

# Batch distillation

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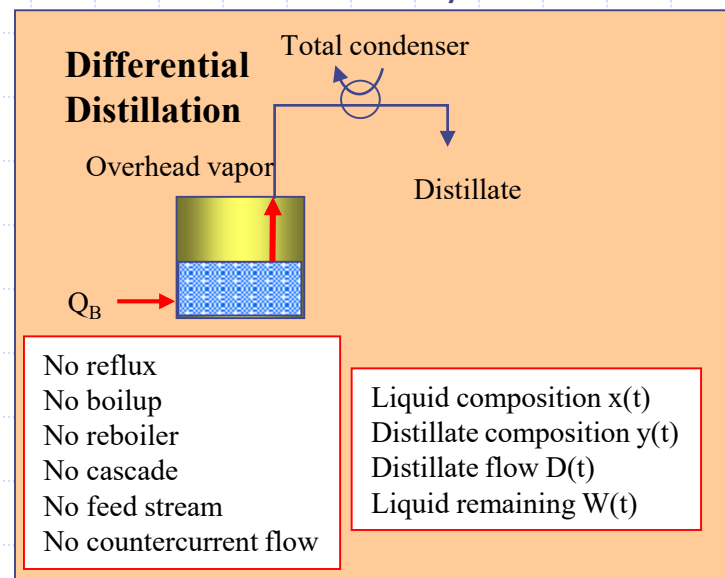
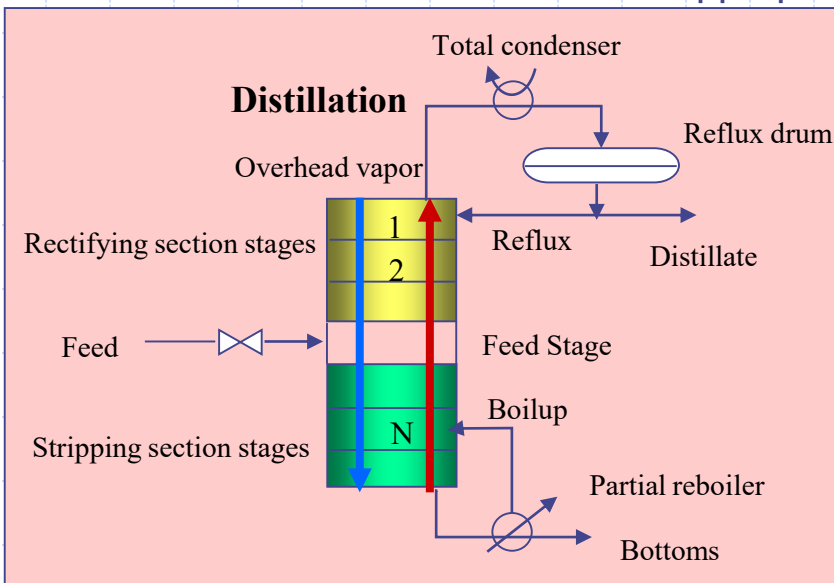


# Agenda

- ◆ Batch distillation principles
- ◆ Multistage batch distillation
- ◆ Binary distillation: Rayleigh equation
- ◆ Batch distillation at total reflux
- ◆ Semi batch distillation
  - Constant  $x_D$  operation
  - Constant reflux operation
- ◆ Multicomponent batch distillation

# Batch Distillation

- ◆ A feed mixture of a given composition is placed in a single stage separator and heated to boiling.
  - The vapor is collected and condensed to a distillate.
  - The composition of the remaining liquid and the distillate are functions of time.
- ◆ There may be several reasons for running a batch process this:
  - Small capacity doesn't warrant continuous operation
  - Separation is to be done only occasionally
  - Separation is preparative to produce a new product
  - Upstream operations are batchwise or feedstocks vary with time or from batch to batch
  - Feed materials are not appropriate for a continuous flow system.



The **Differential Distillation** operation requires a much **simpler** apparatus, but is **complicated** because the process is now a function of time.

# Batch Distillation

## ◆ Batch distillation uses

- Relatively small amounts of product and charge.
- Non-continuous operation (batch).
- Different distillations are to be done using the same equipment.

