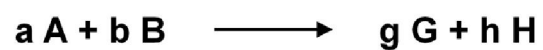


## Chemical kinetic

### Study of the rate of chemical reactions

- Measurements of reactions rates
- How to predict reaction rates
- Determine reaction mechanisms

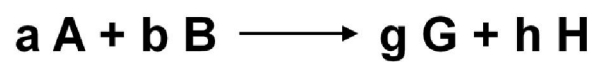


#### General Reaction Rate

$$\text{Rate} = -\frac{1}{a} \frac{\Delta[A]}{\Delta t} = -\frac{1}{b} \frac{\Delta[B]}{\Delta t} = \frac{1}{g} \frac{\Delta[G]}{\Delta t} = \frac{1}{h} \frac{\Delta[H]}{\Delta t}$$

## Chemical kinetic

### General Reaction Rate



$$\text{Rate} = -\frac{1}{a} \frac{\Delta[\text{A}]}{\Delta t} = -\frac{1}{b} \frac{\Delta[\text{B}]}{\Delta t}$$

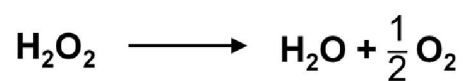
Expressed from  
consumption of reagents

$$\text{Rate} = \frac{1}{g} \frac{\Delta[\text{G}]}{\Delta t} = \frac{1}{h} \frac{\Delta[\text{H}]}{\Delta t}$$

Expressed from  
production of products

## Chemical kinetic

### Study of the rate of chemical reactions



t / s	[H <sub>2</sub> O <sub>2</sub> ] / M	Δ t	Δ [H <sub>2</sub> O <sub>2</sub> ]	Rate / M s <sup>-1</sup>
0	2.32			
200	2.01	200	0.31	1.550E-03
400	1.72	200	0.29	1.450E-03
600	1.49	200	0.23	1.150E-03
800	1.30	200	0.19	9.500E-04
1200	0.98	400	0.32	8.000E-04
1600	0.73	400	0.25	6.250E-04
2000	0.54	400	0.19	4.750E-04
2400	0.39	400	0.15	3.750E-04
2800	0.28	400	0.11	2.750E-04

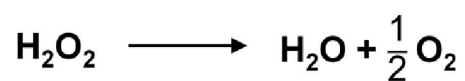
### Average Rate

$$\text{Rate} = - \frac{\Delta[\text{H}_2\text{O}_2]}{\Delta t}$$

$$\text{Rate} = \frac{1}{1/2} \frac{\Delta[\text{O}_2]}{\Delta t}$$

## Chemical kinetic

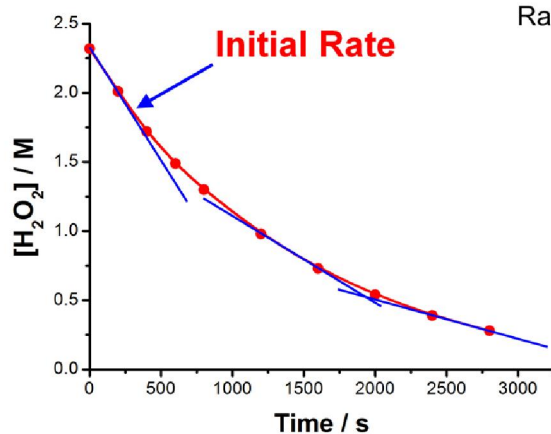
### Study of the rate of chemical reactions



#### Instantaneous Rate

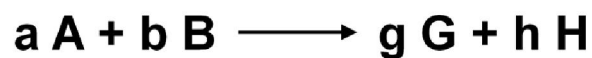
$$\text{Rate} = \lim_{\Delta t \rightarrow 0} \left( - \frac{\Delta[\text{H}_2\text{O}_2]}{\Delta t} \right) = - \frac{d[\text{H}_2\text{O}_2]}{dt}$$

Slope of the tangent



## Chemical kinetic

### Effect of concentration: the Rate Law



$$\text{Rate} = k [A]^m [B]^n \quad \text{Rate Law}$$

**k**: Kinetic constant

**m** and **n**: Partial reaction order with respect to the reagents

**m + n**: Overall reaction order

**m** and **n** are small numbers:

- Positive, negative or zero
- Integer or fractional
- NO CONNECTION with stoichiometric coefficients!!!
- Must be determined experimentally.

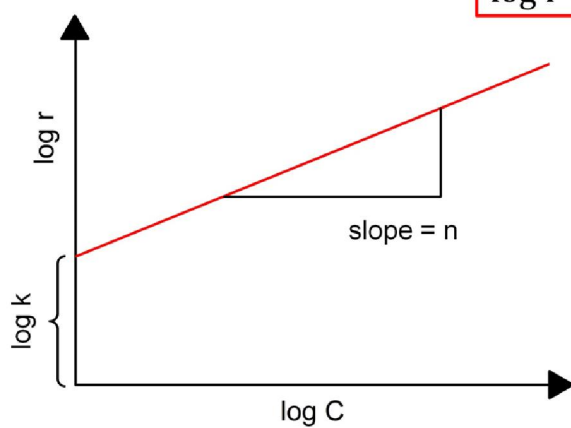
## Chemical kinetic

### Partial reaction order

In the case of a reaction with a only one reagent, for a  $n^{\text{th}}$  reaction order:

$$r = -\frac{dC}{dt} = k C^n$$

$$\log r = \log k + n \log C$$

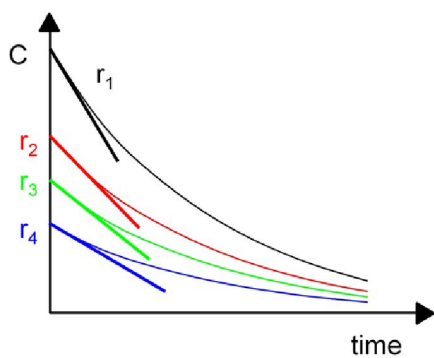


## Chemical kinetic

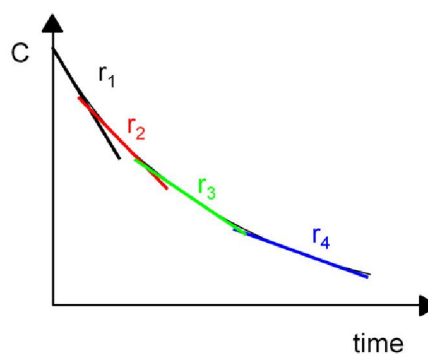
### Partial reaction order

The graph can be obtained in 2 ways:

Measuring initial rate for  
different concentrations:



Measuring the  
instantaneous rate at  
different reaction time:



## Chemical kinetic

### Partial reaction order

In the case of a reaction with more than one reagent, the reaction rate is determined changing the concentration of the specific reagent maintaining constant all the other:

$$r = k C^n$$

$$\frac{r_1}{r_2} = \left( \frac{C_1}{C_2} \right)^n$$

$$\log \frac{r_1}{r_2} = n \log \frac{C_1}{C_2}$$

$$n = \frac{\log \frac{r_1}{r_2}}{\log \frac{C_1}{C_2}}$$



## Chemical kinetic

### Partial reaction order



$$r = k [\text{HgCl}_2]^m [\text{C}_2\text{O}_4^{2-}]^n$$

Experiment	$[\text{HgCl}_2] / \text{M}$	$[\text{C}_2\text{O}_4^{2-}] / \text{M}$	Initial rate / $\text{M min}^{-1}$
1	0.105	0.15	$1.8\text{e-}5$
2	0.105	0.30	$7.1\text{e-}5$
3	0.052	0.30	$3.5\text{e-}5$

$$m = \frac{\log \frac{r_2}{r_3}}{\log \frac{C_2}{C_3}} = \frac{\log \frac{7.1\text{e-}5}{3.5\text{e-}5}}{\log \frac{0.105}{0.052}} = \frac{0.3072}{0.3052} = 1.01 \cong 1$$

$$n = \frac{\log \frac{r_1}{r_2}}{\log \frac{C_1}{C_2}} = \frac{\log \frac{1.8\text{e-}5}{7.1\text{e-}5}}{\log \frac{0.15}{0.30}} = \frac{-0.5960}{-0.3010} = 1.98 \cong 2$$

## Chemical kinetic

### Zero-order reaction

$$r = k$$

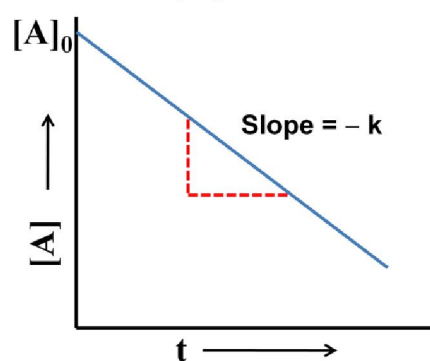
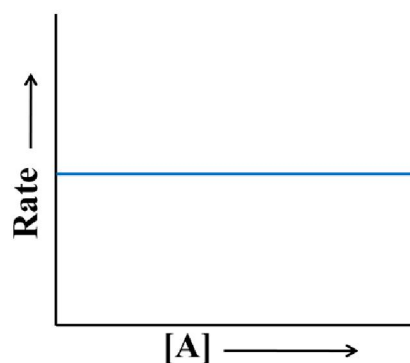
$$-\frac{1}{a} \frac{d[A]}{dt} = k$$

