Course of Geodynamics

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Course Outline:

- 1. Thermo-physical structure of the continental and oceanic crust
- 2. Thermo-physical structure of the continental lithosphere
- 3. Thermo-physical structure of the oceanic lithosphere and oceanic ridges
- **4. Strength and effective elastic thickness of the lithosphere**
- 5. Plate tectonics and boundary forces
- 6. Hot spots, plumes, and convection
- 7. Subduction zones systems
- 8. Orogens formation and evolution
- 9. Sedimentary basins formation and evolution

Stress:

- Force exerted per unit area of a surface (*Pa*). Any stress acting upon a surface can be expressed in terms of a normal stress perpendicular to the surface and two components of shear stress in the plane of the surface.
- The state of stress within a medium is specified by the magnitudes and directions of three *principal stresses* mutually orthogonal and termed σ₁, σ₂, and σ₃ (maximum, intermediate and minimum principal stresses) that act on three planes in the medium along which the shear stress is zero.
- Normal force per unit area on horizontal planes increases linearly with depth: the part due to the weight of the rock overburden is known as lithostatic pressure (or stress). If the normal surface forces are all equal and are equal to the weight of overburden, the rock is in a lithostatic state of stress.

- o In case of tectonic forces acting on a rock mass the normal forces are not equal and the total horizontal surface force has two ϵ omponents: a lithostatic term (ρ_c gh) and a tectonic contribution (deviatoric stress, $\varDelta\sigma_{\rm xx}$) $\sigma_{\rm ij}$ = ρ_c gh + $\sigma'_{\rm ij}$ with ρ_c density of the continents.
- o Normal stresses can be either *tensile* when they tend to pull on planes or *compressive* when they push on planes.
- o Horizontal deviatoric stresses may result from uplift producing excess potential energy.

The state of stress of a single point inside a rock (i.e. a unit cube) is given by nine numbers, all of which have the units of force per area:

$$
\sigma = \left(\begin{array}{ccc} \sigma_{11} & \sigma_{12} & \sigma_{13} \\ \sigma_{21} & \sigma_{22} & \sigma_{23} \\ \sigma_{31} & \sigma_{32} & \sigma_{33} \end{array}\right) = \left(\begin{array}{ccc} \sigma_{xx} & \sigma_{xy} & \sigma_{xz} \\ \sigma_{yx} & \sigma_{yy} & \sigma_{yz} \\ \sigma_{zx} & \sigma_{zy} & \sigma_{zz} \end{array}\right)
$$

The first index indicates the direction in which the stress component acts, while the second one indicates the normal to the plane on which this stress component acts.

The state of stress at a point may always be characterized by only three principal stresses:

$$
\sigma'=\left(\begin{array}{ccc}\sigma'_{xx}&0&0\\0&\sigma'_{yy}&0\\0&0&\sigma'_{zz}\end{array}\right)=\left(\begin{array}{ccc}\sigma_1&0&0\\0&\sigma_2&0\\0&0&\sigma_3\end{array}\right)
$$

- The new coordinate system was chosen so that the x' axis is parallel to the largest of the three principal stresses.
- The principal stresses are often oriented roughly parallel to the vertical and the horizontal directions, since the shear stresses at the earth's surface and base of the lithosphere are both negligible.

Normal stresses are always located on the main diagonal of the matrix, which is symmetric relative to the main diagonal:

$$
\begin{aligned}\n\sigma_{ij} &= \sigma_{ji} \\
\sigma_{xy} &= \sigma_{yx} \quad \sigma_{xz} = \sigma_{zx} \quad \sigma_{yz} = \sigma_{zy}\n\end{aligned}
$$

• The **mean stress** σ_m (or pressure) is given by the mean of the three principal stresses: $\sigma_m = P = \frac{\sigma'_{xx} + \sigma'_{yy} + \sigma'_{zz}}{3} = \frac{\sigma_1 + \sigma_2 + \sigma_3}{3}$

In the case of a *hydrostatic stress state* (which is the state of a fluid *at rest*) all shear stresses are zero and all normal stresses are equal to each other:

$$
\sigma_{xy} = \sigma_{yx} = \sigma_{xz} = \sigma_{zx} = \sigma_{yz} = \sigma_{zy} = 0
$$

$$
\sigma_{xx} = \sigma_{yy} = \sigma_{zz} = P
$$

- Pressure is an invariant: it does not change by changing the coordinate system.
- Pressure is often considered as corresponding to the hydrostatic condition everywhere and it is computed as a function of depth *y* and vertical density profile $\rho(y)$:

 P_0 = 0.1 MPa is pressure on the Earth's surface:

$$
P(y) = P_0 + g \int_0^y \rho(y) dy
$$

Deviatoric **stresses** (*σ' ij* or t) are deviations of stresses from the hydrostatic stress state (mean stress):

where δ_{ij} is the Kronecker delta: δ_{ij} = 1 when *i*=*j* and δ_{ij} = 0 when *i* ≠ *j*, *i* and *j* are coordinate indices (x, y, z)

The **deviatoric stress** is a tensor (τ) , which can be defined as the deviation of the stress tensor from pressure:

$$
\tau = \left(\begin{array}{ccc} \tau_{xx} & \tau_{xy} & \tau_{xz} \\ \tau_{yx} & \tau_{yy} & \tau_{yz} \\ \tau_{zx} & \tau_{zy} & \tau_{zz} \end{array} \right) = \left(\begin{array}{ccc} \sigma_{xx} - P & \sigma_{xy} & \sigma_{xz} \\ \sigma_{yx} & \sigma_{yy} - P & \sigma_{yz} \\ \sigma_{zx} & \sigma_{zy} & \sigma_{zz} - P \end{array} \right)
$$

For a coordinate system parallel to the principal stress directions:

$$
\tau' = \left(\begin{array}{ccc} \tau'_{xx} & 0 & 0 \\ 0 & \tau'_{yy} & 0 \\ 0 & 0 & \tau'_{zz} \end{array} \right) = \left(\begin{array}{ccc} \sigma_1 - \sigma_m & 0 & 0 \\ 0 & \sigma_2 - \sigma_m & 0 \\ 0 & 0 & \sigma_3 - \sigma_m \end{array} \right)
$$

• The sum of the normal deviatoric stresses is zero: $\sigma'_{xx} + \sigma'_{yy} + \sigma'_{zz} = 0$ since $\sigma_{xx} + \sigma_{yy} + \sigma_{zz} = 3P$

The value of the differential stress and the characteristics of deviatoric stress both influence the extent and type of distortion **experienced by a body.** • The **differential stress** is the magnitude of the difference between the largest and the smallest principal stresses: σ_d = σ_1 - σ_3

