

ISTITUZIONI DI FISICA PER IL SISTEMA TERRA

IFST
(138SM)

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System

- 👁️ A **system** is a set of interacting or interdependent component parts forming a complex/intricate whole
- 👁️ Every system is delineated by its spatial and temporal boundaries, surrounded and influenced by its environment, described by its structure and purpose and expressed in its functioning
- 👁️ In engineering and physics, a physical system is the portion of the universe that is being studied (of which a thermodynamic system is one major example)
- 👁️ An **open system** exchanges matter and energy with its surroundings. A **closed system** exchanges energy, but not matter, with its environment; like Earth. An **isolated system** exchanges neither matter nor energy with its environment

<http://www.merriam-webster.com/dictionary/system>

Citation: Pidwirny, M. (2006). "Definitions of Systems and Models".

<http://www.physicalgeography.net/fundamentals/4b.html>

What is a System?

🌀 Systems

🌀 a group of interacting parts that work together to do a job or to form a whole.

🌀 Open Systems

🌀 Closed Systems



What is a System?

Systems

Open System

Matter and energy can flow into and out of the system.

Uncovered pan of boiling water.

Vegetable Garden

Natural Environment



What is a System?

🌀 Systems

🌀 Closed System

🌀 Matter cannot enter or leave, energy can.

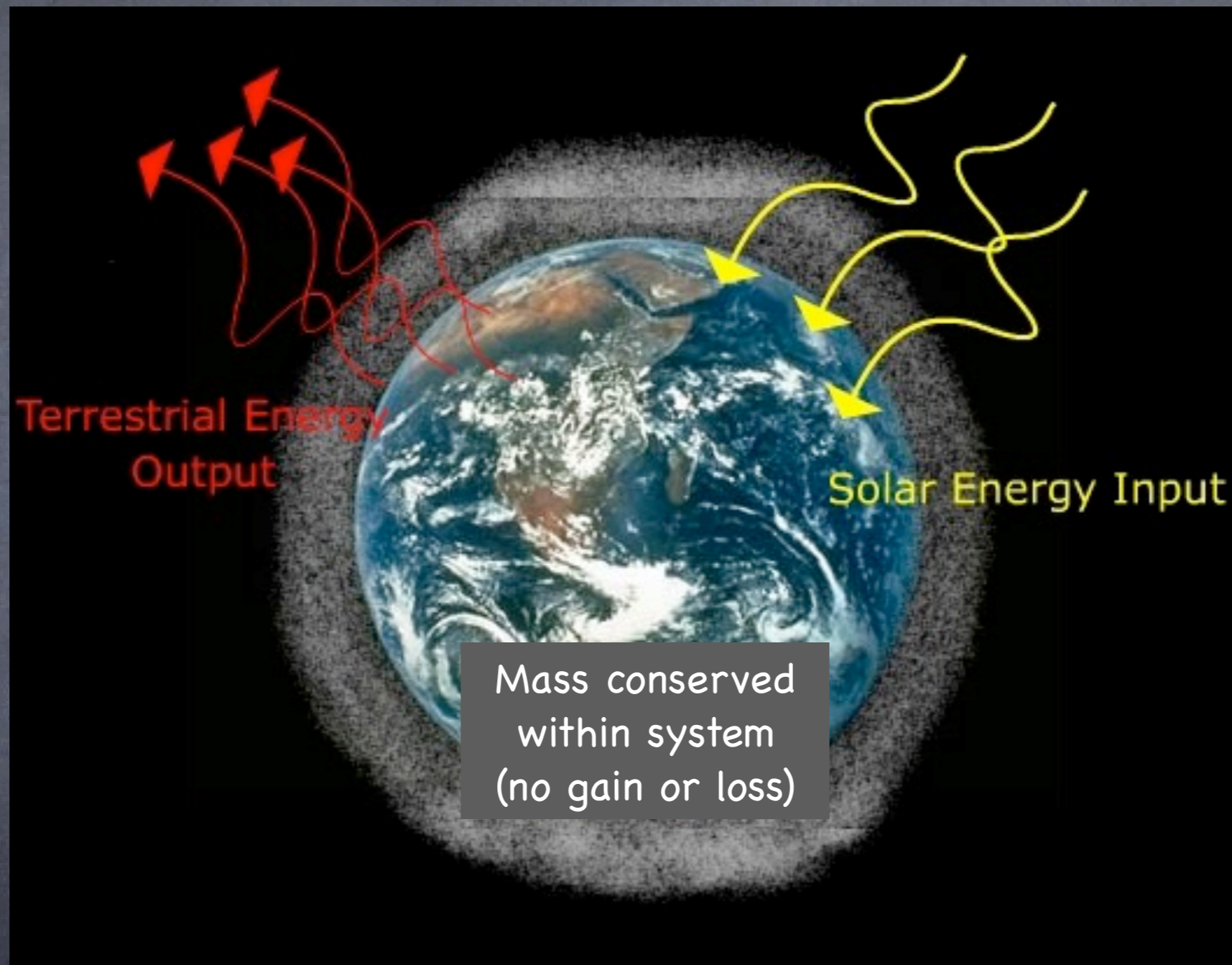
🌀 Covered pan of boiling water.

🌀 Terrarium

🌀 Greenhouse



Earth as a closed System



Closed system: exchange of energy but negligible exchange of mass with surroundings

Earth System Physics

- ① Study the processes and interactions (cycles) among the **atmosphere, hydrosphere, cryosphere, biosphere, and geosphere** from a global to local point-of-view, and across the time scales (minutes to eons) in which these spheres interact.
- ② It requires the use of **physical and chemical laws** with mathematics to describe the physical, chemical and biological processes within each sphere and the interactions between the spheres.
- ③ These descriptions are used along with observations to construct **models** through which complex interactions of the spheres are studied.
- ④ It is through the understanding of these complex interactions that accurate, **predictive models** are developed.

Earth System

Earth System

A complex system made up of:

Matter

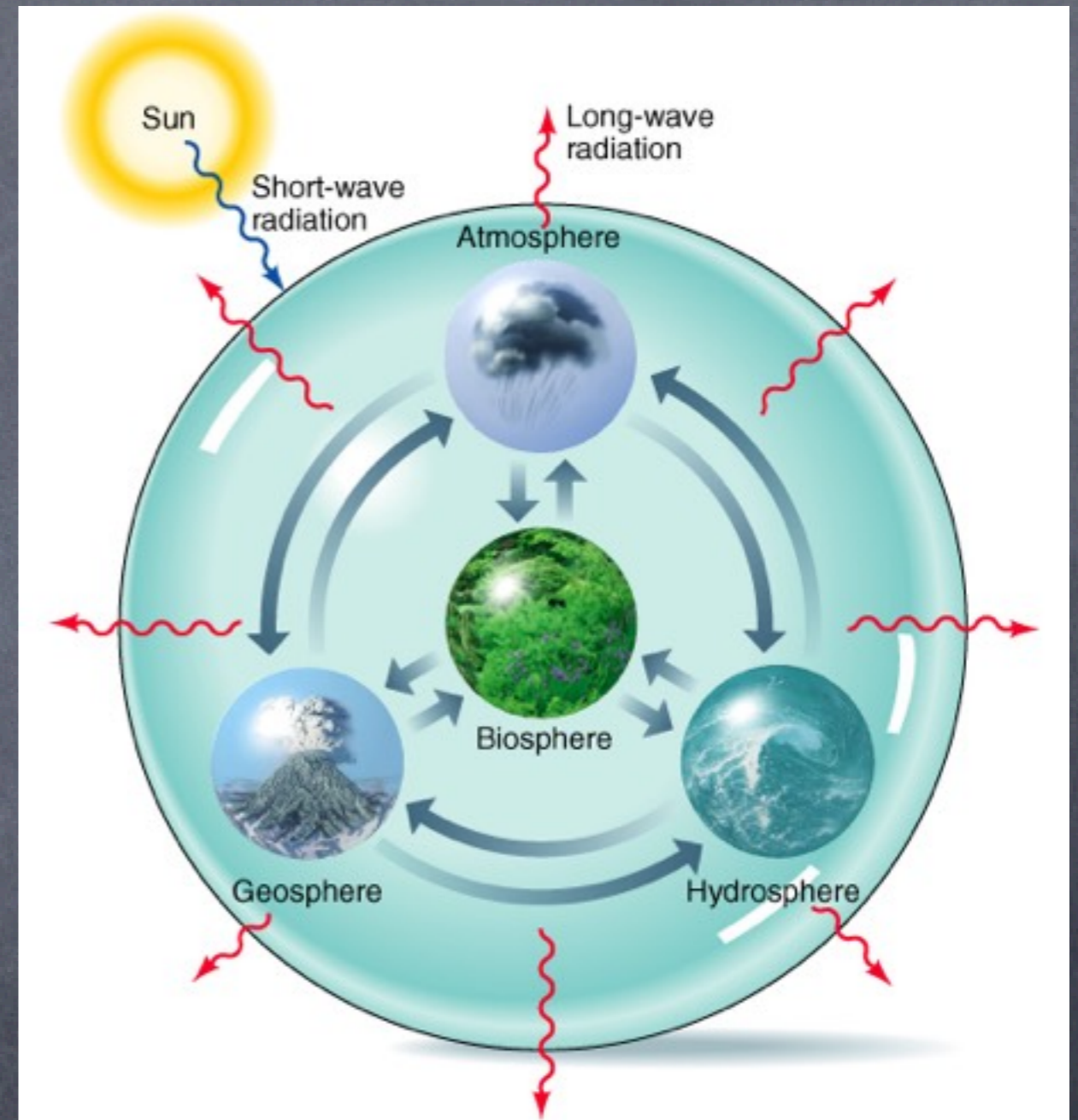
Living Things

Nonliving things.

Energy

Processes within Earth's

Matter and energy continuously cycled through the smaller systems that make up Earth's spheres.



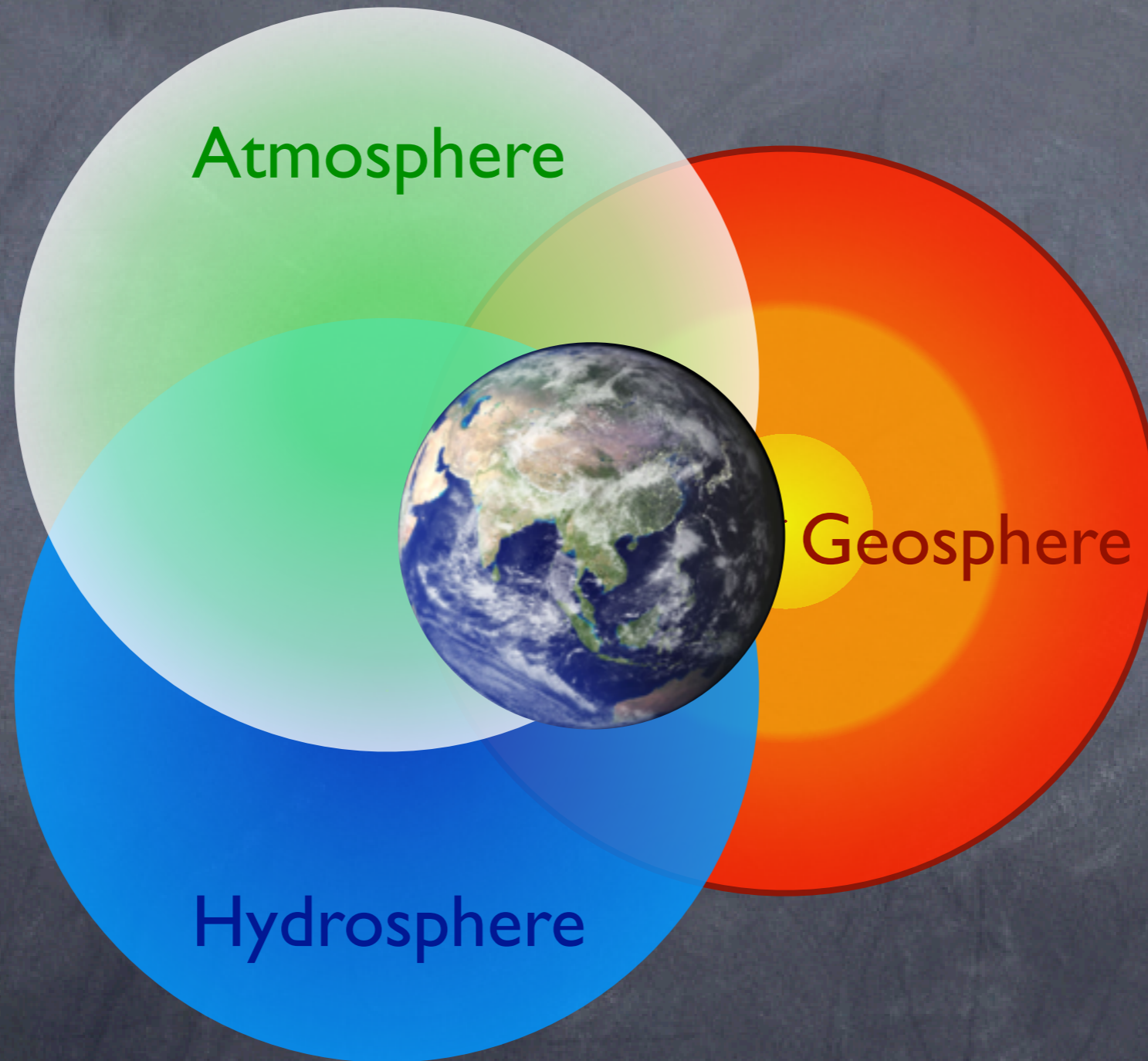
Major Themes

Scale Processes in the Earth system act on length scales of microns to thousands of kilometers, and on time scales of milliseconds to millions of years.

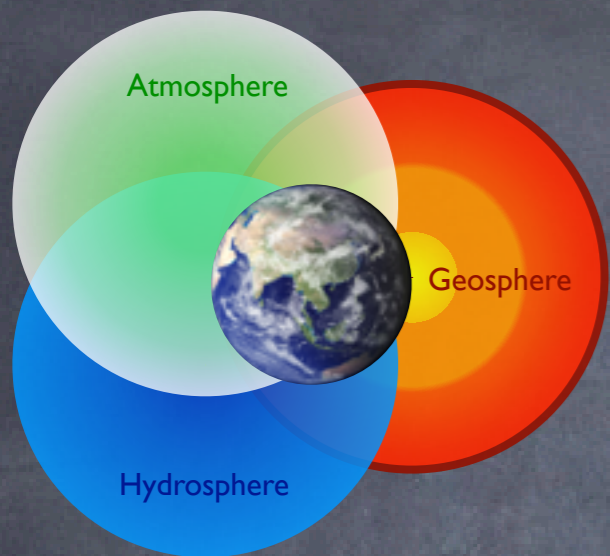
Energy The Earth system is powered by one external source (the Sun) and two internal ones: radioactive decay, and gravitational energy (heat still being lost from planetary formation).

Cycles Material in the Earth system is continually recycled in numerous overlapping cycles.