## ◆ Batch distillation peculiarities

- Unit may be a single pot or multi-staged.
- There is no continuous feed – the pot is charged with liquid and then drained at the end of the run.
- Distillate (usually the desired product) may be withdrawn continuously or collected in an accumulator.
- Batch installations used in 'campaigns'

## ◆ Industries interested

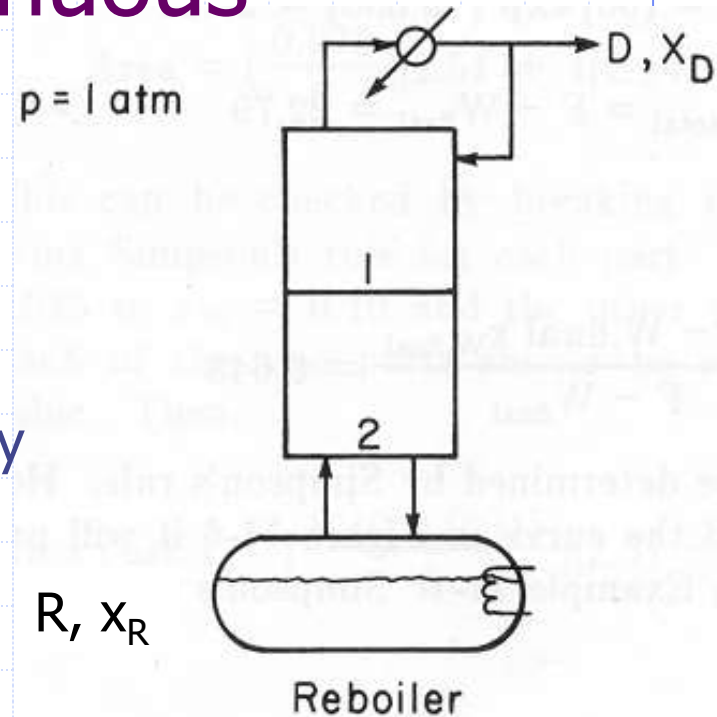
- Pharmaceuticals
- Fine chemistry and specialty chemistry
- Food
- cosmetics

# Batch Distillation

- ◆ One is more interested in the amounts of bottoms and distillate collected rather than the rates.
  - Design of the column is not important
  - Same column may be used for different separations
  - It is important rating a batch distillation equipment
- ◆ The amount and compositions in the pot (bottoms) change as the more volatile component(s) decrease(s) with time and the less volatile component(s) increase(s) with time.
- ◆ Because the bottoms amount and concentrations change with time, the distillate amount,  $D$ , and concentration,  $x_D$ , in general, change with time.
- ◆ Operating a batch distillation may be done in 3 different ways:
  - Constant reflux operation and variable distillate composition (semi-batch)
  - Constant distillate composition and variable reflux (semi-batch)
  - Total reflux operation (fully batch)
- ◆ Each operating mode gives different time concentration profiles in the column

# Multistage Batch vs. Continuous

- ◆ The batch system can be operated with a constant  $L/D$ , which means that  $x_D$  will change with time, or it can be operated with a constant  $x_D$ , which means that the  $L/D$  must be continuously changed.
- ◆ For a constant  $L/D$ , the distillate concentration fed to the accumulator decreases with time.
- ◆ The composition of the desired component in the distillate is at a maximum at the beginning of the batch run and decreases with time as it is distilled from the bottoms pot.
- ◆ The concentration of the more volatile component in the accumulator also decreases with time – the trade off is a lower concentration with more distillate accumulated.



# Multistage Batch Distillation

- ◆ We have only one operating line since there is no feed.
- ◆ We can plot this operating line on a McCabe-Thiele plot along with our equilibrium curve.
- ◆ We can step down the operating line from  $x_D$  to  $x_R$  to determine the number of stages.
- ◆ Note that the bottoms concentration,  $x_R$ , keeps changing with time as the liquid is boiled off.
- ◆ Also note that  $x_D$  changes with time for a constant reflux ratio,  $L/V$  or  $L/D$ .
- ◆ We need to relate  $x_D$  and  $x_R$  with time...

