

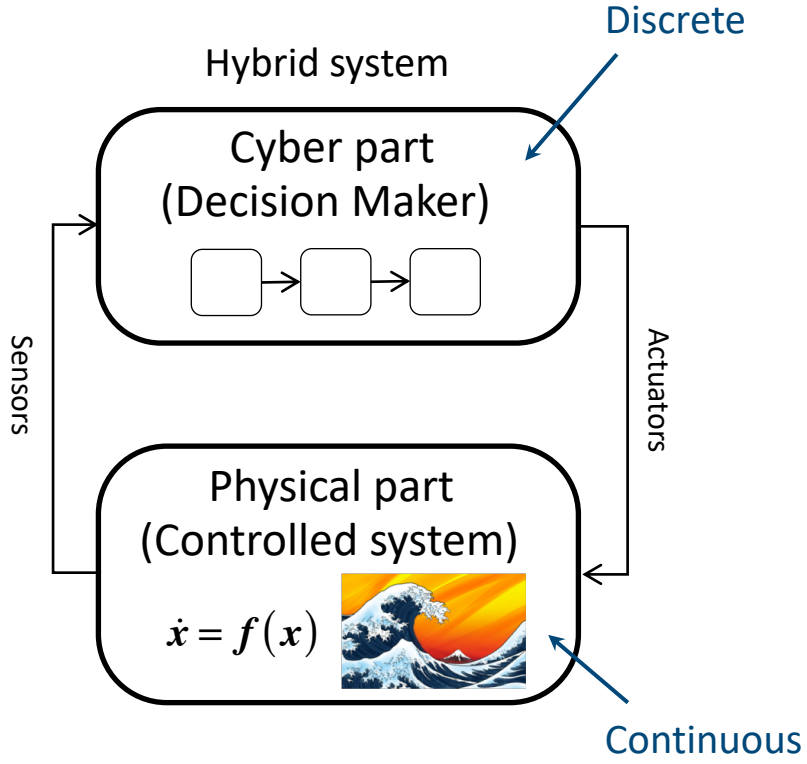
Cyber-Physical Systems

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Università degli Studi di Trieste
II Semestre 2018

Lecture 9: Signal Temporal Logic

Cyber-Physical Systems (CPS)



Amazon drone



Kiva robots



Google self-driving car

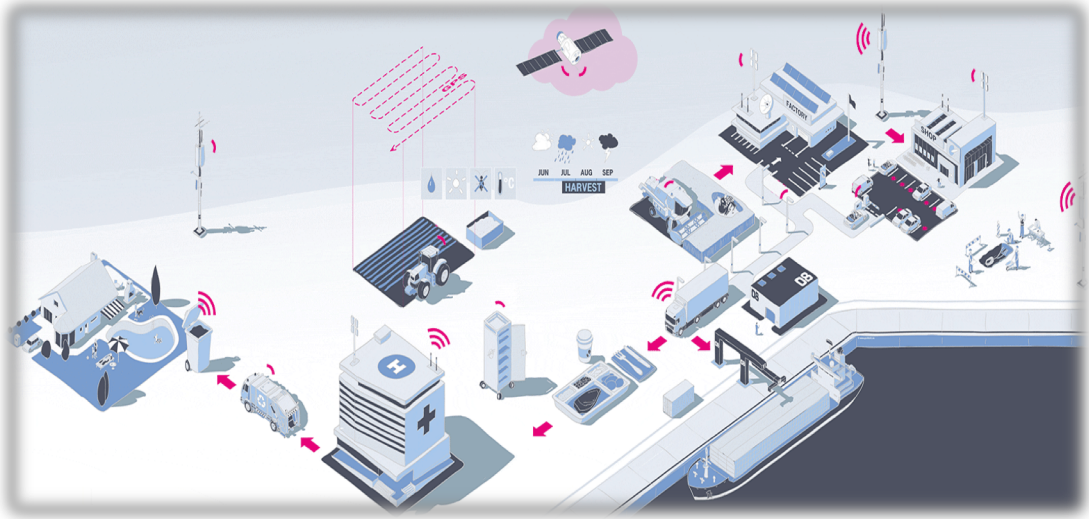
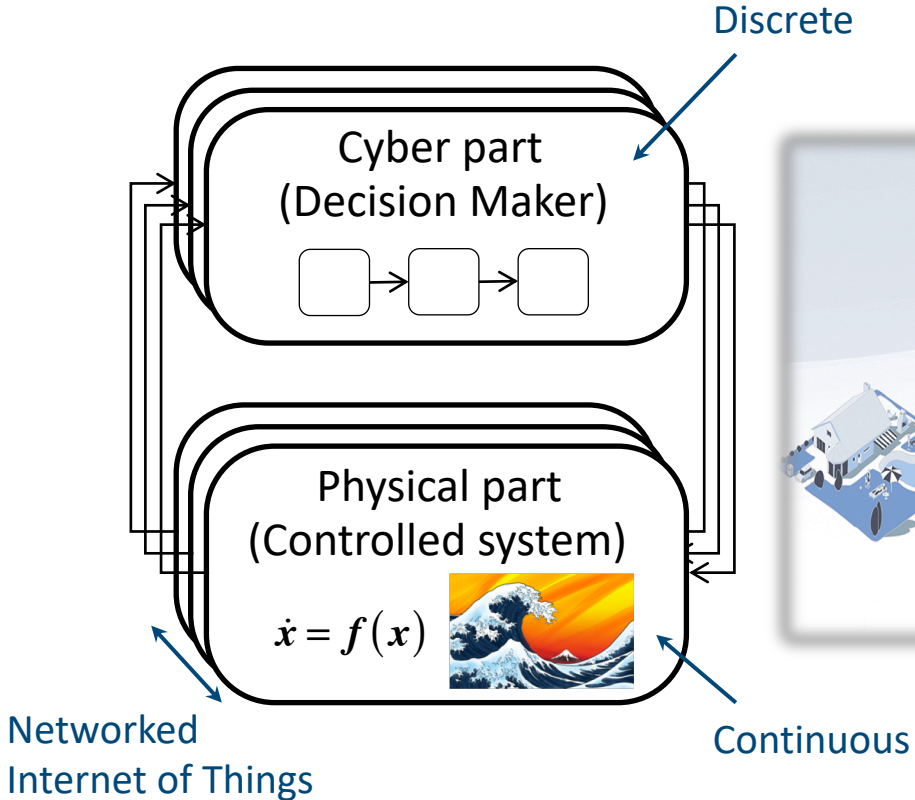


Insulin pump



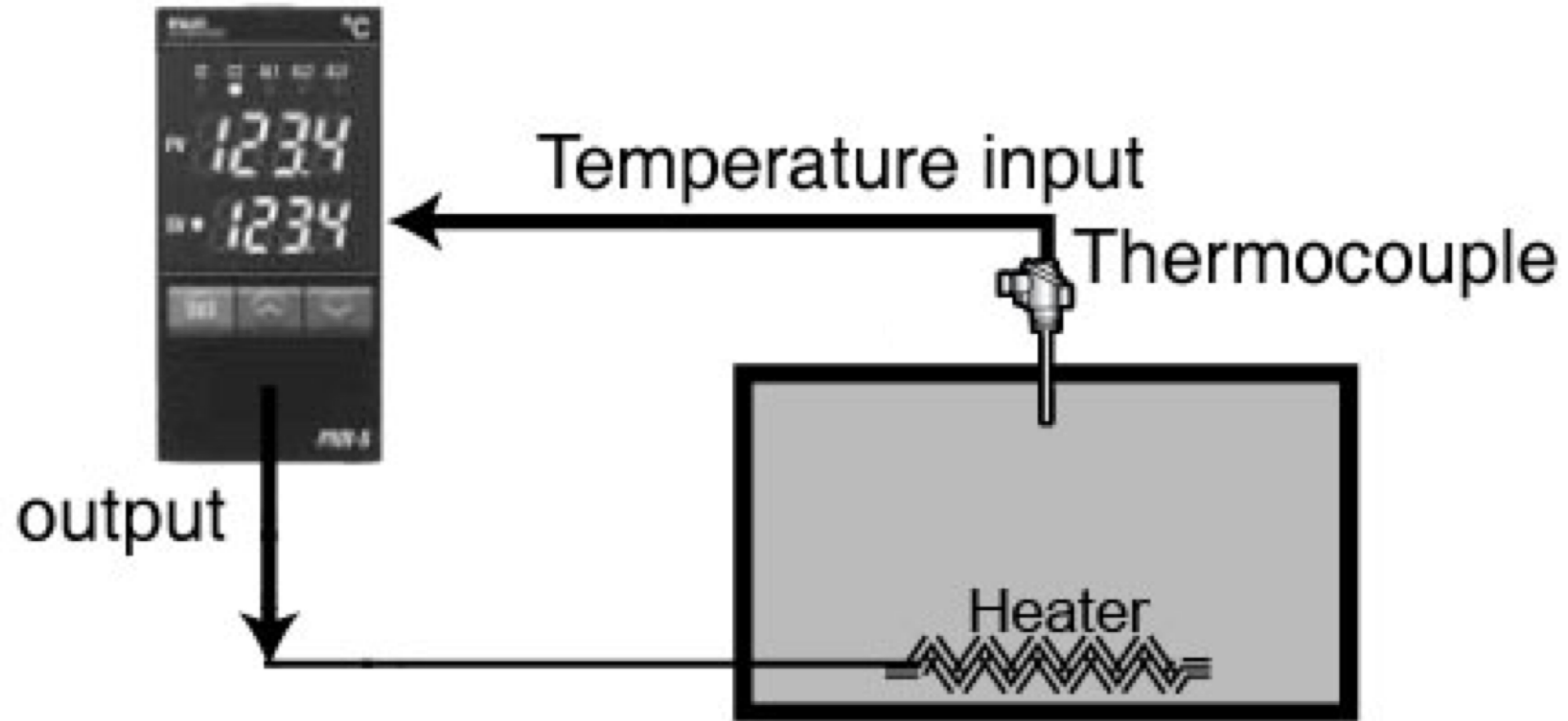
Defibrillator

Cyber-Physical Systems (CPS)



Credits for this picture: <http://kayarvizhy.com/>

Temperature Control



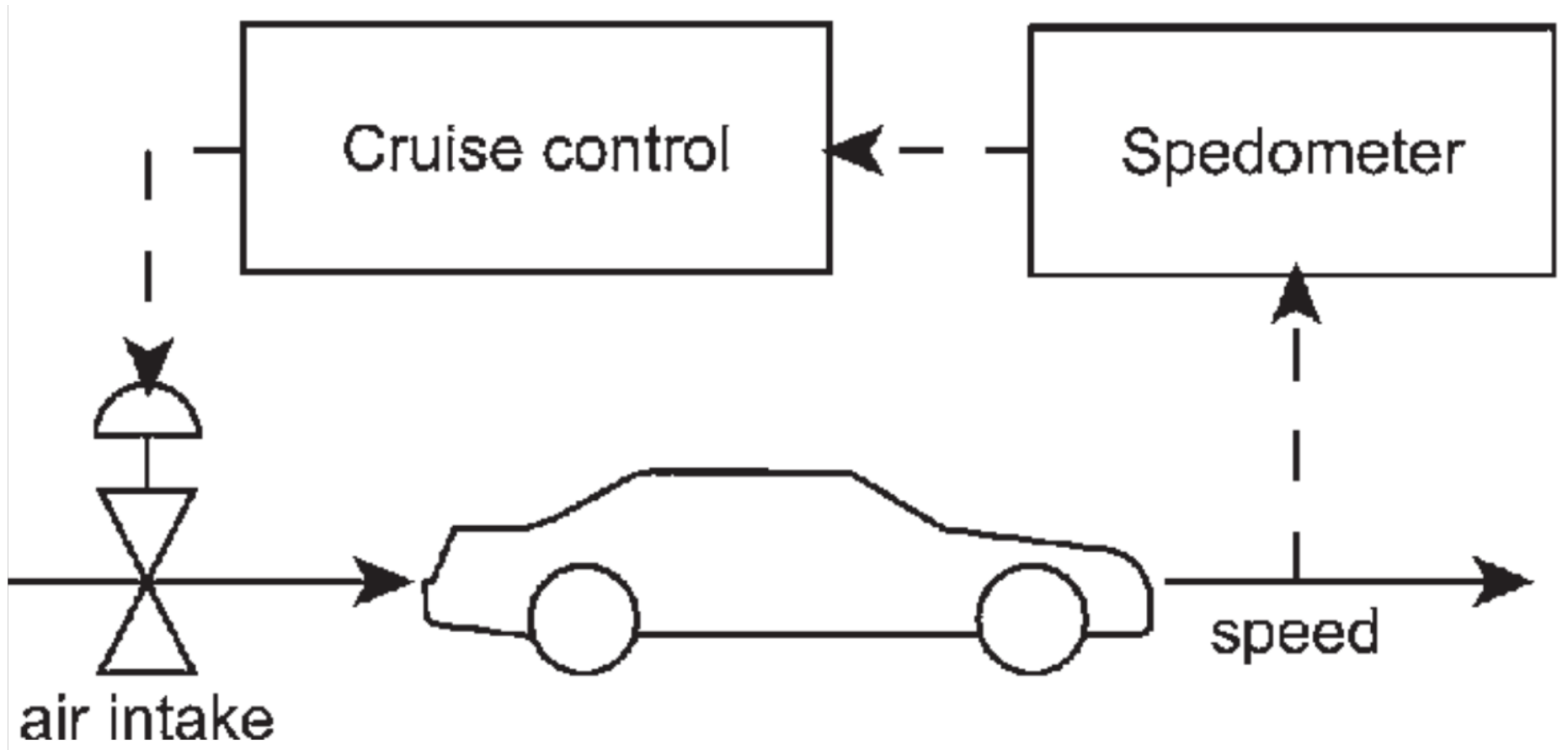
Artificial Pancreas

Type 1 diabetes occurs when the pancreas produces little or none of the insulin needed to regulate blood glucose

