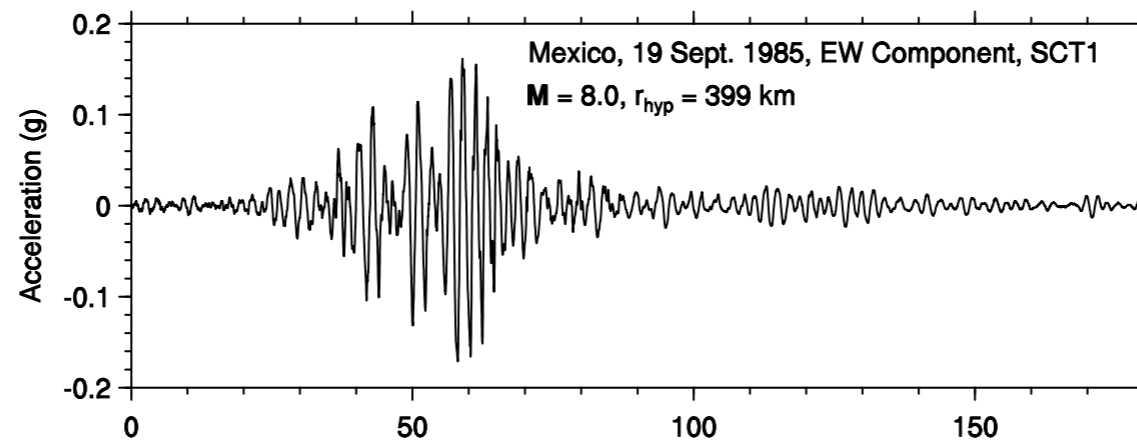
# PGA as a demand parameter...



Acceleration time history. Rocca  
NS record.  
1971 Ancona earthquake  
(ML=4.7)



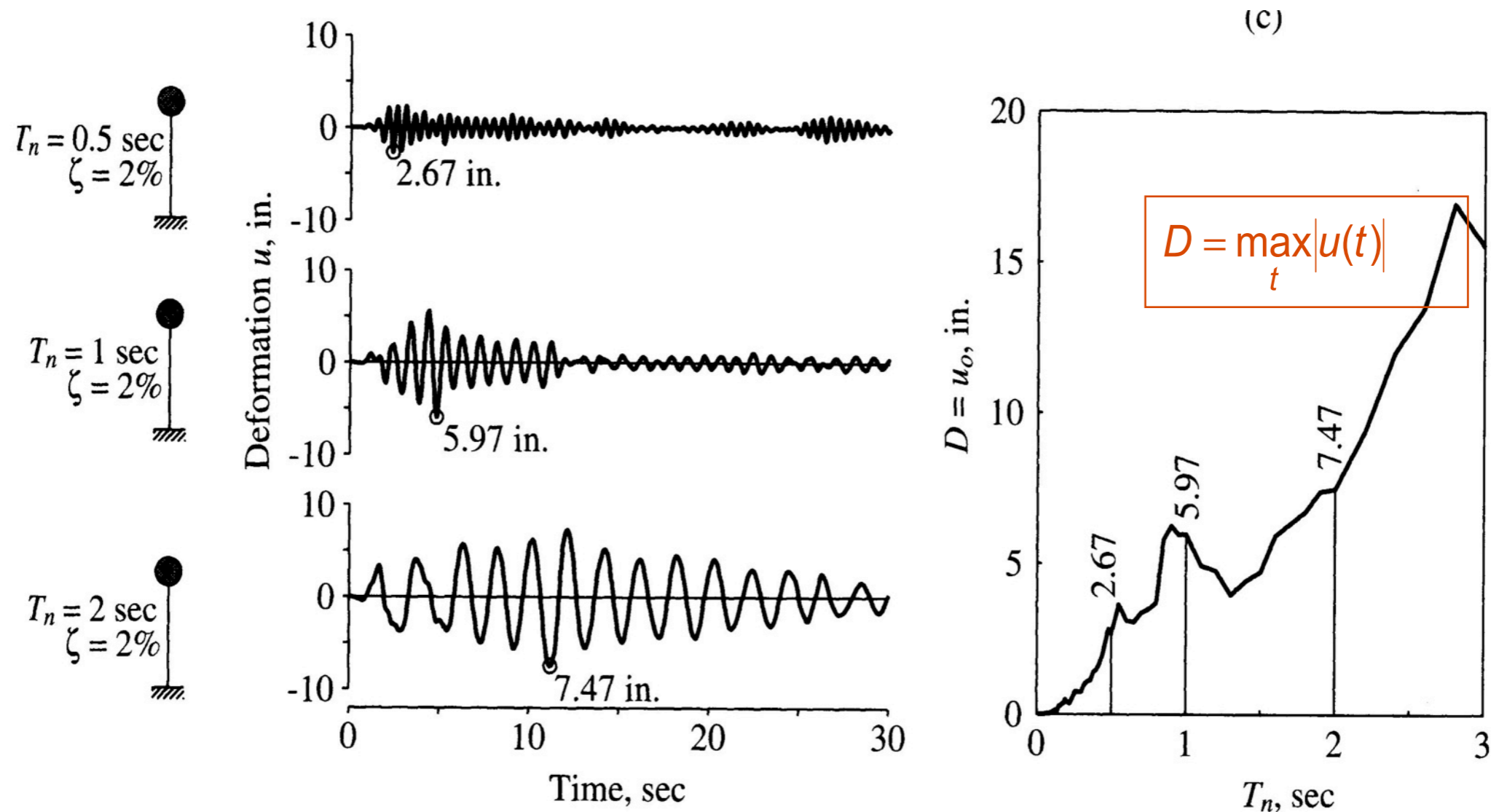
Acceleration time history.  
Sylmar N360 record.  
1994 Northridge earthquake  
(Mw=6.7)



# Response spectra

A response spectrum is a plot of maximum response (e.g. displacement, velocity, acceleration) of SDF systems to a given ground acceleration versus systems parameters ( $T_n$ ,  $\xi$ ).