The total stress tensor is the sum of the isotropic stress tensor plus the deviatoric stress tensor:

$$
\left(\begin{array}{ccc}\sigma_{xx} & \sigma_{xy} & \sigma_{xz} \\ \sigma_{yx} & \sigma_{yy} & \sigma_{yz} \\ \sigma_{zx} & \sigma_{zy} & \sigma_{zz} \end{array}\right) = \left(\begin{array}{ccc} P & 0 & 0 \\ 0 & P & 0 \\ 0 & 0 & P \end{array}\right) + \left(\begin{array}{ccc} \sigma_{xx} - P & \sigma_{xy} & \sigma_{xz} \\ \sigma_{yx} & \sigma_{yy} - P & \sigma_{yz} \\ \sigma_{zx} & \sigma_{zy} & \sigma_{zz} - P \end{array}\right)
$$

The *second invariant* of the deviatoric stress tensor can be calculated as follows:

$$
\sigma_{\rm II}=\sqrt{\frac{1}{2}\sigma_{ij}^{\prime 2}}
$$

(the indices *ij* imply a *summation*)

 $\sigma_{II} = \sqrt{\frac{1}{2} \left(\sigma_{xx}^2 + \sigma_{yy}^2 + \sigma_{zz}^2 + \sigma_{xy}^2 + \sigma_{yx}^2 + \sigma_{xz}^2 + \sigma_{zx}^2 + \sigma_{yz}^2 + \sigma_{zy}^2 \right)}$ Since the stress tensor is symetric:

 $\sigma_{II} = \sqrt{\frac{1}{2} \left(\sigma_{xx}^{\prime 2} + \sigma_{yy}^{\prime 2} + \sigma_{zz}^{\prime 2} \right) + \sigma_{xy}^2 + \sigma_{xz}^2 + \sigma_{yz}^2}$

Strain

Strain (ϵ) is defined as any change in the size or shape of a material caused by the stress application and is usually expressed as ratios that describe changes in the configuration of a solid, such as the change in the length of a line divided by its original length (In case of simple axial and shear deformations):

where *i* and *j are coordinate indices* (*x*, *y*, *z*) and *x^j* and *xⁱ are spatial coordinates*

In 3D, we can define nine tensor components:

Three normal strain components: $\varepsilon_{xx} = \frac{1}{2} \left(\frac{\partial u_x}{\partial x} + \frac{\partial u_x}{\partial x} \right) = \frac{\partial u_x}{\partial x}$ Six shear strain components: $\varepsilon_{xy} = \varepsilon_{yx} = \frac{1}{2} \left(\frac{\partial u_x}{\partial y} + \frac{\partial u_y}{\partial x} \right)$ $\varepsilon_{yy} = \frac{1}{2} \left(\frac{\partial u_y}{\partial y} + \frac{\partial u_y}{\partial y} \right) = \frac{\partial u_y}{\partial y}$ $\varepsilon_{zz} = \frac{1}{2} \left(\frac{\partial u_z}{\partial z} + \frac{\partial u_z}{\partial z} \right) = \frac{\partial u_z}{\partial z}$

 $\varepsilon_{xz} = \varepsilon_{zx} = \frac{1}{2} \left(\frac{\partial u_x}{\partial z} + \frac{\partial u_z}{\partial x} \right)$ $\varepsilon_{yz} = \varepsilon_{zy} = \frac{1}{2} \left(\frac{\partial u_z}{\partial y} + \frac{\partial u_y}{\partial z} \right)$

Strain

Stress and strain tensors are very different physical quantities:

- **Stress characterizes the distribution of forces acting in a continuum at a given moment of time**
- Strain quantifies in an integrated way the entire *deformation history* of the continuum from the initial state, up until this given **moment.**

- Volume change or dilatation is the sum of the strain components $(\epsilon_{xx} + \epsilon_{yy} + \epsilon_{zz})$
- Volume elements may change their position without changing their shape (Displacement)
- Shear strain may distort the shape of an element of a solid (e.g., rectangle) and is determined by the angles through which the sides of the rectangle are rotated (ϕ_1 and ϕ_2).
- If $\phi_1 = \phi_2$ no solid body rotation occurs, deformation is the result only of shear strains (pure shear: uniform extension with depth).
- If $\phi_2 \neq \phi_1 = 0$ the body has undergone simple shear (asymmetrical extension)

Strain Rate

• In geodynamic modelling, it is convenient to use the *strain rate*, which **characterizes the dynamics of changes in the internal deformation** rather then the **strain** which **characterizes the total amount of deformation compared to the initial state**.

The strain rate tensor ϵ_{ij} is the time derivative of the strain tensor ϵ_{ij} : $\dot{\epsilon}_{ij} = \frac{1}{2} \left(\frac{\partial v_i}{\partial x_i} + \frac{\partial v_j}{\partial x_i} \right)$

In 3D we can define nine tensor components:

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\n
$$
\dot{\varepsilon}_{xx} = \frac{1}{2} \left(\frac{\partial v_x}{\partial x} + \frac{\partial v_x}{\partial x} \right) = \frac{\partial v_x}{\partial x}
$$
\n
$$
\dot{\varepsilon}_{xy} = \dot{\varepsilon}_{yx} = \frac{1}{2} \left(\frac{\partial v_x}{\partial y} + \frac{\partial v_y}{\partial x} \right)
$$
\n
$$
\dot{\varepsilon}_{yy} = \frac{1}{2} \left(\frac{\partial v_y}{\partial y} + \frac{\partial v_y}{\partial y} \right) = \frac{\partial v_y}{\partial y}
$$
\n
$$
\dot{\varepsilon}_{zz} = \frac{1}{2} \left(\frac{\partial v_z}{\partial z} + \frac{\partial v_z}{\partial z} \right) = \frac{\partial v_z}{\partial z}
$$
\n
$$
\dot{\varepsilon}_{yz} = \dot{\varepsilon}_{zy} = \frac{1}{2} \left(\frac{\partial v_y}{\partial z} + \frac{\partial v_z}{\partial y} \right)
$$

By analogy to the stress tensor, the strain rate tensor can also be subdivided to isotropic $\dot{\varepsilon}_{kk}$ (which is an invariant) and deviatoric components $\dot{\varepsilon}_{ii}$ $\Omega_{\rm{eff}}$ $\Omega_{\rm{eff}}$ $\Omega_{\rm{eff}}$

$$
\dot{\varepsilon}_{kk} = \dot{\varepsilon}_{xx} + \dot{\varepsilon}_{yy} + \dot{\varepsilon}_{zz} = \frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} + \frac{\partial v_z}{\partial z} = \text{div}(\bar{v}).
$$

$$
\dot{\varepsilon}'_{ij} = \dot{\varepsilon}_{ij} - \delta_{ij}\frac{1}{3}\dot{\varepsilon}_{kk},
$$

The second invariant of the deviatoric strain rate tensor is calculated as follows: $\dot{\epsilon}_{II} = \sqrt{\frac{1}{2} \dot{\epsilon}_{ij}^2}$.