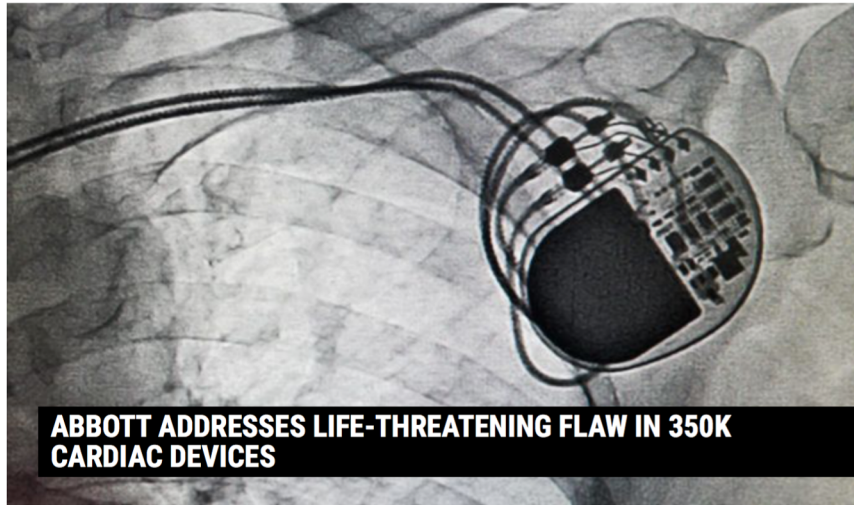
They rely on external administration of insulin to manage their blood glucose levels.



Automotive Car



Are we safe ?



by **Tara Seals**

May 4, 2018 , 3:27 pm

About 350,000 implantable defibrillators are up for a firmware update, to address potentially life-threatening vulnerabilities.

Abbott (formerly St. Jude Medical) has released another upgrade to the firmware installed on certain implantable cardioverter defibrillator (ICD) or cardiac resynchronization therapy defibrillator (CRT-D) devices. The update will strengthen the devices' protection against unauthorized access, as the provider said in a [statement](#) on its website: "It is intended to prevent anyone other than your doctor from changing your device settings."

The patch is part a planned series of updates that began with pacemakers, programmers and remote monitoring systems in 2017, following 2016 claims by researchers that the then-St. Jude's cardiac implant ecosystem was rife with cybersecurity flaws that [could result in "catastrophic results."](#)

<https://threatpost.com/abbott-addresses-life-threatening-flaw-in-a-half-million-pacemakers/131709/>

Vehicle safety notices - Prestige models among cars recalled in April



A number of Britain's biggest car makers issued vehicle safety recalls in the last month, covering issues from minor missing pieces of trim to engine and steering failure.

Audi, BMW, Lexus, Porsche and Hyundai were among manufacturers to issue mandatory recalls for their cars.

<https://inews.co.uk/essentials/lifestyle/cars/car-news/vehicle-safety-recalls-notices-prestige-cars-recalled-april/>

Some tragic accidents

Tesla driver dies in first fatal crash while using autopilot mode

The autopilot sensors on the Model S failed to distinguish a white tractor-trailer crossing the highway against a bright sky



The first known death caused by a self-driving car was disclosed by **Tesla Motors** on Thursday, a development that is sure to cause consumers to second-guess the trust they put in the booming autonomous vehicle industry.

The 7 May accident occurred in Williston, Florida, after the driver, Joshua Brown, 40, of Ohio put his Model S into **Tesla's autopilot mode**, which is able to control the car during highway driving.

Against a bright spring sky, the car's sensors system failed to distinguish a large white 18-wheel truck and trailer crossing the highway, Tesla said. The car attempted to drive full speed under the trailer, "with the bottom of the trailer impacting the windshield of the Model S", Tesla said in a **blogpost**.

Uber Self-Driving Car 'Detected' Pedestrian Killed In Crash, But Decided It Didn't Need To Stop: Report



Ryan Felton

5/07/18 5:00pm • Filed to: UBER

42.3K 157 7

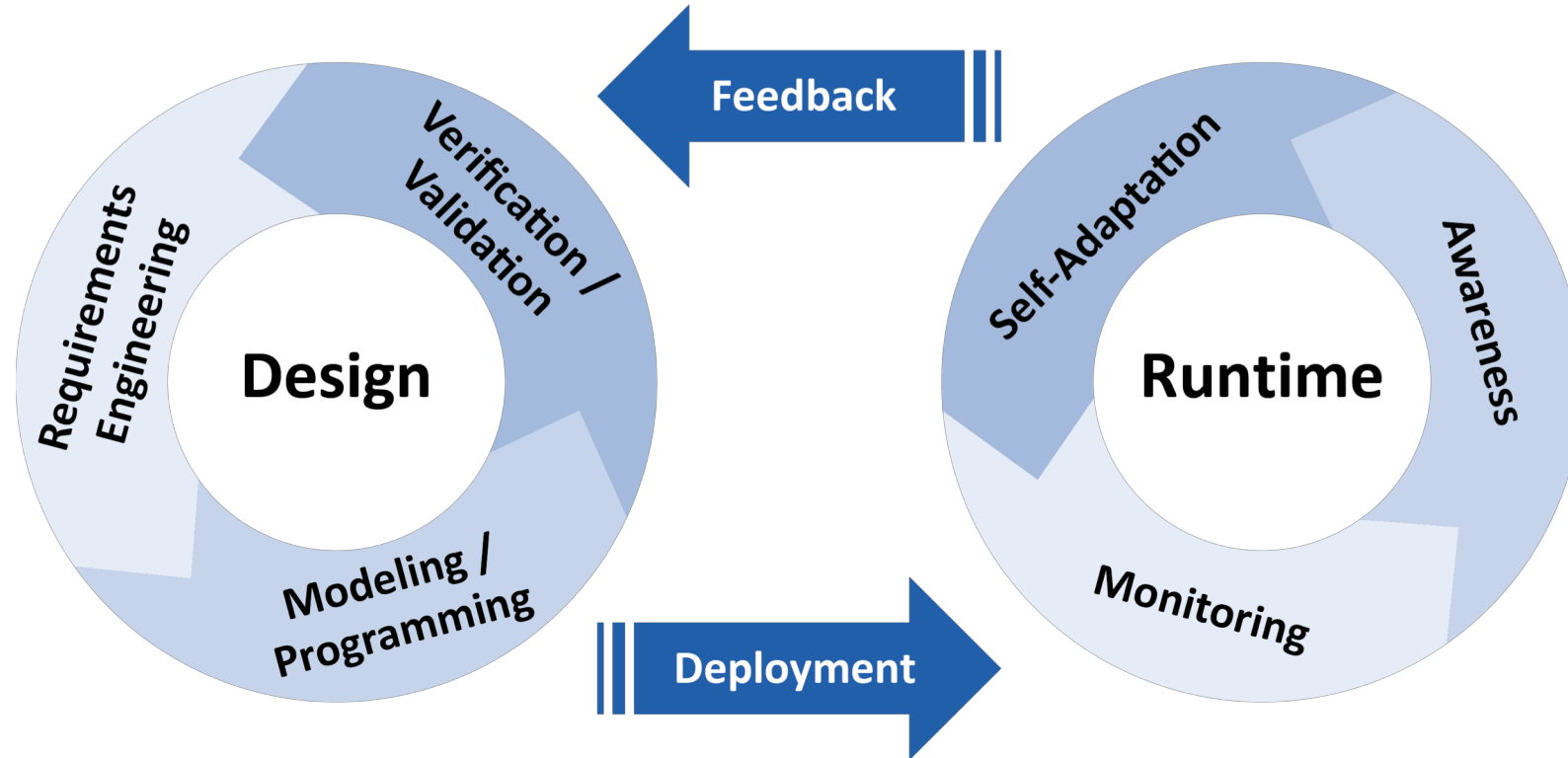


Self-driving Uber
Photo: Uber ATG

Like other autonomous vehicle systems, Uber's software has the ability to ignore "false positives," or objects in its path that wouldn't actually be a problem for the vehicle, such as a plastic bag floating over a road. In this case, Uber executives believe the company's system was tuned so that it reacted less to such objects. But the tuning went too far, and the car didn't react fast enough, one of these people said.

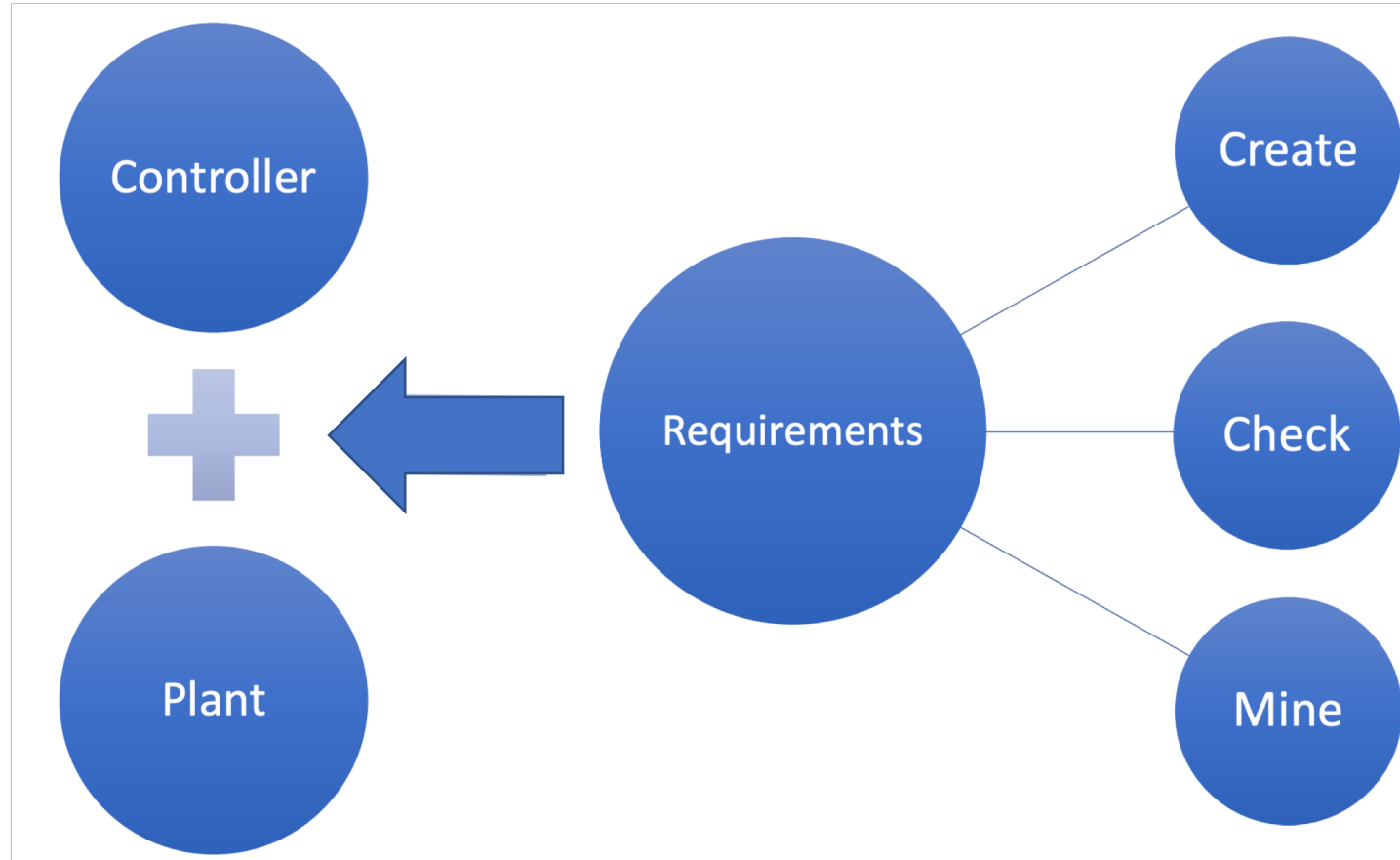
8 <https://jalopnik.com/uber-self-driving-car-detected-pedestrian-killed-in-cra-1825834016>