EXAMPLE : Deformation response spectrum for El Centro earthquake



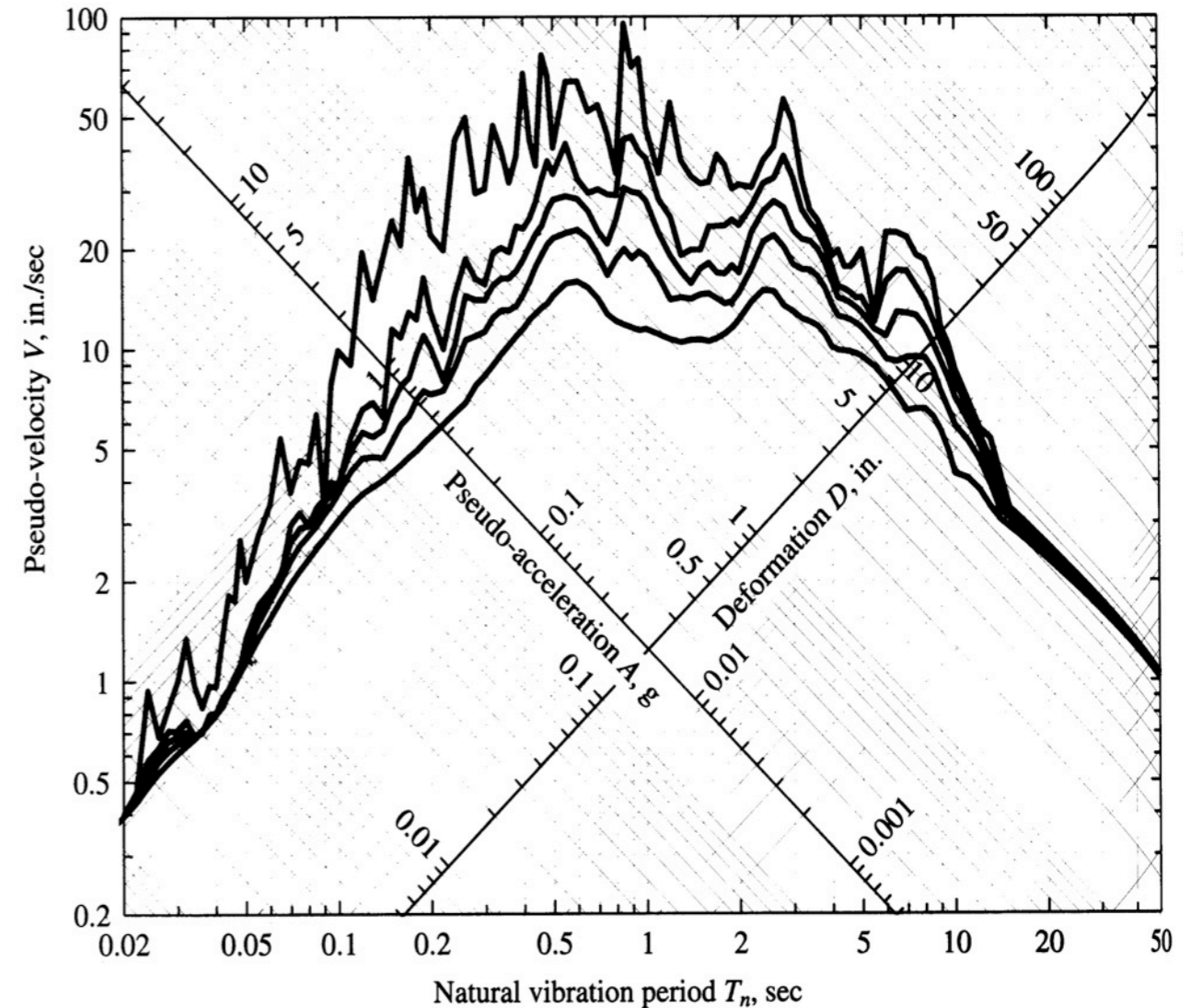
# Response spectra

**Deformation, pseudo-velocity** and **pseudo-acceleration** response spectra can be defined and plotted on the same graphs

Peak Deformation	$D = \max u(t) $
Peak Pseudo-velocity	$V = \omega_n D$
Peak Pseudo-acceleration	$A = \omega_n^2 D$

$\omega_n$  : natural circular frequency of the SDF system.

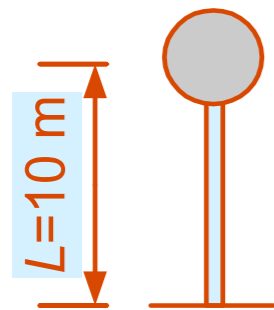
## COMBINED D-V-A SPECTRUM



**Figure 6.6.4** Combined D-V-A response spectrum for El Centro ground motion;  $\zeta = 0, 2, 5, 10,$  and  $20\%$ .

## EXAMPLE

A water tank is subjected to the El Centro earthquake. Calculate the maximum bending moment during the earthquake.



$$m = 10000 \text{ kg}$$

$$k = 98.7 \text{ kN/m}$$

$$\xi = 2\%$$

$$\omega_n = \sqrt{\frac{k}{m}} = 3.14 \text{ rad/s} \quad T_n = \frac{2\pi}{\omega_n} = 2 \text{ s}$$

$$\text{Spectrum} \rightarrow \begin{cases} D = 7.47 \times 25.4 = 190 \text{ mm} \\ A = 0.191 \times 9.81 = 1.87 \text{ ms}^{-2} \end{cases}$$