Earth system



Earth system

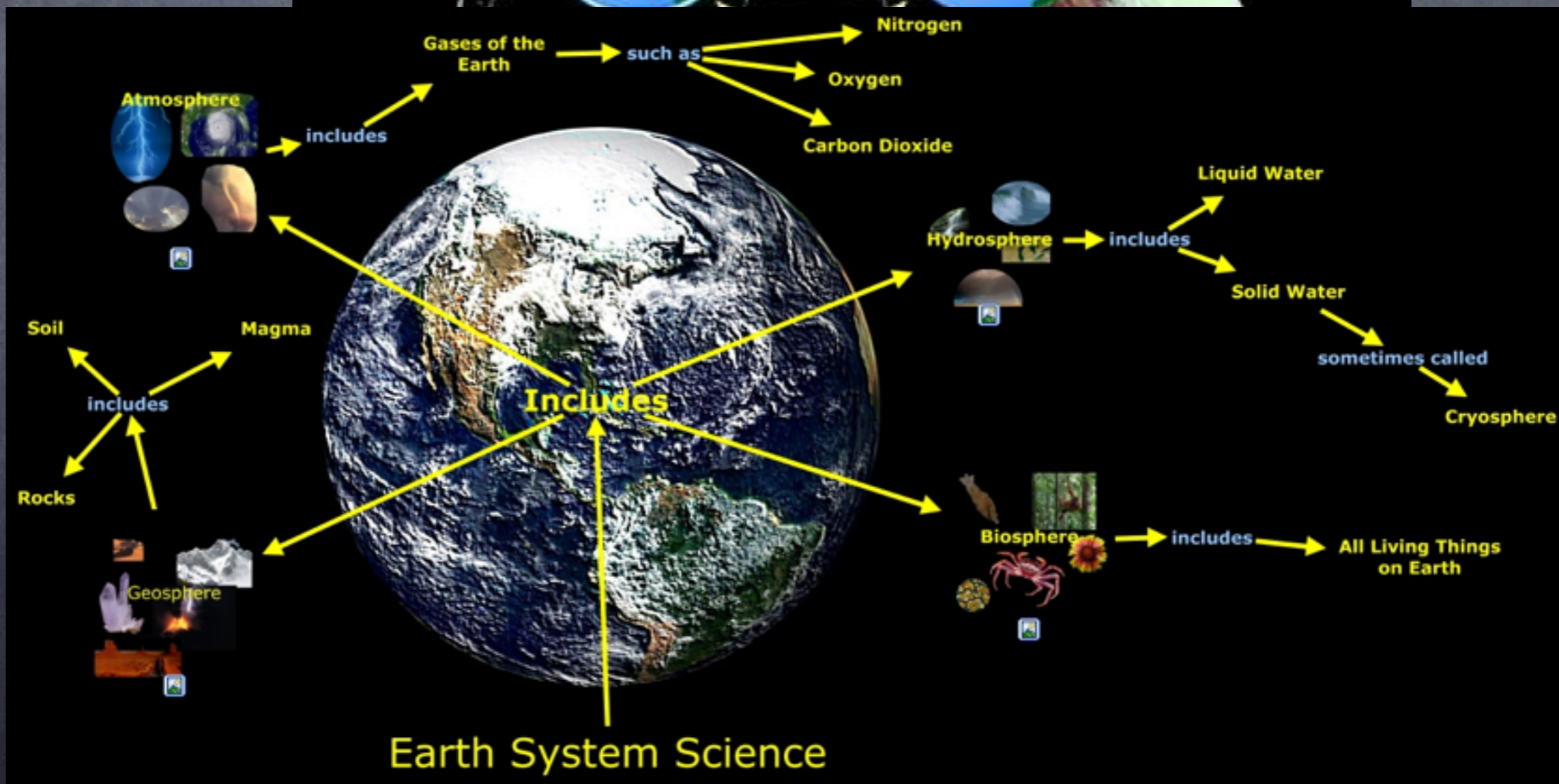


The Atmosphere

This part of the Earth System includes the mixture of gases that surround the planet.

The Biosphere

This part of the Earth System includes all living things, including plants, animals, and other organisms.



What is the Earth's Geosphere?

Geosphere

Mostly solid, rocky part of the Earth.

Divided into 3 Layers

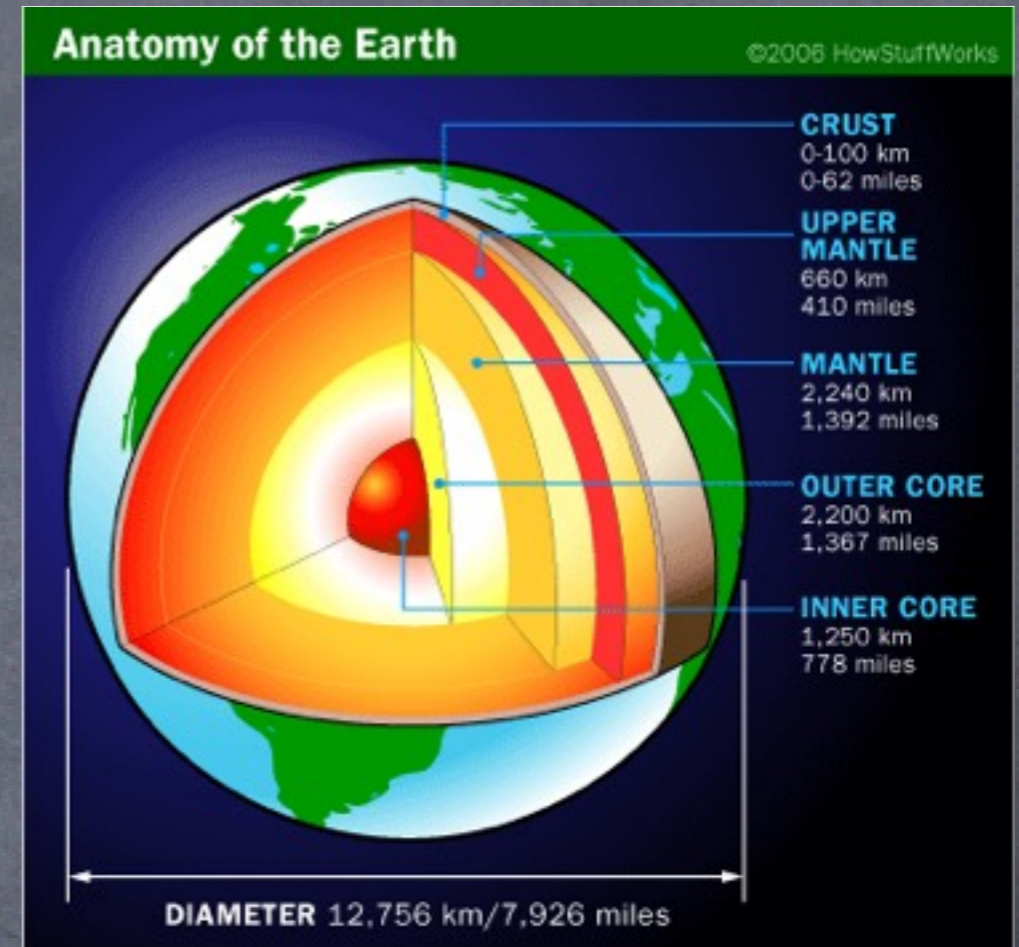
1. Crust

2. Mantle

3. Core

a. Inner Core

b. Outer Core



What is the Earth's Hydrosphere?

Hydrosphere

- Part of the Earth that is liquid water.
- Always moving, through all spheres.
- 71% of Earth's surface is the ocean.
- Lakes, Rivers, Marshes
- Rain
- Underground water
- Droplets in clouds.



What is the Earth's Cryosphere?

🌀 Cryosphere

🌀 Made up of all frozen water on Earth.

🌀 Ice

🌀 Sea Ice

🌀 Glaciers

🌀 Ice Shelves

🌀 Ice Bergs

🌀 Snow



What is the Earth's Atmosphere?

👁 Atmosphere

👁 Mostly made of invisible gases that surround the Earth

👁 Contains the air we breathe

👁 Composition

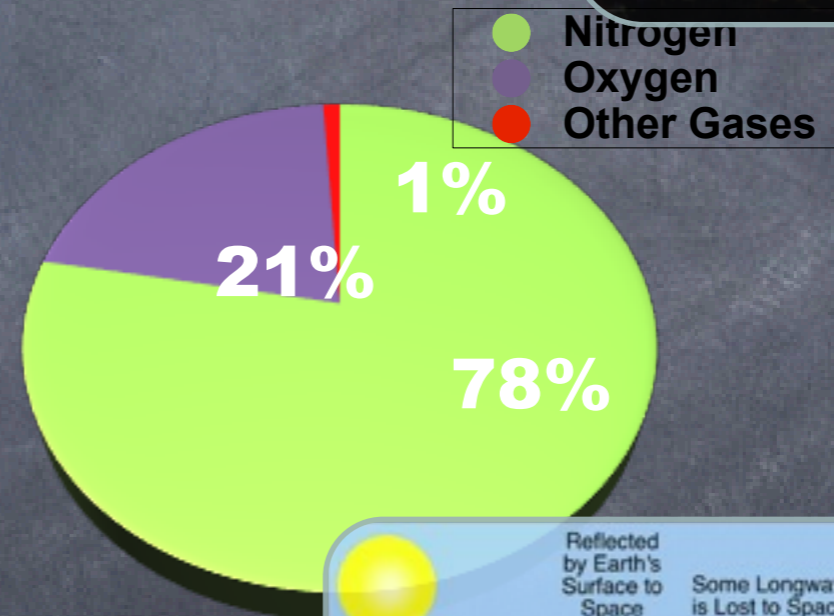
👁 71% Nitrogen

👁 23% Oxygen

👁 1% Trace Gases

👁 Traps Heat Energy from the sun

👁 Greenhouse effect, keeps the planet warm



What is the Earth's Biosphere?

🌀 Biosphere

🌀 Made up of living things and their habitats

🌀 Must Have:

🌀 Oxygen

🌀 Carbon Dioxide

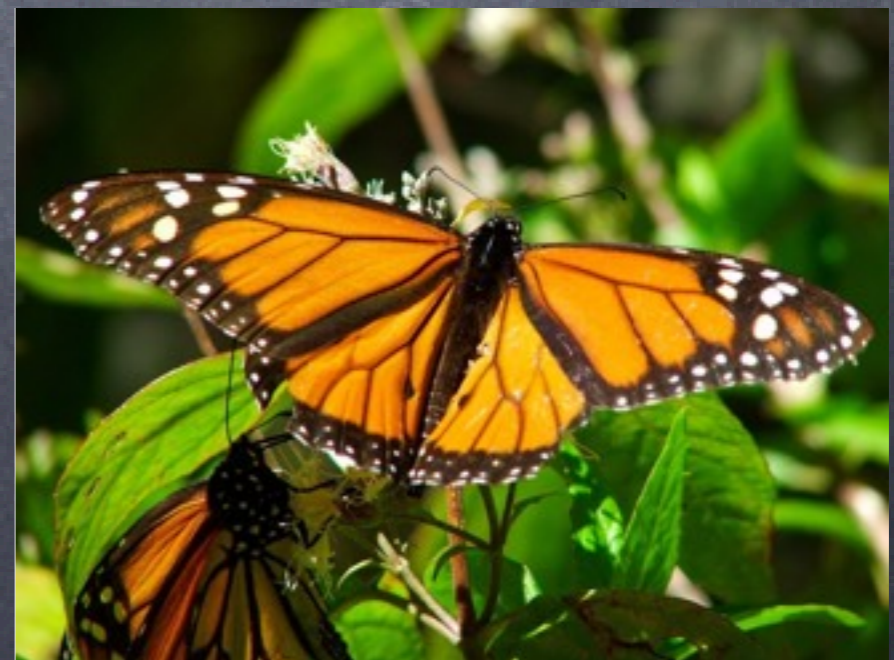
🌀 Liquid Water

🌀 Moderate Temperatures

🌀 Source of Energy

🌀 Sun

🌀 Plants and Algae (photosynthesis)



How Do Earth's Spheres Interact?

Matter and Energy

1. By exchange of matter

Water Cycle

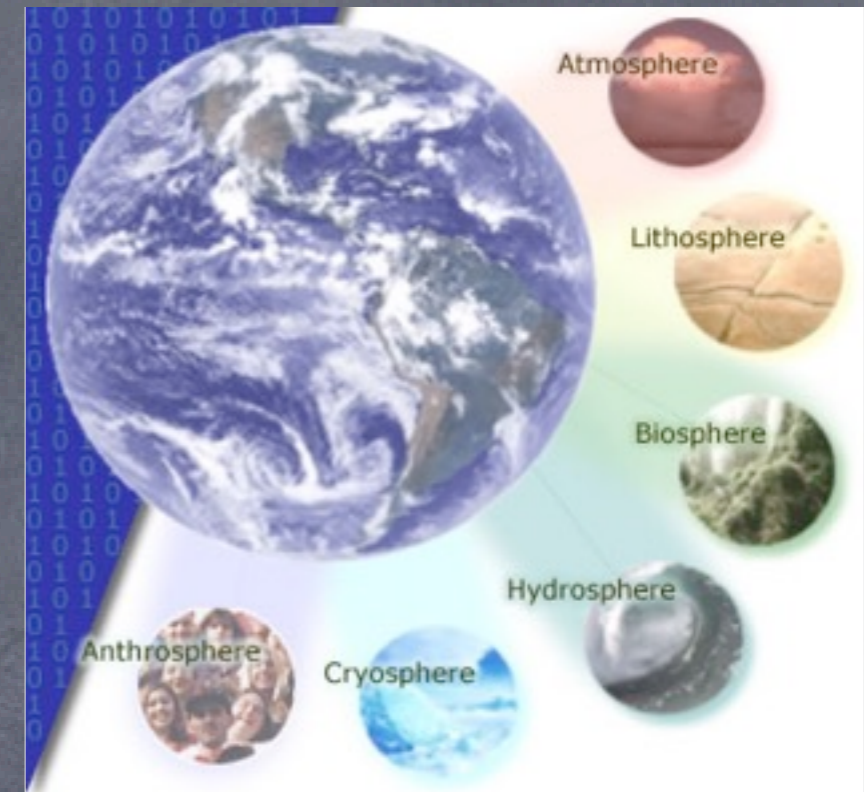
Water evaporates into the atmosphere

Water condenses forming clouds

Nitrogen Cycle

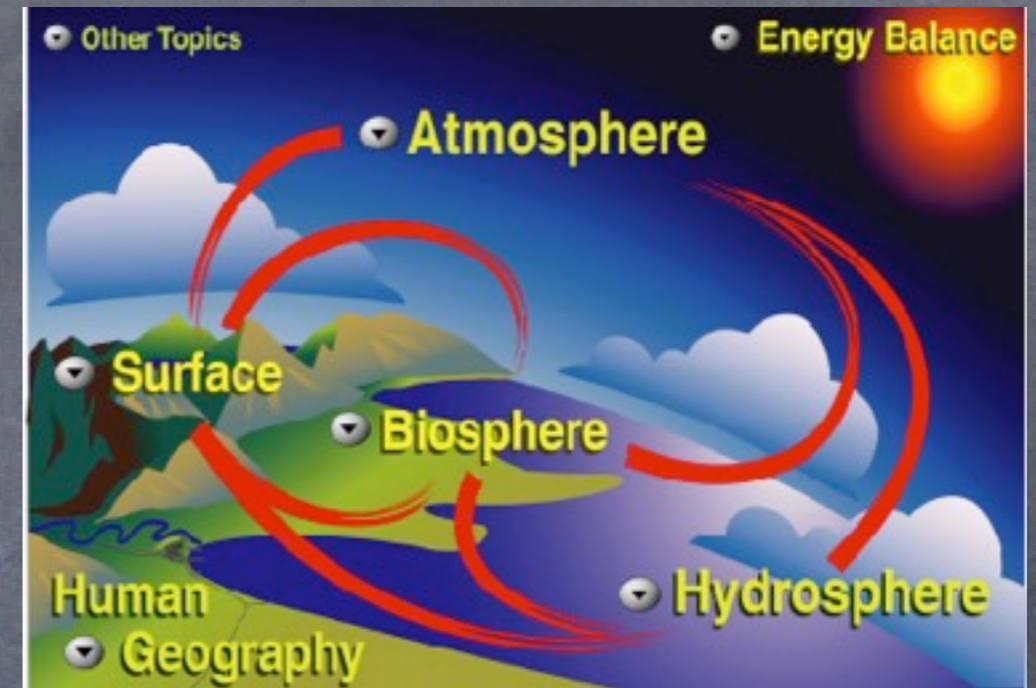
Bacteria release nitrogen into the soil from the atmosphere

Plants use nitrogen to grow



How Do Earth's Spheres Interact?