Deformation Laws

When the stress applied to rocks cannot be compensated elastically permanent (brittle/plastic) deformation will occur (continuous, irreversible deformation without fracturing).

On geological time scales and lithospheric length scales deformation mechanisms can be described:

- Brittle deformation: It only describe a stress state and not a relationship between stress and strain.
- Plastic deformation: It states that a constant stress is required to deform the rock: irregardless how much or how fast we deform, the required force is all the same.
- Ductile deformation: It is a generic term, indicating that the deformation is not elastic and not brittle.
- Elastic deformation: It states that the *strain* of a rock is proportional to the applied *total stress* (it is the only deformation mechanism which is not permanent).
- Viscous deformation: It is the law that is most commonly used to describe ductile deformation on the crustal scale. Viscous means that the strain *rate* of a rock is proportional to the applied *deviatoric stress.*

Rocks' deformation

- Beyond the elastic limit (depending on *T* and *P*), rocks deform by either brittle fracturing or by ductile flow. The *yield stress* (or yield strength) is the value of the differential stress above the elastic limit at which deformation becomes permanent.
- Rock rheology in the short term (seconds or days) is different from that of the same material stressed over durations of months or years. Lithosphere behaves as strong material over geological time (> 10⁶) and thus it is able to bend under surface loads, store elastic stresses responsable for seismicity, and trasmit stresses over large horizontal distances.

Relationship between stress σ and strain rate ϵ for elastic and ductile deformation

When the stress applied to rocks cannot be compensated elastically permanent (brittle/plastic) deformation will occur (continuous, irreversible deformation without fracturing).

- In the viscous regime, only deviatoric stresses cause deformation
- Elastic deformation occurs in response to the total stress state: Considering only uniaxial loading:

$$
\sigma_{xx}=E\epsilon_{xx}
$$

E=Young's Modulus

- Rocks deform by creating new cracks or by friction along pre-existing cracks.
- Brittle failure is described with Mohr-Coulomb criterion, representing the critical state at which failure occurs.
- Failure occurs when the shear stress on a given plane reaches a critical value τ_c ($\sigma^c{}_{\rm s}$) that is a function of the normal stress acting on that plane σ_n : $\tau_c = \sigma_0$ + $\mu\sigma_n$ (Byerlee's law), where σ_0 is the cohesion (the resistance of the material to shear fracture on a plane of zero normal stress) and μ (tan(ϕ)) is the friction coefficient.

The brittle failure of a rock occurs when: $\sigma_s^c = \sin 2\theta (\sigma_1 - \sigma_3)/2$.

- The shear stress (σ_S^{max}) is the largest on planes that lie at an angle of 45° to the principal stress direction.
- The maximum shear stress (σ_S^{max}) a rock can support is half as large as the applied differential stress:

$$
\sigma_{\rm s}^{\rm max} = \frac{\sigma_1-\sigma_3}{2}
$$

- o tan $\phi = \mu$, ϕ *is the angle* between the considered plane and the directions of the principal stresses.
- \circ ϕ is about 30°-40°, equivalent to an internal coefficient of friction between 0.6-0.8.

- Brittle fracture is likely caused by progressive failure along a network of micro- and meso-scale cracks and occurs where the local stress maxima exceed the strength of the rock
- The crack orientations relative to the applied stress determine the location and magnitude of local stress maxima.
- When the magnitude of the tensile stress exceeds the tensile strength of the material, cracks orthogonal to this stress fail first and an extension fracture occurs.
- Cracks close under compression (probably at depths of >5 km) due to increasing overburden pressure, which implies that the compressive strength of a material is much greater than the tensile strength. Where all cracks are closed, fracturing depends upon the inherent strength of the material and the magnitude of the differential stress.
- Faults preferentially form at angles of <45° on either side of the maximum principal compressive stress when a critical shear stress on the planes is exceeded.
- This critical shear stress (τ_c) depends upon the normal stress (σ_n) on planes of potential failure and the coefficient of internal friction (μ) on those planes (0.6-0.8 for the rocks), which resists relative motion across them:

Mohr-Coulomb criterion: $\tau_c = \sigma_0 + \mu \sigma_n$

If fluid pressure plays a role, Mohr-Coulomb criterion is formulated as:

 $\tau_c = \sigma_0 + \mu(\sigma_n - P_f)$, where P_f is the pore fluid pressure, then $\tau_c = \sigma_0 + \mu\sigma_n(1-\lambda)$, where $\lambda = P_f/\sigma_L$ (if $\sigma_n \sim \sigma_L$) is the ratio of pore fluid pressure to lithostatic stress (σ_l) . If $\lambda = 1$, $\sigma_c = \sigma_0$. λ =0, 'dry' conditions. λ =0.7 wet conditions. λ =0.37 intermidiate conditions (when the stress state is hydrostatic). If preexisting cracks occur in a rock the remaining cohesion is negligeble compared to the cohesion of an intact rock (Amonton's law): $\tau_c = \mu \sigma_n$ At pressure below 200 MPa, the crust may be charcterized by an internal coefficient of friction around: 0.85, then: $\tau_c = 0.85\sigma_{\rm n}$ and $\tau_c = 0.85\sigma_{\rm n}$ (1- λ) Rocks at a depth between 5 km – 15 km will fail at roughly 100 – 300 MPa

- Pore fluid pressure enhances fracturing by reducing the frictional coefficient and counteracting the normal stresses (σ_n) across the fault.
- The effect of pore fluid pressure explains faulting at depth, which would otherwise appear to require very high shear stresses because of the high normal stresses.

Under compressional closed crack regime, the type of faulting which results depends upon which of the principal stresses is vertical: normal, strike-slip, and thrust faults occur depending on whether σ_1 , σ_2 or σ_3 is vertical.