Model-based Design Approach



Requirements Driving Design

Requirements **formally** capture what it means for a system to operate correctly in its operating environment



Typical day in a control designer's life

Check **transient response** of x
when driving with highway
101 pattern with
temperature around 40°C



Chief Engineer



SPECS

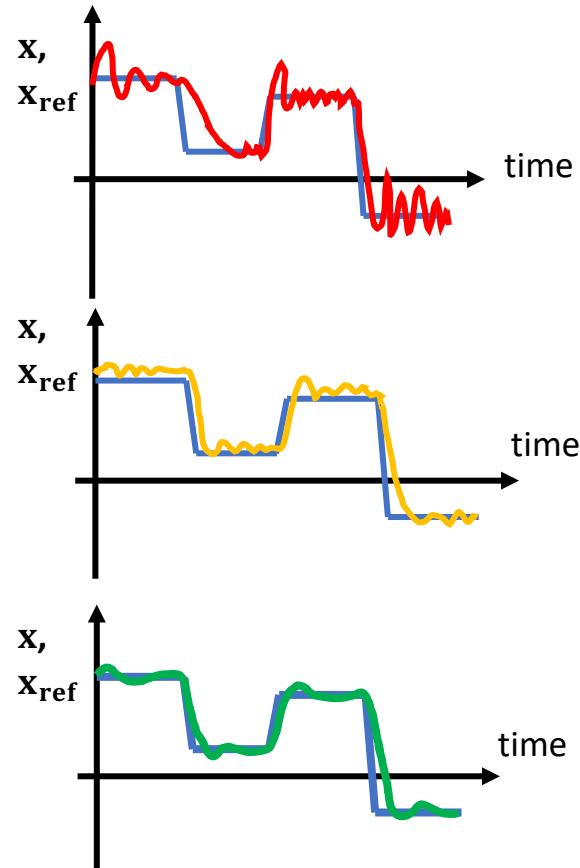


Control Designer



- Normally in natural language (ambiguous, error-prone)
- Sometime absent
- If you are LUCKY, they are written in English

Typical day in a control designer's life



Uh Oh!

... should be okay

Looks good



Linear Temporal Logic (LTL)

It is a logic interpreted over infinite discrete-time traces

E.g. It is always true that the highest temperature will be below 75 degree and the lowest temperature will be above 60 degree

Key ingredients:

- ▶ Propositions
E.g. $p = T < 75$, $q = T > 60$
- ▶ Boolean operators: \wedge , \vee , \neg
E.g. $p \wedge q$
- ▶ Temporal Operators: always (G or \square), eventually (F or \diamond), until (U), next (X or \bigcirc)
E.g. $G(p \wedge q)$

t Typ

Linear Temporal Logic (LTL)

It is a logic interpreted over infinite discrete-time traces

E.g. **For the next 3 days** the highest temperature will be below 75 degree and the lowest temperature will be above 60 degree

$X a \wedge X X a \wedge X X X a$ with $a = T < 75 \wedge T > 60$

Metric Interval Temporal Logic (STL)

Invented by R. Alur, T.Feder, T.A. Henzinger (1991)

It extended LTL by adding **dense time intervals**:

$$G_{[0,3]}(p \wedge q)$$

Signal Temporal Logic (STL)

Invented by D. Nickovic and O. Maler from Verimag (2004)

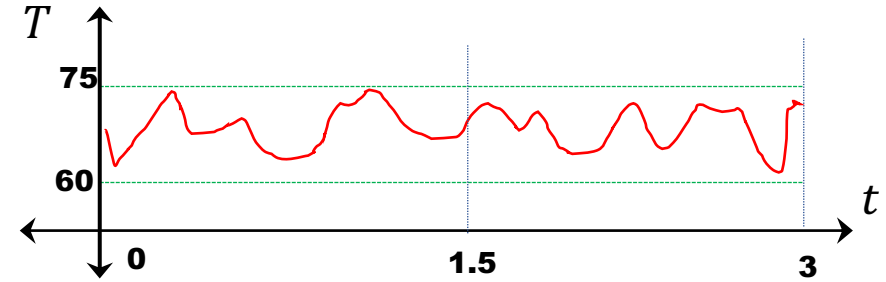
It extended MITL by having **signal predicates over real values as atomic formulas**:

$$G_{[0,3]}(T(t) < 75 \wedge T(t) > 60)$$

Expressing specifications in STL

Always_[0,3] ($60 < T(t) < 75$)

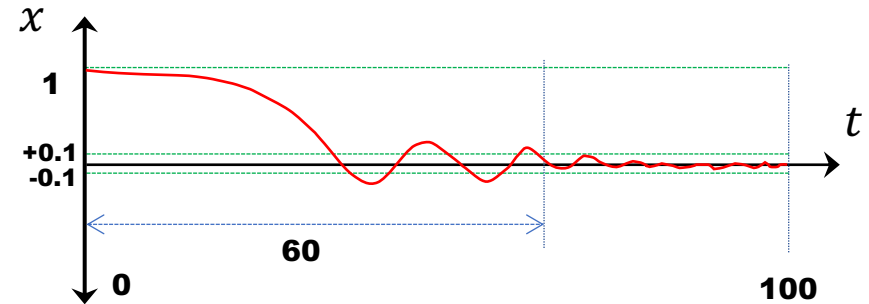
Always between time 0 and 3



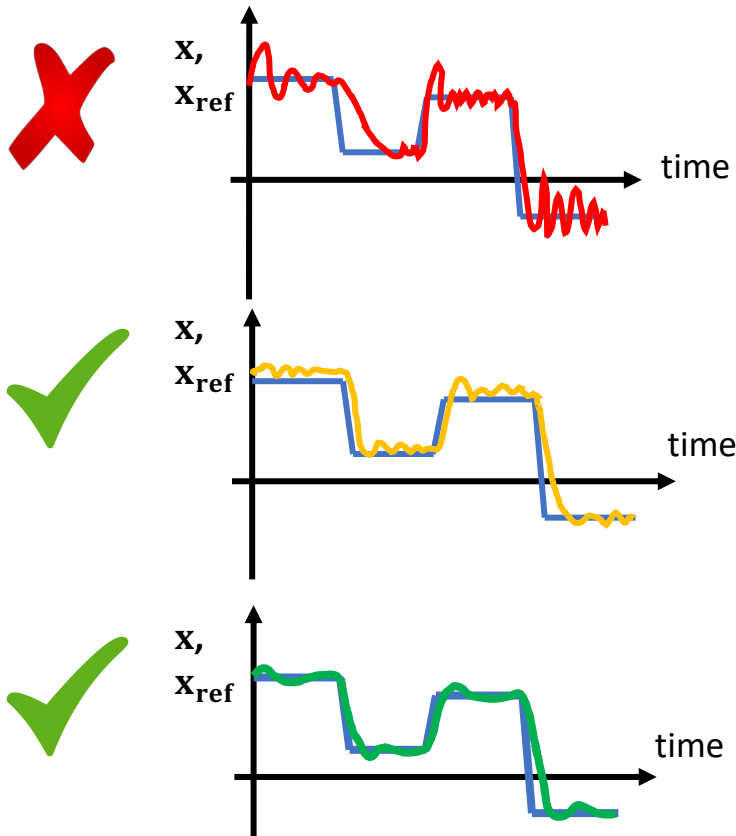
Eventually_[0,60] (**Always** ($|x(t)| < 0.1$))

Eventually at **some time t**
between time 0 and 60

From that time **t**, always till the
end of the signal trace



Can we express our engineer's requirements?



Uh Oh!