# Binary batch distillation: Rayleigh equation

- ◆ Mass balance around the entire system for the entire operation time:

$$F = R_{final} + D_{total}$$

$$Fz_F = R_{final}x_{R,final} + D_{total}x_{D,avg}$$

- ◆  $F$ ,  $z_F$  and the desired value of  $x$  (one) are specified

- An additional equation is required to solve for 3 unknowns (Rayleigh equation)
- Assumption: column and accumulator hold-up is negligible  
 $\rightarrow$  -out=accumulation in reboiler  $\rightarrow -x_D dR = -d(Rx_R)$

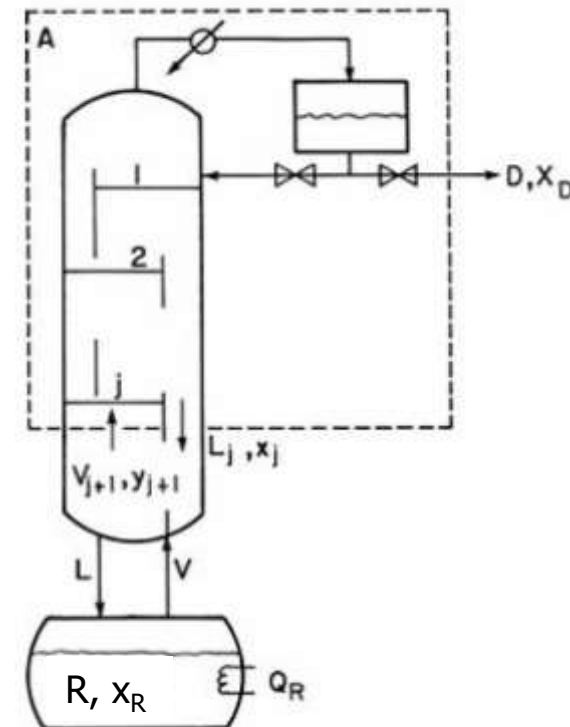
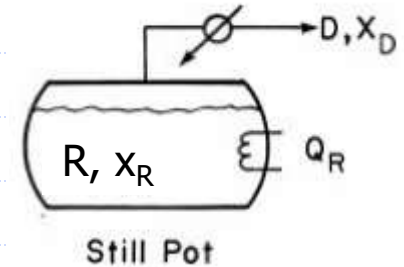
- rearranging:  $-x_D dR = -R d(x_R) - x_R d(R)$

- Finally:

$$\ln \frac{R}{F} = \int_{z_F}^{x_R} \frac{dx_R}{x_D - x_R}$$

- ◆ Rayleigh equation

- is valid for simple and multistage batch distillation.
- We must relate  $x_D$  to  $x_R$  and do the appropriate integration





# Rayleigh Equation Notes

◆ Note that  $x_R$  will change with time starting at  $z_F$  ( $t = 0$ ) and ending at  $x_{R,final}$  ( $t = final$ ).

- However,  $x_D$  also changes over time (note that it is not the same as the  $x_{D,average}$ ).
- Thus, in order to integrate the right-hand side of Eq. (11-6), we need a relationship between  $x_D$  and  $x_R \rightarrow x_D = f(x_R)$

◆ If we have a column

- with an  $N$  number of stages,
- and we are operating at constant  $L/D$ ,
- we can use the McCabe-Thiele analysis to step off the stages from  $x_D$  and determine the resulting  $x_R$  to give us an  $x_D = f(x_R)$ .
- We just assume different  $x_D$ 's, step-off, and determine the resulting  $x_R$ 's.

◆ Simple binary batch distillation

- Rayleigh equation can be integrated analytically

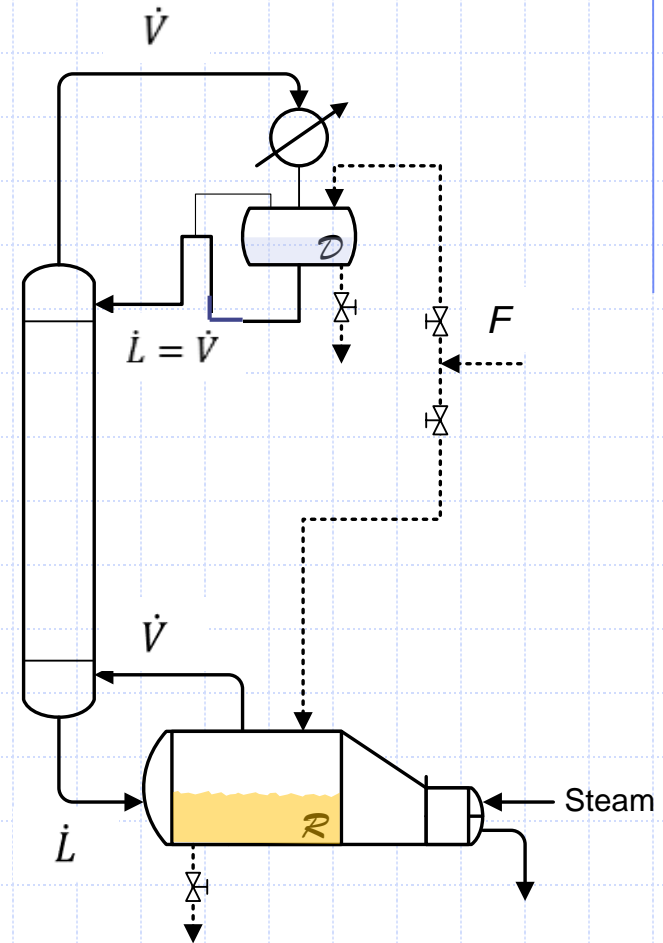
$$\ln \frac{R}{F} = \int_{z_F}^{x_R} \frac{dx}{x - f(x)}$$