$$(\text{obs: } A = \omega_n^2 D)$$

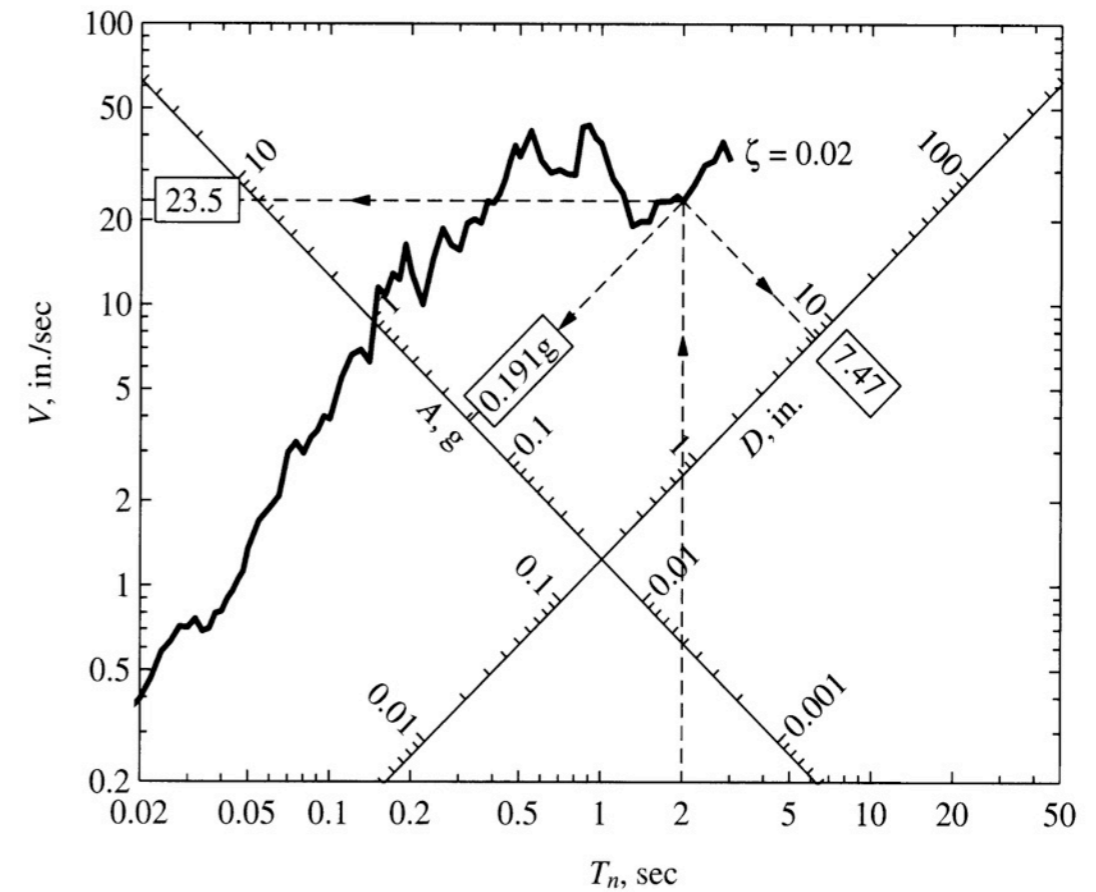
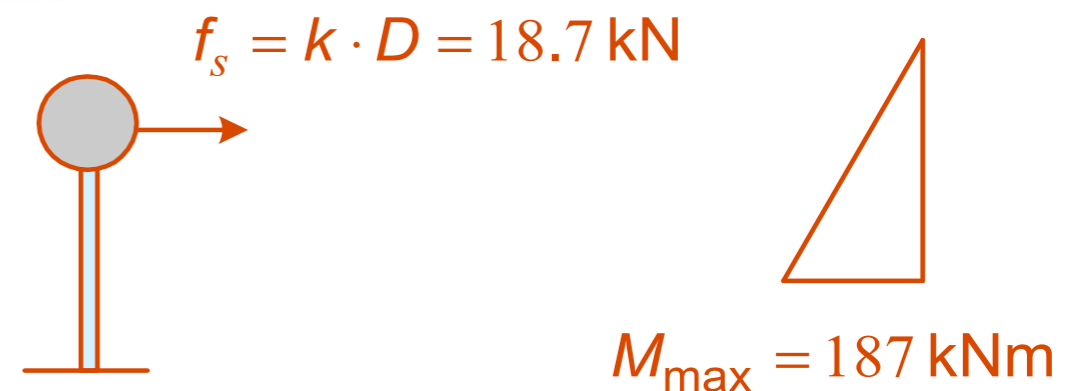


Figure 6.6.3 Combined  $D$ - $V$ - $A$  response spectrum for El Centro ground motion;  $\zeta = 2\%$ .



When the equivalent static force has been determined, the internal forces and stresses can be determined using statics.



# Response spectrum characteristics

General characteristics can be derived from the analysis of response spectra.

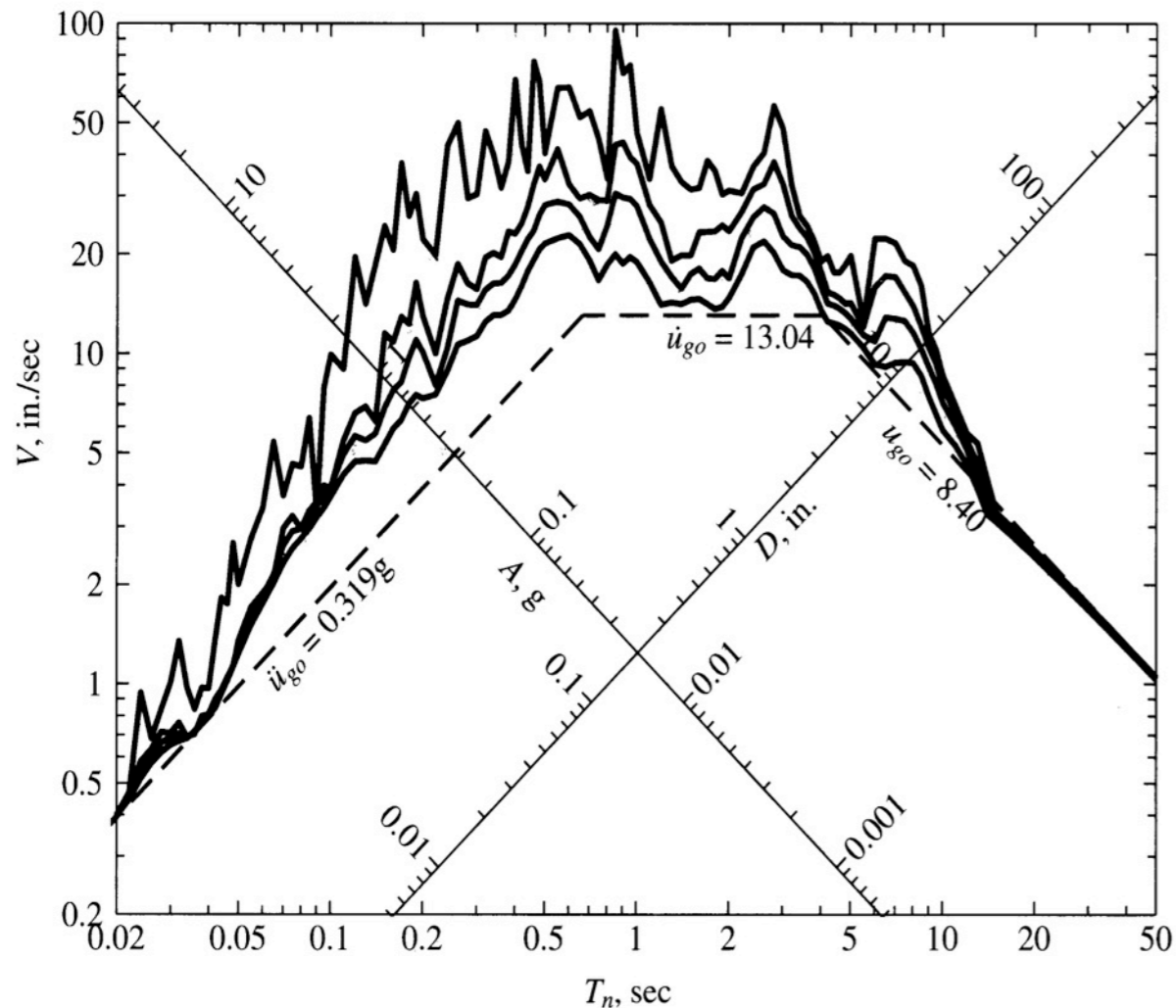
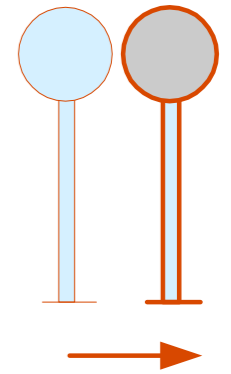


