

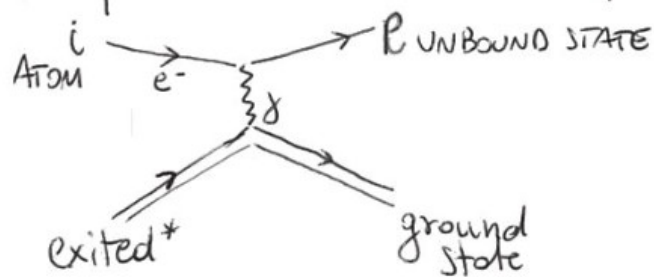
INTERNAL CONVERSION

(93)

$0^+ \rightarrow 0^+$ transitions cannot occur via e.m. γ transition. This is because the e.m. operator does not have an $l=0$ component, since photon's intrinsic spin is $S=1$.
 However there is an e.m. process that can cause $0^+ \rightarrow 0^+$ transition, a process called INTERNAL CONVERSION

The classical visualization is that an electron (from k-shell) enters the nucleus, feels the e.m. force from a nucleus in an excited state, or a collection of nucleus in an excited state, and acquires enough energy to liberate the e^- from the nucleus to transition to lower energy level. A nucleus as a whole, recalls to conserve energy.

The quantum mechanical picture is similar:



Whether we adopt quantum electro-dynamics or Fermi Golden Rule approach, the most important part, which is also the less known part, is the transition element $M^{i \rightarrow f}$

for internal conversion this is

$$M_{ic}^{i \rightarrow f} = \langle \psi_N^f \psi_e^{free} | \mathcal{D}_{em} | \psi_e^{bound} \psi_N^i \rangle$$

which has to be compared with that of γ conversion

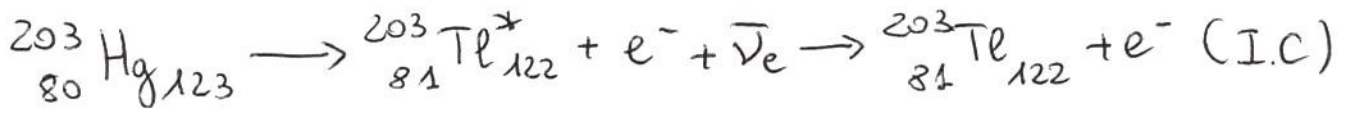
$$M_{\gamma}^{i \rightarrow f} = \langle \psi_N^f \psi_{\gamma}^{free} | \mathcal{D}_{em} | \psi_N^i \rangle$$

they look similar, they contain many physical similarity, that are accompanied by mathematical similarity.

In fact, every γ decay is in competition with internal conversion. The only one that stands alone is $0^+ \rightarrow 0^+$ internal conversion, that has not counterpart.

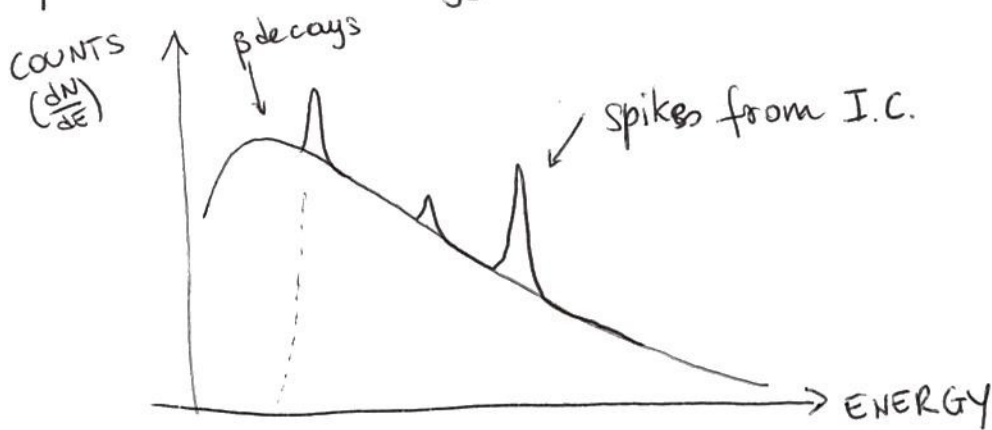
When a nucleus decays, it does so via α , β , γ decay. Often a decay can proceed via more than one decay channel, and the daughter can decay as well.