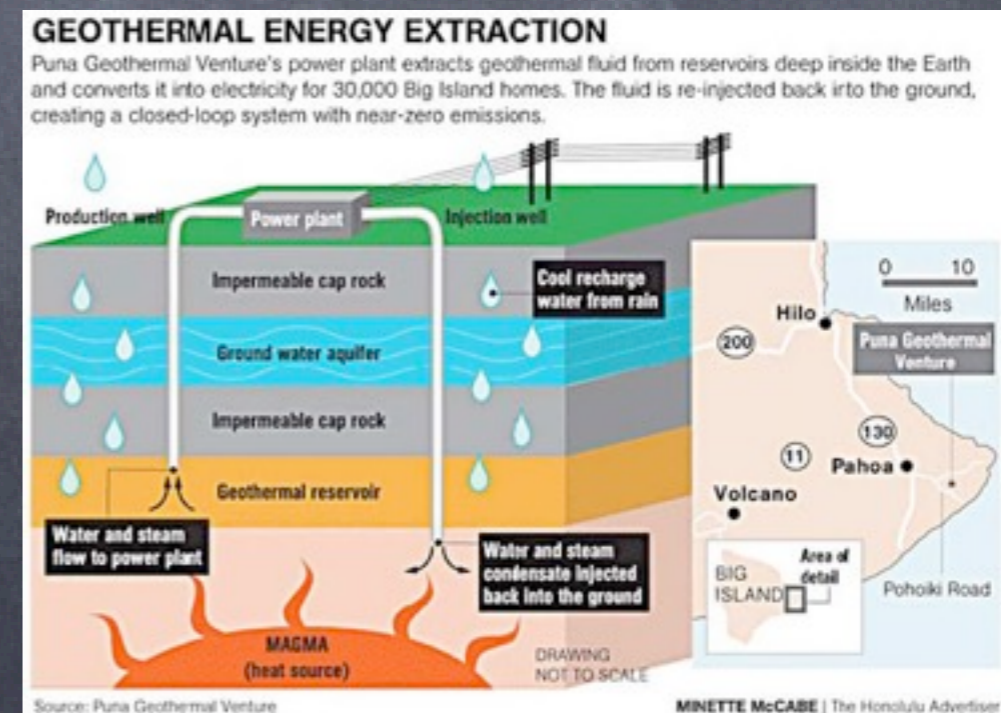
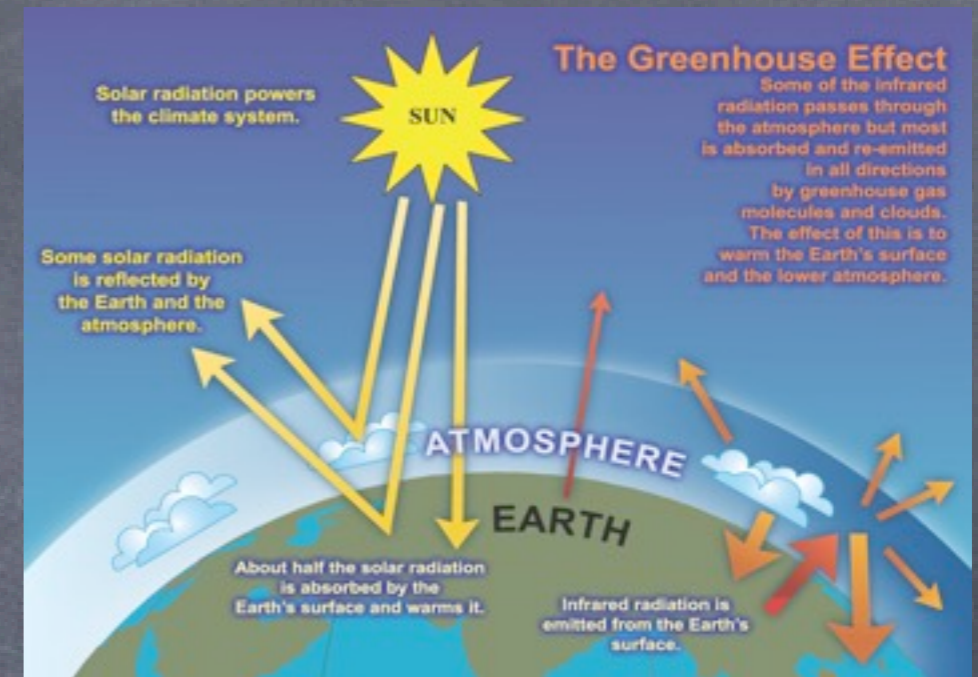
- 2. By exchange of energy
 - Moves back and forth between spheres
 - Plants use solar energy to make food
 - Animals eat plants for energy
 - Solar Energy
 - Drives winds and Weather



Source of Earth's Energy?

Earth's Energy

- Most comes from the Sun
- A tiny fraction
- Ocean Tides
- Geothermal
- Lava & Magma
- Moves or Changes form
- Not created or destroyed
- Transferred between spheres



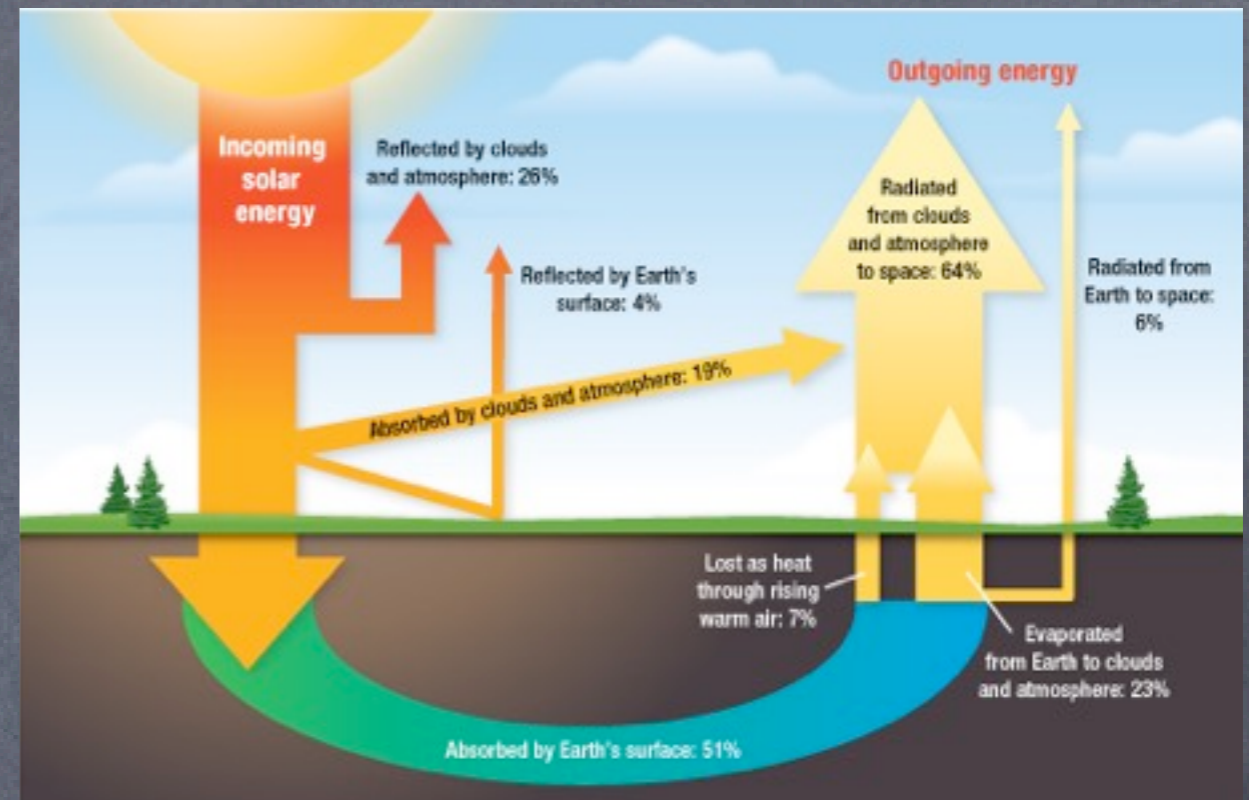
Source of Earth's Energy?

Energy Budget

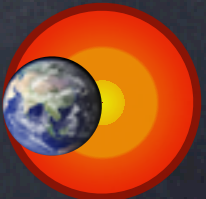
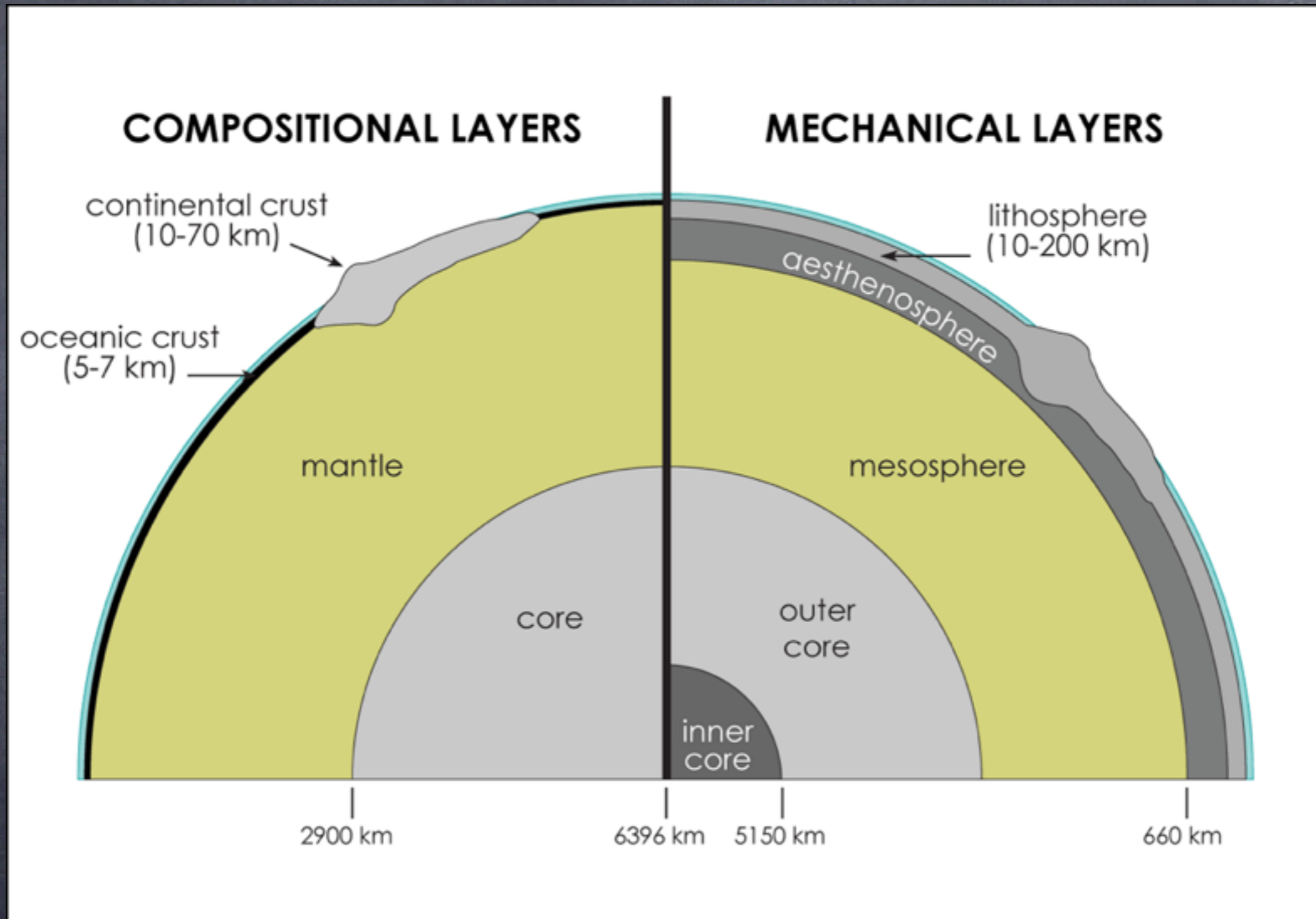
A way to keep track of energy transfers into and out of Earth's system

Unbalanced budget

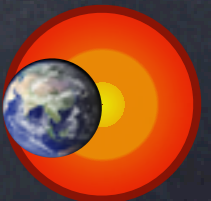
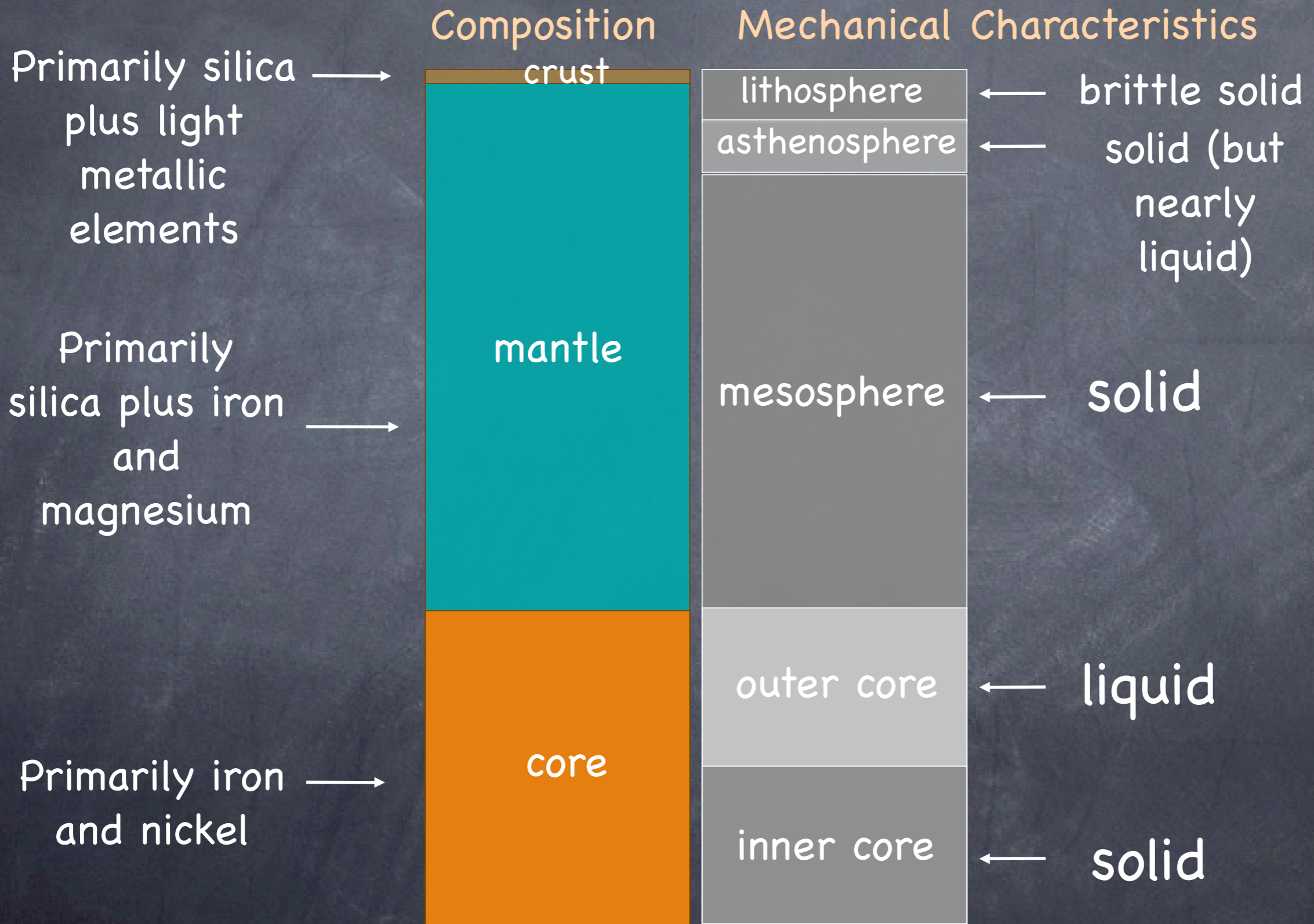
Can increase or decrease Earth's temperatures