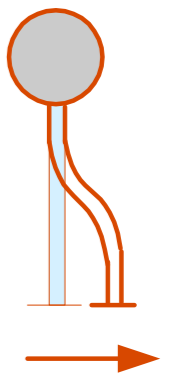
Figure 6.8.1 Response spectrum ( $\zeta = 0, 2, 5, \text{ and } 10\%$ ) and peak values of ground acceleration, ground velocity, and ground displacement for El Centro ground motion.

$$T_n = 2\pi\sqrt{m/k}$$

$T_n < 0.03 \text{ s}$  : rigid system  
no deformation  
 $u(t) \approx 0 \rightarrow D \approx 0$



$T_n > 15 \text{ s}$  : flexible system  
no total displacement  
 $u(t) = u_g(t) \rightarrow D = u_{go}$



The spectrum can be divided in 3 period ranges :

$T_n < 0.5 \text{ s}$  : acceleration sensitive region

$0.5 < T_n < 3 \text{ s}$  : velocity sensitive region

$T_n > 3 \text{ s}$  : displacement sensitive region

# Elastic design spectrum

**Problem:** how to ensure that a structure will resist future earthquakes.

The elastic design spectrum is obtained from ground motions data recorded during past earthquakes at the site or in regions with near-similar conditions

## EXAMPLE

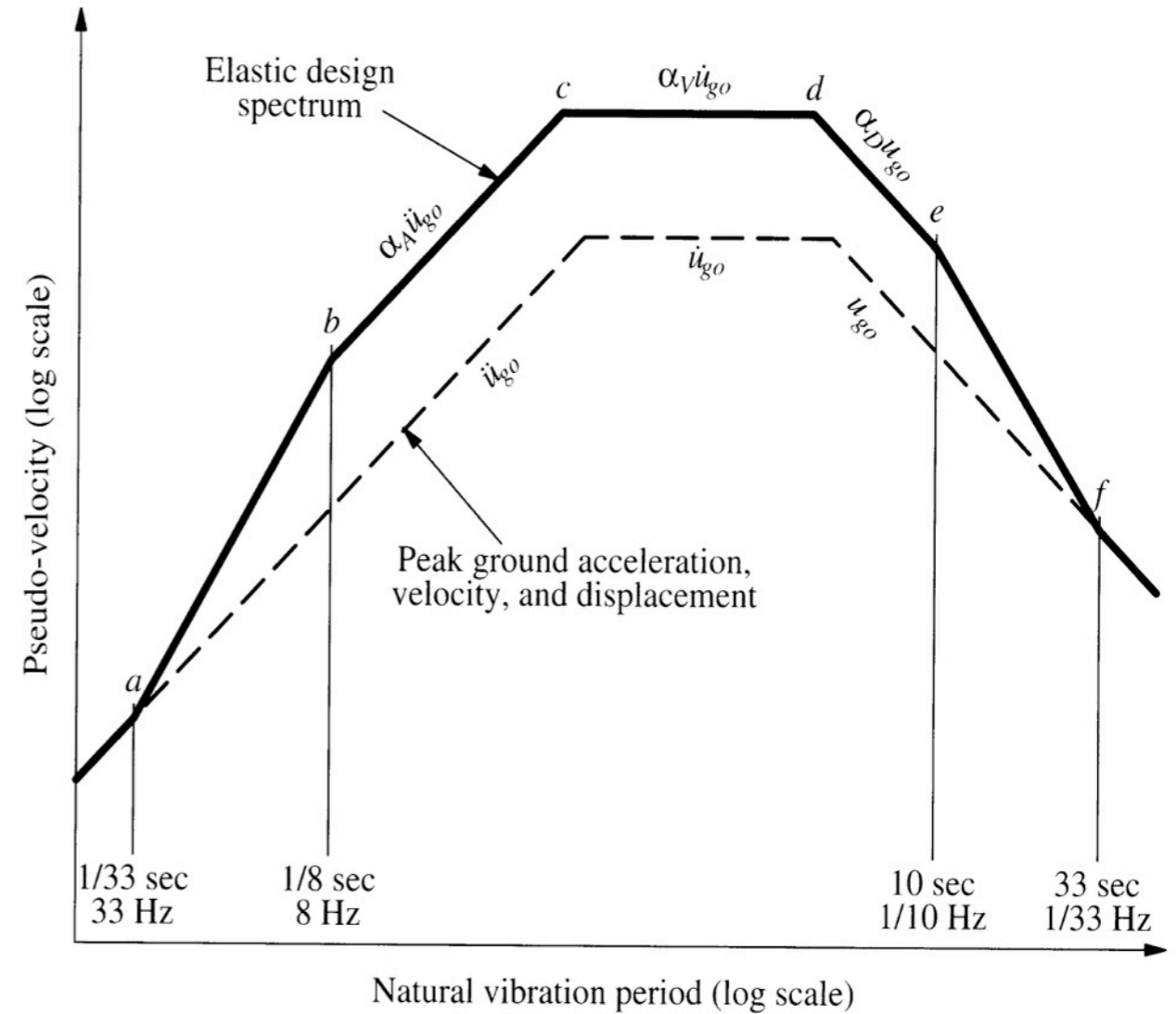


Figure 6.9.3 Construction of elastic design spectrum.