A particularly interesting case is when β decay and internal conversion happen in close temporal proximity. For example:



\Rightarrow A measurement of the electrons being emitted from ${}^{203}\text{Hg}$ sees both β decay electrons and IC electrons.

However, the signature of both these processes are very distinct. The β e^- gives a continuous energy spectrum, while I.C. e^- are seen as sharp lines of the energy of nuclear transition (minus recoil)



The kinetic energies of electrons is given by:

$$T_e = \frac{Q-B}{1 + \frac{m_e}{M_{X'}}} \left[\frac{1 + \frac{Q-B}{2m_{X'}c^2}}{1 + \frac{Q-B}{(m_{X'}+m_e)c^2}} \right] \approx Q-B$$

\downarrow

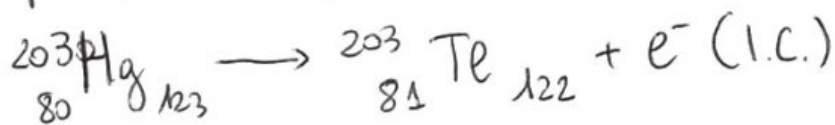
$$\frac{m_e}{M_{X'}} \propto \frac{0.0005}{A} \rightarrow \approx 0 \quad \approx 1 \rightarrow \text{If "corrections" are ignored}$$

The correction may be needed for lighter elements with large Q .

One of the worse case is observed for ${}^{16}\text{O}$ decay $0^+ \rightarrow 0^+$ which is a clear I.C. : in this case the correction is $\approx 0.5\%$ in corrections are ignored.

D = binding energy of converted electron; this cannot be ignored⁽³⁴⁾ and depends upon the atomic shell from which the electron was converted.

Specific example:



$$Q = 279,910 \text{ KeV}$$

X-ray NOTATION	Spectroscopic notation	Be (KeV)	Tl (KeV)
K	1S _{1/2}	85,5	193,7
L ₁	2S _{1/2}	15,4	263,8
L ₂	2P _{1/2}	14,7	264,5
L ₃	2P _{3/2}	12,7	266,5
M ₁	3S _{1/2}	3,7	275,5

Internal conversion contribution to decay rate

Since γ & IC both contribute to e.m. decay rate, the total decay rate can be written as:

$$\lambda_{em} = \lambda_{\gamma} + \lambda_e$$

$$\alpha \equiv \lambda_e / \lambda_{\gamma} \Rightarrow$$

$$\lambda_{em} = \lambda_{\gamma} \left(1 + \frac{\lambda_e}{\lambda_{\gamma}}\right)$$

$$\lambda_{em} = \lambda_{\gamma} (1 + \alpha)$$

$$\lambda_{em} = \lambda_{\gamma} + \lambda_{eK} + \lambda_{eL_i} + \lambda_{eM} + \dots$$

$$\text{or } \lambda_{\gamma} (1 + \alpha_K + \alpha_L + \alpha_M + \dots)$$

Using hydrogenic wave function it is possible to estimate:

$$\alpha(El) \approx \frac{Z^3}{n^3} \left(\frac{\ell}{\ell+1}\right) \alpha^4 \left(\frac{2m_e c^2}{E_{\gamma}}\right)^{\ell+5/2}$$

$$\alpha(Me) \approx \frac{Z^3}{n^3} \alpha^4 \left(\frac{2m_e c^2}{E_{\gamma}}\right)^{\ell+3/2}$$

Z = Atomic number of daughter nucleus

The expressions are approximate but a number of features of I.C. can be illustrated:

1) They increase as $Z^3 \Rightarrow$ I.C. is more important for heavy nuclei.