$$\int_{[A]_0}^{[A]_t} d[A] = -ak \int_0^t dt$$

$$[A]_t = [A]_0 - akt$$

**Integrated rate law**

$k$  in  $\text{mol L}^{-1} \text{s}^{-1}$



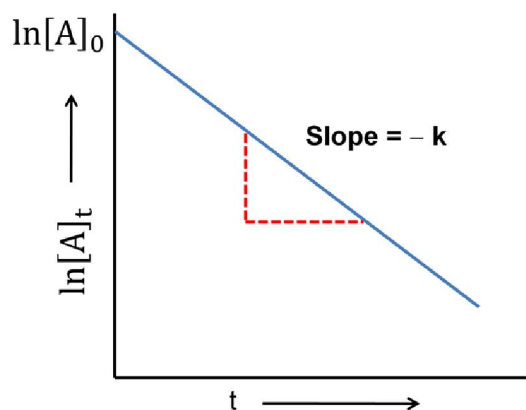
## Chemical kinetic

### First-order reaction

$$-\frac{1}{a} \frac{d[A]}{dt} = k[A]$$

$$\int_{[A]_0}^{[A]_t} \frac{d[A]}{[A]} = -ak \int_0^t dt$$

$$\ln \frac{[A]_t}{[A]_0} = -akt$$



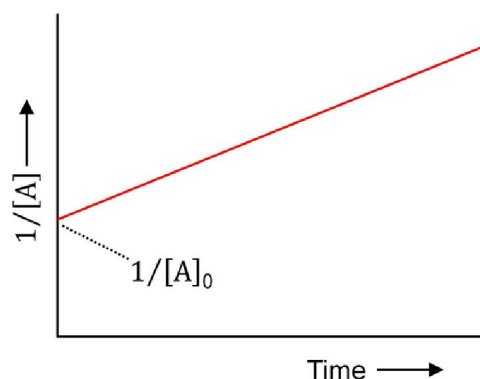
$k$  in  $s^{-1}$

## Chemical kinetic

### Second-order reaction

$$-\frac{1}{a} \frac{d[A]}{dt} = k[A]^2$$

$$\int_{[A]_0}^{[A]_t} \frac{d[A]}{[A]^2} = -ak \int_0^t dt$$



$$\frac{1}{[A]_t} = akt + \frac{1}{[A]_0}$$

$k$  in  $\text{L mol}^{-1} \text{s}^{-1}$

## Chemical kinetic

### Half-time

For a reaction the half-life  $t_{1/2}$  of a particular reactant is defined as the time required to **reduce the concentration to half of its initial value**.

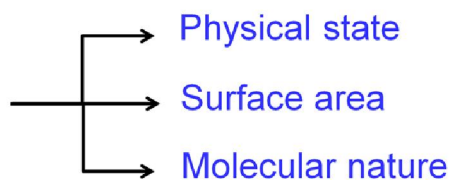
Order	Half-time $t_{1/2}$
0	$\frac{[A]_0}{2ak}$
1	$\frac{0.693}{ak}$
2	$\frac{1}{ak[A]_0}$

## Chemical kinetic

### Factors Affecting the Rate of a Reaction

#### 1. Concentration of the reactants

#### 2. Nature of reactants



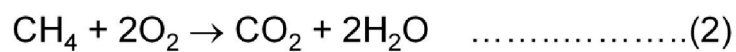
- ❖ Rate of reactions with reactants in  
gaseous phase > solution phase > solid phase
- ❖ Larger the surface area, larger is the area of contact  
hence faster is the rate of the reaction

## Chemical kinetic

### Molecular nature of the reactant

More is the structural similarity between the reactant and the product  $\Rightarrow$  faster is the reaction (**Not always**)

Lesser the rearrangement of bonds needed in the reaction  $\Rightarrow$  faster is the reaction

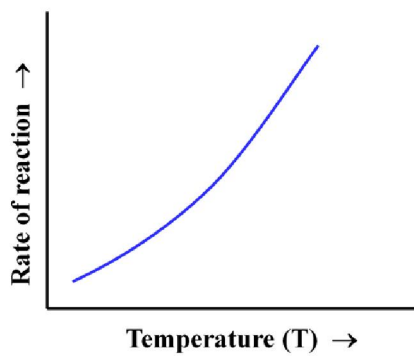


## Chemical kinetic

### Effect of temperature

Temperature has a marked effect on the reactions

- (i) Can initiate a reaction
- (ii) Increases the rate of the reaction





## **Chemical kinetic**

### **Theories of Chemical Reactions**

There are various theories proposed to explain chemical reactions.

The most important theories are

1. Collision Theory
2. Transition-State Theory or Activated Complex Theory or Absolute Reaction Rate Theory

## **Chemical kinetic**

### **Collision theory**

- ❖ This is the oldest theory based on kinetic theory of collisions.
- ❖ Originally suggested for gas phase reactions.
- ❖ This suggests that we can understand the rates of reactions by analysing the molecular collisions.
- ❖ All assumptions of kinetic theory of gases are applicable

## Chemical kinetic

### Collision theory - Assumptions

- ❖ The molecules/atoms are hard spheres
- ❖ The molecular motions are explained by classical mechanics or Newtonian mechanics
- ❖ The size of the molecules is negligible as compared to the typical distance between them
- ❖ Due to the kinetic energy of molecules, they move around and collide with each other
- ❖ The molecular collisions are perfectly elastic *i.e.* energy is conserved

## Chemical kinetic

### Collision theory

The velocity of the molecules is distributed according to Maxwell distribution.

The mean velocity of a molecule is given as

$$\bar{u} = \sqrt{\frac{8k_B T}{\pi m}}$$

$k_B$	Boltzmann constant,
$T$	Temperature,
$m$	mass of a molecule

Considering collision between two types of molecules A and B of mass  $m_A$  and  $m_B$  then the mean relative velocity is given by

$$\bar{u}_{rel} = \sqrt{\frac{8k_B T}{\pi \mu}}$$

Where  $\mu = \frac{m_A m_B}{m_A + m_B}$

## Chemical kinetic

### Collision theory

The rate of the reaction can be calculated from the rate at which the reactant molecules are colliding

So the collision rate or collision number (number of collisions per unit volume per unit time) is expressed as

$$Z_{AB} = N_A N_B \pi (r_A + r_B)^2 \bar{u}_{rel}$$

$$Z_{AB} = N_A N_B \sigma \sqrt{\frac{8k_B T}{\pi \mu}}$$

$$\sigma = \pi (r_A + r_B)^2 = \text{Collision cross section}$$

## Chemical kinetic

### Collision theory

The collision between A and B will result in a reaction provided the energy of the collision is sufficient to overcome the energy barrier  $E_a$  (effective collision).