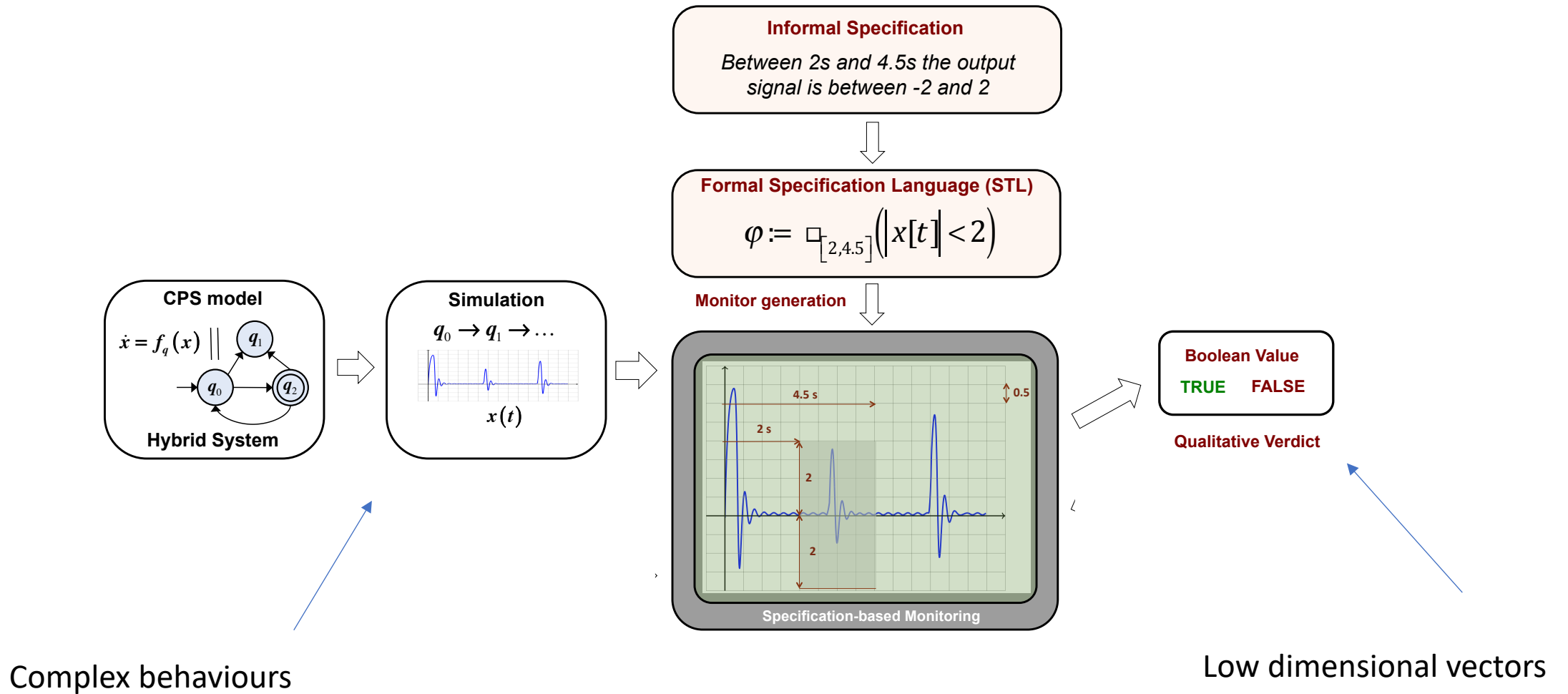
... should be okay

Looks good

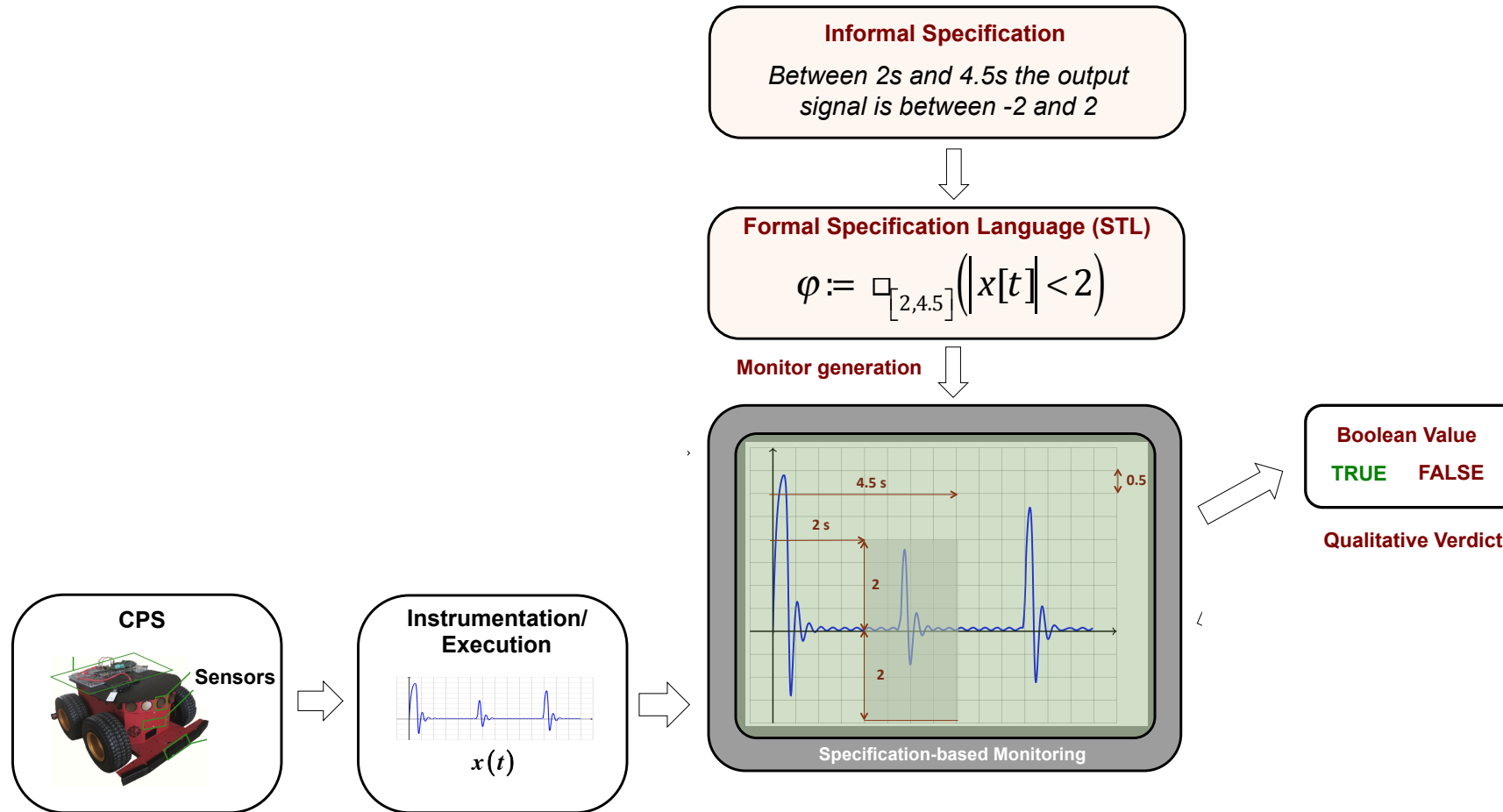


$$\varphi \equiv \text{Alw}_{[0,10]}(\text{step} \Rightarrow \text{Alw}_{[0,2]}(|x - x_{ref}| < 0.05))$$

Specification-based Monitoring



Specification-based Monitoring



STL Syntax

Syntax of STL

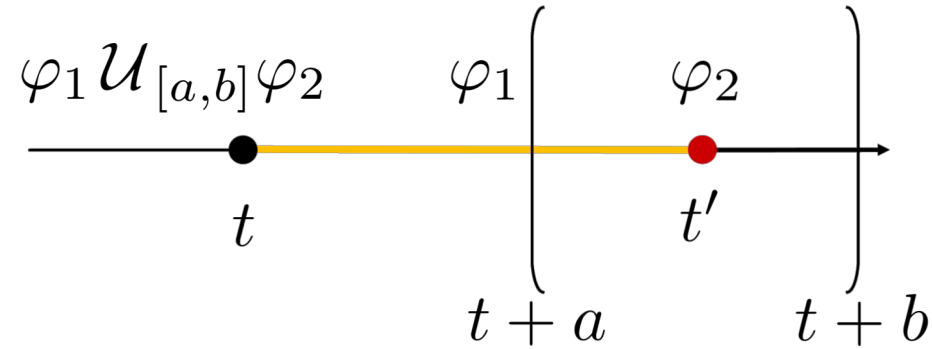
$\varphi ::=$	$f(\mathbf{x}) \sim 0$		$f: \mathbb{D} \rightarrow \mathbb{R}$ is a function over the signal $\mathbf{x}: \mathbb{T} \rightarrow \mathbb{D}$, $\sim \in \{\leq, <, >, \geq, =, \neq\}$
	$\neg \varphi$		Negation
	$\varphi \wedge \varphi$		Conjunction
	$\mathbf{F}_{[a,b]} \varphi$		At some F uture step in the interval $[a, b]$
	$\mathbf{G}_{[a,b]} \varphi$		G lobally in all times in the interval $[a, b]$
	$\varphi \mathbf{U}_{[a,b]} \varphi$		In all steps U ntil in interval $[a, b]$

Recursive Boolean Semantics of STL

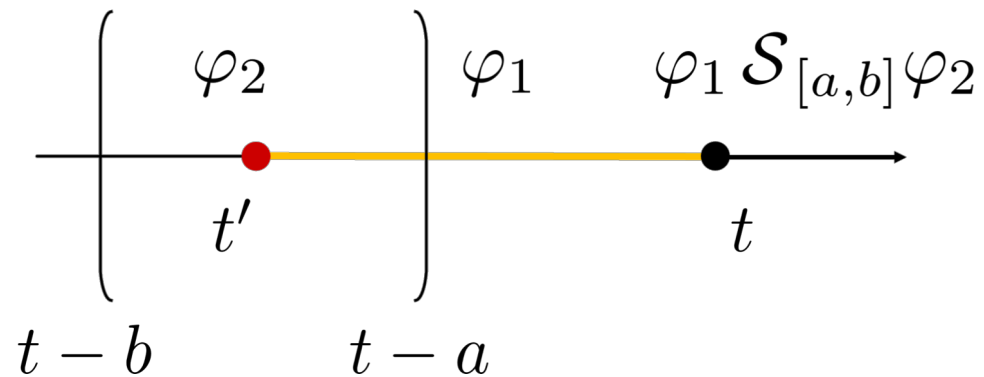
φ	$\beta(\varphi, \mathbf{x}, t)$
$f(\mathbf{x}) \sim 0$	$f(\mathbf{x}(t)) \sim 0, \quad \sim \in \{\leq, <, >, \geq, =, \neq\}$
$\neg\varphi$	$\neg\beta(\varphi, \mathbf{x}, t)$
$\varphi_1 \wedge \varphi_2$	$\beta(\varphi_1, \mathbf{x}, t) \wedge \beta(\varphi_2, \mathbf{x}, t)$
$\mathbf{F}_{[a,b]}\varphi$	$\exists\tau \in [t + a, t + b] \beta(\varphi, \mathbf{x}, \tau)$
$\mathbf{G}_{[a,b]}\varphi$	$\forall\tau \in [t + a, t + b] \beta(\varphi, \mathbf{x}, \tau)$
$\varphi \mathbf{U}_{[a,b]}\psi$	$\exists\tau \in [t + a, t + b] (\beta(\psi, \mathbf{x}, \tau) \wedge \forall\tau' \in [t, \tau) \beta(\varphi, \mathbf{x}, \tau'))$

Since and Until Operators

- Until



- Since

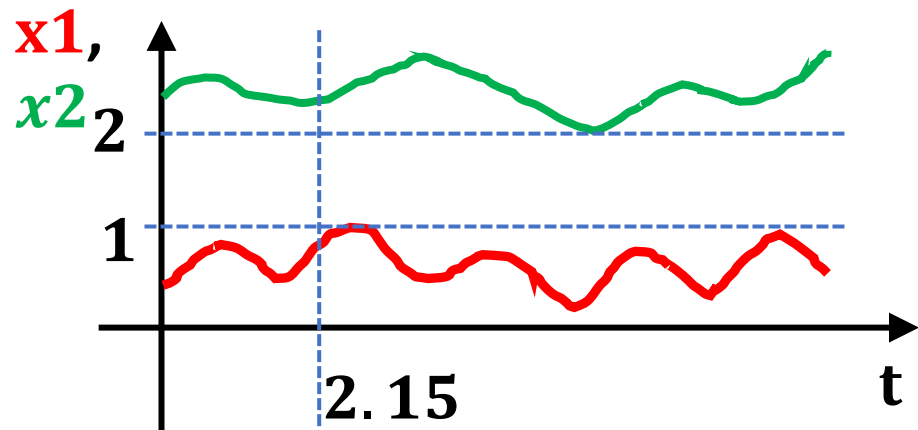


STL semantics

- ▶ Semantics of STL specified recursively over a signal $\mathbf{x}: \mathbb{T} \rightarrow \mathbb{D}$ at each time,

For each STL formula φ , here's how we define it's semantics:

- ▶ If φ is the signal predicate $\mu = f(\mathbf{x}) > 0$, then
 $\beta(\varphi, \mathbf{x}, t) = \text{true}$ iff $f(\mathbf{x}(t)) > 0$