E.g.: ${}_{10}^{22}\text{Ne} \rightarrow \alpha_K = 6.8 \cdot 10^{-6}$ 1.27 MeV E_2 transition

${}_{74}^{182}\text{W} \rightarrow \alpha_K = 2.5 \cdot 10^{-3}$ 1.22 MeV E_2 transition

ratio is $\approx (10/74)^3$ as expected while $\frac{6.8 \cdot 10^{-6}}{2.5 \cdot 10^{-3}} = 2.72 \cdot 10^{-3}$
 $\hookrightarrow 2.5 \cdot 10^{-4}$

2) The conversion coefficient decrease rapidly with increasing transition energy (In contrast with γ)

E.g. ${}_{26}^{56}\text{Co} \rightarrow M_1$ with energies: $\alpha_K = 0.011$ 158 keV, $\alpha_K = 0.0034$ 270 keV, $\alpha_K = 0.00025$ 812 keV
 these decrease $\propto E^{-2.5}$

3) The conversion coefficient increase rapidly as multipole order increases: for high L conversion may be for more probable than γ emission.

E.g. ${}_{43}^{99}\text{Tc}$ M1 141 keV $\alpha_K = 0.10$
 M4 143 keV $\alpha_K = 30$

Expected value of ratio: $\frac{\alpha_K(143)}{\alpha_K(141)} \approx \left(\frac{2 \text{ meV}}{E}\right)^3 \approx 370$

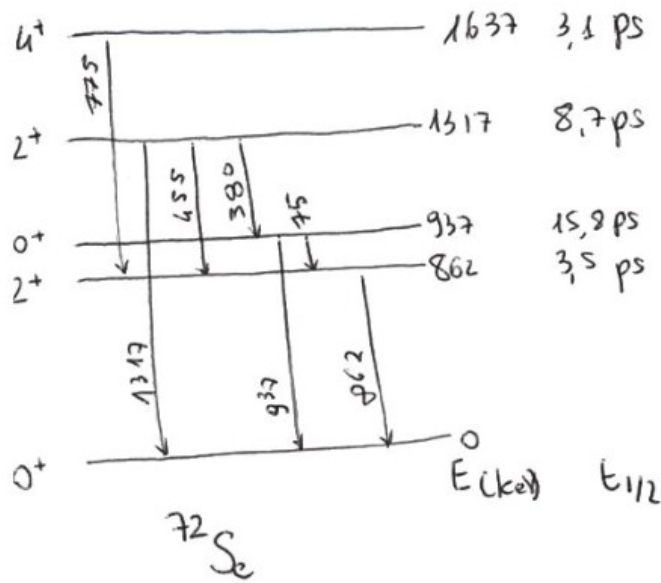
Measured " : ≈ 300

4) The atomic conversion coefficient for higher atomic shells ($n > 1$) decrease like $1/n^3$. Roughly we would expect $\alpha_K / \alpha_L \approx 8$. Using the correct e^- w.f. the ratio varies within 3-6 \Rightarrow The estimate is rather good.

While the estimates gives reasonable qualitative values, for quantitative results the detailed computations of conversion coefficient are needed. \Rightarrow It will be possible to get insight of the different matrix elements \Rightarrow Informations of the nuclear structure.

