

From Eq. 5-25, 5-26 to 5.27

5-25 →
 $\omega = (i(\vec{k} \cdot \vec{x} - \omega t))$
 $\vec{k} \downarrow$
 $f_e e^{i\omega} + f_e \bar{v} e^{i\omega} [\hat{i}(k_1, k_2, k_3)] - \phi_e e^{i\omega} [\hat{i}(k_1, k_2, k_3)]$
 $\cdot \frac{\partial f}{\partial \bar{v}} = 0$

(ii) $\phi_e e^{i\omega} [-i(k^2)] = 4\pi G e^{i\omega} \int f_e d^3v$

(i) → $f_e = \frac{\phi_e \bar{k} \frac{\partial f_0}{\partial \bar{v}}}{\bar{k} \bar{v} - \omega}$

↙ + (ii)

$$-k^2 \phi_e = 4\pi G \int \frac{\phi_e \bar{k} \frac{\partial f_0}{\partial \bar{v}}}{\bar{k} \bar{v} - \omega} d^3v$$

$$k^2 \phi_e + 4\pi G \int \frac{\phi_e \bar{k} \frac{\partial f_0}{\partial \bar{v}}}{\bar{k} \bar{v} - \omega} d^3v = 0$$

/ divide
 $k^2 \phi_e$

$$1 + \frac{4\pi G}{k^2} \int \left(\frac{\bar{k} \frac{\partial f_0}{\partial \bar{v}}}{\bar{k} \bar{v} - \omega} \right) d^3v = 0 \rightarrow 5.27$$

dispersion relation