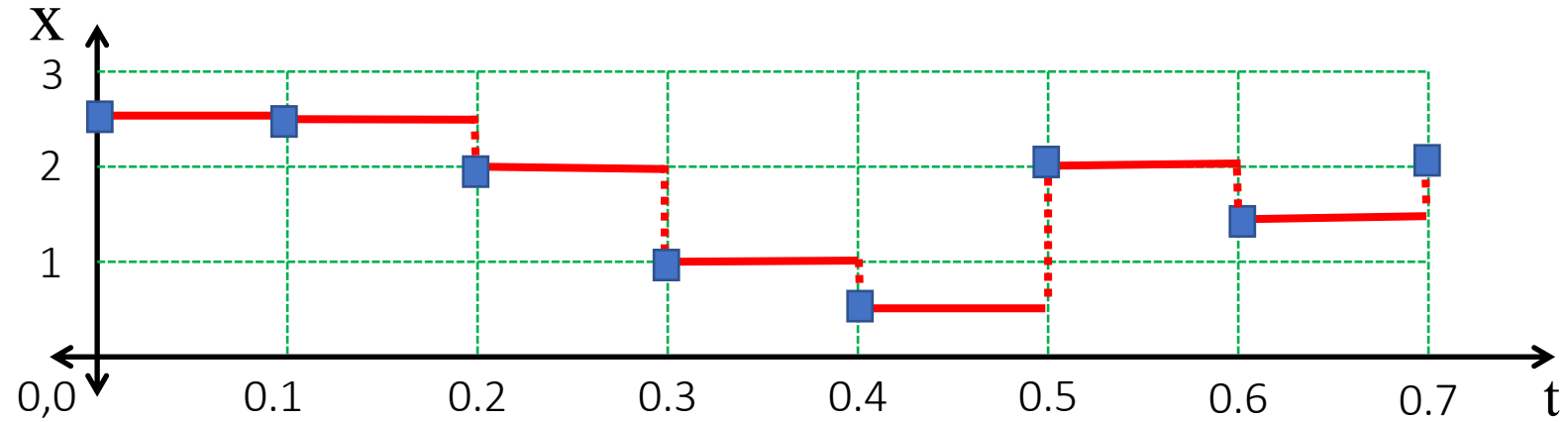
$$\mathbf{x} = (x1, x2)$$

$$f = x2 - x1 - 1$$

$$\beta(f(\mathbf{x}) > 0, \mathbf{x}, 2.15)?$$

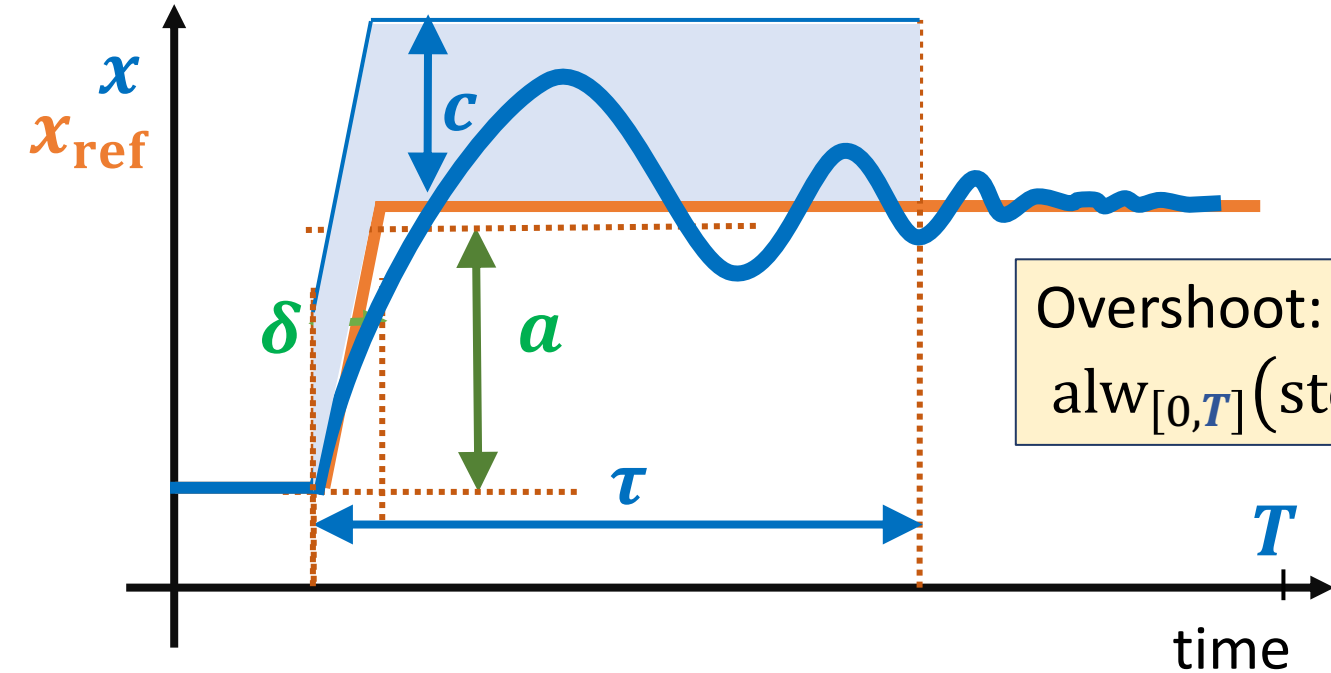
Recursive Boolean Semantics of STL

$$\varphi \equiv \mathbf{G}_{[0,0.7]} \mathbf{F}_{[0,0.2]} (x(t) \geq 1.5)$$



$x(t) - 1.5 > 0$	T	T	T	F	F	T	T	T
$Ev_{[0,0.2]} \mu$	T	T	T	T	T	T		
$Alw_{[0,0.7]} Ev_{[0,0.2]} \mu$	T							

Example STL formulas: Overshoot



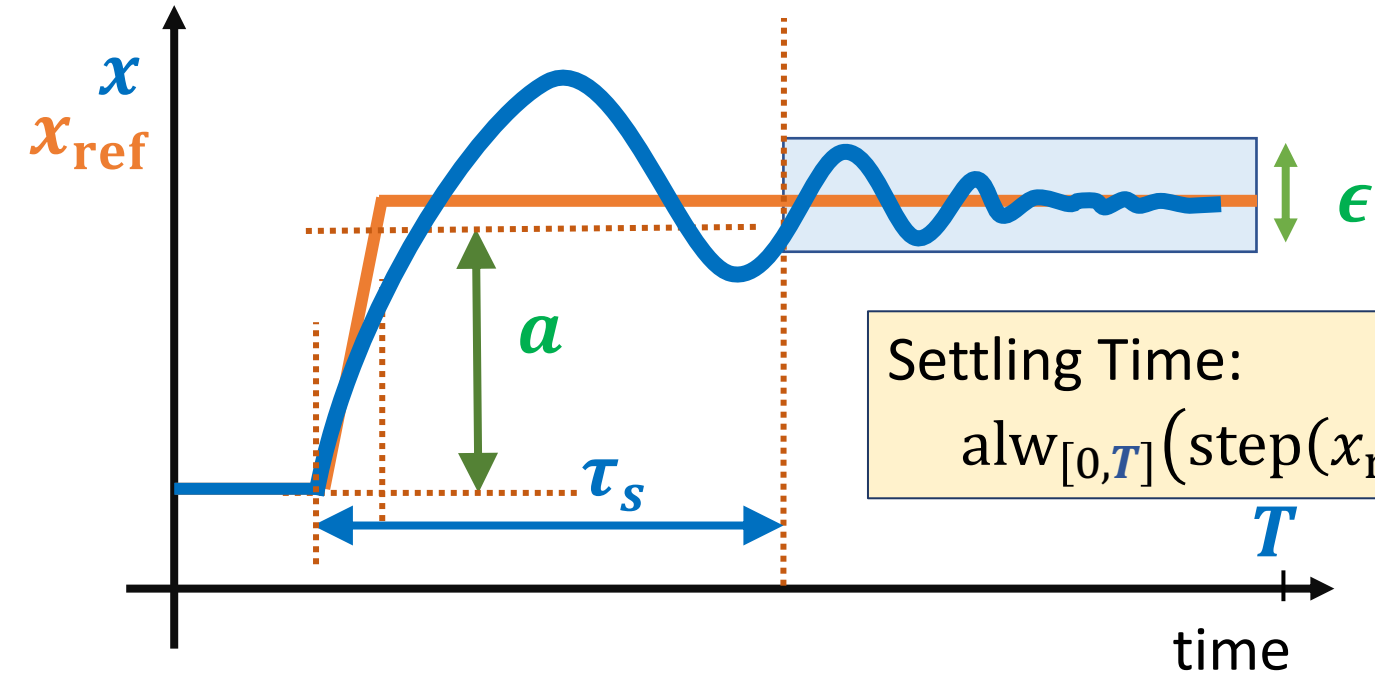
Step:

$$\text{step}(y, t) := y(t + \tau) - y(t) > a$$

Overshoot:

$$\text{alw}_{[0, T]}(\text{step}(x_{\text{ref}}, t) \Rightarrow \text{alw}_{[0, \tau]}(x(t) - x_{\text{ref}}(t) < c))$$

Example STL formulas: Settling Time



Step:

$$\text{step}(y, t) := y(t + \delta) - y(t) > a$$

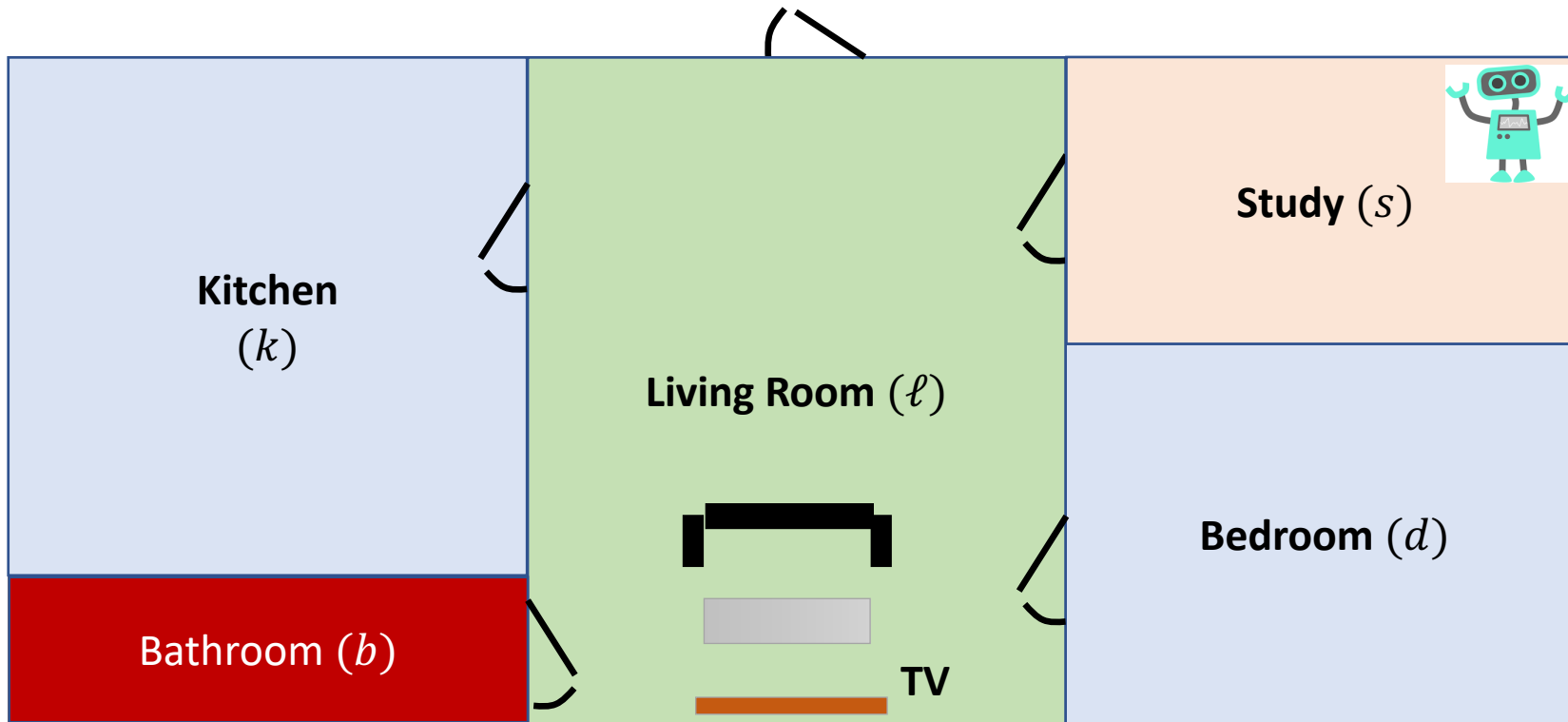
Settling Time:

$$\text{alw}_{[0, T]}(\text{step}(x_{\text{ref}}, t) \Rightarrow \text{alw}_{[\tau_s, \infty]}(|x(t) - x_{\text{ref}}(t)| < \epsilon))$$