LIFETIME FOR γ EMISSION

Let's consider this example:



The $t_{1/2}$ of 1317 keV level has been measured to be 8.7 ps

$$\lambda_t = \frac{\ln 2}{t_{1/2}} = 8 \cdot 10^{10} \text{ s}^{-1}$$

The decay rate which is measured is the sum of the 3 transitions that de-populate the state:

$$\begin{aligned} \lambda_t &= \lambda_{t,1317} + \lambda_{t,455} + \lambda_{t,380} \\ &= \lambda_{\gamma,1317} (1 + \alpha_{1317}) + \lambda_{\gamma,455} (1 + \alpha_{455}) + \lambda_{\gamma,380} (1 + \alpha_{380}) \end{aligned}$$

$$\alpha_{xxx} \ll 1 \Rightarrow \lambda_t = \lambda_{\gamma,1317} + \lambda_{\gamma,455} + \lambda_{\gamma,380}$$

The relative intensities can be measured \Rightarrow

$$\lambda_{\gamma,1317} : \lambda_{\gamma,455} : \lambda_{\gamma,380} = 51 : 39 : 10$$

$$\begin{aligned} \Rightarrow \lambda_{\gamma,1317} &= 0,51 \times (8 \cdot 10^{10} \text{ s}^{-1}) = 4,1 \times 10^{10} \text{ s}^{-1} \\ \lambda_{\gamma,455} &= 0,39 \times (8 \cdot 10^{10} \text{ s}^{-1}) = 3,1 \times 10^{10} \text{ s}^{-1} \\ \lambda_{\gamma,380} &= 0,10 \times (8 \cdot 10^{10} \text{ s}^{-1}) = 0,8 \times 10^{10} \text{ s}^{-1} \end{aligned}$$

These partial rates for γ emission can be compared with calculated

Values, eg. Weisskopf estimates:

For E_2 transitions:

$$\lambda_{E_2, 1317} = 8,7 \cdot 10^{10} \text{ s}^{-1}$$

$$\lambda_{E_2, 455} = 4,3 \cdot 10^8 \text{ s}^{-1}$$

$$\lambda_{E_2, 380} = 1,7 \cdot 10^8 \text{ s}^{-1}$$

Doing the same passages done for measurement for data and model one gets results which are similar, but not identical. Why?

Because this is a strong evidence of collective aspect of nuclear structure, as discussed previously.

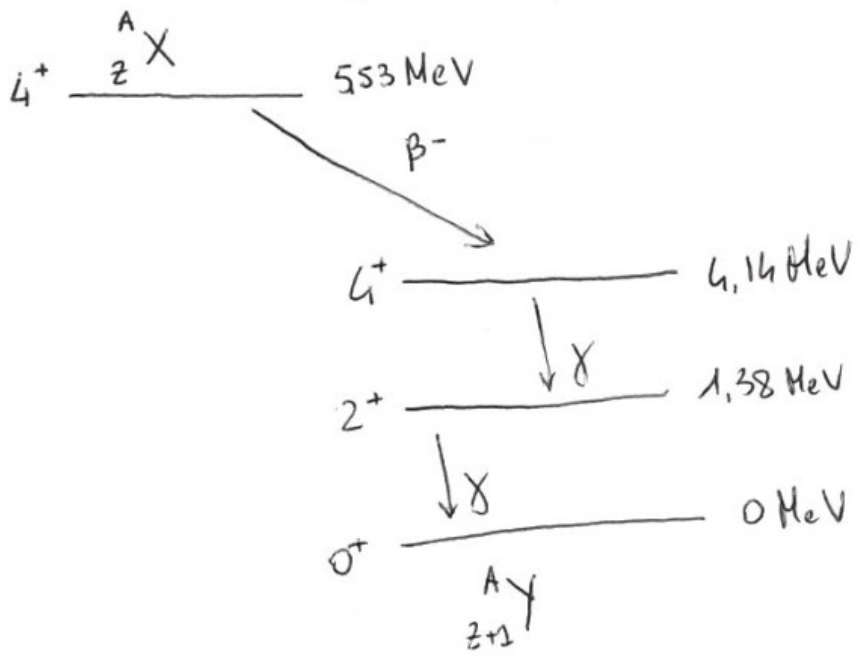
The Weisskopf estimates are based on the assumption that the transition arises from a single nucleon motion, and in fact the "model coefficients" are smaller than the measurement! This means that there must be many nucleons that takes part to the transitions.