According to Boltzmann distribution the fraction of collisions with energy of  $E_a$  is proportional to  $e^{-E_a/RT}$

So the number of effective collisions per unit volume per unit time = number of product molecules formed per unit volume per unit time

$$Z_{AB} e^{-E_a/RT}$$

Number of moles of product formed per unit volume per unit time

$$\left( Z_{AB} e^{-E_a/RT} \right) / N$$

## Chemical kinetic

### Collision theory

The rate expressed in moles/unit volume/unit time is

$$r = (Z_{AB} e^{-E_a/RT})/N$$

$$r = \frac{1}{N} N_A N_B \sigma \sqrt{\frac{8k_B T}{\pi \mu}} e^{-E_a/RT}$$

If the reaction is first order w.r.t. both A and B



$$\mathbf{r = k [A] [B]}$$

$$r = k \frac{N_A}{N} \frac{N_B}{N}$$

$$\frac{N_A}{N} = [A], \quad \frac{N_B}{N} = [B]$$

## Chemical kinetic

### Collision theory

Comparing the two equations we get

$$k = N\sigma \sqrt{\frac{8k_B T}{\pi \mu}} e^{-E_a/RT}$$

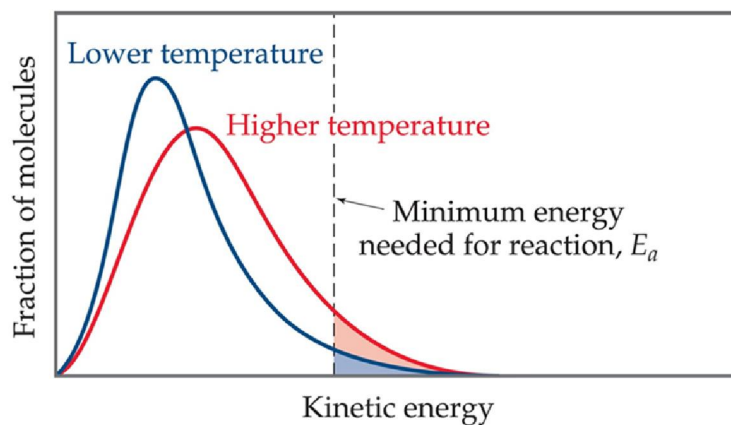
'k' is the bimolecular rate constant or second order rate constant



## Chemical kinetic

### Collision theory – Effect of temperature

The velocity of the molecules is distributed according to Maxwell distribution.



Increasing  $T$ , the fraction of molecules having at least  $E_a$  increases, accelerating the reaction.

## Chemical kinetic

### Arrhenius equation

The equation:

$$k = N\sigma \sqrt{\frac{8k_B T}{\pi \mu}} e^{-E_a/RT}$$



$$k = A e^{-E_a/RT}$$

### Arrhenius equation

with

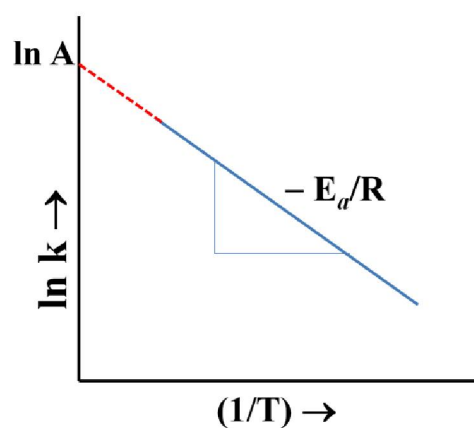
$$A = N\sigma \sqrt{\frac{8k_B T}{\pi \mu}}$$

## Chemical kinetic

### Arrhenius equation

$$\ln k = \ln A - \frac{E_a}{RT}$$

$$k = A e^{-E_a/RT}$$



'A' and ' $E_a$ ' are called Arrhenius parameters

A: Pre-exponential factor or Frequency factor or Limiting rate constant

$E_a$ : Activation energy

*A higher activation energy signifies that the rate constant depends strongly on temp.*

## Chemical kinetic

### Arrhenius equation

If the activation energy ( $E_a$ ) and pre-exponential factor ( $A$ ) are independent of temperature:

$$\ln k_1 = \ln A - \frac{E_a}{RT_1}$$

$$\ln k_2 = \ln A - \frac{E_a}{RT_2}$$

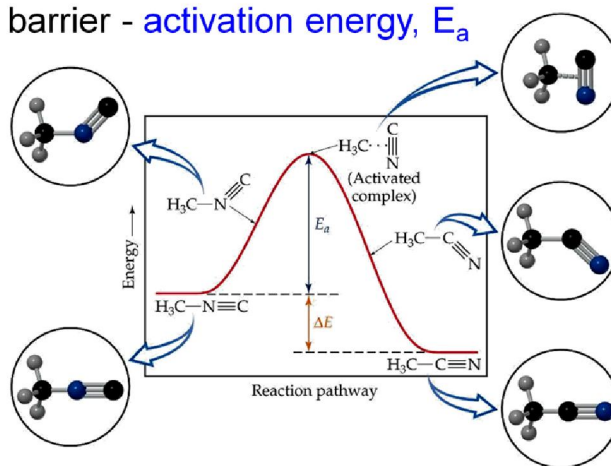
$$\ln \frac{k_1}{k_2} = \frac{E_a}{R} \left( \frac{1}{T_2} - \frac{1}{T_1} \right)$$

## Chemical kinetic

### Activation energy

Molecules need a minimum amount of energy to react.

Visualized as an energy barrier - **activation energy,  $E_a$**

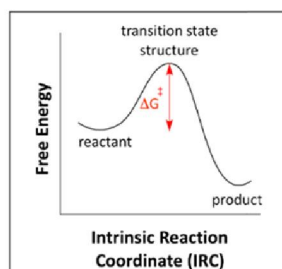


*The lower the Activation barrier, the faster the reaction*

# Chemical kinetic

## Reaction coordinate

It's a pathway within a 3D space.