Anderson's Theory

(in terms of differential stress and lithostatic stress)

 $\sigma_{\sf n}$ and $\sigma_{\sf s}$ are related to the maximum and minimum principal stresses: $\sigma_{\sf n}$ = $\sigma_{\sf 1}$ cos² $\theta_{\sf s}$ + $\sigma_{\sf 3}$ sin² $\theta_{\sf s}$

 σ_3 =minimum principal stress

Near to the surface, at low temperatures, rocks deform in a brittle manner following an elasto-plastic rheology:

Presence of fluids decreases brittle strength by a factor of 5

Before breaking, they follow a linear relation between stress and strain

The activation of broken bodies follows Byerlee's law

The strength of a non-fractured and of a fractured body depend only on the confining pressure (=depth). It does not depend on:

- temperature
- lithology (very weakly dependence through density)
- strain rate

Byerlee's law

Rheological parameters for the brittle deformation

Rheology and strength of the lithosphere

Byerlee's law differs for tension and compression as a result of corresponding differences in brittle deformation (fault development)

Rocks Ductile Deformation

mylonites

Soft (viscous) bands go through the entire rock and reflect huge deformations

Viscous deformation

- Plastic deformation describes the stress state at which rocks start to flow but not the amount of stress that occurs.
- **Ductile deformation is related to the ability of materials to change form irreversibly, without fracturing.**
- **Viscous behaviour applies when the deformationalstress is a function of strain rate.**

Viscous deformation of ideal fluids is described by a proportionality between deviatoric stress (t**) and strain rate**

 $\tau = 2\eta\dot{\epsilon}$ where η is the dynamic viscosity

A fluid that behaves according to a linear relationship is called *Newtonian fluid* (the larger the deviatoric stress that is applied, the faster the rock will deform) The factor two derives from definition used in fluidodynamics: $\dot{\gamma} = 2\dot{\epsilon}$

Viscosity is strongly temperature dependent (*Arrhenius relationship*)

 $A₀$ = pre-exponenet costant $\eta = A_0 e^{Q/RT}$ Q=Activation energy (Jmol⁻¹) R=universal gas costant (8.314472 J mol⁻¹ K⁻¹) *T*=absolute temperature

Viscosity trends toward infinity for *T*=0 and and decreases exponentially to asymtotically approach the value A₀ at high temperatures

Rocks rarely defom as a Newtonian fluid, usually there is not a linear relationship between τ and η

 $\tau^n = A_{\text{eff}}\tilde{\epsilon}$ $n=$ A_{eff} $\dot{\epsilon}$ with *n* power law exponent (between 2 and 4 for most of rocks) and A_{eff} is a material costant (Paⁿ s)

Viscous deformation (Diffusion creep)

- Ductile deformation is extremely rock-type dependent: Even small variations of mineral composition may result in quite different ductile properties.
- Solid-state creep (the ability of crystalline substances to deform irreversibly under applied stresses) is the major deformation mechanism of the Earth's crust and mantle.
- There are two major mechanisms of ductile deformation: **diffusion creep** and **dislocation creep** (different types: dislocation climb, glide, screw, edge, etc.).
- Diffusion creep results from the diffusion of atoms through the interior and along the boundaries of crystalline grains subjected to **stresses and is dominant at T >> 1330 °C at relatively low stress.**

Diffusion creep is characterised by a linear (*Newtonian*) relationship between the strain rate ε and an applied shear stress $\sigma_{\!s}$:

$$
\dot{\epsilon} = A_{\text{diff}} \sigma_{s}
$$

where A_{diff} is a proportionality coefficient which depends on grain size, *P-T* conditions, oxygen and water fugacity.

Diffusion creep (as dislocation creep) is often calibrated from experimental data using a simple parameterized relationship (also called *flow law*) between the applied *differential stress Δσ* (the difference between maximal and minimal applied stress) and the resulting *ordinary strain rate*:

$$
\dot{\varepsilon}^d = A a^{-m} \Delta \sigma^n \exp(-H (RT)^{-1})
$$

ε^d is the shear strain rate, *α* is a grain size, *m* is a diffusion constant, *A* is a material constant, *n* is power law constant, *A*σ=σ₁-σ₃, *R* is Boltzmann's gas constant, *H* is creep activation enthalpy (*H*=*Q*+*PV*, where *Q* is activation energy, *P* is pressure, and *V* is activation volume), and *T* is absolute temperature.

Viscous deformation

(Dislocation creep and Dorn Law)

- Dislocation creep results from migration of dislocations (imperfections in the crystalline lattice structure) and is dominant at higher **stresses (< 200 MPa) and low temperature (T> 300 °C <1330 °C) .**
- Dislocation density strongly depends on stresses and results in a non-linear (non-Newtonian) relationship between the strain rate and **deviatoric stress:**

$$
\dot{\boldsymbol{\xi}} = A_{disl} \; \boldsymbol{\tau}^n
$$

where A_{disc} is a proportionality coefficient which is independent on grain size, but depends on P-T conditions, oxygen and water fugacity, and $n=2-4$ is the stress exponent.

Parameterized relationship between the applied *differential stress* ^D*σ* (the difference between maximal and minimal applied stress) and the resulting *ordinary strain rate* for dislocation creep gives:

$$
\dot{\varepsilon}^d = A \Delta \sigma^n \exp(-H (RT)^{-1})
$$

At moderate-temperature–high-stress conditions, *m*=0 and *n*=2-4 (Non Newtonian Fluid)

The **Peierls mechanism or Dorn Law** is a temperature-dependent mode of plastic deformation (also called *exponential creep*) which takes over from the dislocation creep mechanism at elevated stresses (> 200 MPa):

$$
\sigma_{DL}=\sigma_D(1-[-\frac{RT}{E_D}ln(\frac{\dot{\varepsilon}}{A_D})]^{\frac{1}{2}})^2 \qquad \qquad \text{Demoughy et al., 2013, PEPI, 220}
$$

 σ is the Peierls stress that limits the strength of the material, A_D is a material constant for the Peierls creep (Pa⁻²s⁻¹), E_D is the activation energy (J mol⁻¹).

o Stress during viscous deformation depends on temperature, strain rate, and material costants, but not on confining pressure.

