

# Statistical mechanics

Emanuele Coccia

Dipartimento di Scienze Chimiche e Farmaceutiche

- ecoccia@units.it
- C11 building, fourth floor, room 453/454
- Wednesday 15h-17h (or whenever you want, just send an email to me)
- Register on Moodle
- Teams group:
  - "597SM - STATISTICAL MECHANICS - COCCIA EMANUELE (2020)"
  - Search it on <https://corsi.units.it/didattica-a-distanza> (insert "Coccia")

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- Definition of statistical mechanics and concepts of thermodynamics

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- Computational methods: molecular dynamics, Monte Carlo

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- Computational methods: molecular dynamics, Monte Carlo
- Quantum ideal gas: Fermi-Dirac and Bose-Einstein statistics

# Where studying

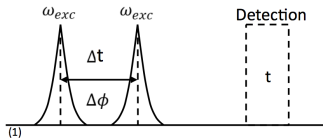
- Lesson notes
- *Statistical mechanics: A concise introduction for chemists*, Benjamin Widom, Cambridge
- Notes on Moodle
- “Extra”: *An Introduction to Statistical Thermodynamics*, Terrell L. Hill, Dover Publications



- Oral exam: (at least) three questions, possible simple numerical problems to solve
- Exam done in a lecture room (two rounds in winter session, two rounds in summer session, one round in september)

Simulating **time-resolved ultrafast spectroscopies**:  
role of **quantum coherence** in molecules,  
metallic clusters and nanostructures

Collaboration with the University of Padova

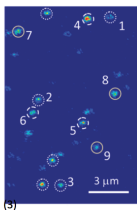


**Ultrafast Spectroscopy**

Ultrashort pulses to interrogate system dynamics  
Femtosecond timescale processes

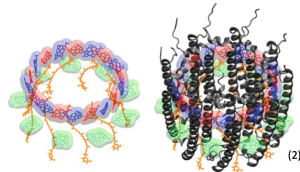
**Coherence**

Superposition of quantum states



**Single Molecules**

High spatial resolution  
Prevent intrinsic inhomogeneity of molecules



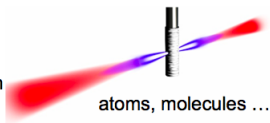
Simulating nonlinear optical responses in strong electric fields: **high-harmonic generation** spectroscopy of molecules ( $H_2$ ,  $CO_2$ , thymine, uracil, benzene etc.)

Collaboration with Sorbonne University in Paris (TCCM)

# HHG is a nonlinear optical process

**Laser source:**

$\omega_L = 800 \text{ nm}$   
 $10^{14}\text{-}10^{15} \text{ W/cm}^2$   
linear polarization

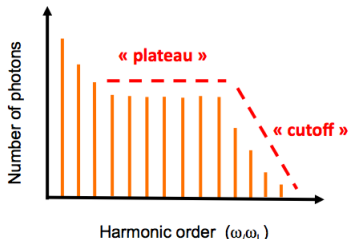


- Energy: *XUV/Soft-X rays*
- Temporal resolution: *attosecond pulses*

P. M. Paul et al. Nature **414**, 509 (2001)

**Harmonic spectrum**

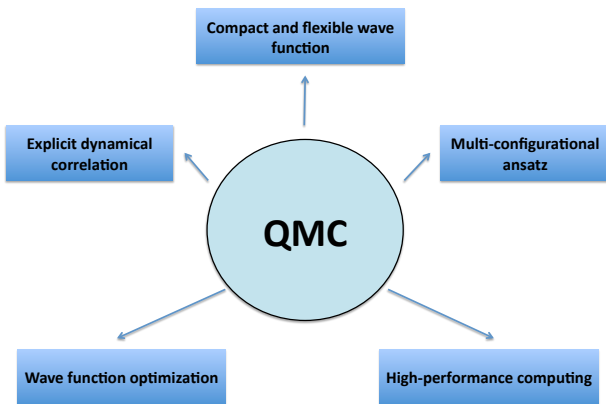
LASER output



McPherson et al.  
JOSA B **4**, 595 (1987)

# Development and application of quantum Monte Carlo methods to the computation of electronic ground- and excited-state properties of molecules

Collaboration with Sorbonne University in Paris (TCCM)



- **Pros:** Accurate, parallel,  $N_{\text{el}}^3 - N_{\text{el}}^4$
- **Cons:** prefactor, error, no “black-box”