Example specifications in LTL

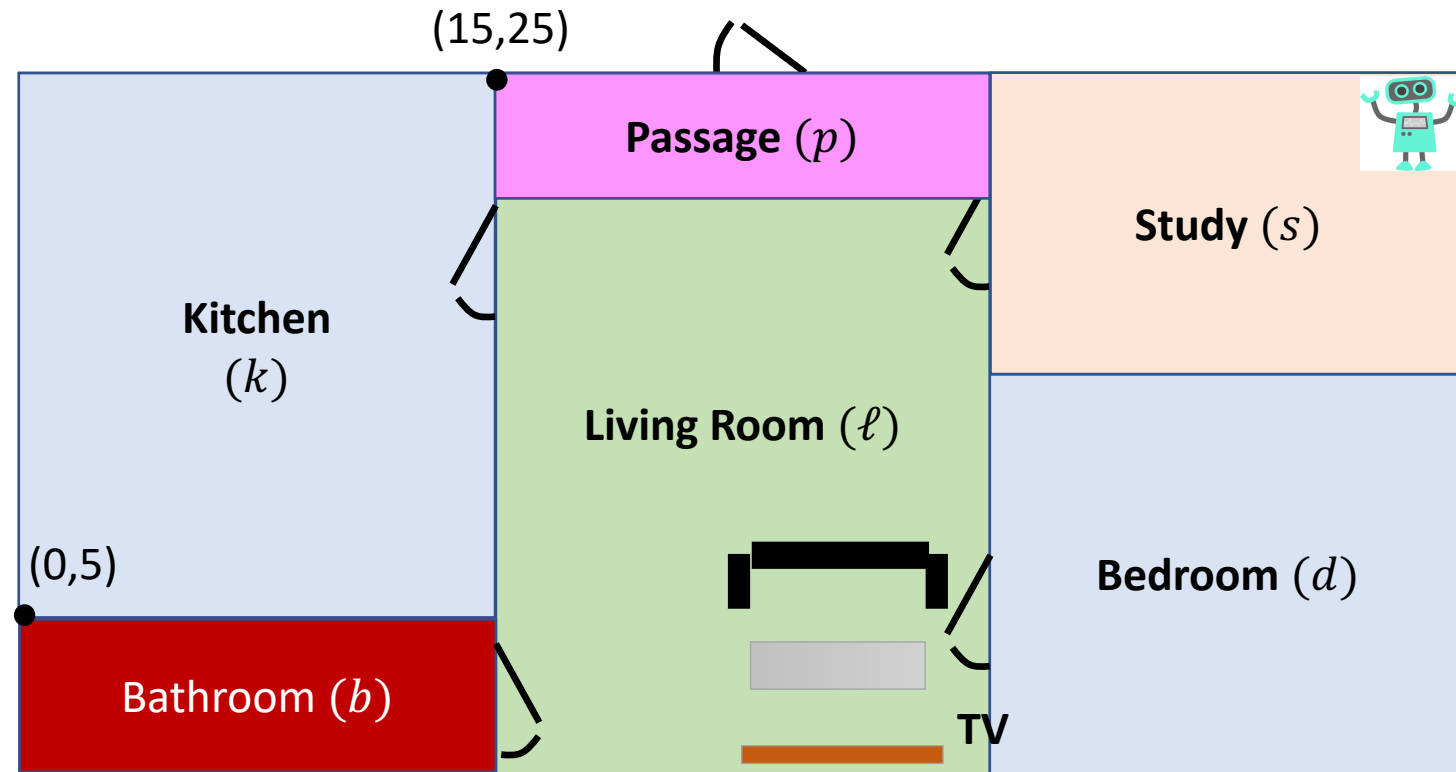


- ▶ Suppose you are designing a robot that has to do a number of missions



- ▶ Whenever the robot visits the kitchen, it should visit the bedroom after.
$$\mathbf{G}(k_r \Rightarrow \mathbf{F} d_r)$$
- ▶ Robot should never go to the bathroom.
$$\mathbf{G}\neg b_r$$
- ▶ The robot should keep working until its battery becomes low
working \mathbf{U} *low_battery*

Robot Path Specification



- ▶ Whenever the robot visits the kitchen, it should visit the bedroom within **the next 15 mins**.

$$\mathbf{G} \left((p(t) \in B_k) \Rightarrow \mathbf{F}_{[0,15]}(p(t) \in B_b) \right)$$

B_r : Box describing room r

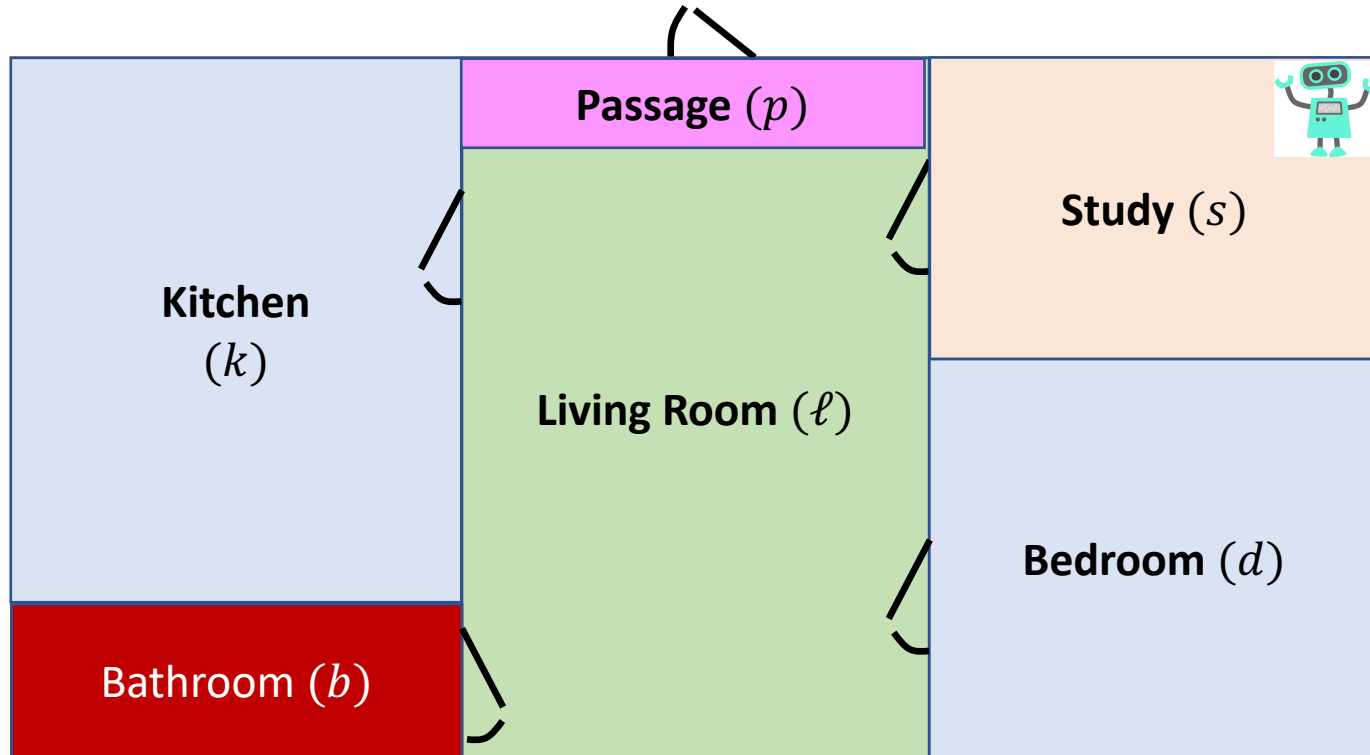
$p(t)$: Position of robot at time t

- ▶ Robot should not go to the bathroom **in the first 60 mins**.

$$\mathbf{G}_{[0,60]}(p(t) \notin B_{bath})$$

$$p(t) \in B_k : (0 < p_x(t) < 15) \wedge (5 < p_y(t) < 25)$$

Robot Path Specification

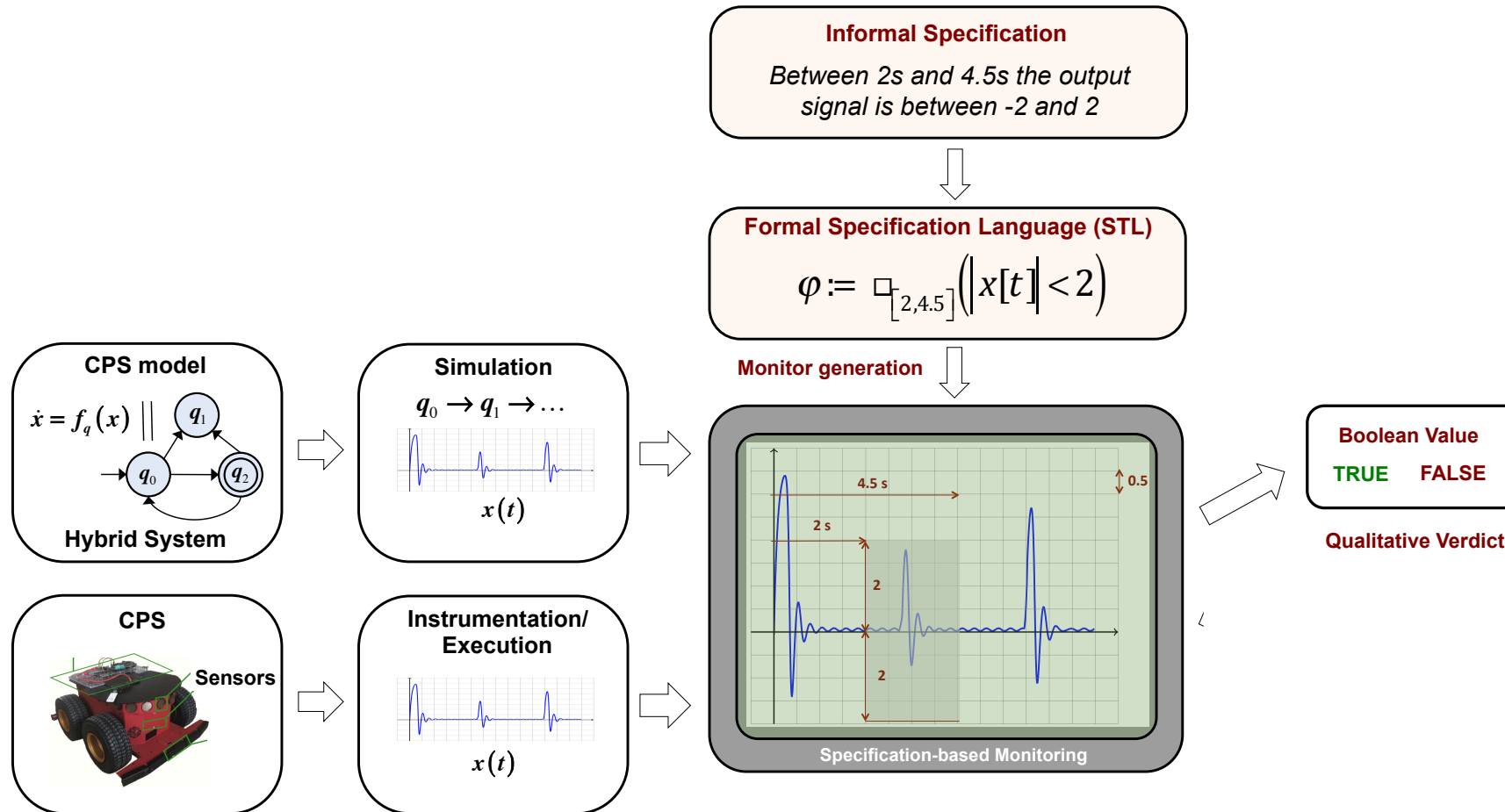


▶ The robot battery should last between 4 hours and 6 hours
 $(Q(t) \geq Q_{low}) \mathbf{U}_{[240,360]}(Q(t) < Q_{low})$

▶ For the first 10 hours, the robot is never in any room for more than 30 minutes

