

Problem set 1

1. Read the section 3.4 Quasiconcavity and quasiconvexity in the math tutorial of Martin Osborne (<http://www.economics.utoronto.ca/osborne/MathTutorial/QCCF.HTM>) and check quasiconcavity for the following functions:
 - a. $y + \ln x$ for $x, y > 0$
 - b. $4xy + 4x$ for $x, y < 0$
2. Check if the following matrix is positive/negative semi-definite
$$\begin{matrix} -4 & 0 & 1 \\ 1 & -2 & 0 \\ 0 & 2 & 1 \end{matrix}$$
3. Check if the following functions are concave/convex
 - a. \sqrt{xy}
 - b. $\ln x + \ln y$
4. Find the all stationary points of the following functions. Then check the second order conditions and state if they are local/global maximizers/minimizers
 - a. $x^3 - 12x + y^3 - 27y + z^3 - 3z$
 - b. $-y^2 - 2x^2 + xy$
 - c. $-y^2 - 2x^2 + 2xy$
 - d. $e^x - xy$
 - e. $\ln x + \ln y + \ln z - 4x - 5y - 6z$ for $z, x, y > 0$
5. Suppose that a firm that uses 2 inputs has the production function $f(x, y) = 12x^{\frac{1}{3}}y^{\frac{1}{2}}$ and faces the input prices (p_x, p_y) and the output price q .
 - a. Show that f is concave, so that the firm's profit is concave.
 - b. Find a global maximum of the firm's profit (and give the input combination that achieves this maximum).