# EPA

Realizing the limitation of using peak instrumental values, since damage can not be related only to the peak values, but it may require the occurrence of several repeated cycles, Applied Technology Council (1978) ATC introduced the concept of effective peak acceleration, EPA.

The effective peak acceleration EPA is defined as the average spectral acceleration over the period range 0.1 to 0.5 s divided by 2.5 (the standard amplification factor for a 5% damping spectrum), as follows:

$$EPA = \frac{\bar{S}_{pa}}{2.5}$$

where  $\bar{S}_{pa}$  is the mean pseudo-acceleration value. The empirical constant 2.5 is essentially an amplification factor of the response spectrum obtained from real peak value records. Thus EPA is correlated with the real peak value, but not equal to nor even proportional to it. If the ground motion consists of high frequency components, EPA will be obviously smaller than the real peak value.

It represents the acceleration which is most closely related to the structural response and to the damage potential of an earthquake. The EPA values for the two records of Ancona and Sylmar stations are 205 cm/s<sup>2</sup> and 774 cm/s<sup>2</sup> respectively, and describe in a more appropriate way, than PGA values, the damage caused by the two earthquakes.



# Duration

Several observations derived from analyses of strong motion records of recent earthquakes indicate the considerable influence of the duration on the cumulative damage of the structures. For example, time histories with high amplitudes but short duration can be associated to moderate damages compared to ground motion with lowest amplitude but with longest duration. Moreover, it is well known that the major drawback in the use of elastic response spectra is the neglecting of the duration.

Different approaches have been taken to the problem of evaluating the duration of strong motion in an accelerogram. The bracketed duration (Bolt, 1973) is defined as the time between the first and the last exceedances of a threshold acceleration (usually 0.05g). Among the different duration definitions that can be found in the literature, one commonly used is that proposed by Trifunac e Brady (1975):

$$t_D = t_{0.95} - t_{0.05}$$

where  $t_{0.05}$  and  $t_{0.95}$  are the time at which respectively the 5% and 95%, of the time integral of the history of squared accelerations are reached, which corresponds to the time interval between the points at which 5% and 95% of the total energy has been recorded.

# Arias Intensity

The Arias Intensity (Arias, 1969),  $I_A$ , is defined as follows:

$$I_A = \frac{\pi}{2g} \int_0^{t_t} a_g^2(t) dt$$

where  $t_t$  and  $a_g$  are the total duration and ground acceleration of a ground motion record, respectively. The Arias intensity has units of velocity.  $I_A$  represents the sum of the total energies, per unit mass, stored, at the end of the earthquake ground motion, in a population of undamped linear oscillators.

Arias Intensity, which is a measure of the global energy transmitted to an elastic system, tends to overestimate the intensity of an earthquake with long duration, high acceleration and broad band frequency content. Since it is obtained by integration over the entire duration rather than over the duration of strong motion, its value is independent of the method used to define the duration of strong motion.

# Housner Intensity

Housner (1952) defined a measure expressing the relative severity of earthquakes in terms of the area under the pseudo-velocity spectrum between 0.1 and 2.5 seconds. Housner's spectral intensity  $I_H$  is defined as:

$$I_H = \int_{0.1}^{2.5} S_{pv}(T, \xi) dT = \frac{1}{2\pi} \int_{0.1}^{2.5} S_{pa}(T, \xi) T dT$$

where  $S_{pv}$  is the pseudo-velocity at the undamped natural period  $T$  and damping ratio  $\xi$ , and  $S_{pa}$  is the pseudo-acceleration at the undamped natural period  $T$  and damping ratio  $\xi$ . Thus, Housner's spectral intensity is the first moment of the area of  $S_{pa}$  ( $0.1 < T < 2.5$ ) about the  $S_{pa}$  axis, implying that the Housner spectral intensity is larger for ground motions with a significant amount of low frequency content.

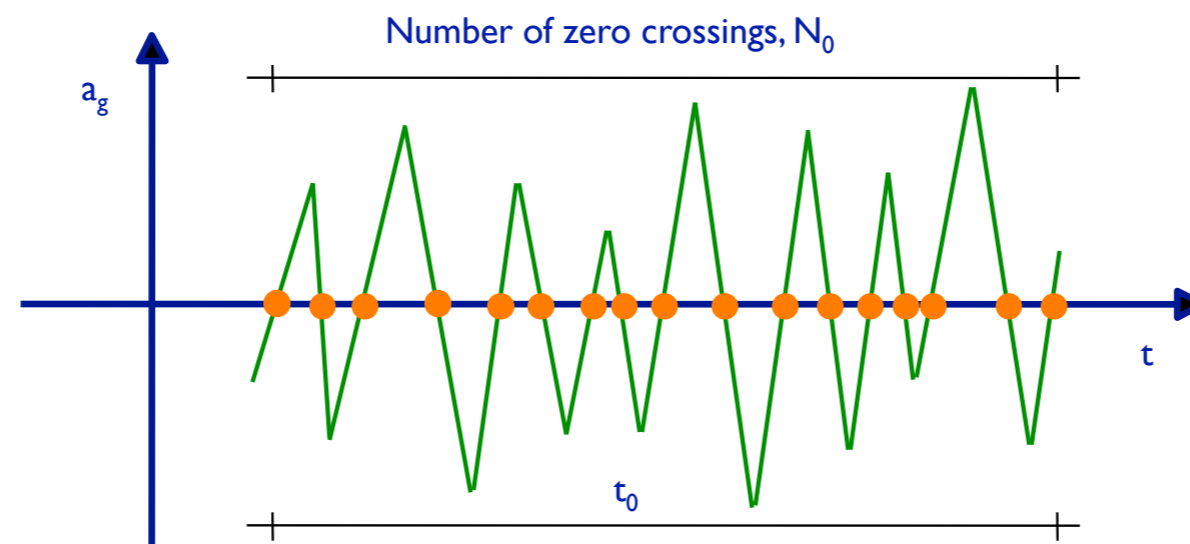
The  $I_H$  parameter captures important aspects of the amplitude and frequency content in a single parameter, however, it does not provide information on the strong motion duration which is important for a structural system experiencing inelastic behaviour and yielding reversals.