Viscous deformation (Effective Viscosity)

In rocks and mineral aggregates, both dislocation and diffusion creep can occur simultaneously under applied stress, which can be expressed in the following relation for the effective viscosity:

$$
\dot{\varepsilon}_{ij} = \dot{\varepsilon}_{ij(disl)} + \dot{\varepsilon}_{ij(diff)} \qquad \dot{\varepsilon}_{ij} = \frac{\sigma'_{ij}}{2\eta_{\text{eff}}}, \ \dot{\varepsilon}_{ij(disl)} = \frac{\sigma'_{ij}}{2\eta_{\text{dist}}}, \ \dot{\varepsilon}_{ij(diff)} = \frac{\sigma'_{ij}}{2\eta_{\text{diff}}}
$$

In order to use the experimentally parameterized equations in numerical modelling, one needs to reformulate it in terms of an **effective viscosity** (η_{eff}), written as a function of the second invariant of either the deviatoric stress ($\sigma_{\rm II}$), or strain rate ($\epsilon_{\rm II}$).

$$
\sigma_{\text{II}} = 2\eta_{\text{ eff}} \dot{\varepsilon}_{\text{II}}, \qquad \eta_{\text{eff}} = \frac{\sigma_{\text{II}}}{2\dot{\varepsilon}_{\text{II}}}, \qquad \eta_{\text{eff}} = \frac{\tau_s}{\dot{\varepsilon}} = A_{\text{eff}}^{1/n} \times \varepsilon^{(1/n)-1}
$$

The reformulation should also take into account the type of performed rheological experiments in order to establish the proper relations between σ_{II} and σ_{d} , as well as between and $\left|\varepsilon_{d}\right|$ and $\left|\varepsilon_{i}\right|$

 $\epsilon_d = 2\dot{\epsilon}_H$

 \bigcap

In case of an axial compression experiment:
$$
\sigma_d = \sqrt{3}\sigma_H
$$
 $\mathcal{E}_d = \frac{2}{\sqrt{3}}\dot{\varepsilon}_H$

 $\sigma_{\rm d}=2\sigma_{\rm H}$.

In case of simple shear experiments:

Viscous deformation

(Diffusion creep and Dislocation creep)

Typical example of experimental data on ductile flow in rocks (olivine aggregates, power, and Dorn flow laws for different temperature–stress domains)

 μ = predicted viscosity values, for 100 MPa stress level.

• The typical strain rates used in experiments (10⁻⁶10⁻⁴ s⁻¹) are 10 orders of magnitude higher than those in nature (10⁻¹⁴10⁻¹⁷ s⁻¹), which poses a serious question on the possibility of extrapolation.

Strength of the Lithosphere

rheology

Strength of the Lithosphere (Yield Strength Envelopes)

Strength describes the critical value which the differential stress must reach to cause permanent deformation

- **The strength profile describes the rheology of the continental lithosphere.**
- It is composed of straight lines for brittle frature (increases with depth because of pressure) and curved lines for viscous **deformation (decreases with depth because of the increase of temperature).**
- **A rock at a given depth will deform according to the deformation mechanism that requires less stress.**

Diffusion creep at T >> 1330 °C

 $\dot{\varepsilon}^d = A a^{-m} \Delta \sigma^n \exp(-H (RT)^{-1})$

Power Law for stress < 200 MPa

 $\dot{\mathcal{E}} = \sigma^n_{\mathit{ductile}} A \exp(-Q \, / \, RT)$ $= \sigma_{\text{ductile}}^{\text{v}} A \exp(-Q/KI)$

Dorn Law for stress > 200 MPa

$$
\sigma_{DL}=\sigma_D(1-[-\frac{RT}{E_D}ln(\frac{\dot{\varepsilon}}{A_D})]^{\frac{1}{2}})^2
$$

Creep parameters

Commonly inferred parameters for diffusion creep, $n = 1$ Table 1

Karato S (1986) Does partial metting reduce the creep strength of the upper mantle? Nature 319: 309-310.

Table 2 Commonly inferred parameters of dislocation creep

Rheology of the Lithosphere including elasticity

Elastic deformation is istantaneous and may be used to infer a stress state.

- In a downward bent elastic lithosphere there is a stress neutral layer in the middle of the lithosphere (above the lithosphere is in compression and below in extension).
- In the central part of the lithosphere elastic stress can support internal loads, since it is smaller of brittle and viscous stresses.

Rheology of the Lithosphere

Dependency of viscous deformation on temperature, strain rates, and regime of deformation

Characteristic geometry of strength profiles:

- Oceanic geotherms are time dependent and there is no radiogenic heat production in the oceanic lithosphere.
- The rheology of oceanic lithosphere is therefore largely governed by the rheology of olivine (only one maximum in the strength profile).
- Continental lithosphere is very heterogeneous in terms of thickness and composition and thus its strength profile has a variable number of maxima.

Oceanic lithosphere Continental lithosphere

YSEs crustal thickness dependency

YSEs rheology dependency YSEs strain rates dependency

Influence of compositional variation, plate thickness (100 or 200 km), and fluid content on continental YSE

Upper Crust: Q_{bc} dry quartzite, Qtz wet quartzite, G_{ct} is wet granite Q_r is for extra strong dry quartz; CD, dry Columbia diabase; MD, dry Maryland diabase; WC, Pikwitonei granulate; ST and C, diabase, $O|_{div}$ and $O|_{wet}$, dry and wet dunite;

Temperature and Deformation of Continental Lithosphere

There is a strong correlation between regions high crustal temperature and regions of high deformation rate in terms of high seismic hazard.

Global Strain Rate Moodel from Geodetic Velocities

White areas were assumed to be rigid plates and no strain rates is calculated there

Integrated Strength of the Lithosphere

- To consider the defomation of the entire continental plates we need to estimate the mean stresses averaged over the entire lithosphere or vertically integrated strength, F_1 (Pa m or N m⁻¹).
- F_l is the the force acting in the direction normal to the plate per meter length of plate that is required to deform a plate for a given strain rate.

Construction of 3D rheological strength models of the continental lithosphere

Integrated Strength of the Lithosphere, (Dependency on Crustal Thickness, and Differentiation Index)

- Crustal differentiation effectively lowers the temperature at the base of the crust, allowing stabilization of a thicker crust.
- The effect of temperature on thermal conductivity results in higher Moho temperature than in calculations with uniform conductivity.

Low Integrated Strength < 1x10¹³ N m-1 (Pa m) High Integrated Strength > 1x10¹³ N m-1 (Pa m)

Enriched Crustal Thickness of *HPE*, D=15 km

Mareschal and Jaupart, 2013, Tectonophysics 609

Integrated Strength of the Oceanic Lithosphere

 -16

80

80

100

60

60

100

- Integrated strength of oceanic lithosphere increases with age and is higher than for continental lithosphere.
- An oceanic plate is a passive transmitter of stresses from the mid-oceani ridge to the continents.
- Strain rate with which oceanic lithsophere would deform under its own ridge push against age of oceanic lithosphere shows that ε is negligeble.

Strain Rates variations

(Total integrated strength fixed to \sim 3x10¹² N m⁻¹)

- **a) Meso-Cenozoic Rifts**: Most of the total tectonic force is located in the strong brittle crust. Little force is required to cause deformation at a relatively high strain rate $(10^{16}$ -1), because of the high lithospheric temperatures.
- **b) Archean Cratons**: Lower crust and upper mantle are considerably stronger and the total force available is sufficient to only deform the lithosphere at a negligible strain rate (10²⁹ s⁻¹).

