

# Cosmology 1

2019/2020  
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## Third intermediate test

Topic: early universe. Deadline: June 12, 14:00

This is an extended version of proposed problem 22 (exercise 3.2 of Vittorio textbook), a reposition of the argument proposed by Gamow, Alpher and Hermann in the 1940s to estimate the temperature of the CMB.

Start from the assumption that  $He$  is produced during the first minutes of life of the universe. You know that the present baryon density is  $n_{b0} \sim 10^{-7} \text{ cm}^{-3}$ , and that the cross section for deuterium formation is  $\sigma \sim 10^{-29} \text{ cm}^{-2}$ , but the CMB has not been detected yet. Deuterium forms when the age of the Universe is not much smaller than the interaction time-scale, and the temperature is low enough to limit the number of photons able to dissociate it. Follow this path:

- (a) assume that nucleosynthesis happens when the deuterium bottleneck opens at  $T_{\text{db}}$ ,
- (b) compute the age of a radiative universe  $t_u$  for that temperature,
- (c) work out the thermal speed of baryons at that temperature,
- (d) the timescale for deuterium formation is  $t_d \sim 1/n_b \sigma v$ , where  $n_b$  is the baryon number density at nucleosynthesis time,
- (e) deuterium production starts when the age of the universe is  $t_u \sim t_d$ ,
- (f) CMB temperature evolves like  $T = T_0 a^{-1}$ ,
- (g) baryon density evolves like  $n = n_0 a^{-3}$ .

This allows to work out a relation between the CMB temperature today  $T_0$  and the temperature of deuterium bottleneck opening  $T_{\text{db}}$ . Another relation is obtained when the leading term of the Saha equation  $\exp(-B_d/k_B T_{\text{db}})$  is of the same order of the ratio  $\eta$  of baryon and photon number densities.

Use these two relations to find both  $T_0$  (in K) and  $T_{\text{db}}$  (in keV). Try also to argue how a neutrino component would change the result. Two pages of text will be enough to present the result.