

EXERCISE: Consider a galaxy cluster (populated by elliptical galaxies E, mainly) having $M/L_B = 250 (M/L)_{\text{sun}}$. Using tables below, compute M/L_R .

SOLUTION: From table of the sun mag, $(B-R)_{\text{sun}} = 5.48 - 4.31 = 1.17$.

From table of galaxy colors (at $z=0$), $(B-R)_E = (B-V)_E + (V-R)_E = 0.96 + 0.61 = 1.57$. This is true for the cluster, too.

From color definition $(B-R)_E = -2.5 \log(L_B/L_R)$, i.e. $(L_B/L_R)_E = 10^{-0.4 \cdot (B-R)_E}$

and similarly $(L_B/L_R)_{\text{sun}} = 10^{-0.4 \cdot (B-R)_{\text{sun}}}$

$$\begin{aligned} \text{Now: } (M/L_R)/(M/L_R)_{\text{sun}} &= (M/L_B) \cdot (L_B/L_R) / [(M/L_B)_{\text{sun}} \cdot L_{B,\text{sun}}/L_{R,\text{sun}}] = \\ &= (M/L_B)/(M/L_B)_{\text{sun}} \cdot (L_B/L_R)/(L_{B,\text{sun}}/L_{R,\text{sun}}) = 250 \cdot 10^{-0.4 \cdot (B-R)_E} / 10^{-0.4 \cdot (B-R)_{\text{sun}}} = \\ &= 250 \cdot 10^{-0.4 \cdot [(B-R)_E - (B-R)_{\text{sun}}]} = 250 \cdot 10^{-0.4 \cdot 0.4} = 250 \cdot 0.692 = 173 \end{aligned}$$

i.e. $(M/L_R) = 173 (M/L_R)_{\text{sun}}$

SUN ABS MAG

Filter B&M

U	5.61
B	5.48
V	4.83
R	4.42
I	4.08
J	3.64
H	3.32
K	3.28

Galaxy Colors

(a) Standard Johnson-Morgan/Cousins (A0V)

type	$U - B$	$B - V$	$V - R_C$	$R_C - I_C$	$V - R_J$	$R_J - I_J$
E	0.64	0.96	0.61	0.70	0.71	0.73
S0	0.42	0.85	0.54	0.61	0.63	0.63
Sab	0.33	0.78	0.56	0.65	0.66	0.68
Sbc	0.00	0.57	0.52	0.62	0.60	0.65
Scd	-0.08	0.50	0.50	0.57	0.57	0.60
Im	-0.35	0.27	0.31	0.33	0.34	0.33