Differential stress is estimated, so that the integrated strength does not exceed the assumed total force/length available to deform the lithosphere (3x10¹²Nm⁻¹).

World Strength Maps

Integrated lithospheric strength (Pa m) Percentage of crustal strength (%)

'Soft' rheology (UC=Dry Quartzite; LC=Wet Diorite)

'Soft' rheology (UC=Dry Quartzite; LC=Wet Diorite)

Tesauro et al., 2013, Tectonophysics, 602

North America Thermal and Rheological model of the Lithosphere

Tesauro et al., 2015, G3

8 Granite - Mafic Granulite

-50

9 Quartzite - Diorite

10 - Diabase -

North America Strength model of the Lithosphere

Tesauro et al., 2015, G3

Pa

North America Strength model of the Lithosphere (strain rates influence)

Evolution in time of rheological strength models

Rheological strength evolution during crustal thinning

Uncertainties on strength and integrated strength estimates

1) Uncertainties of rocks mechanics data:

- In the lab experiments refer to uniaxial deformation, but rocks deform in several planes.
- Experimental stain rates $(10^{-8}-10^{-4} s^{-1})$ are ten times faster than geological strain rates $(10^{-18}-10^{-14} s^{-1})$.
- Experiments refer to simple monophase minerals or representative rocks (small samples and homogeneous structure).
- Water content influences rock strength ('dry' and 'wet' are generic terms).
- Volatile fugacities and chemical reactions modify the mechanical behaviour of rocks.
- Temperature-pressure (P-T) conditions in the lab are not the same occuring in natural conditions.

2) Uncertainties of the Synthetic Yield Strength Envelopes

• Uncertainties of values of temperature and strain rate

3) Uncertainties on deformation mechanisms in nature

• Elastic, brittle, ductile deformation can occur simultaneously

4) Other factors (frictional heating, pressure, fluid content)

- Frictional heating may decrease ductile strength, cause metamorphic changes, or change fluid content
- Few data on the rheology of the metamorphic rocks.

Flexural Rigidity

Development of thick ice sheet: lithosphere is subjected to additional weight

Isostatic response: flexural bending

Melting of ice sheet: isostatic response is uplift now

Recovery towards starting situation

- Bending of the lithosphere can occur as result of the growth of major ice masses, magmatic and topographic growth of oceanic seamount chains, load of major river deltas.
- Amplitude and wavelength of the deflection depend on the material properties and effective elastic thickness of the plate.

What relations do you have with your neighbours?

None: local compensation

- **Vertical movements are confined to the area where load changes take place**
- **Nothing happens in the surroundings**

A lot contacts: regional compensation

- **the width of the area affected increases**
- **the amplitudes decrease**

In the extreme case of a lithosphere with infinite strength

- **No subsidence**
- **All changes in mass translate in topography**

Lithospheric strength (changing in space and time) controls the reaction to changing loads

Flexural isostasy is a stress balance that considers horizontal elastic stress

- Elastic Deformation of Oceanic Lithosphere: seamount, bending of subducting plate.
- Elastic Deformation of Continental Lithosphere: passive continental margin, molasse basin (weight of the mountain belt is partly compensated by an internal loads).

When integrating the horizontal normal stresses σ_{xx} , over the thickness of the elastic plate *h*, the bending moment *M* is proportional to the curvature of the plate:
 $M = \int_{-h/2}^{h/2} \sigma_{xx} z dz \longrightarrow M = -D \frac{d^2 w}{dx^2}$ proportional to the curvature of the plate:

coupled with a force balance equation that relates bending moments, the vertical load *q,* any applied horizontal forces *F* and the shear forces, we obtain the general flexural equation:

 q_x =a series of internal and external loads acting upwards and downwards onto a plate (stress)

 $M = -D\frac{\mathrm{d}^2 w}{\mathrm{d} x^2}$

A downward force per unit area *q*(*x*) is exerted on the plate by the applied load, and on the end sections there is a net shear force per unit length *V* and horizontal force *F* per unit length, which is independent of *x.*

q(x)=qext-qint=^r*cgH(x)-(*^r*m-*^r*^c)gw* The downward force exerted by the mountain range on the plate is given by the vertical normal stress (the *external* or *positive* load) q_{ext} = ρ_c gH. The buoyancy force (the internal or negative load) has the magnitude q_{int} = ($\rho_m-\rho_c$)gw, where w is the deflection of the plate. The net load that is applied to the plate is:

In oceanic lithosphere (narrow island chains on large oceanic plates):

- 1. We assume that there are no horizontal forces applied to the plate
- 2. We assume that the vertical load ($V₀$ or q_a) is only applied at a single location (there is no dependence of the load on *x*)*.*

Assuming that the downwards deflected region is filled with water:

$$
q = q_{\rm a} - (\rho_{\rm m} - \rho_{\rm w})gw
$$
 The flexural equation becomes:
$$
D\frac{d^4w}{dx^4} = -(\rho_{\rm m} - \rho_{\rm w})gw
$$

After integration, the constants *D*, *g*, $\rho_{\rm m}$ and $\rho_{\rm w}$ often occur in the following relationship: $\alpha = \left(\frac{4D}{g(\rho_{\rm m} - \rho_{\rm w})}\right)^{1/4}$ α =flexure parameter

For appropriately formulated boundary and initial conditions (e.g. the load applies only at *x =* 0, symmetry of the deflection, so that $dw/dx=0$ at $x=0$)

 $w = w_0 e^{-x/\alpha} (\cos(x/\alpha) + \sin(x/\alpha))$ We solve the previous equation:

 w_0 = maximum deflection of the plate directly underneath the load $w \rightarrow w_0$ for $x \rightarrow 0$

Subducting oceanic plate :

The loading of the subducting oceanic plate may be viewed as a line-loading by the margin of the upper plate. Boundary conditions must be assumed that describe a broken half plate which is subjected to a load at its end. For appropriately formulated boundary conditions the flexural equation can be solved:

 $w = w_0 e^{-x/\alpha} (\cos(x/\alpha))$

Shape of elastically bent plates

- Lithosphere responds to surface and subsurface loads by bending, characterized by vertical deflection, *w(x)*, and local radius of curvature, $R_{xy}(x)$ or curvature $K(x) = -R_{xy}^{-1} = \partial^2 w / \partial x^2$
- The amplitude and wavelength, λ , of bending depend on the flexural rigidity D or equivalent elastic thickness Te: $D = ET^3/12(1-\nu^2)$

where $E =$ Young's Modulus and $v =$ Poisson Coefficient

• *Te* is the geometric measure of the flexural rigidity of the lithosphere, which describes the resistance to bending under the application of vertical loads (it is a measure of the integrated bending stress).