EXERCISE

Radioactive nucleus ${}^A_Z X$ is known to undergo β^- decay to ${}^A_{Z+1} Y$.

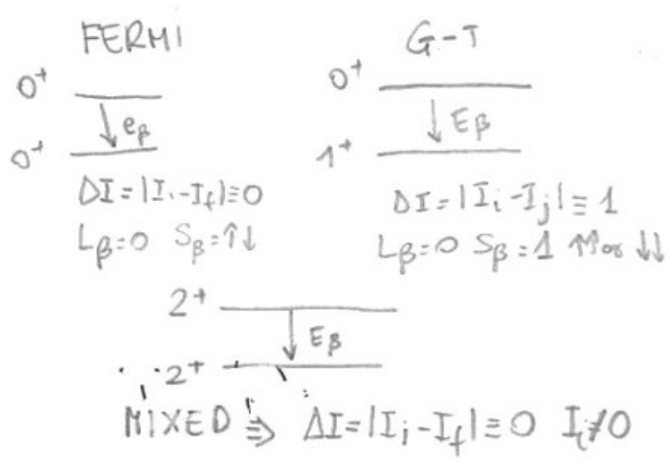
In a measurement one finds a distribution of electrons, but in addition two groups of positrons with discrete end-point energies are observed.

- a) What could be the process giving rise to the positrons?
- b) What are the expected end-point energies of the 2 positron groups?
- c) What are the decay modes for the indicated transitions?



2) Two possible explanations:

- 1) Pair production from γ
- 2) Internal conversion \leftarrow



- c) End-point energies:
 $E(g_1) = (4.14 - 1.38) = 2.76 \text{ MeV}$
 $E(g_2) = 1.38 \text{ MeV}$

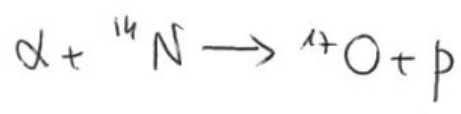
- d) Decay modes: $\beta^- \quad 4^+ \rightarrow 4^+$
 $\gamma_1 \quad 4^+ \rightarrow 2^+$
 $\gamma_2 \quad 2^+ \rightarrow 0^+$

$\Delta T = 0 \Rightarrow \Delta S = 0$
 allowed, F and GT
 $E_2 \quad \Delta T = 0 \quad 2 \leq J \leq 6$
 $\Gamma \sim E_2, \Delta \pi = 0, J = 2$

NUCLEAR REACTIONS

If energetic particles from a reactor or accelerator (or even radioactive source) are allowed to fall upon bulk matter, there is the possibility of nuclear reactions taking place.

The first nuclear reactions were done by Rutherford: in the first experiment the α ptc merely rebounded elastically: this phenomenon known as "Rutherford scattering" gave the first evidence for the existence of atomic nuclei. In other experiments Rutherford was able to observe a change or "transmutation" of nuclear species, e.g:



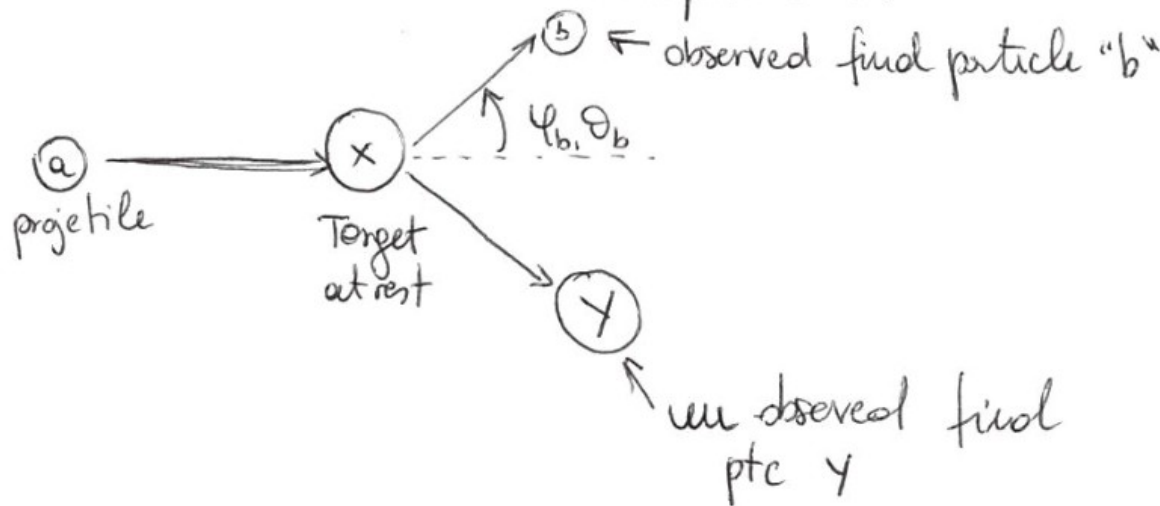
The first particle accelerator capable of introducing nuclear reactions was built in '30 and observed the reaction



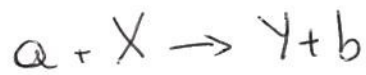
This is a "Nuclear reaction".

In most cases the "projectile" is a light nucleus ($A \leq 4$) incident on heavy target. The energy of the reaction can be "low" if $E \leq 10 \text{ MeV}$, "Medium" for a range $10 \text{ MeV} \div 1 \text{ GeV}$ (meson production \Rightarrow exchange of π and n) or "High" energy if the latter all sort of exotic particles can be produced.

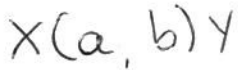
A typical nuclear reaction can be depicted as



The symbolic shorthand of the reaction is



An alternative and compact way of indicating the same reaction is:



The reactions can be classified in many ways: If the incident particle is the same as the outgoing one, the process is a "scattering"; elastic if Y or b are in the ground state and inelastic if Y or b are an excited state (from which it generally decays quickly by γ emission).

Sometimes, a and b are the same particle, but the reaction causes an other nu nucleus to be ejected separately. This is called knockout reaction. In transfer reactions, one or two nucleons are transferred between projectile and target.

Reactions can also be classified by the mechanism that governs the reaction. Direct reactions are reactions where only a few nucleons take part in the reaction and the remaining nuclei are called "spectators". Such reactions might insert or remove a single nucleon from a shell state, and therefore might be used to study nuclear structure.

The other extreme is compound nucleus mechanism, in which the incoming and target nuclei merge briefly.

Between the two mechanisms, there is the resonance reaction in which the incoming particle forms a "quasi-bound" state before the outgoing particle is ejected.

EXAMPLE OF NUCLEAR REACTIONS

$X(a, \gamma)Y$ radiative capture

$X(\gamma, b)Y$ nuclear photoeffect

$X(a, a)Y$ nuclear elastic scattering

$X(a, a)Y^*$ " inelastic "

DIRECT REACTIONS: Short time ~~of~~ w.r.t. the time needed ^{transmission} to transit the target ($\sim 10^{-22}$ s) (92)

- KNOCK-OUT REACTIONS
- STRIPPING "
- PICK-UP "

INDIRECT REACTIONS: COMPOUND REACTIONS (Formation of a compound state) After a certain time the intermediate state decays and produces final pte.

- ELASTIC CHANNEL: $a + A \rightarrow C^* \rightarrow a + A$
- INELASTIC " : $a + A \rightarrow C^* \rightarrow a + A^*$
- NEAR REACTION : $a + A \rightarrow C^* \rightarrow b + B + \dots$
- RADIATIVE CAPTURE: $a + A \rightarrow C^* \rightarrow \gamma + C$

In general indirect reactions have reaction time $> 10^{-6}$ s