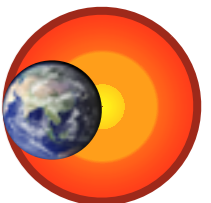
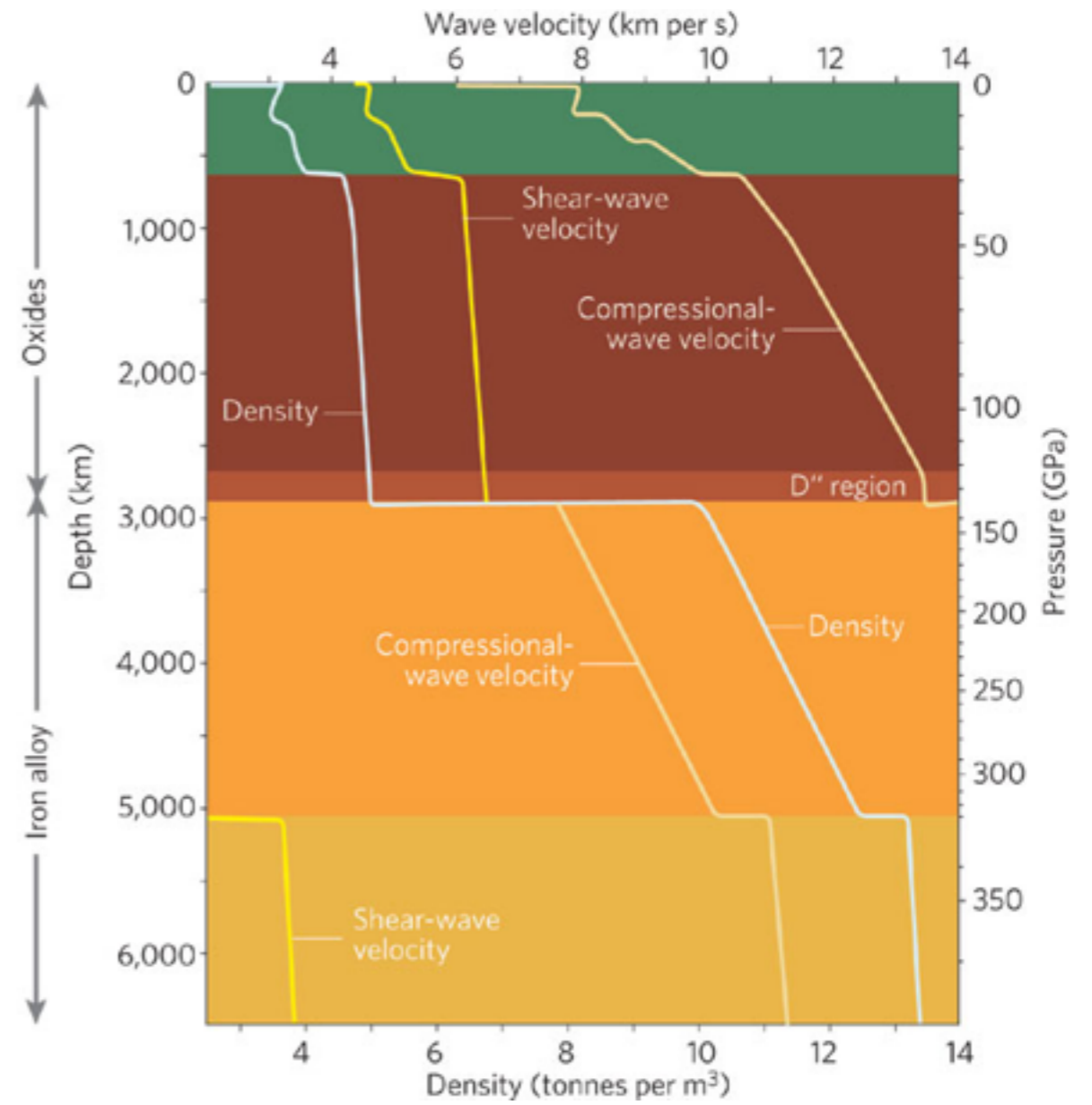
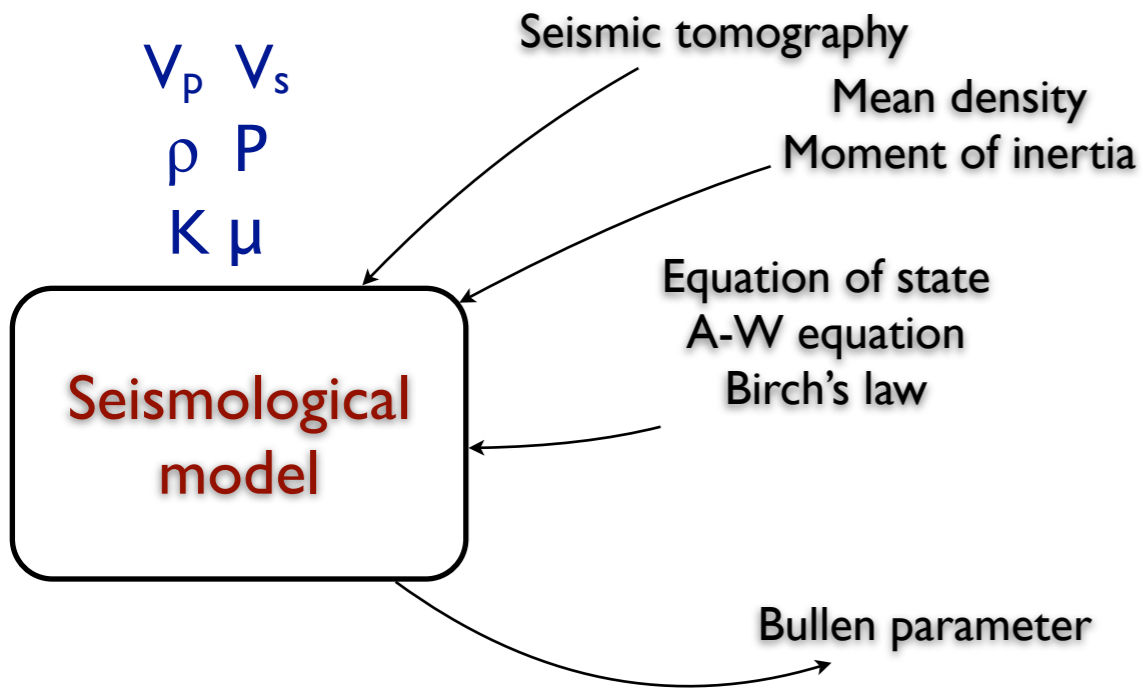


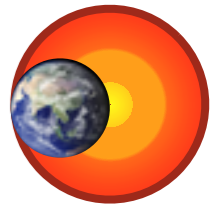
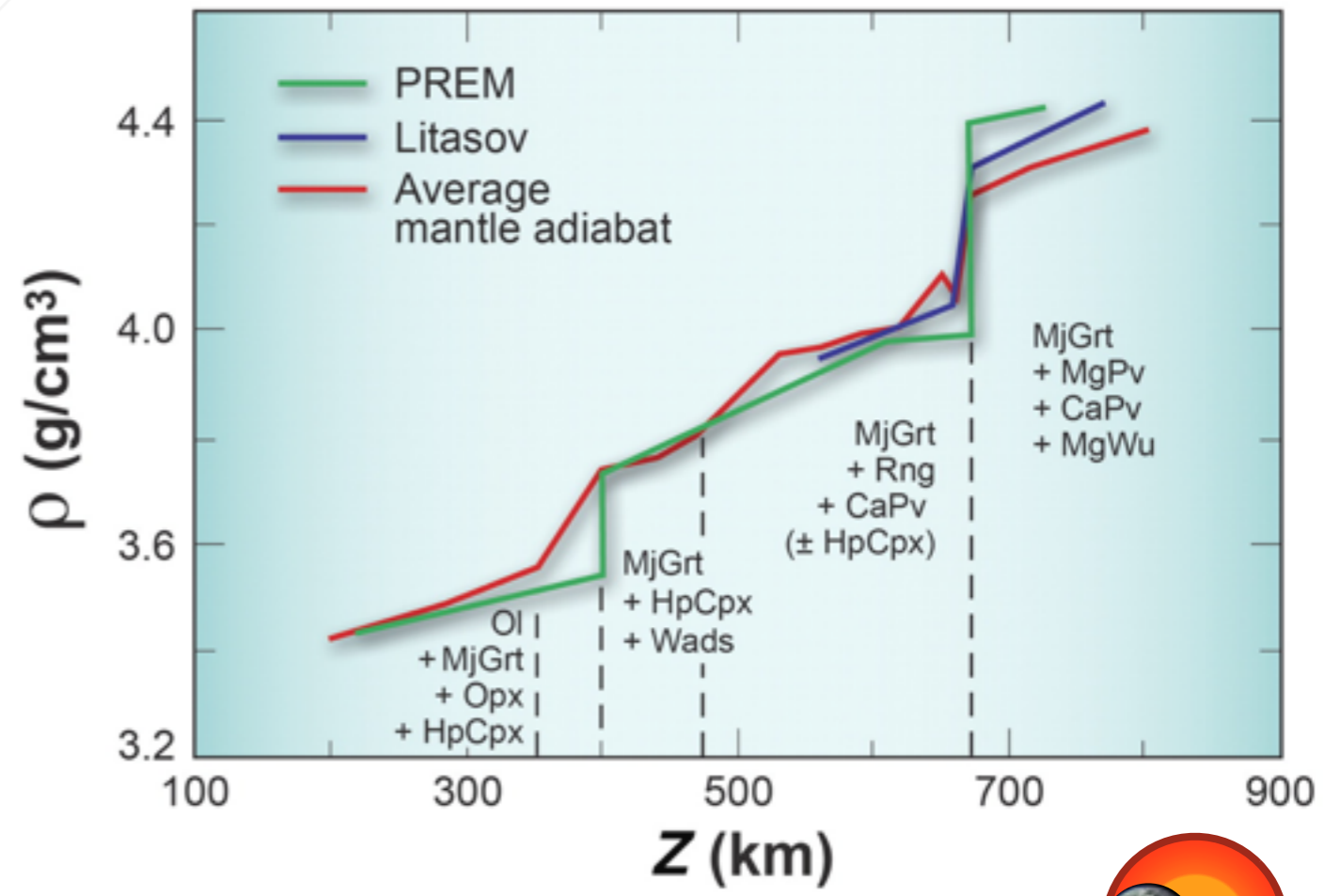
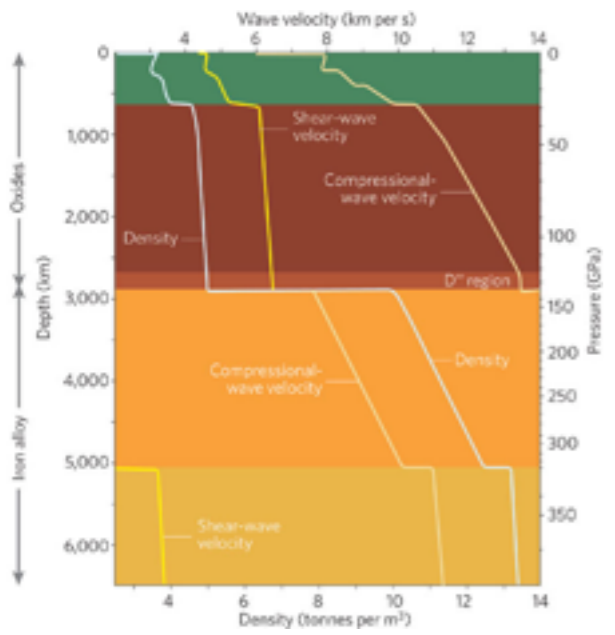
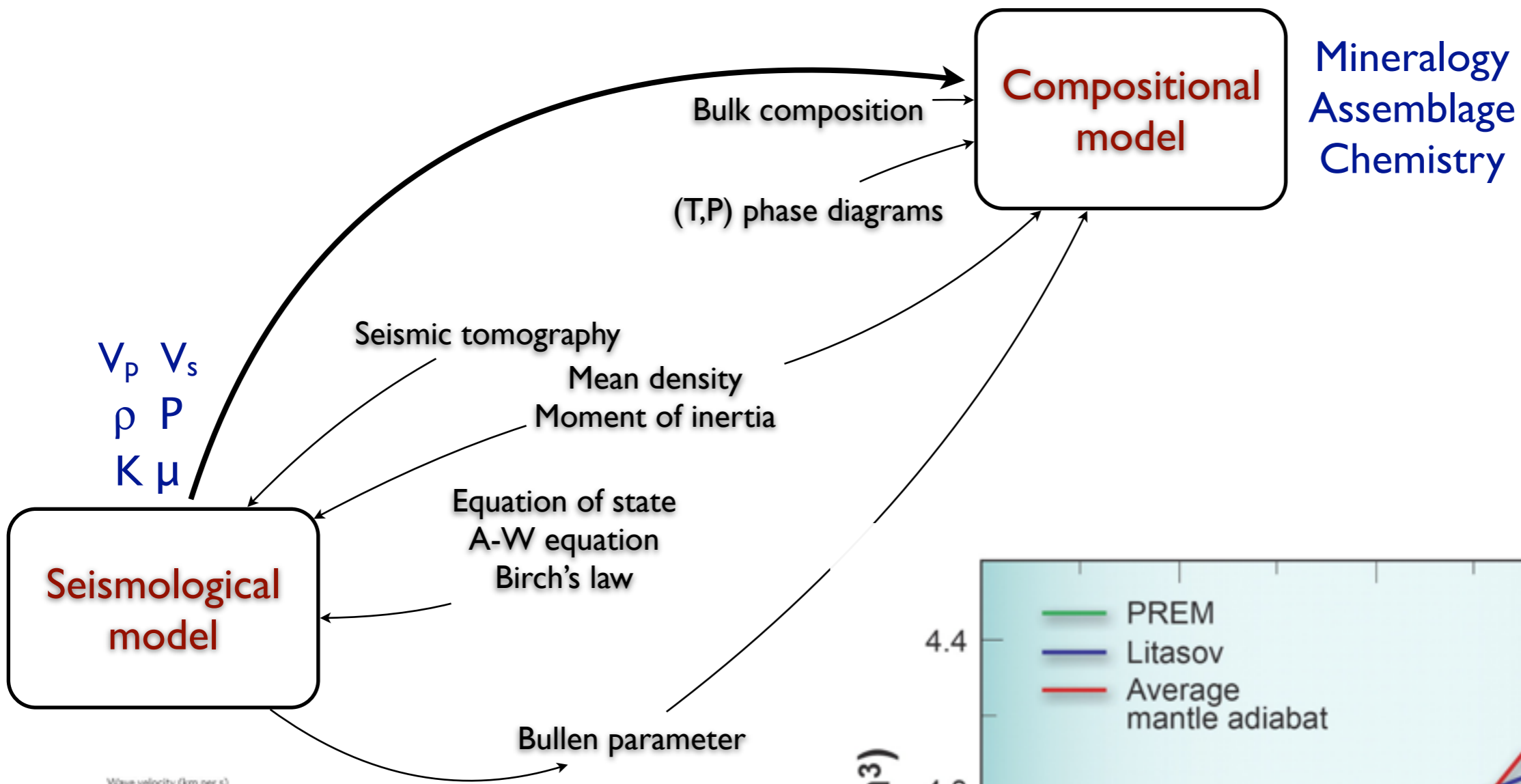
Earth system: geosphere