Te **of oceanic lithosphere**

- Flexural strain in a bending plate increases with distance from the neutral plane.
- The uppermost and lowermost parts of the plate are subject to higher strains and may experience brittle or ductile deformation as soon as the strain cannot be supported elastically.
- *Te* approximately equals the size of the 'elastic core' plus half size of the underlying brittle zone and half size of the ductile zone beneath.
- *Ts* (seismogenic thickness) corresponds to the depth of the intersection of the moment curvature curve (red dashed lines) with the brittle deformation field, but could extend from the surface, *Ts* (min), to the brittle–ductile transition (BDT), *Ts* (max).
- *Te* could extend from the thickness of the elastic core, *Te* (min), to the thickness of the entire elastic plate, *Te* (max).
- Both *Ts* and *Te* depend on the moment generated by the load and, hence, the plate curvature. Yet, *Ts* increases with curvature while *Te* decreases.

Te **of oceanic lithosphere**

Correlation between the observed flexural strength *Te* **and age-***T* **of the oceanic lithosphere**

YSE and *Te* **of the oceanic lithosphere as function of age and** *T*

• A load emplaced on the lithosphere will be supported partly by the strength of the elastic core and partly by the brittle and ductile strength of the plate.

- *Te* is between 2-40 km (correlates with the isotherm 400-500 °C) and depends on load and plate age.
- *Ts* and *Te* seem to correlate, but Ts << Te.

Seismogenic Thickness (*Ts***) vs Effective Elastic Thickness (***Te***)**

- Extensional earthquakes are shallower since extensional failure requires nearly two times smaller stress: earthquake depths are controlled by intraplate stress levels and decrease with increasing integrated strength of the lithosphere (*B*) if *B*>*F* (tectonic force), since plate remains integer.
- Flexural stress may increase the value of *T*s by a factor of 2–3, but at the same time it would decrease *T*e by the same factor.
- Strong mechanical core associated with *T*e is centered at the neutral plane of the plate, *Zⁿ* , while *T*s is shifted to the surface.
- The upper crustal layers should fail easier than the lower mantle layers: At 50 km depth (the maximal depth of distributed seismicity), brittle rock strength is 2 GPa. Assuming 100 km thick lithosphere, one needs a horizontal tectonic force of 10^{14} Nm to reach this strength.
- For an elastic plate or brittle–elasto–ductile plate, *Zⁿ* is located roughly in its middle, at a depth $Z \sim 1/2$ *Te(max)*. In this case $Ts < 1/2Te$.
- Regions where earthquakes extend to great depths (>40 km), such as in subduction–collision zones, are related to metastable mechanisms weakly related to rock strength.

The equivalent elastic thickness *T*e of a plate with arbitrary rheology is given by:

where
$$
G = 12(1 - v^2)E^{-1}
$$

$$
M = -D\frac{\partial^2 w}{\partial x^2} = -E\frac{T_e^3}{12(1 - v^2)}\frac{\partial^2 w}{\partial x^2} \qquad T_e = \sqrt[3]{-M\frac{12(1 - v^2)}{E}}\left(\frac{\partial^2 w}{\partial x^2}\right)^{-1} = \sqrt[3]{MK^{-1}G}
$$

Te(YSE) reflects the integrated effect of all competent layers that are involved in the support of a load (including the weak ones). For a single-layer plate composed of *n* mechanically coupled rheological layers of thickness *hⁱ* : Te = nh if $h_1 = h_2 = h_3 ...$

In a lithosphere composed of *n* mechanically decoupled layers (multilayer plates) there are several 'elastic' core inside the bending plate, Te reflects the combined strength of all the brittle, elastic, and ductile layers. Then, Te is not simply a sum of the thickness of these layers:

$$
T_e(\text{YSE}) \sim (b_1^3 + b_2^3 + b_3^3 + \cdots)^{1/3} = \left(\sum_{l=1}^n b_l^3\right)
$$

Te= $n^{1/3}$ h, if h₁=h₂=h₃... Then, *Te* is reduced by a factor of $n^{2/3}$ = 40-50% for *n*<4.

The base of the mechanical competent layer in the continental mantle lithosphere, h_{m} , is referred to as isotherm of 700–750°C, below which the yielding stress is less than $10-20$ MPa (for a strain rate = 10^{-15} s⁻¹).

- \Box For 'typical' continental lithosphere the weak ductile zones in the lower crust do not allow flexural stresses to be transferred between the strong brittle, elastic, or ductile layers of the 'jelly sandwich'.
- \Box As result, there are several 'elastic' cores inside the bending plate. In such a multilayer plate stress levels (and thus *Te*) are reduced, for the same amount of flexure, compared to a single plate.
- \Box If the continental lithosphere is subject to large loads, it flexes, and the curvature of the deformed plate, *K*, increases. *T*e(YSE) is a function of *K* and is given by: $T_e(YSE) = T_e$ (elastic) $C(K, t, b_{c1}, b_{c2}, \dots)$

where *C* is a function of the curvature *K*, the thermal age *t*, and the rheological structure

Relationships between rheological structure, age, and Moho depth

Dependence of continental *Te* **on age and curvature of the lithosphere**

Te *vs* **age and temperature of continental lithosphere**

MSL=base of the mechanically strong lithosphere

E.A, Eastern Alps;W.A.,Western Alps; AD, Andes (Sub Andean); AN, Apennines; AP, Appalachians; CR, Carpathians; CS, Caucuses; DZ, Dzungarian Basin; HM, Himalaya; GA, Ganges; KA, Kazakh shield (North Tien Shan); KU, Kunlun (South Tarim); NB, North Baikal; TA, Central and North Tarim; PA, Pamir; TR, Transverse Ranges; UR, Urals; VE, Verkhoyansk; ZA, Zagros. Post-glacial rebound zones: L.A., lake Algonquin; FE, Fennoscandia; L.AZ, lake Agassiz; L.BO, lake Bonneville; L.HL, lake Hamilton.

- Crème brûlée model: strength prevalently concentrated in the crust
- Jelly Sandwich model: strength distributed in both crust and upper mantle
- In the crème brûlée model, the strength is confined to the uppermost brittle layer of the crust and compensation is achieved mainly by flow in the weak upper mantle.
- In the jelly-sandwich model, the mantle is strong and the compensation for surface loads occurs mainly in the underlying asthenosphere.

Plate curvature, Te, and Ts Strength vs Effective Elastic Thickness (*Te***)**

For curvatures up to 10-6 m-1 *T*e is always larger than *T*s.