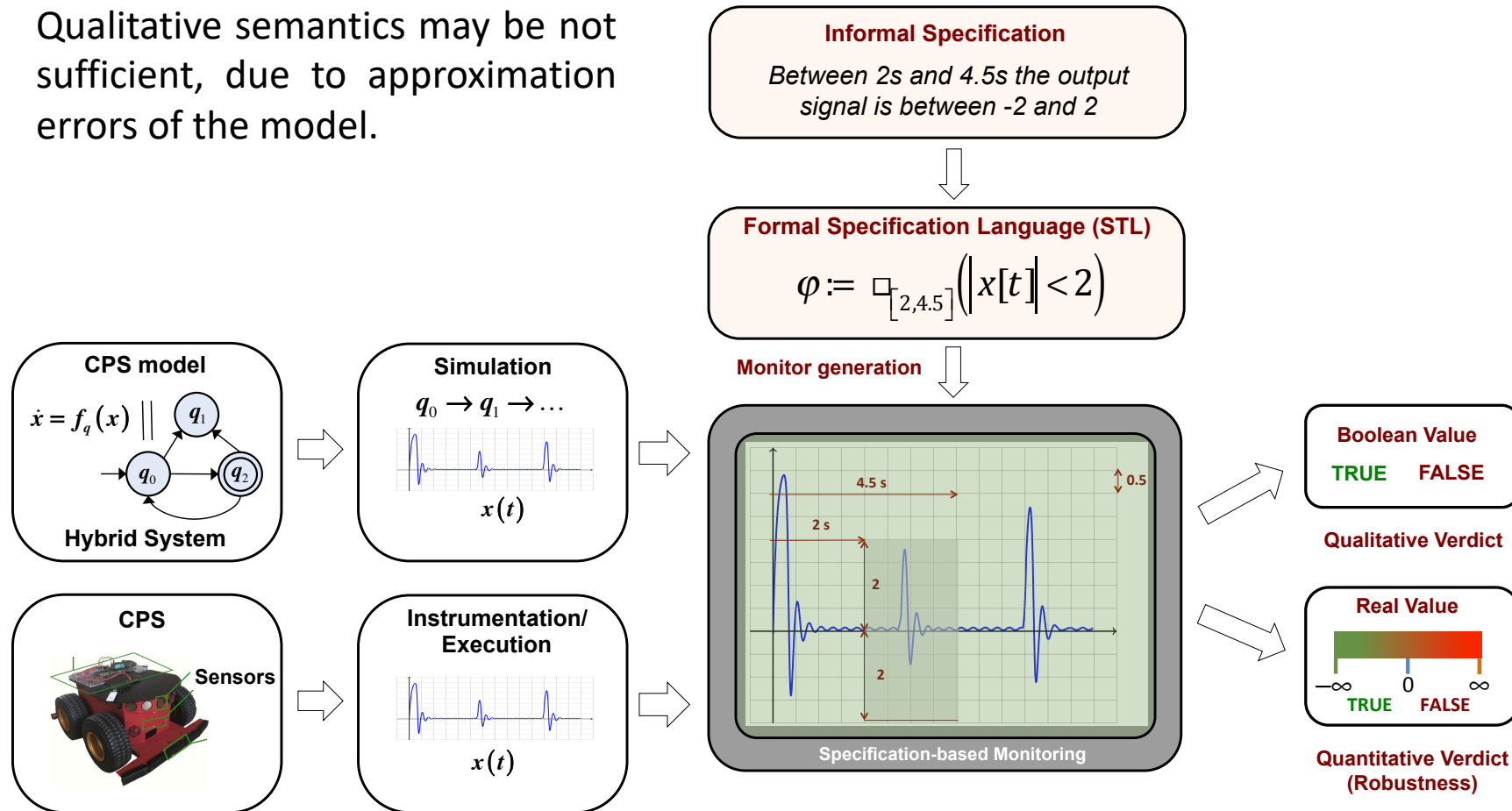
$$\mathbf{G}_{[0,600]} \left(\bigwedge_r \left((p(t) \in B_r) \Rightarrow \mathbf{F}_{[0,30]}(p(t) \notin B_r) \right) \right)$$

Specification-based Monitoring



Specification-based Monitoring

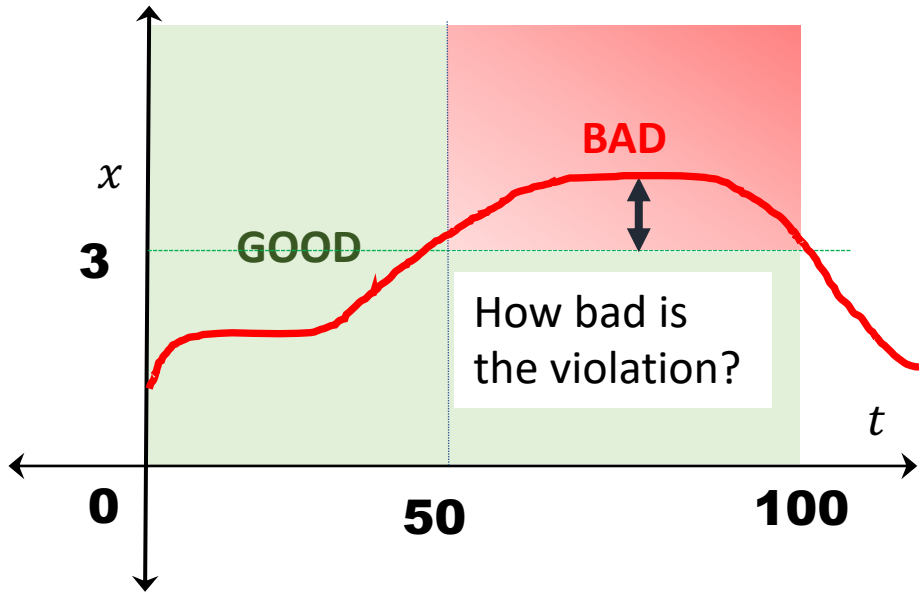
Qualitative semantics may be not sufficient, due to approximation errors of the model.



STL has quantitative semantics

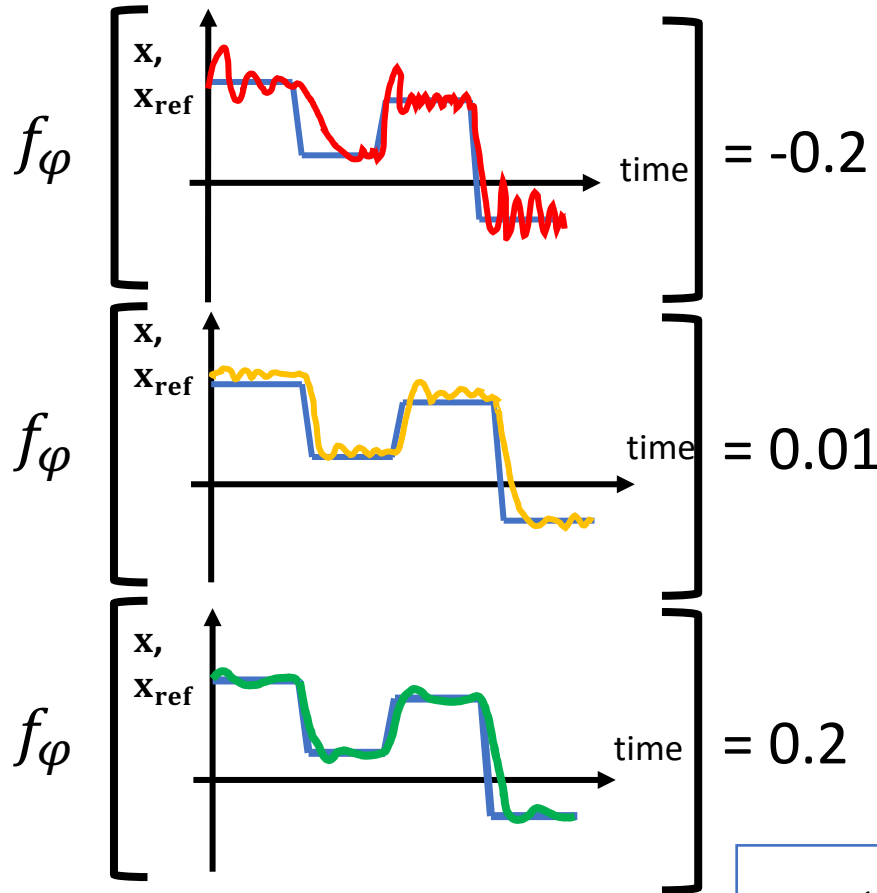
- ▶ Quantitative semantics defined using the notion of a *Robust Satisfaction Value*, or *Robustness Value*
- ▶ Robustness ρ is a function that maps
 - ▶ a given trace $\mathbf{x}(t)$,
 - ▶ a formula φ ,
 - ▶ and a time tto some real value
- ▶ We can interpret robustness as “distance to violation” of a given formula

Distance to violation/satisfaction



$$\mathbf{G}_{[50,100]}(x(t) < 3)$$

How do quantitative semantics help our engineer?



Uh Oh!

... should be okay

Looks good



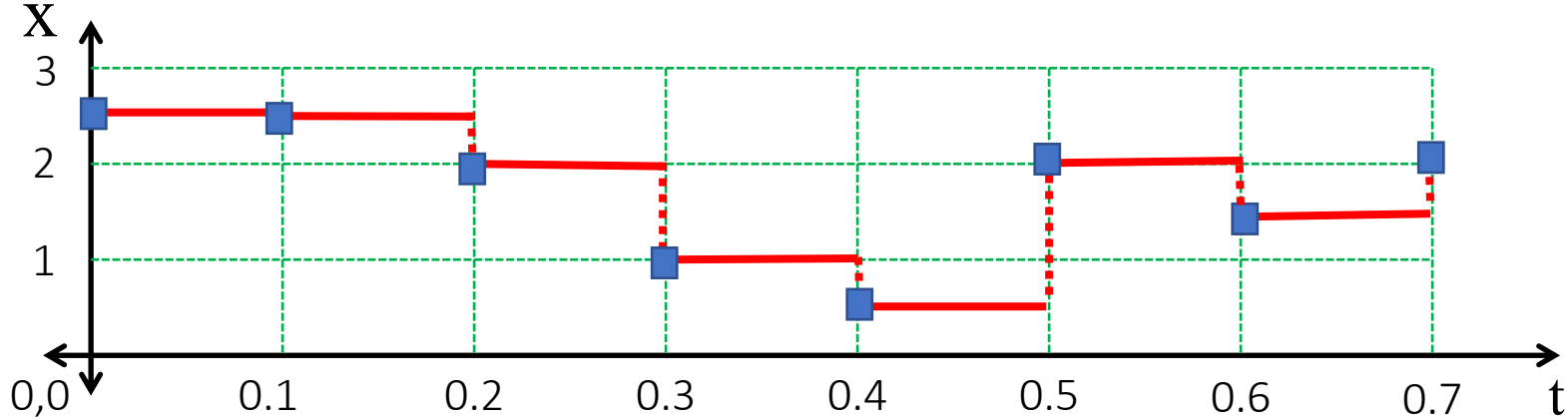
$$\varphi \equiv \text{Alw}_{[0,10]}(\text{step} \Rightarrow \text{Alw}_{[0,2]}(|x - x_{ref}| < 0.05))$$

Recursive Quantitative Semantics

 φ $\rho(\varphi, \mathbf{x}, t)$ $f(\mathbf{x}) > 0, f(\mathbf{x}) \geq 0 \quad f(\mathbf{x}(t))$ $\neg\varphi$ $-\rho(\varphi, \mathbf{x}, t)$ $\varphi_1 \wedge \varphi_2$ $\min(\rho(\varphi_1, \mathbf{x}, t) \wedge \rho(\varphi_2, \mathbf{x}, t))$ $\mathbf{F}_{[a,b]}\varphi$ $\sup_{\tau \in [t+a, t+b]} \rho(\varphi, \mathbf{x}, \tau)$ $\mathbf{G}_{[a,b]}\varphi$ $\inf_{\tau \in [t+a, t+b]} \rho(\varphi, \mathbf{x}, \tau)$ $\varphi \mathbf{U}_{[a,b]} \psi$ $\sup_{\tau \in [t+a, t+b]} \left(\min \left(\rho(\psi, \mathbf{x}, \tau), \inf_{\tau' \in [t, \tau]} \rho(\varphi, \mathbf{x}, \tau') \right) \right)$

Robustness computation example

$\varphi \equiv$
 $\mathbf{G}_{[0,0.7]} \mathbf{F}_{[0,0.2]} (x(t) > 1.5)$



$x(t) - 1.5$	1	1	0.5	-0.5	-1	0.5	0	0.5
$Ev_{[0,0.2]} \mu$	1	1	0.5	0.5	0.5	0.5		
$Alw_{[0,0.7]} Ev_{[0,0.2]} \mu$	0.5							

$f(x(t)) > 0$ at time t	$f(x(t))$
Always $_{[a,b]} \varphi$ at time t	Minimum over robustness of φ for $t' \in t \oplus [a, b]$
Eventually $_{[a,b]} \varphi$ at time t	Maximum over robustness of φ for $t' \in t \oplus [a, b]$

Property of Robust Satisfaction Signal

- ▶ Sign indicates satisfaction status (soundness):

$$\begin{aligned}\rho(\varphi, \mathbf{x}, t) > 0 &\Rightarrow \beta(\varphi, \mathbf{x}, t) = 1 \\ \rho(\varphi, \mathbf{x}, t) < 0 &\Rightarrow \beta(\varphi, \mathbf{x}, t) = 0\end{aligned}$$

- ▶ Absolute value indicates tolerance (correctness)

$$\|\mathbf{x} - \mathbf{x}'\|_{\infty} < \rho(\varphi, \mathbf{x}, t) \Rightarrow \beta(\varphi, \mathbf{x}, t) = \beta(\varphi, \mathbf{x}', t)$$