Earth layers



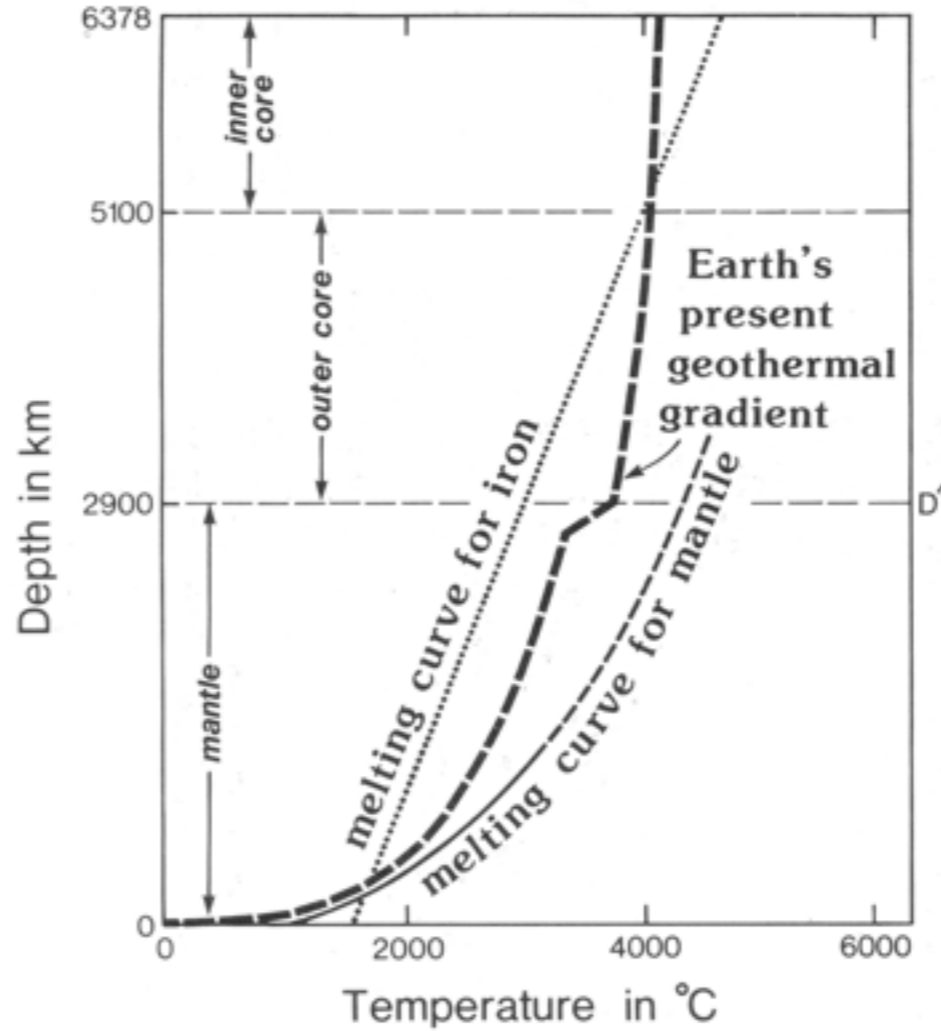




V_p V_s
 ρ P
 K μ

Seismic tomography
 Mean density
 Moment of inertia
 Equation of state
 A-W equation
 Birch's law

Seismological model



Bullen parameter

Heat flux

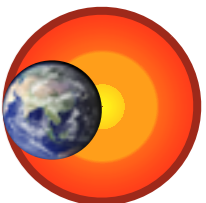
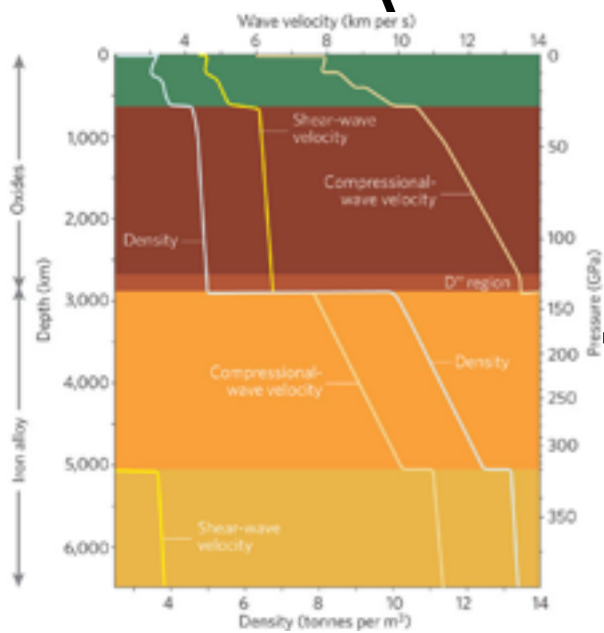
Mantle viscosity

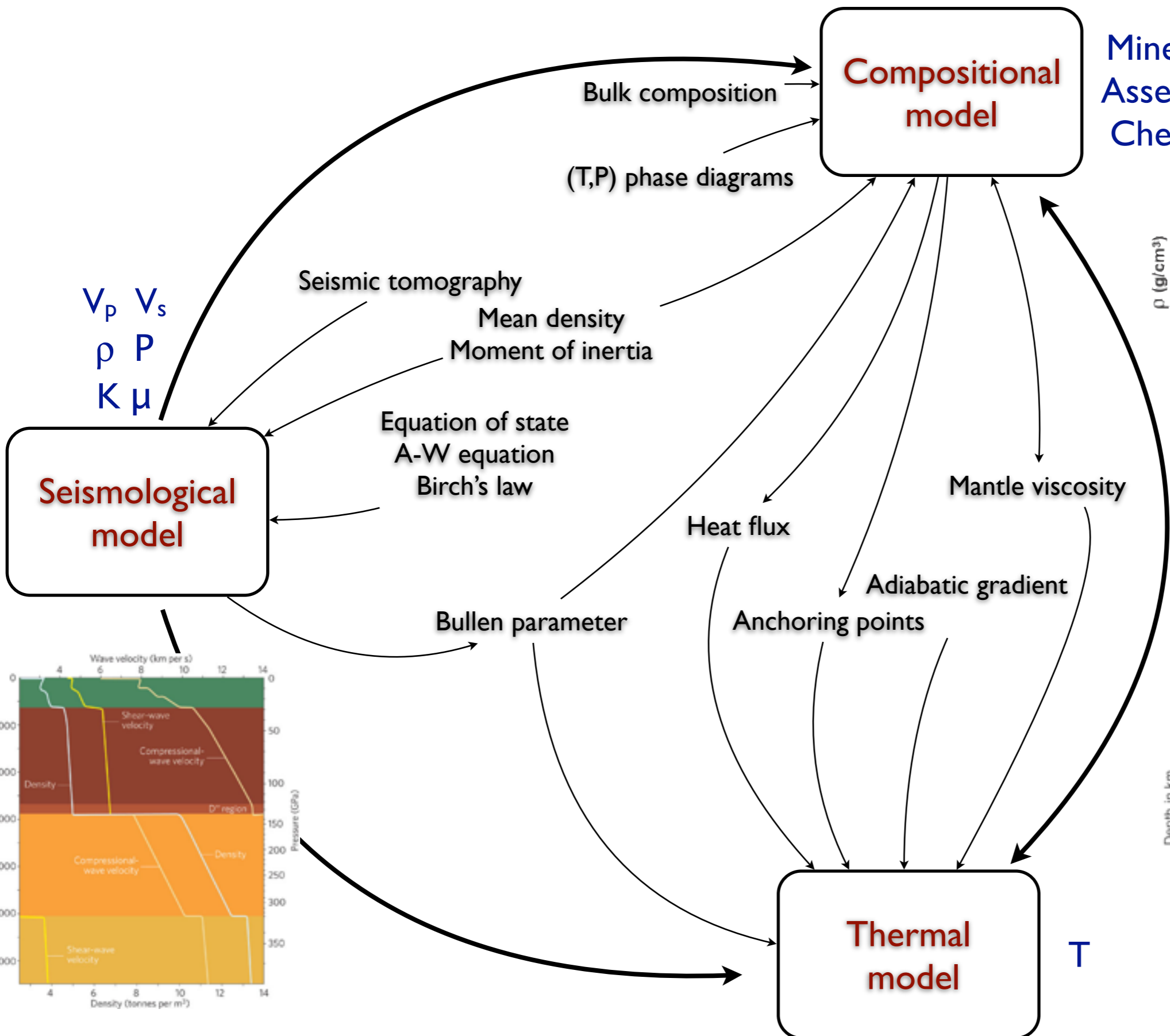
Anchoring points

Adiabatic gradient

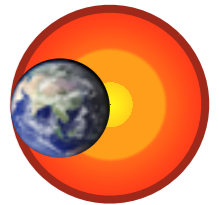
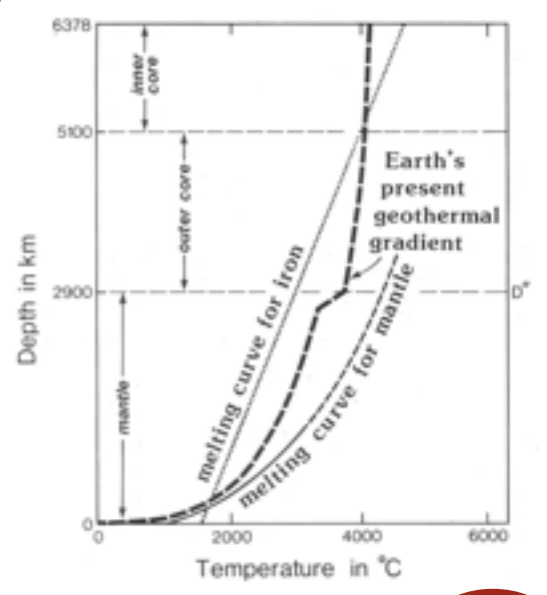
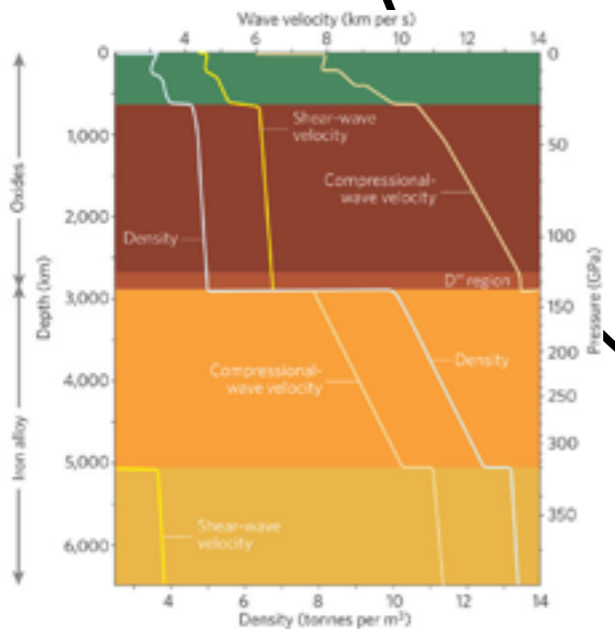
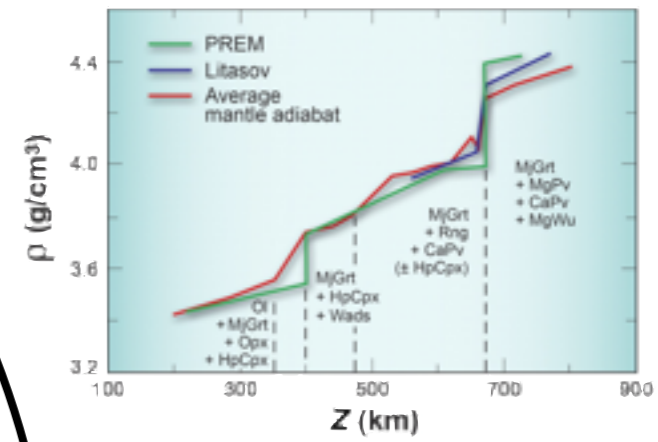
Thermal model

T

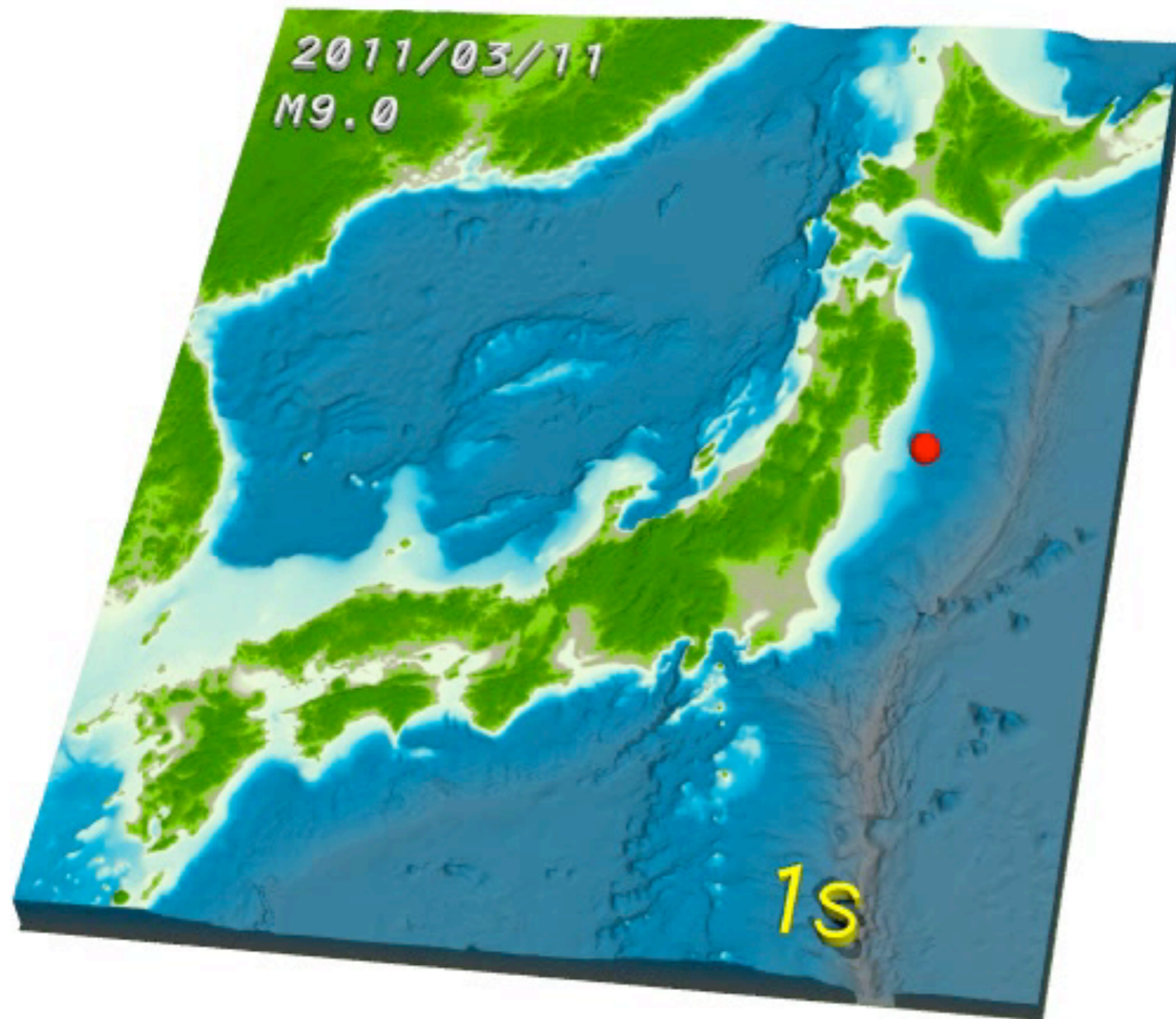




Mineralogy
Assemblage
Chemistry



Ground motion animation: time scales...