# Destructiveness potential factor

Araya & Saragoni (1984) proposed the destructiveness potential factor,  $P_D$ , that considers both the Arias Intensity and the rate of zero crossings,  $\nu_0$  and agrees with the observed damage better than other parameters. The destructiveness potential factor, which simultaneously considers the effect of the ground motion amplitude, strong motion duration, and frequency content on the relative destructiveness of different ground motion records, is defined as:

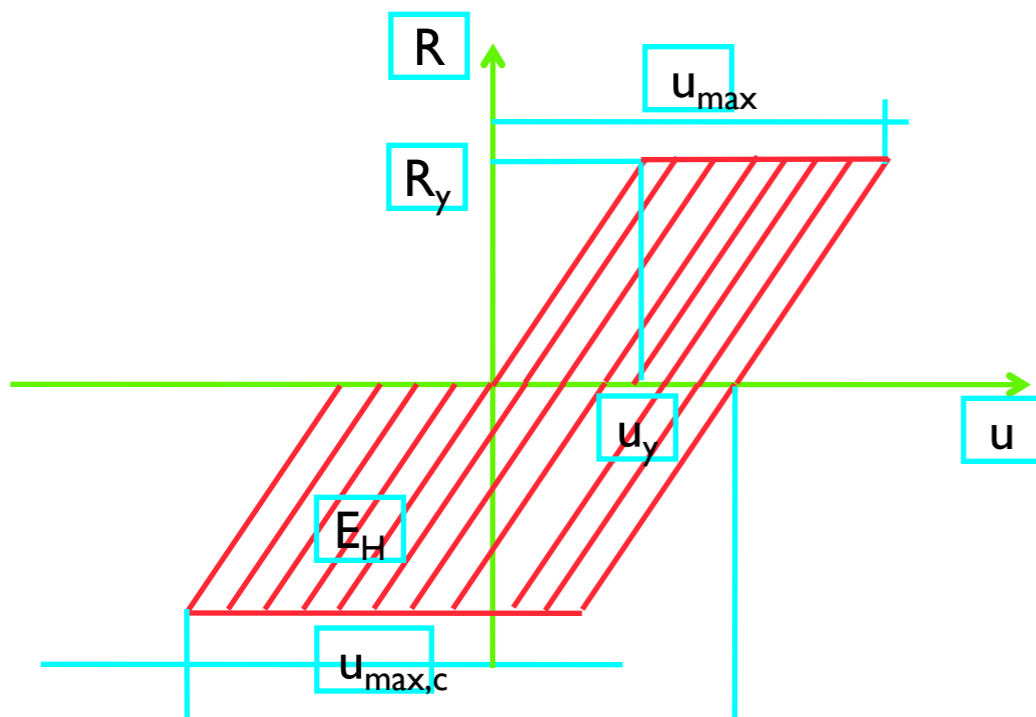
$$P_D = \frac{\pi}{2g} \frac{\int_0^{t_0} a_g^2(t) dt}{\nu_0^2} = \frac{I_A}{\nu_0^2} \quad \nu_0 = \frac{N_0}{t_0}$$

where  $t$  is the time,  $a_g$  is the ground acceleration,  $\nu_0 = N_0/t_0$  is the number of zero crossings of the acceleration time history per unit of time,  $N_0$  is the number of the crossings with the time axis,  $t_0$  is the total duration of the examined record (sometimes it could be a particular time-window), and  $I_A$  is the Arias intensity.



# Ductility

In current seismic regulations, the displacement **ductility** ratio  $\mu$  is generally used to reduce the elastic design forces to a level which implicitly considers the possibility that a certain degree of inelastic deformations could occur. To this purpose, employing numerical methods, constant ductility response spectra were derived through non-linear dynamic analyses of viscously damped SDOF systems by defining the following two parameters:



$$\mu = \frac{u_{max}}{u_y} \quad C_y = \frac{R_y}{mg}$$

$$\eta = \frac{R_y}{m\ddot{u}_{g(max)}} = \frac{C_y}{\ddot{u}_{g(max)}/g}$$

where  $R_y$  is the **yielding resistance**,  $m$  is the mass of the system, and  $\ddot{u}_{g(max)}$  is the maximum ground acceleration.

The parameter  $C_y$  represents the structure's **yielding seismic resistance coefficient** and  $\eta$  expresses a system's **yield strength** relative to the maximum inertia force of an infinitely rigid system and reveals the strength of the system as a fraction of its weight relative to the peak ground acceleration expressed as a fraction of gravity.

# Input Energy

The elastic and inelastic (in terms of displacement ductility) response spectra are not sufficient for the estimation of the damage potential of the earthquake ground motion because they do not give a precise description of the quantity of the energy that will be dissipated through hysteretic behaviour; in the inelastic case they give only the value of the maximum ductility requirement. To overcome this problem other ductility definitions, e.g. hysteretic or cyclic ductility, were introduced.

Among all the different parameters proposed for defining the damage potential, perhaps the most promising is the Earthquake Input Energy ( $E_I$ ) and associate parameters (the damping energy  $E_\xi$  and the plastic hysteretic energy  $E_H$ ) introduced by Uang & Bertero (1990). This parameter considers the inelastic behavior of a structural system and depends on the dynamic features of both the strong motion and the structure.

