Exercise for the examination

Description of the exercise

- Let's consider an experimental setup composed by two layers of pixel detectors. Each detector has an area of 10x10 cm², and it is composed a matrix of pixel detectors with a pitch of 200 μ m.
- The two detectors are separated by 20 cm and are used to detect cosmic rays.
- Cosmic rays are generated as straight lines ("tracks"), generates according to a the distributions

 $\Phi(m{artheta}) \propto \cos^2{(m{artheta})}$

 $\Phi(\varphi) \propto ext{isotropic}$

- When the tack hit the detector, a "Point" is reconstructed in each detector. The (x,y) coordinates of the point are discretized according to the pitch of the pixel. The information of "generated (x,y)" and the discretized position can be stored in the object.
- For each event 1 track is generated.

Description of the exercise

- For each event, a "Track" object (i.e. a vector object) can be defined: each track is defined from two "Point" object and it is characterized by the two reconstructed angles, α and β.
- Generate 10 6 events and reconstruct the distribution of α .
 - Compare the obtained distribution with the expected one $\Phi(m{artheta})\propto\cos^2{(m{artheta})}$
 - If you define a track as "two joined points" how does the "tracking efficiency" varies as a function of ϑ ?
 - How does your results change if you have a pitch of 100 μm or 400 $\mu m?$
- Possible complications (not mandatory):
 - Introduce an "inefficiency" of your detector (e.g. 100% efficiency means that all your pixels works fine, 95% means that 5% of the total number of pixels are off)
 - Include multiple scattering assuming that each detector has a width of 300 μm
- The simulation can be done either in "pure" C++ or using ROOT

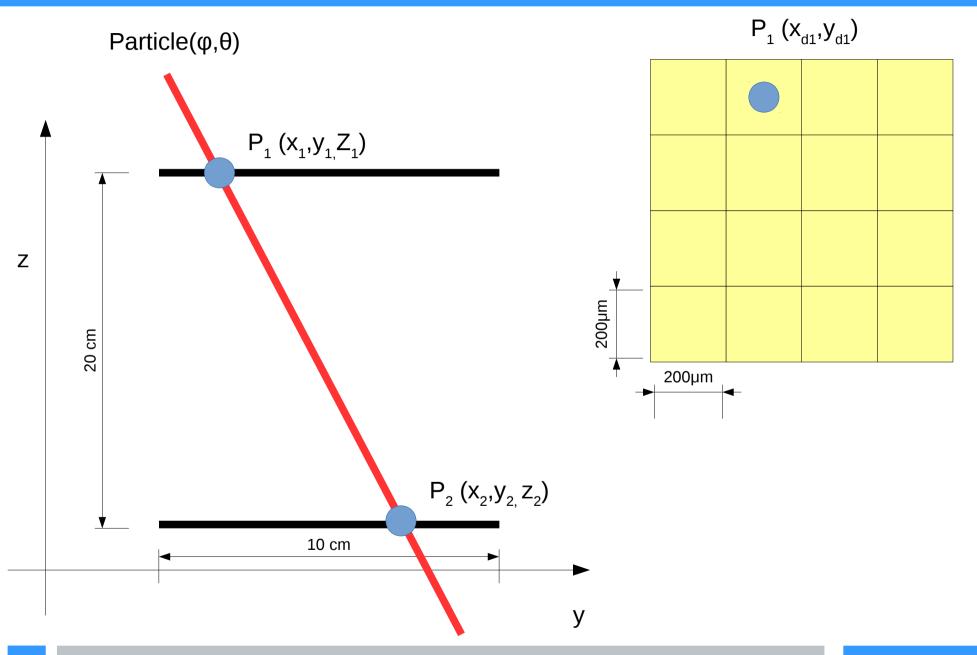
Multiple scattering

- The Coulomb scattering distribution is well represented by the theory of Moliere. It is roughly Gaussian for small deflection angles, but at larger angles it behaves like Rutherford scattering, having larger tails than does a Gaussian distribution.
- For many applications to use a Gaussian approximation for the central 98% of the projected angular distribution, with a <u>width</u> given by

$$\Theta_0 = \frac{13.6 \, MeV}{\beta \, c \, p} \, z \sqrt{\frac{x}{X_0}} \left[1 + 0.038 \ln\left(\frac{x}{X_0}\right) \right]$$

- Here p, β c, and z are the momentum, velocity, and charge number of the incident particle, and x/X₀ is the thickness of the scattering medium in radiation lengths.
- In your case assume a muon, with 1 GeV momentum crossing $300\mu m$ of silicon (X₀ = 21,82 g cm⁻², ρ = 2,329 g cm⁻³)

Schematic view of the apparatus



Angles in 3D

2D: $\theta = \arctan(x, y)$ 3D: $r = \sqrt{x^2 + y^2 + z^2}$ $\theta = \arctan(\sqrt{x^2 + y^2}, z)$ $\phi = \arctan(y, x)$ Angle calculation in 2D and 3D

The spherical coordinate system is illustrated below.