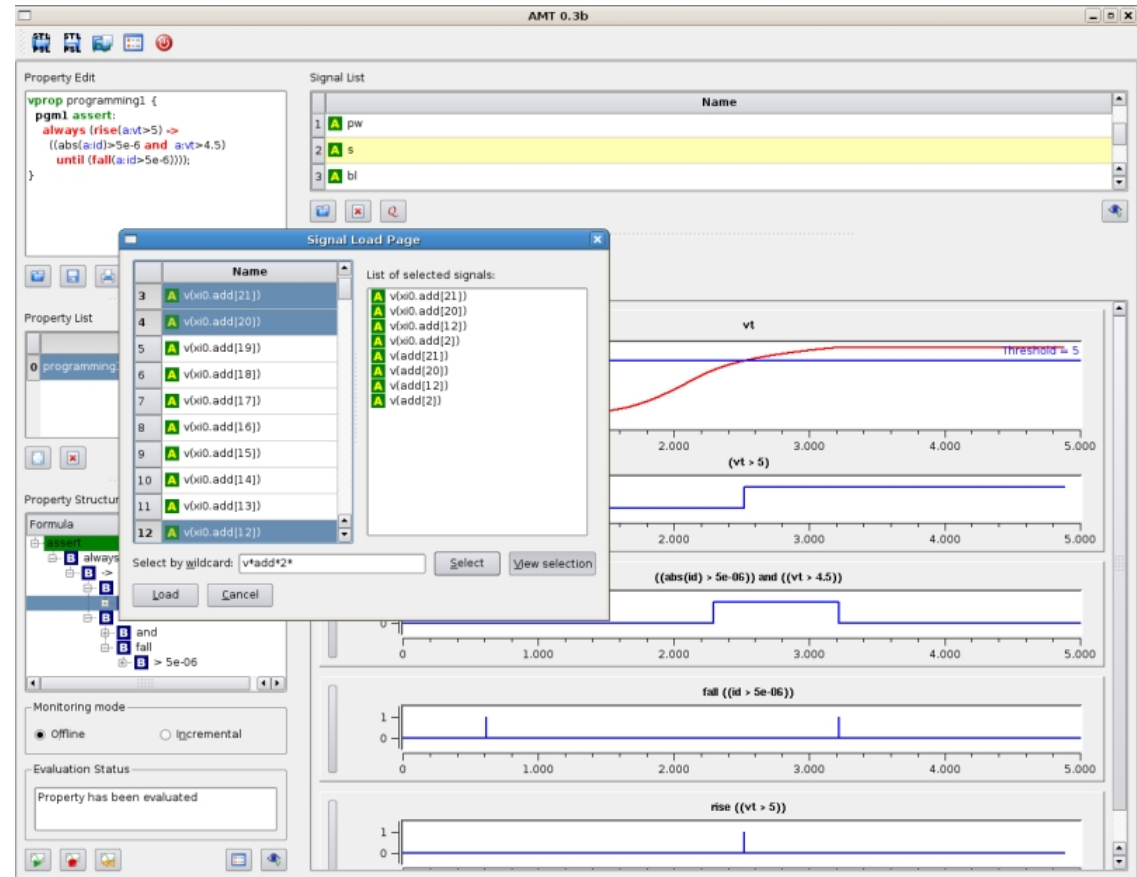
The many uses of STL

- ▶ Requirement-based testing for closed-loop control models
- ▶ Falsification Analysis
- ▶ Parameter Synthesis
- ▶ Mining Specifications/Requirements from Models
- ▶ Online Monitoring
- ▶ ...

Analog Monitoring Tool (AMT)

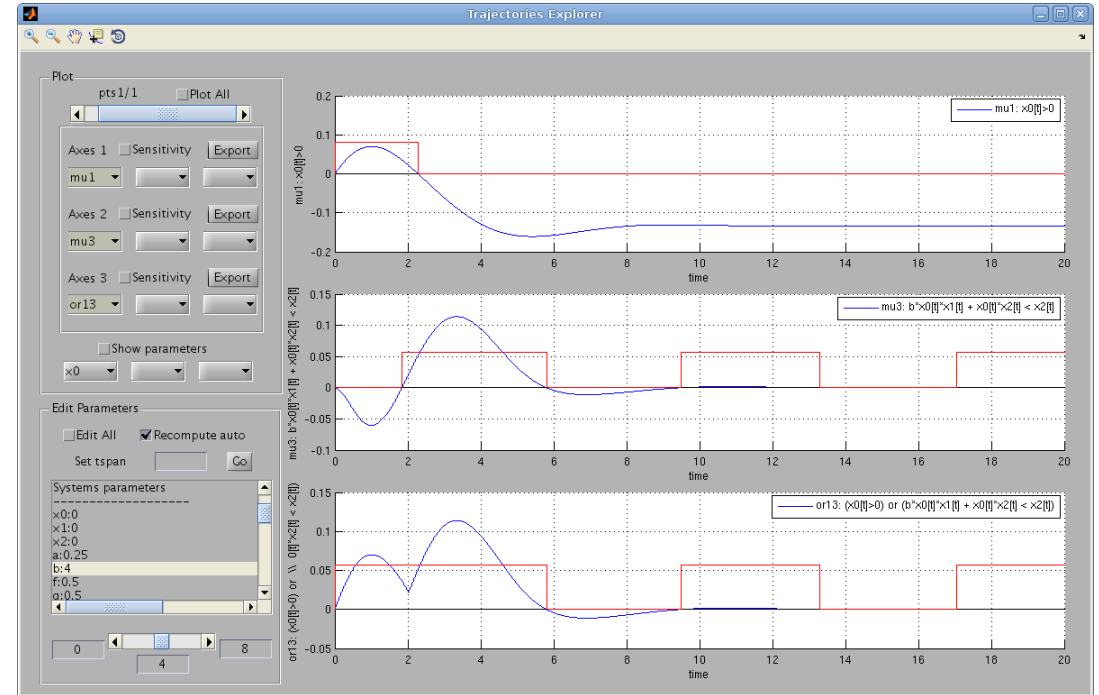
<http://www-verimag.imag.fr/DIST-TOOLS/TEMPO/AMT/content.html>

- ▶ STL with qualitative semantics
 - ▶ Correctness
- ▶ Offline monitoring
- ▶ Incremental monitoring



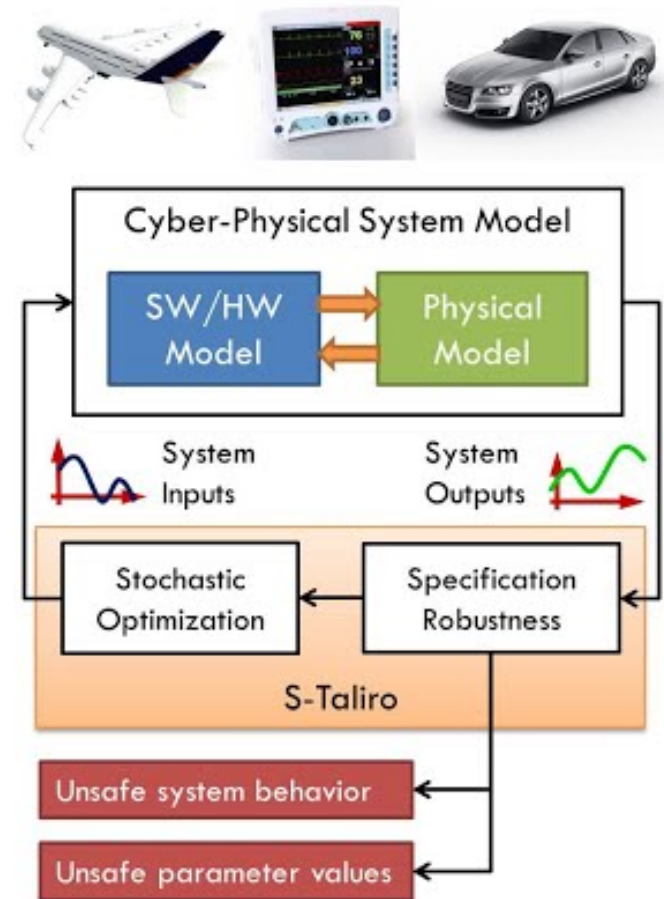
Breach

- ▶ MATLAB toolbox for
 - ▶ Simulation
 - ▶ Verification of temporal properties
 - ▶ Reachability
- ▶ STL with qualitative and quantitative semantics
 - ▶ Correctness
 - ▶ Robustness

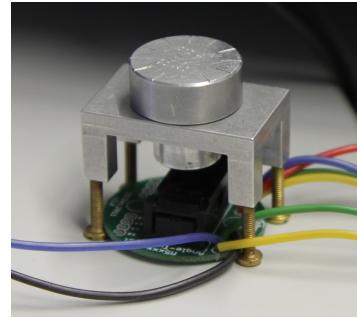
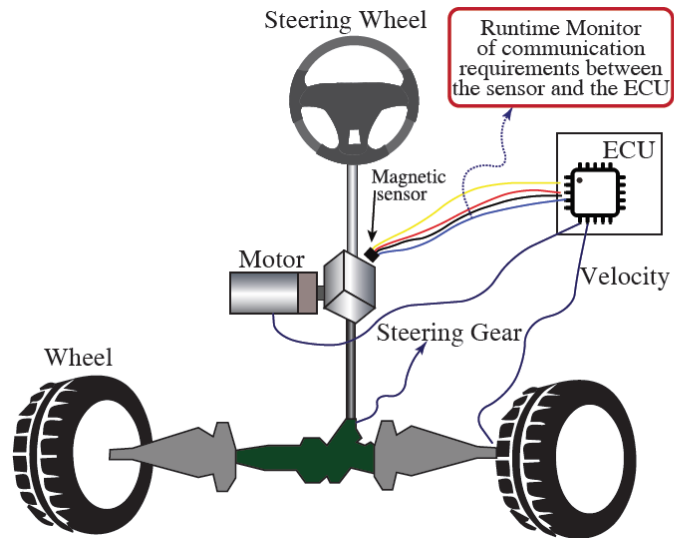


S-TaLiRo

- ▶ MATLAB toolbox for searching trajectories with minimal robustness
 - ▶ Randomized testing
 - ▶ Monte-Carlo simulation
 - ▶ Ant-colony optimization
 - ▶ Simulated annealing
 - ▶ Genetic algorithms
 - ▶ Cross entropy
- ▶ MTL with quantitative semantics
 - ▶ Robustness

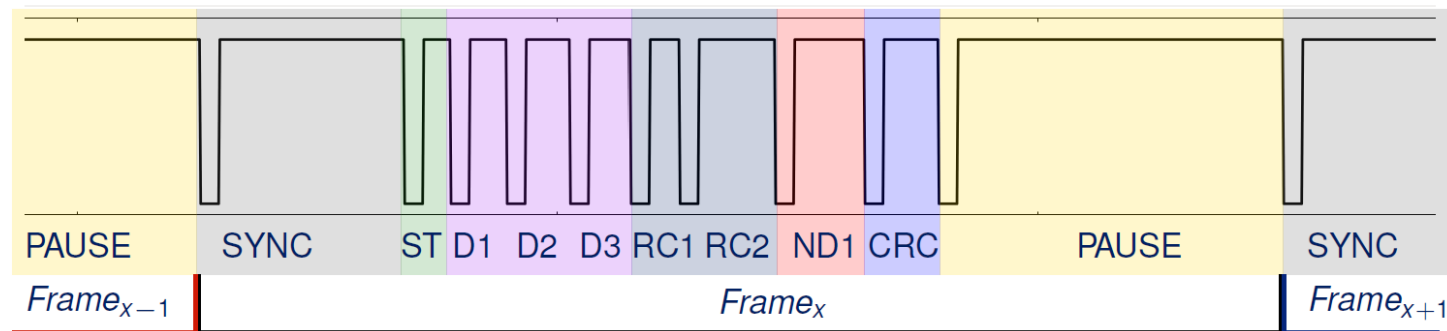


Hardware Monitoring of STL



Magnetic Angular Sensor

- Formalize SENT protocol requirements
 - STL & TRE
- Real-Time Correctness Monitors
 - With Recovery



Bibliography

1. G. Fainekos, and G. J. Pappas. *Robustness of temporal logic specifications for continuous-time signals*. Theoretical Computer Science 2009.
2. Maler, Oded, and Dejan Nickovic. "Monitoring temporal properties of continuous signals." Formal Techniques, Modelling and Analysis of Timed and Fault-Tolerant Systems. Springer, Berlin, Heidelberg, 2004. 152-166.
3. Donzé, Alexandre, and Oded Maler. "Robust satisfaction of temporal logic over real-valued signals." International Conference on Formal Modeling and Analysis of Timed Systems. Springer, Berlin, Heidelberg, 2010.