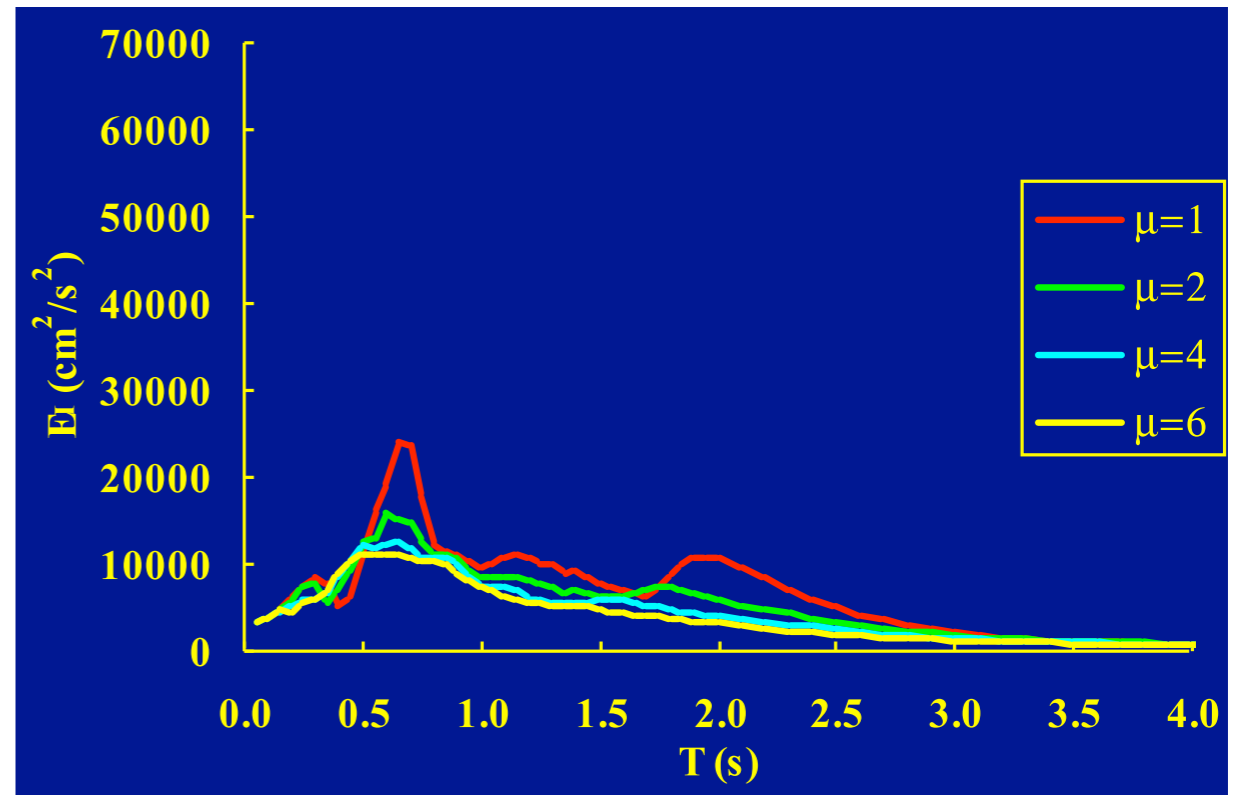
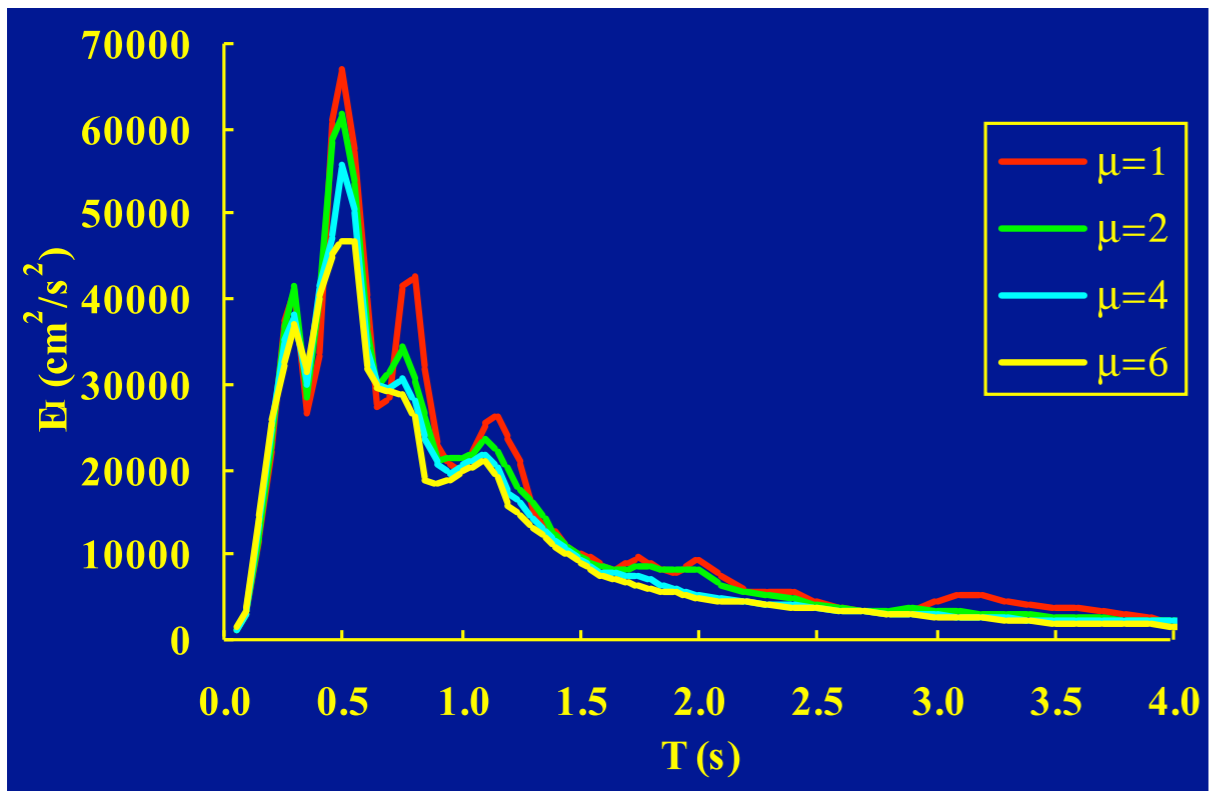
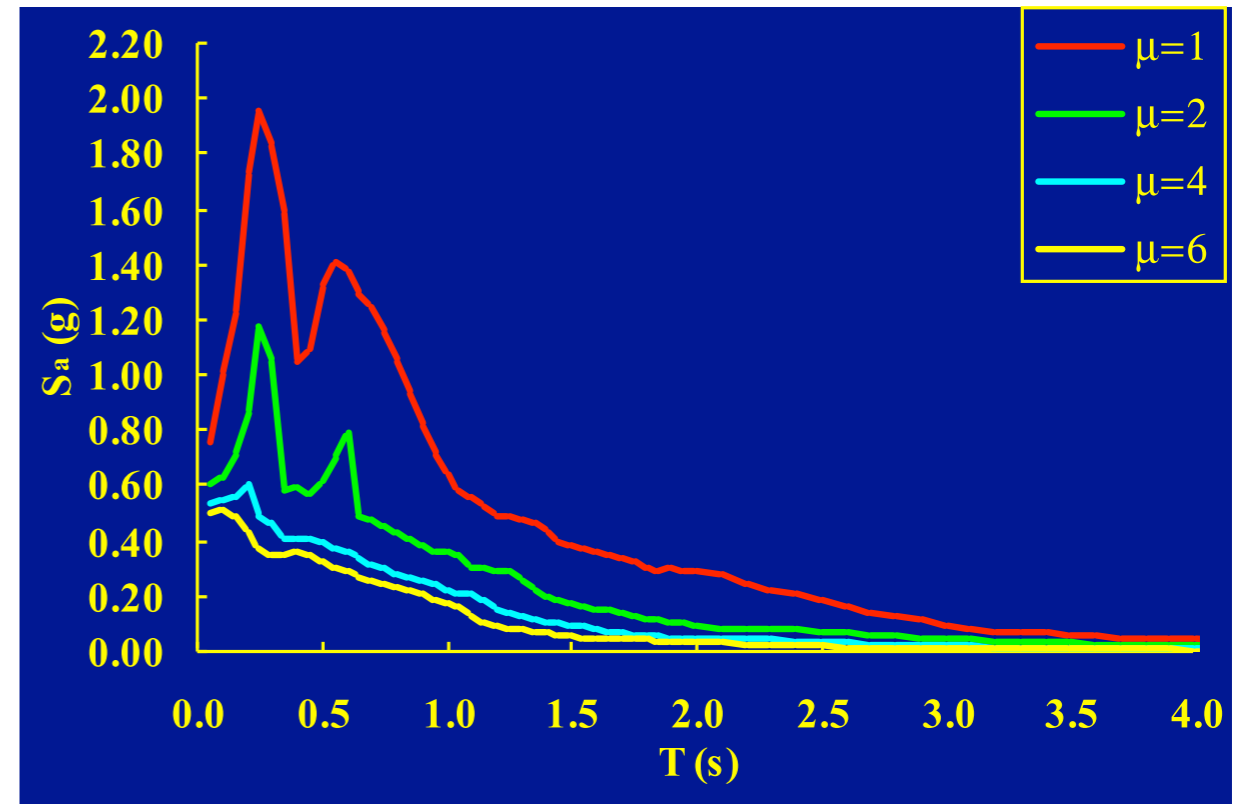
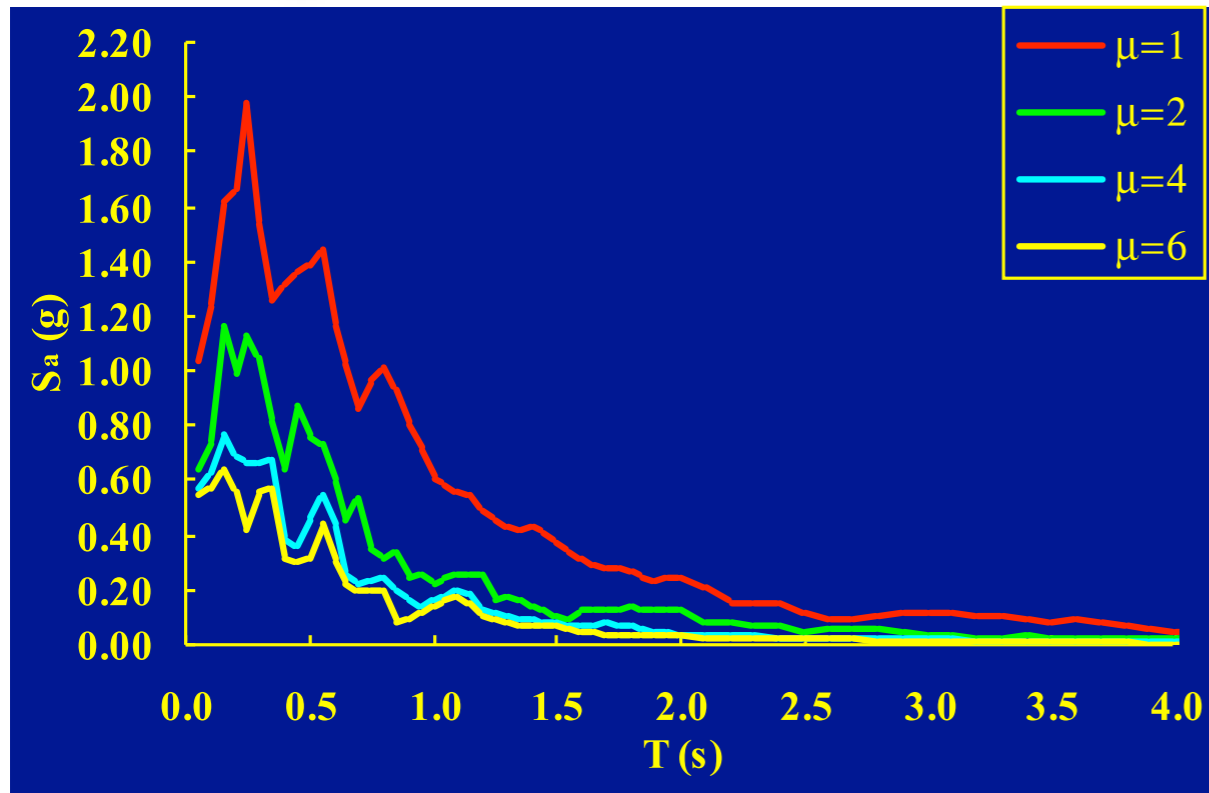
The formulation of the energy parameters derives from the following balance energy equation (Uang & Bertero, 1990), where ( $E_I$ ) is the input energy, ( $E_k$ ) is the kinetic energy, ( $E_s$ ) is the elastic strain energy:

$$E_I = E_k + E_\xi + E_s + E_H$$

$E_I$  represents the work done by the total base shear at the foundation displacement.



# Comparison



Chile Earthquake 1985  
LLOLLEO N10,  $M=7.8$ ,  $D_f=33$  km

San Salvador Earthquake 1986  
CIG N90,  $M=5.4$ ,  $D_f=1.6$  km