- *Ts* reflects the thickness of the uppermost weak brittle layers that respond on historical timescales to stresses by faulting and earthquakes.
- *Te reflects the integrated strength of the entire lithosphere that responds to long-term (~ Myr) geological loads by flexure.*
- The onset of brittle failure in the mantle does not occur until the amount of flexure and thus the curvature is very large (>10 6 m $^{-1}$).

Plate curvature, Te, and Ts Strength vs Effective Elastic Thickness (*Te***)**

- In regions of **low curvature** the mantle is largely involved in the support of long-term flexural-type loads.
- In regions of **high curvature** the mantle may be seismic, but the support of long-term loads is confined to the crust.
- High *T*e values limit the amount of curvature due to flexure and the ratio of *Te* to *Ts* increases with thermal age (and strength).
- In the de-coupled case, *T*s does not exceed 15km, while in the coupled case the values of *T*s may grow, but as *T*e increases the curvature decreases.
- Oceanic lithosphere is associated with the highest values of *T*s, since the crust is thin (7 km), then always coupled with mantle lithosphere.
- Upper mantle can be weak at geological timescale (crème brûlée model) but not at seismic timescale: ductile creep cannot be activated at seismic timescale (for strain rate: 10^{1} - 10^{4} s^{-1} we need stress > 1GPa).
- Seismicity is mostly confined in the upper crust because of upper crust–mantle decoupling and/or insufficient level of intraplate stress compared to high brittle strength.
- Cases of deep seismicity occurr more often in extensional settings (2-3 times higher stress for brittle failure in compression than in tension).

World *Te* **Maps**

'Hard' rheology: UC= 'dry granite' and LC= 'mafic granulite'

1 crustal layers and mantle lithosphere coupled (in blue); **2** crustal layers coupled and mantle lithosphere decoupled (in azure); **3** crustal layer decoupled and mantle lithosphere coupled (in pink); **4** crustal layers and mantle lithosphere decoupled (in red).

'Soft' rheology: UC: 'dry quartzite' and LC='wet diorite'

Te

190

175

160

145

130

115

100

85

70

55

40

25

 10

km

'Hard' rheology: UC= 'dry granite' and LC= 'mafic granulite'

America *Te* model of the Litho! **North America** *Te* **model of the Lithosphere**

Coupling/Decoupling Conditions

0 20 40 60 80 100 120 140 160 180 200

Tesauro et al., 2015, G3

Te **from gravity models**

Forward modeling: the gravity anomaly due to a load (i.e. topographic surface) and its flexural compensation is calculated for different values of *T*e and compared to the observed gravity anomaly. The 'best fit' *T*e is then determined as the one that minimizes the difference between observed and calculated gravity anomalies.

In inverse (e.g., spectral) models: gravity and topography data are used to estimate *T*e directly by computing the transfer function between them as a function of wavelength (e.g., admittance or coherence) and comparing it to model predictions.

Te estimates derived from studies of gravity anomaly and topography/bathymetry using both forward and inverse (i.e., spectral) modeling techniques. The map is based on a 2x2 grid of the *Te* estimates.

Strength and stability Crème-brulée *vs* **Jelly sandwich model**

Depending on its viscosity the mantle lithosphere has the potential to sink as a result of Rayleigh–Taylor (RT) instability (ρ_m > ρ_a)

Instability growth time (*t***)**: the time it takes for the instability of a mantle root to be amplified with respect to its initial value.

The growing instability wavelength λ of a lithospheric mantle is Ad where 2.5<*A* <3.0 and *d* the thickness of the lithospheric mantle. The corresponding growth time, t_{min} = $B\mu$ ((ρ _m- ρ _a)gd)⁻¹ where 6.2.< B<13.0 and *g* is the average gravity. We can evaluate t_{min} for a particular μ (mantle viscosity) by assuming ($\rho_{\rm m}$ - $\rho_{\rm a}$)=20 kgm⁻³ and 80<*d*<100 km.

- For a **jelly-sandwich model** the continental mantle can support large stresses (>2 GPa) and has a high viscosity ($10^{22}10^{24}$ Pas), then t_{min} will be long (>0.05–2 Gyr), comparable with age of cratons.
- For a **crème brûlée model**, the stresses are small (0–10 MPa) and the viscosity is low (10¹⁹10²⁰ Pa s), then t_{min} will be short (0.2-2.0 Myr). This model implies that the tectonic features will collapse (surface tectonic feature will disappear) in few Myr.

 \square By 10 My, the lithosphere disintegrates due to delamination of the mantle followed by its convective removal and replacement with hot asthenosphere.

Strength and stability Crème-brulée *vs* **Jelly sandwich model**

Deformation after 5 Myr, producing 300 km of shortening at 60mm yr-1

Jelly sandwich model

Crème-brulée model

An incerasse of Moho temperature promotes RT instability

- Crème brûlée models are unable to explain those features of collisional systems that require subduction.
- Jelly-sandwich models produce stable subduction and can explain structural styles of collisional systems (e.g., those associated with slab flattening).

Folding models for continental lithosphere

A very hot lithosphere causes one dominant small wave-length controlled by the upper crust (monoharmonic pattern).

Typical values: tens of kms

A normal lithosphere produces two dominant wave-lengths controlled by the crust and the upper mantle (decoupled biharmonic pattern).

A very cold lithosphere causes one dominant large wave-length controlled by the entire lithosphere (monoharmonic pattern).

Typical values: 150-400 km

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Faults are controlled by the wavelength of folding and tend to localize at the inflection points of folds.

Folding models for continental lithosphere

Wavelength of crustal and lithospheric folding increases with thermal age of the lithosphere: The wavelengths, λ , of smallamplitude folding are proportional to 5-10 thickness of the competent layers: λ < 5-10h \sim 5-10Te

In continental lithosphere, there may be several competent layers, which yield different folding wavelengths:

- In case of Central Asian lithosphere, two wavelengths are depictable: crustal (50–100 km) and mantle (300–350 km).
- In case of cratons (Central Australia), the folding wavelength reaches 600–700 km indicating a 60-km-thick competent layer.

 \mathcal{C} folding versus age of the continental lithosphere continental litera High ratios λ /Te (e.g., λ /Te > 10) may be due to very weak lithosphere loaded by >> h_{sed}, while small ratios λ /Te (e.g., λ /Te < 4) may be related to the amount of shortening.

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(1) Indian Ocean, (2) Russian platform, (3) Arctic Canada, (4) Central Austaralia, (5) Western Goby, (6) Paris Basin, (7) North Sea Basin, (8) Ferghana and Tadjik Basin, (9) Pannonian Basin, (10) Iberian Basin, (11) Southern Tyrrhenian Sea, (12) Gulf of Lion, (13) Transcontinental Arch of North America; (14) Norwegian sea.

Squares=regular folding Stars=irregular folding