Courtesy of Takashi Furumura

Tsunami animation: time scales...

http://outreach.eri.u-tokyo.ac.jp/eqvolc/201103_tohoku/eng/

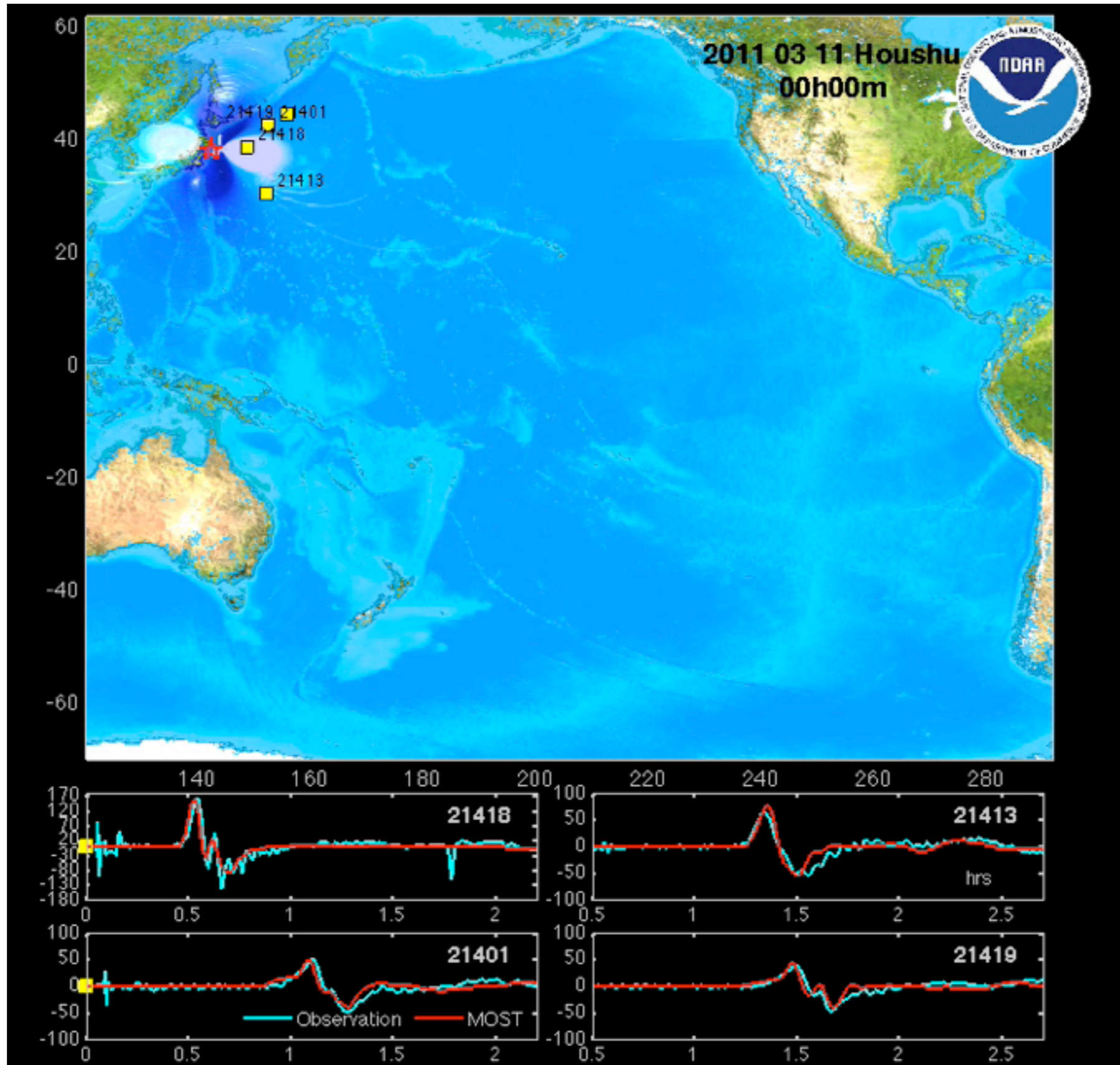
<http://supersites.earthobservations.org/honshu.php>

<http://eqseis.geosc.psu.edu/~cammon/Japan2011EQ/>



“Earthquake Research Institute, University of Tokyo, Prof. Takashi Furumura and Project Researcher Takuto Maeda”

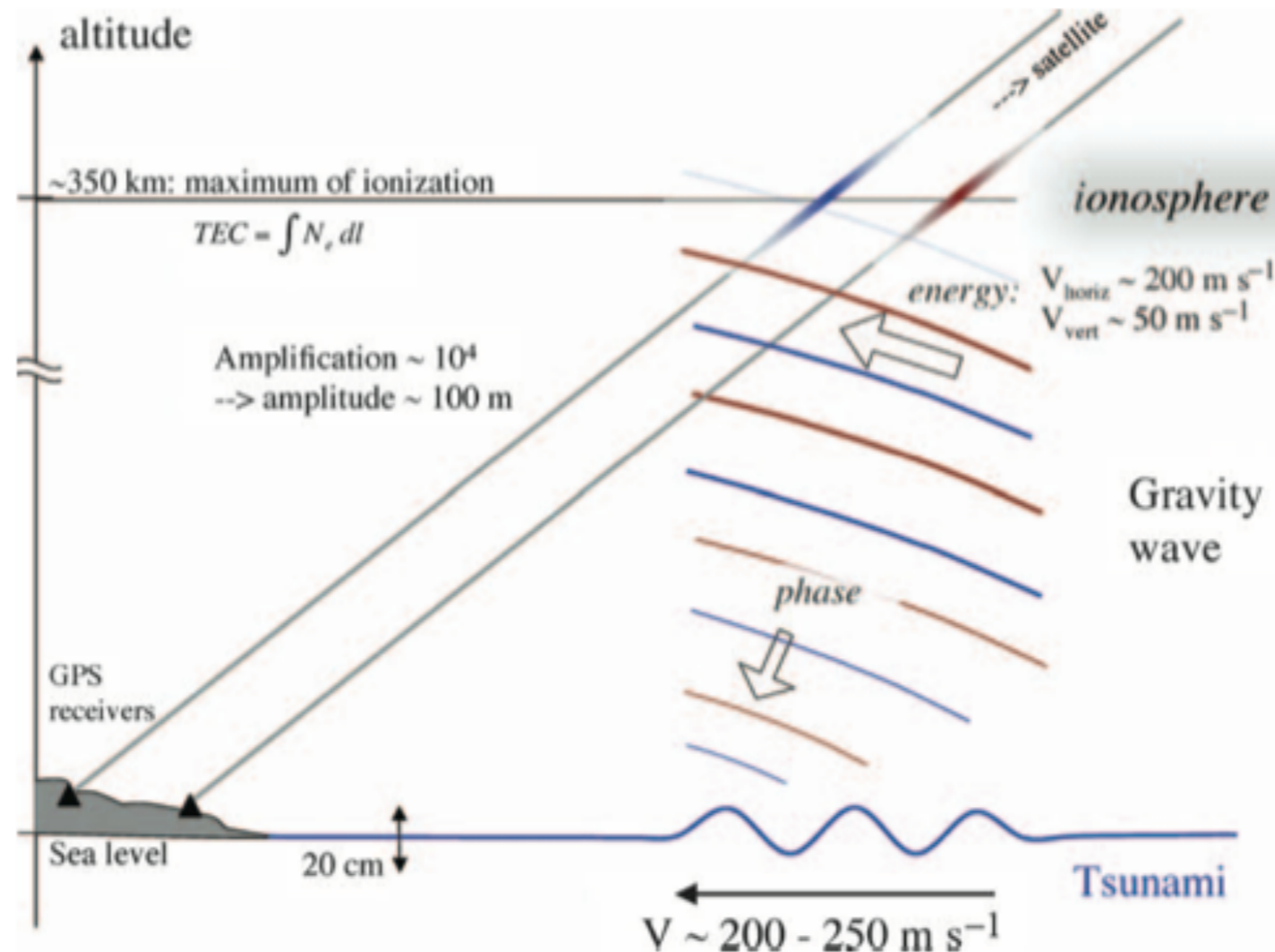
Tsunami animation - NOAA



Tsunami signature in the ionosphere

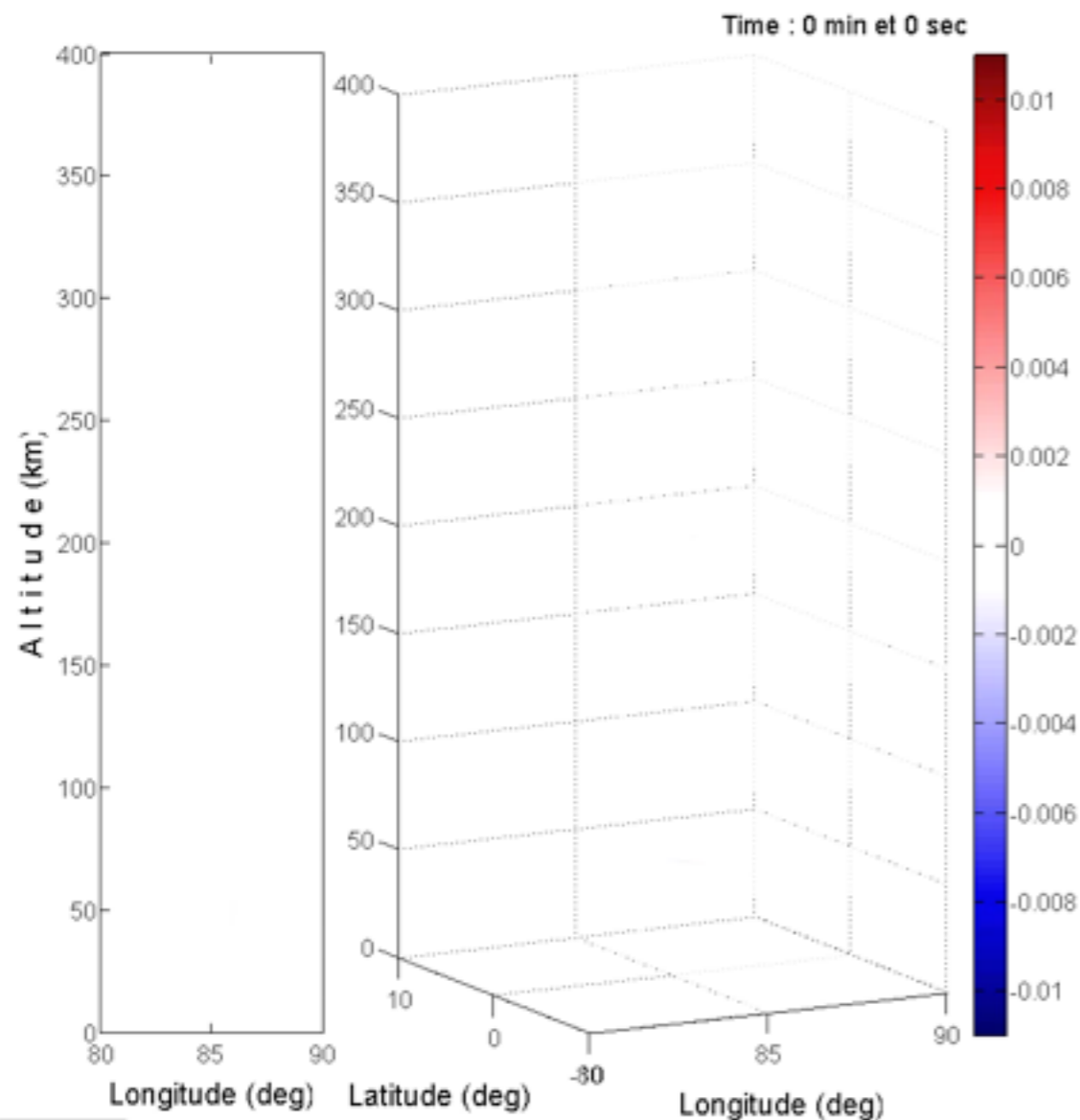
By dynamic coupling with the atmosphere, **acoustic-gravity waves** are generated

Traveling Ionospheric Disturbances (TID) can be detected and monitored by high-density GPS networks

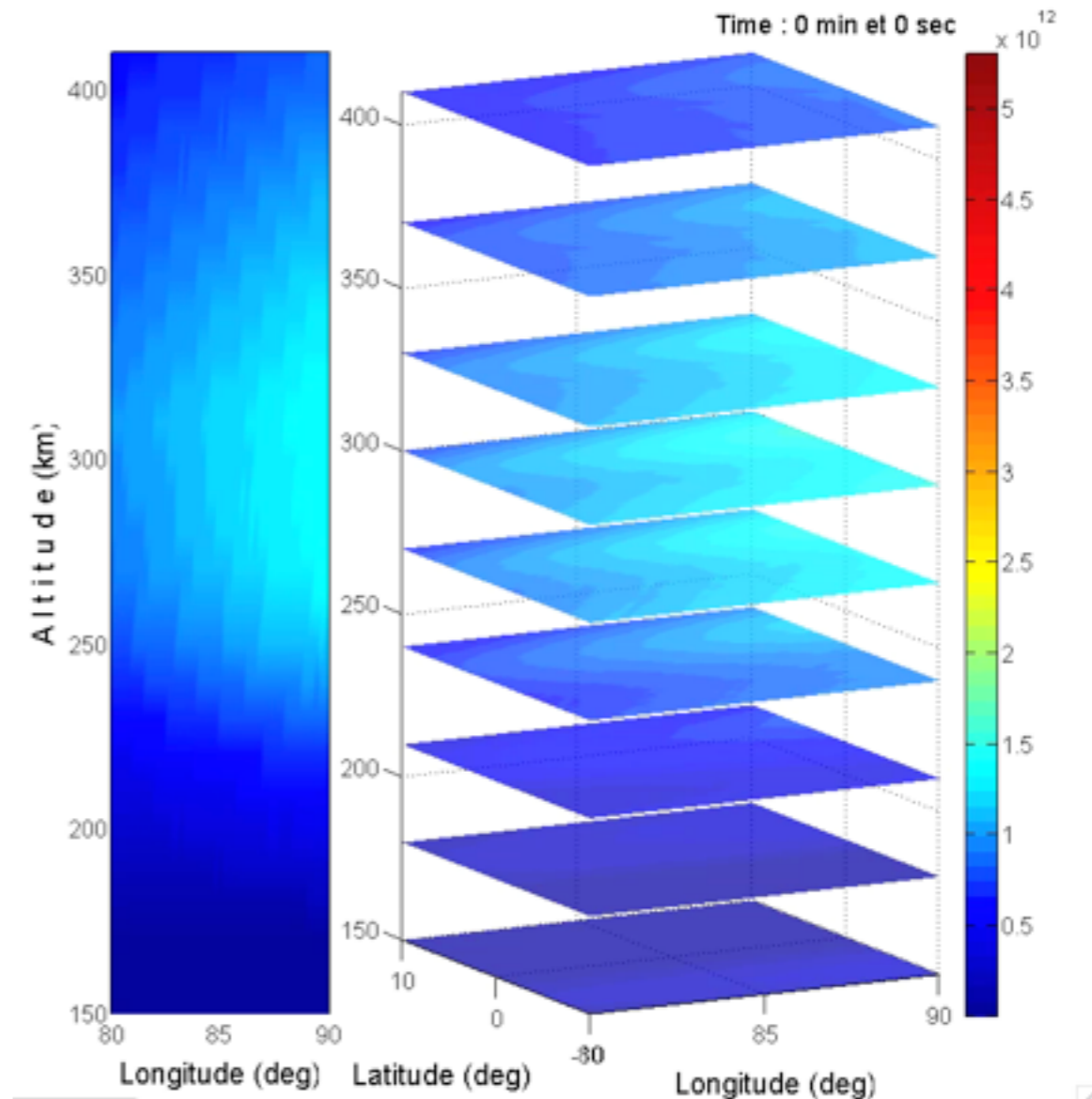


Tsunami signature in the ionosphere

Tsunami-generated IGWs and the response of the ionosphere to neutral motion at 2:40 UT.