Eyring equation:

$$k = \frac{k_B T}{h} e^{-\frac{\Delta G^\ddagger}{RT}}$$

$\Delta G^\ddagger$  = activation free energy

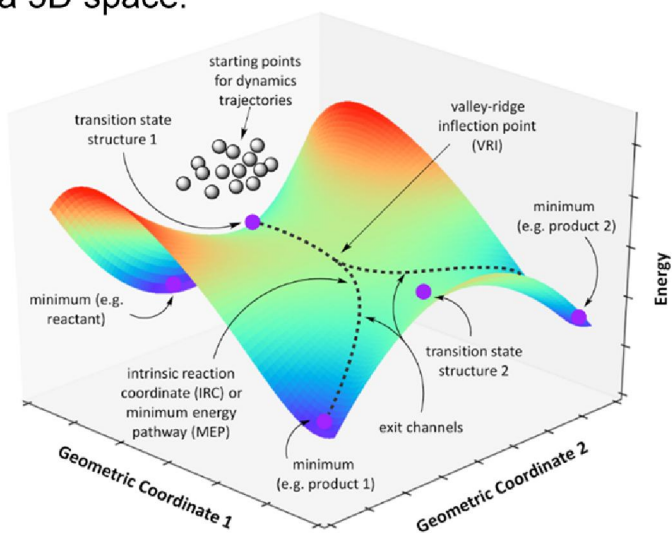
$k$  = rate constant

$k_B$  = Boltzmann's constant

$T$  = temperature

$h$  = Planck's constant

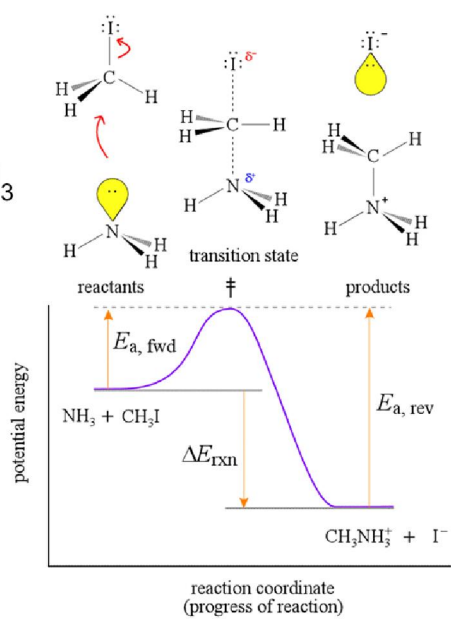
$R$  = gas constant



## Chemical kinetic

### Reaction coordinate

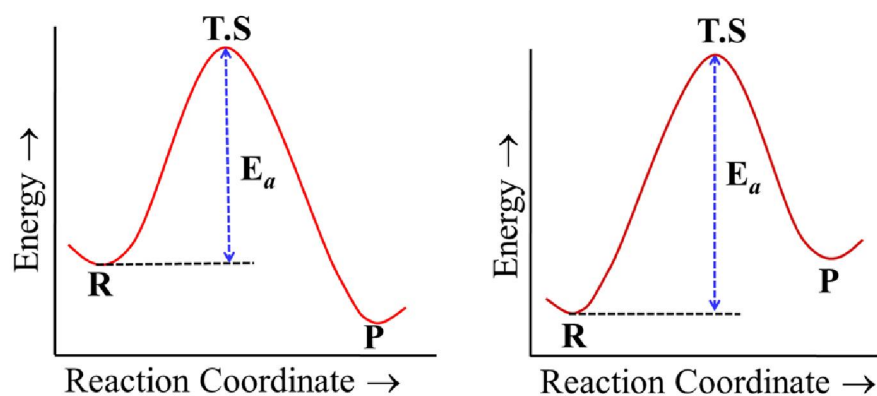
Substitution of  $\text{CH}_3\text{I}$  with  $\text{NH}_3$



## Chemical kinetic

### Transition-state Theory

The reactants form some sort of complex with a structure somewhere between the reactant and the product and called as **Transition-state** or **Activated complex**





## Chemical kinetic

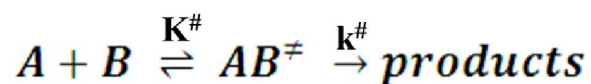
### Transition-state Theory - Assumptions

- ❖ The reactants A and B and the activated complex ( $AB^\ddagger$ ) in the T. S. are in quasi-equilibrium with each other and characterized by the pseudo-equilibrium constant ( $K^\ddagger$ )
- ❖ The rate of the product formation is influenced by the rate of decomposition of the activated complex. The concentration of the activated complex that are becoming product can be calculated using equilibrium theory
- ❖ Molecules that have passed through activated complex configuration in the direction of product can't turn back and form reactant
- ❖ The energy distribution among the reactant molecules is in accordance with the Maxwell distribution.
- ❖ The activated complex has one special vibrational degree freedom associated with the mode of product formation along the reaction coordinate *i.e.* it has been converted to a translational degree of freedom along the reaction coordinate

## Chemical kinetic

### Transition-state Theory

Let's consider a simple bimolecular reaction



$$\text{Rate of the reaction} = k^\# [AB^\ddagger]$$

In  $AB^\ddagger$  one of the vib. degree of freedom = translational degree of freedom which is responsible for the product formation

The rate at which the activated complex moves across the energy barrier is proportional to the vibrational frequency ' $\nu$ '

## Chemical kinetic

### Transition-state Theory

The rate constant ( $k^\ddagger$ ) is related to the vibration frequency ( $\nu$ ) as  $k^\ddagger = \kappa \nu$  where  $\kappa = \text{kappa} = \text{transmission coefficient}$  and  $0 < \kappa \leq 1$

For convenience the value of  $\kappa$  is taken = 1 and we know

$$k_B T = h \nu$$

$$\text{Rate} = \left( \frac{k_B T}{h} \right) [AB^\ddagger]$$

$$K^\ddagger = \frac{[AB^\ddagger]}{[A][B]}$$

$$[AB^\ddagger] = K^\ddagger [A][B]$$

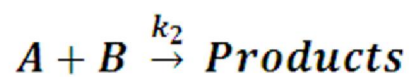
$$\text{Rate} = \left( \frac{k_B T}{h} \right) [AB^\ddagger]$$

$$\text{Rate} = \left( \frac{k_B T}{h} \right) K^\ddagger [A][B]$$

## Chemical kinetic

### Transition-state Theory

Considering the rate law for the reaction:



$$\text{Rate} = k_2 [A][B]$$

Comparing the above two equations:

$$k_2 = \text{bimolecular rate constant} = \left( \frac{k_B T}{h} \right) K^\ddagger$$

$$k_2 = k^\ddagger K^\ddagger$$

## Chemical kinetic

### Transition-state Theory

The equilibrium constant  $K^\ddagger$  can be expressed in terms of standard Gibbs free energy change of activation ( $\Delta^\ddagger G^\circ$ )

$$\Delta^\ddagger G^\circ = -RT \ln K^\ddagger \quad \Delta^\ddagger G^\circ = \Delta^\ddagger H^\circ - T\Delta^\ddagger S^\circ$$

$$K^\ddagger = e^{-\Delta^\ddagger G^\circ / RT} = e^{-\Delta^\ddagger H^\circ / RT} e^{\Delta^\ddagger S^\circ / R}$$

$$k_2 = k^\ddagger e^{-\Delta^\ddagger H^\circ / RT} e^{\Delta^\ddagger S^\circ / R}$$

$$k_2 = \left( \frac{k_B T}{h} \right) e^{-\Delta^\ddagger H^\circ / RT} e^{\Delta^\ddagger S^\circ / R} \quad \text{Eyring Equation}$$

$\Delta^\ddagger S^\circ = \text{entropy of activation}$

$\Delta^\ddagger H^\circ = \text{enthalpy of activation}$

## Chemical kinetic

### Transition-state Theory

$$\ln k_2 = \ln \frac{k_B}{h} + \ln T - \frac{\Delta^\ddagger H^\circ}{RT} + \frac{\Delta^\ddagger S^\circ}{R}$$

$$\frac{d \ln k_2}{dT} = \frac{1}{T} + \frac{\Delta^\ddagger H^\circ}{RT^2} = \frac{\Delta^\ddagger H^\circ + RT}{RT^2}$$

According to Arrhenius equation  $k_2 = A e^{-E_a/RT}$

$$\frac{d \ln k_2}{dT} = \frac{E_a}{RT^2}$$

Comparing the above two equations  $E_a = \Delta^\ddagger H^\circ + RT$

If the enthalpy of activation is close to the activation energy :

$$A e^{-E_a/RT} = \left( \frac{k_B T}{h} \right) e^{-E_a/RT} e^{\Delta^\ddagger S^\circ/R} \quad A = \left( \frac{k_B T}{h} \right) e^{\Delta^\ddagger S^\circ/R}$$

## Chemical kinetic

### Mechanisms of reaction

A **reaction mechanism** is a sequence of elementary reactions (called “steps”) involved in the conversion of reactants to products.

For each elementary step:

$$\text{Rate} = k [A]^a[B]^b$$

Where **a** and **b** are the stoichiometric coefficients in the step.

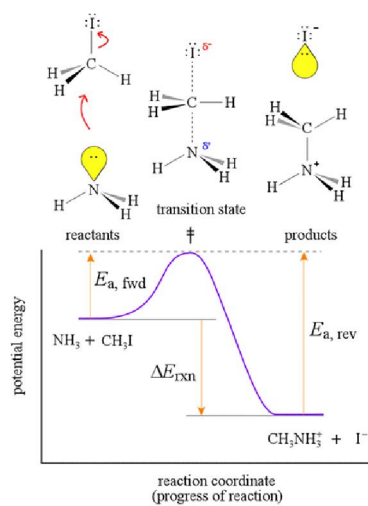
**a + b** = **MOLECULARITY** of the step.

**Rate determining step**: the **slowest step** in a chemical reaction determines the kinetics for the entire reaction. Steps that are **faster than the slow step** are “invisible.”