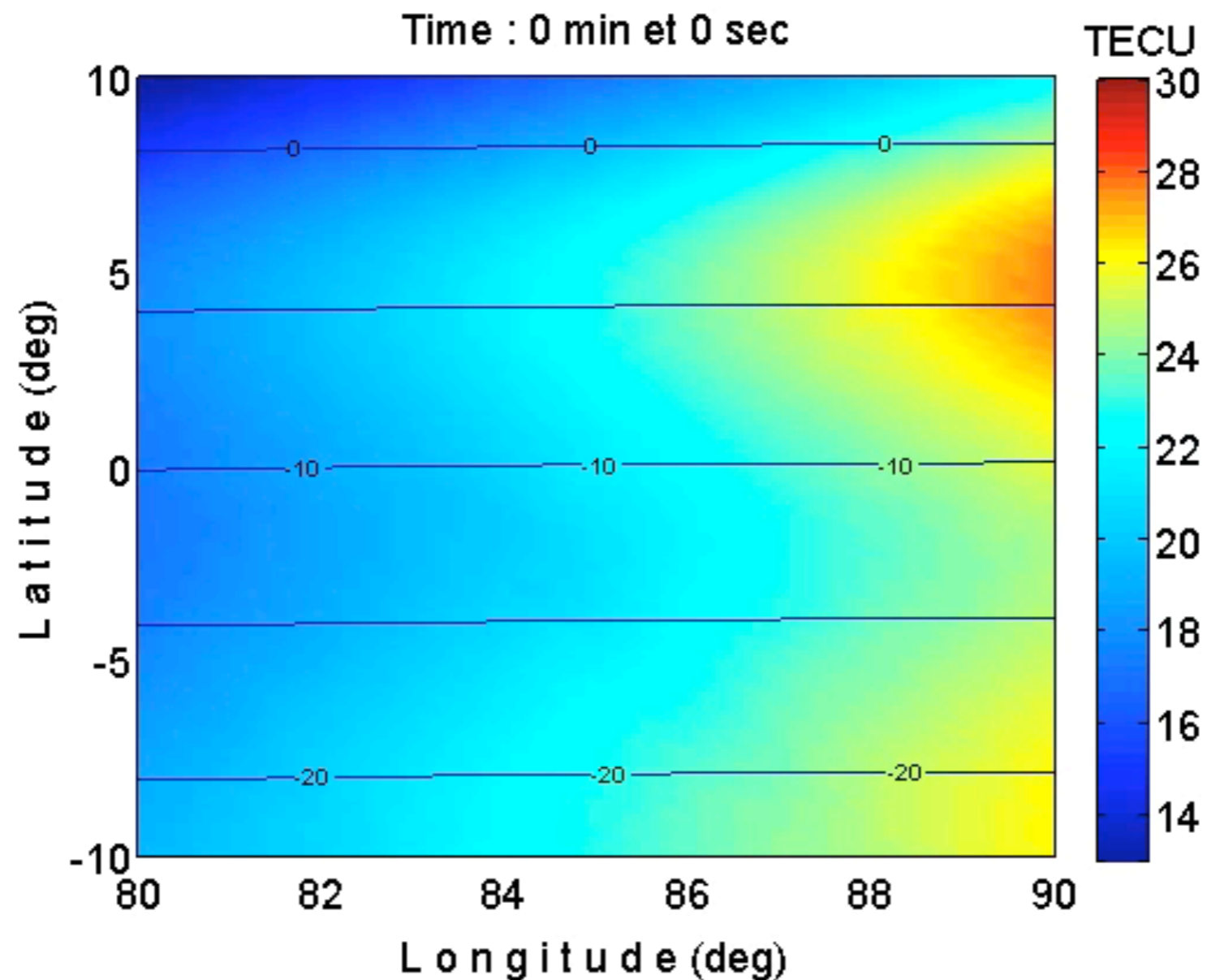
Normalized vertical velocity



Perturbation in the ionospheric plasma

Tsunami signature in the ionosphere

- The TEC (Total Electron Content) perturbation induced by tsunami-coupled IGW is superimposed on a broad local-time (sunrise) TEC structure.



Mathematical reference: PDE

Classification of Partial Differential Equations (PDE)

Second-order PDEs of two variables are of the form:

$$a \frac{\partial^2 f(x, y)}{\partial x^2} + b \frac{\partial^2 f(x, y)}{\partial x \partial y} + c \frac{\partial^2 f(x, y)}{\partial y^2} + d \frac{\partial f(x, y)}{\partial x} + e \frac{\partial f(x, y)}{\partial y} = F(x, y)$$

$$b^2 - 4ac < 0$$

elliptic LAPLACE equation

$$b^2 - 4ac = 0$$

parabolic DIFFUSION equation

$$b^2 - 4ac > 0$$

hyperbolic WAVE equation

Elliptic equations produce **stationary and energy-minimizing** solutions

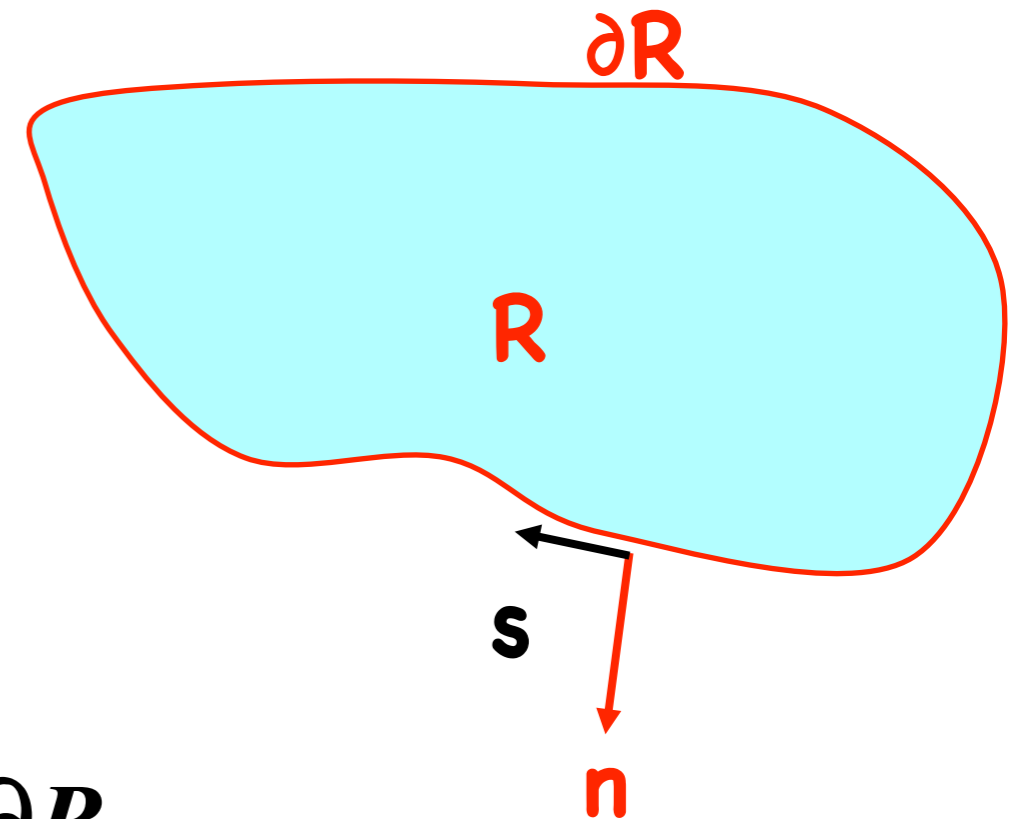
Parabolic equations a **smooth-spreading flow** of an initial disturbance

Hyperbolic equations a **propagating disturbance**

Boundary and Initial conditions

Initial conditions: starting point for propagation problems

Boundary conditions: specified on domain boundaries to provide the interior solution in computational domain



(i) Dirichlet condition : $u = f$ on ∂R

(ii) Neumann condition : $\frac{\partial u}{\partial n} = f$ or $\frac{\partial u}{\partial s} = g$ on ∂R

(iii) Robin (mixed) condition : $\frac{\partial u}{\partial n} + ku = f$ on ∂R

Elliptic PDEs

Steady-state two-dimensional heat conduction equation is prototypical elliptic PDE

Laplace equation - homogeneous (no source)

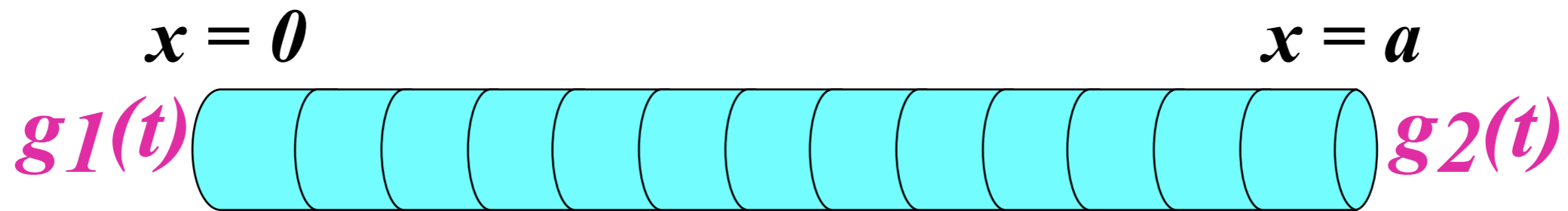
$$\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} = 0$$

Poisson equation - with source (e.g. heat)

$$\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} = f(x, y)$$

Heat Equation: parabolic PDE

Heat transfer in a one-dimensional rod



$$\frac{\partial u}{\partial t} = d \frac{\partial^2 u}{\partial x^2}, \quad 0 \leq x \leq a, \quad 0 \leq t \leq T$$

$$\text{I.C.s} \quad u(x, 0) = f(x) \quad 0 \leq x \leq a$$

$$\text{B.C.s} \quad \begin{cases} u(0, t) = g_1(t) \\ u(a, t) = g_2(t) \end{cases} \quad 0 \leq t \leq T$$

Wave Equation: hyperbolic PDE

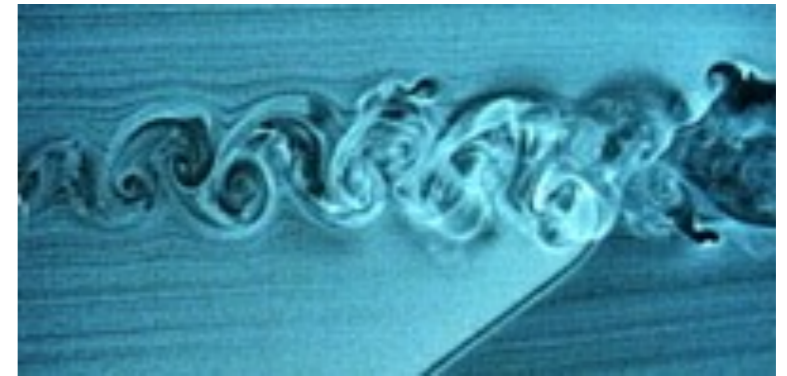
$b^2 - 4ac = 0 - 4(1)(-c^2) > 0$: Hyperbolic

$$\frac{\partial^2 u}{\partial t^2} = v^2 \frac{\partial^2 u}{\partial x^2}, \quad 0 \leq x \leq a, \quad 0 \leq t$$

$$\text{I.C.s} \quad \begin{cases} u(x, 0) = f_1(x) \\ u_t(x, 0) = f_2(x) \end{cases} \quad 0 \leq x \leq a$$

$$\text{B.C.s} \quad \begin{cases} u(0, t) = g_1(t) \\ u(a, t) = g_2(t) \end{cases} \quad t > 0$$

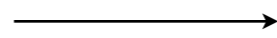
Navier-Stokes Equations



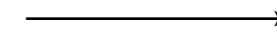
$$\begin{cases} \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0 \\ \frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = -\frac{1}{\rho} \frac{\partial p}{\partial x} + \nu \left(\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right) \\ \frac{\partial v}{\partial t} + u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} = -\frac{1}{\rho} \frac{\partial p}{\partial y} + \nu \left(\frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} \right) \end{cases}$$

What is a wave?

Small perturbations of a **stable** equilibrium point

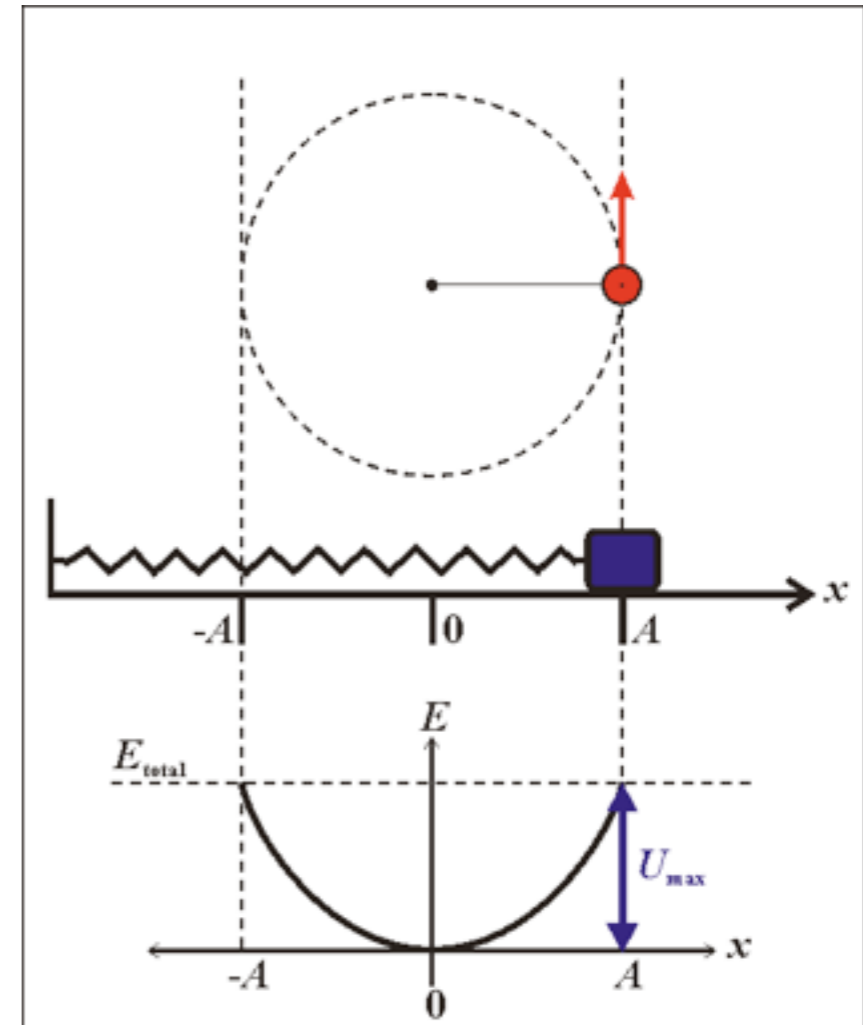
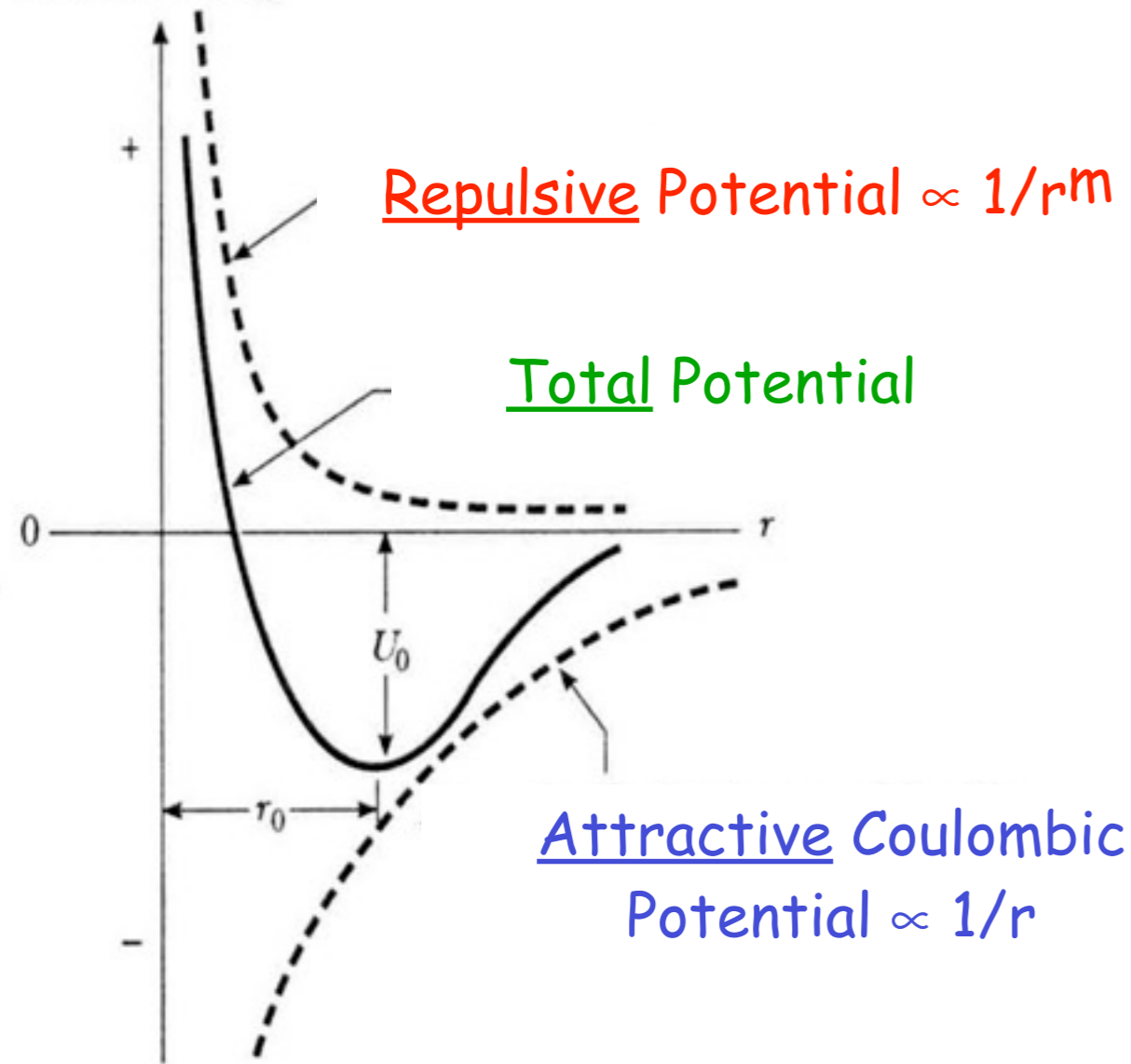


Linear restoring force



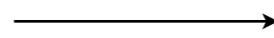
Harmonic Oscillation

Potential energy

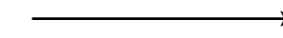


What is a wave? - 2

Small perturbations of a
stable equilibrium point

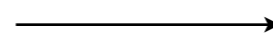


Linear restoring
force

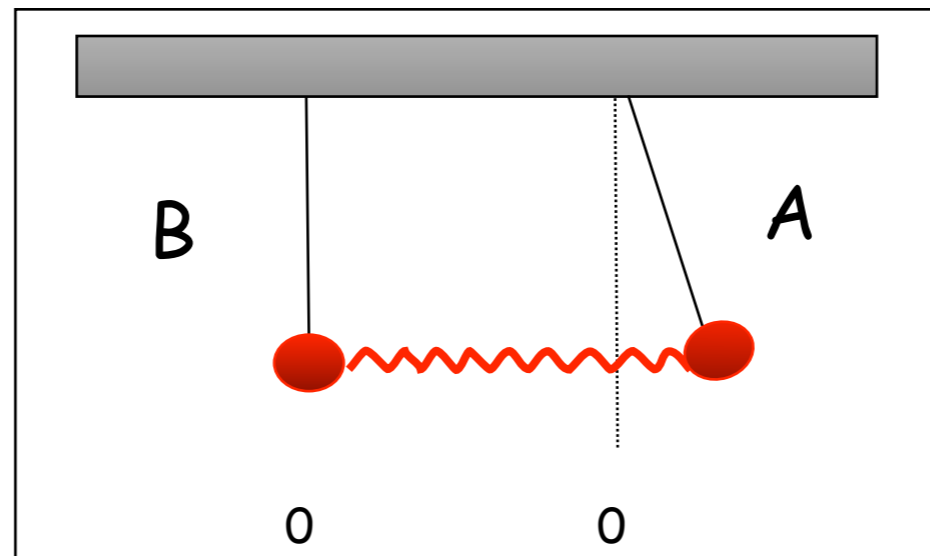


Harmonic
Oscillation

Coupling of
harmonic oscillators

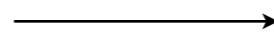


the disturbances can
propagate

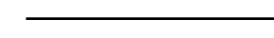


What is a wave? - 2

Small perturbations of a stable equilibrium point

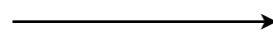


Linear restoring force

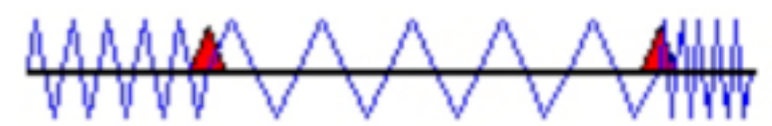
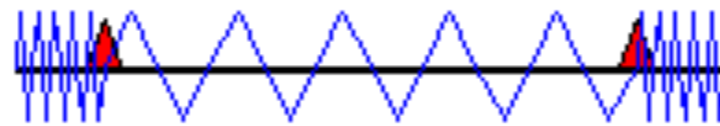


Harmonic Oscillation

Coupling of harmonic oscillators



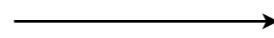
the disturbances can propagate, superpose and **stand**



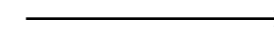
Normal modes of the system

What is a wave? - 3

Small perturbations of a
stable equilibrium point



Linear restoring
force



Harmonic
Oscillation

Coupling of
harmonic oscillators



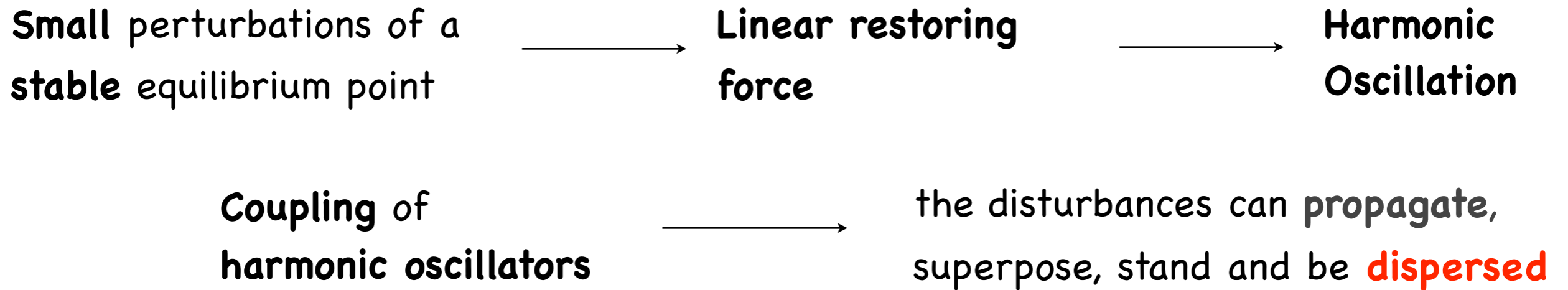
the disturbances can
propagate, superpose and
stand

WAVE: organized propagating imbalance,
satisfying differential equations of motion

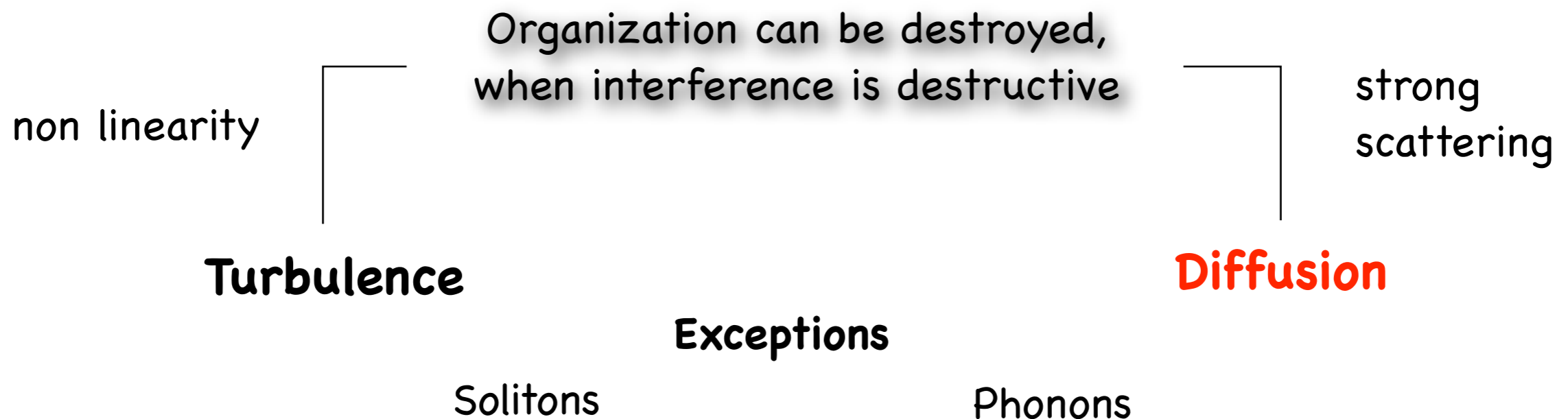
$$\frac{\partial^2 y}{\partial x^2} = \frac{1}{v^2} \frac{\partial^2 y}{\partial t^2}$$

General form of LWE

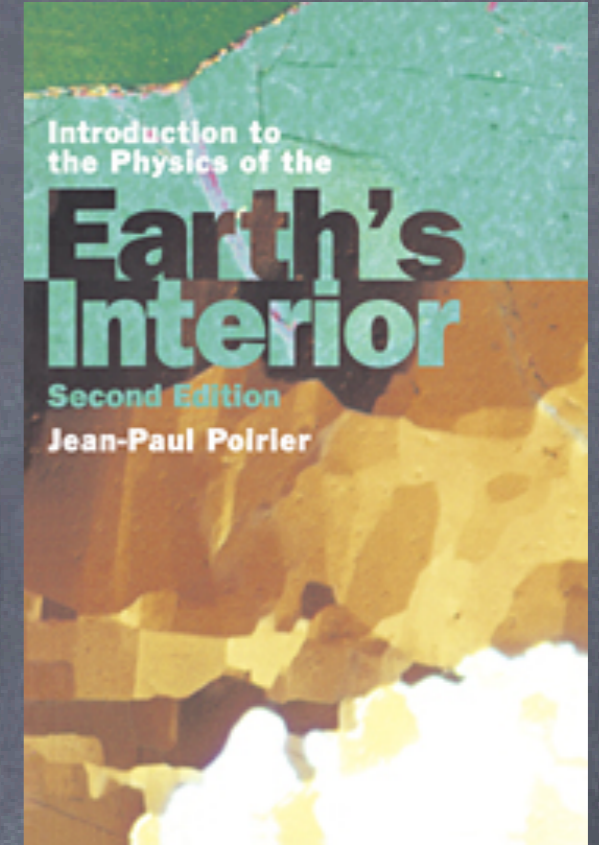
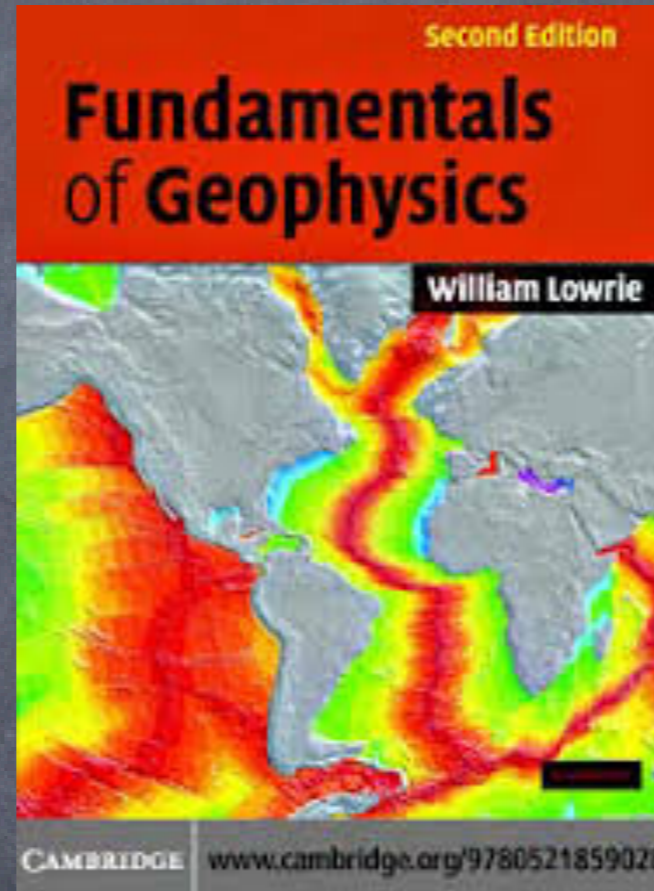
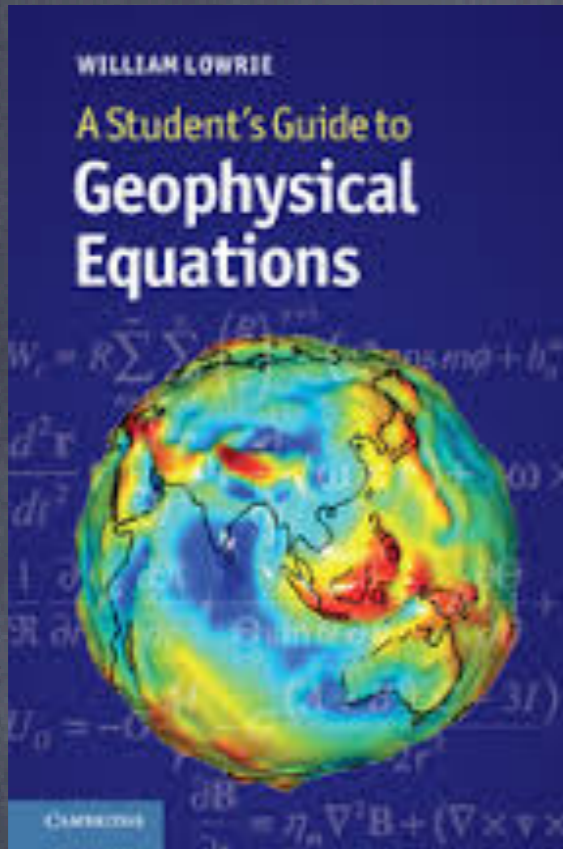
What is a wave? - 4



WAVE: organized propagating imbalance, satisfying differential equations of motion



Alcuni Links



<http://www.physicalgeography.net/fundamentals/contents.html>