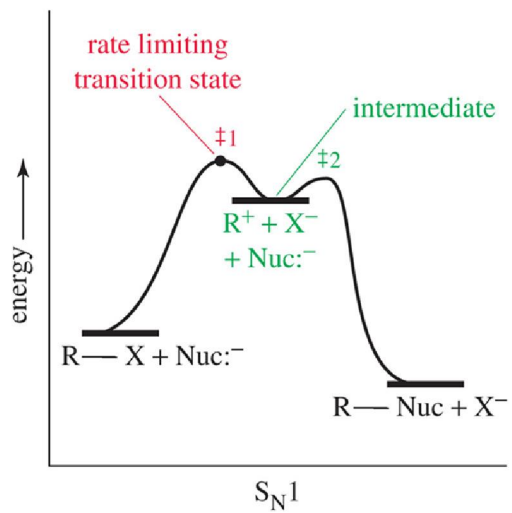
# Chemical kinetic

## Mechanisms of reaction

### 1 single step



### More than one step





## Chemical kinetic

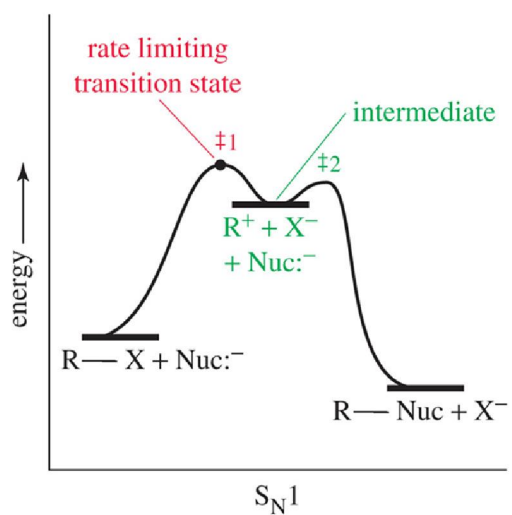
### Mechanisms of reaction

Reaction intermediates can be detected experimentally and sometimes isolated.

R.D.S. is the step with the higher  $E_a$ .

No more than two molecules are involved in each elementary step!!!

More than one step



## Chemical kinetic

### Mechanisms of reaction

We are going to analyze two types of reaction mechanisms:

- Reactions where the **first step** in the mechanism is the **slow step**.
- Reactions involving one (or more) **fast equilibrium steps**

### General procedure

- Start by **writing the rate law** for the **slow step**.
- Steps after the slow step will not be used in writing the rate law.
- **Substitute for intermediates** using other steps, if necessary.

## Chemical kinetic

### Analyzing Reaction Mechanisms with a Slow First Step

Overall reaction:



**Proposed mechanism:**



**Experimental rate law**       $r = k[\text{NO}_2]^2$

Could this mechanism be correct?

## Chemical kinetic

### Analyzing Reaction Mechanisms with a Slow First Step

Overall reaction:



**Proposed mechanism:**



Write the rate law for the slow step in the mechanism...

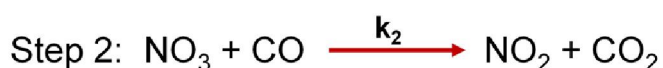
## Chemical kinetic

### Analyzing Reaction Mechanisms with a Slow First Step

Overall reaction:



**Proposed mechanism:**



Rate law derived from mechanism:  $\text{Rate} = k_1[\text{NO}_2][\text{NO}_2]$   
or....  $r = k_1[\text{NO}_2]^2$

Does it match the observed rate law?

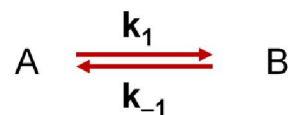
Yes! We're done. The mechanism may be correct.

## Chemical kinetic

### Analyzing Reaction Mechanisms with One (or More) Fast Equilibrium Step(s)

What is a **fast equilibrium step**?

For the reaction



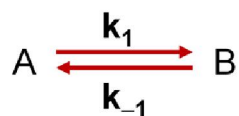
The forward reaction is  $A \xrightarrow{k_1} B$

The backward reaction is  $B \xrightarrow{k_{-1}} A$

## Chemical kinetic

### Analyzing Reaction Mechanisms with One (or More) Fast Equilibrium Step(s)

For the reaction



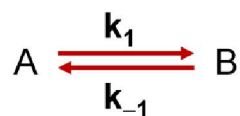
The rate law for the forward reaction is  $r = k_1[A]$

The rate law for the backward reaction is  $r = k_{-1}[B]$

## Chemical kinetic

### Analyzing Reaction Mechanisms with One (or More) Fast Equilibrium Step(s)

For the reaction



The forward reaction rate is equal to the backward rate at equilibrium, so set them equal to each other.

$$k_1[A] = k_{-1}[B]$$

$$\text{rate of fwd rxn} = \text{rate of back rxn}$$



## Chemical kinetic

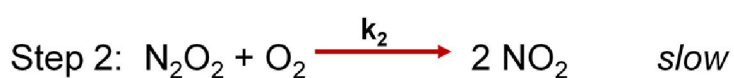
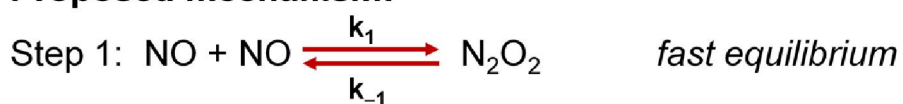
### Analyzing Reaction Mechanisms with One (or More) Fast Equilibrium Step(s)

Overall reaction:



**Question:**  
Could this mechanism  
be correct?

**Proposed mechanism:**

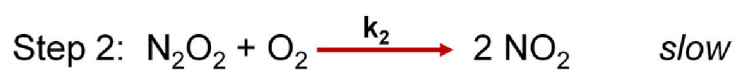
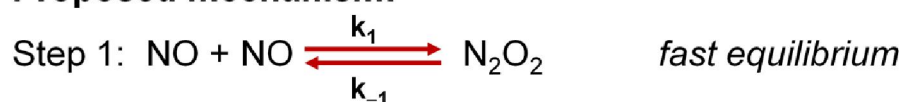


Observed rate law:  $r = k_{\text{obs}} [\text{NO}]^2 [\text{O}_2]$

## Chemical kinetic

### Analyzing Reaction Mechanisms with One (or More) Fast Equilibrium Step(s)

Proposed mechanism:



Write the rate law for the slow step:

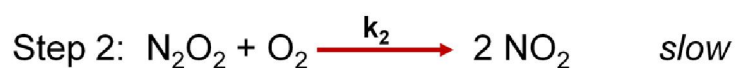
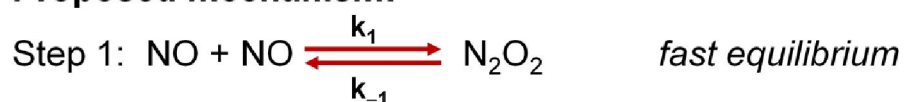
$$r = k_2 [\text{N}_2\text{O}_2][\text{O}_2]$$

There is an intermediate in the rate law... **not allowed!**

## Chemical kinetic

### Analyzing Reaction Mechanisms with One (or More) Fast Equilibrium Step(s)

Proposed mechanism:



Use the fast equilibrium step to substitute for the intermediate.

Write the forward rate equal to the backward rate:

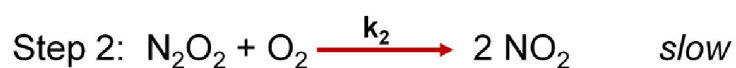
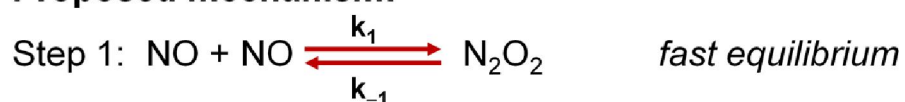
$$k_1[\text{NO}][\text{NO}] = k_{-1}[\text{N}_2\text{O}_2]$$

$$\text{rate of fwd rxn} = \text{rate of back rxn}$$

## Chemical kinetic

### Analyzing Reaction Mechanisms with One (or More) Fast Equilibrium Step(s)

Proposed mechanism:



Solve for the intermediate  $[\text{N}_2\text{O}_2]$  by dividing both sides by  $k_{-1}$

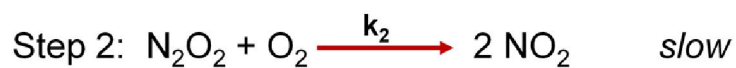
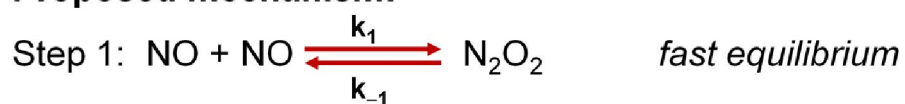
$$[\text{N}_2\text{O}_2] = \left( \frac{k_1 [\text{NO}]^2}{k_{-1}} \right)$$

Plug this quantity into the rate law for  $[\text{N}_2\text{O}_2]$

## Chemical kinetic

### Analyzing Reaction Mechanisms with One (or More) Fast Equilibrium Step(s)

Proposed mechanism:



Rate law for slow step:  $r = k_2 [\text{N}_2\text{O}_2][\text{O}_2]$

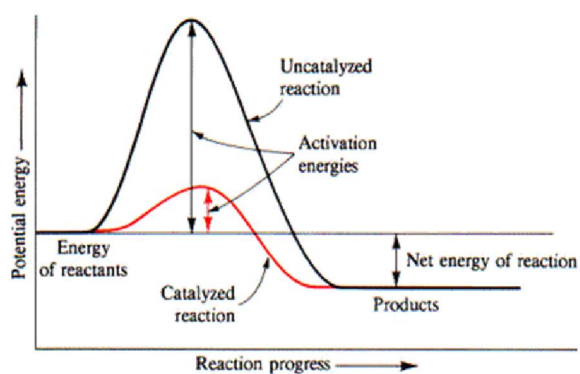
Substitute...  $r = \frac{k_2 k_1}{k_{-1}} [\text{NO}]^2 [\text{O}_2]$

Observed rate law:  $r = k_{\text{obs}} [\text{NO}]^2 [\text{O}_2]$

## Chemical kinetic

### Catalysis

A **catalyst** is a substance that modify the reaction mechanism, accelerating the reaction but without comparing in the chemical equation.



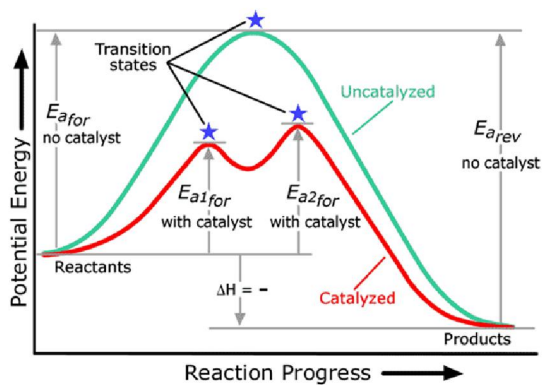
The presence of a catalyst opens a new reaction pathway, characterized by a lower  $E_a$ .

## Chemical kinetic

### Catalysis

Usually, several reactions steps are present with the formation of different intermediates.

The overall reaction rate is determined by the slowest step.



## **Chemical kinetic**

### **Type of catalysis**

#### **Homogeneous catalysis**

Catalyst and reactants are in the same phase (gaseous or liquid)

#### **Heterogeneous catalysis**

Catalyst and reactants are in different phase (gaseous/solid or liquid/solid)

#### **Enzymatic catalysis**

Catalyst is an enzyme (macromolecules made by amino acids)