# Total Reflux

- ◆ Note that a multistage batch still, operated such that all of the distillate is returned to the top of the column, is essentially the same as a multi-stage distillation column operated under **total reflux**.
- ◆ For a binary separation, given a column containing an  $N$  number of equilibrium stages, one can measure  $x_D$  at the top of the column and  $x_B$  at the bottom of the column and perform a McCabe-Thiele analysis to determine the theoretical  $N_{\min}$ .

# Multistage Fully Batch operation (total reflux)

- ◆ Feed  $F$  is divided between the boiler and the top accumulator
- ◆ After start up (stages flooding) the column is operated at total reflux:  $L=V$  at all times  $\rightarrow D$  and  $R$  are constant
  - the light component will concentrate at the top and the heavy at the bottom
  - Operation is stopped when specification for both product is reached.
- ◆ Note:
  - Final compositions  $x_D$  and  $x_R$  depend on how the feed is divided
  - if  $D < D_{spec}$  bottom will be polluted by light components
  - If  $D > D_{spec}$  top will be polluted by heavy components



$$\frac{D}{F} = \frac{z_F - x_{R,spec}}{x_{D,spec} - x_{R,spec}} \quad \frac{R}{F} = \frac{x_{D,spec} - z_F}{x_{D,spec} - x_{R,spec}}$$

# Multistage Fully Batch operation (total reflux)

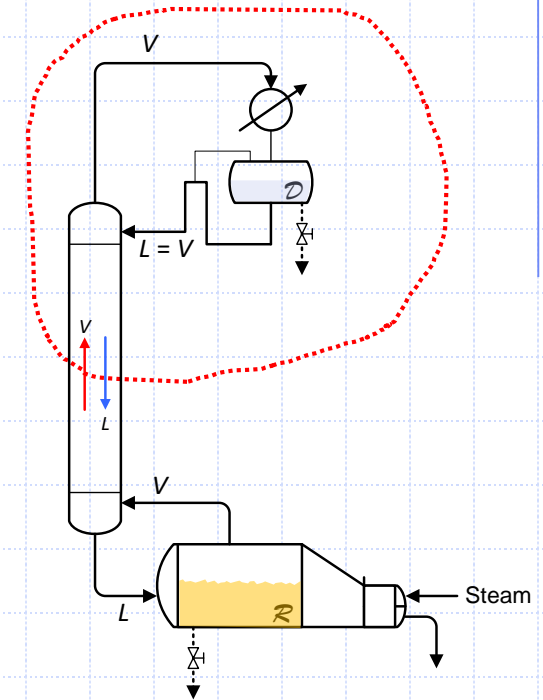
- ◆ Tank compositions varies continuously during operation
- ◆ At each time the global material balance is:  

$$F = D + R \qquad Fz_F = Dx_D + Rx_R$$
- ◆ Balance of the upper part of the column:

$$\frac{dDx_D}{dt} = \dot{V}y_{j+1} - \dot{L}x_j \xrightarrow{D = \text{const}, \dot{L} = \dot{V}} \boxed{y = x + \frac{D}{\dot{V}} \frac{dx_D}{dt}}$$

- ◆ Assuming negligible hold-up in the column with respect to the tanks:

$$D \frac{dx_D}{dt} = -R \frac{dx_R}{dt}$$

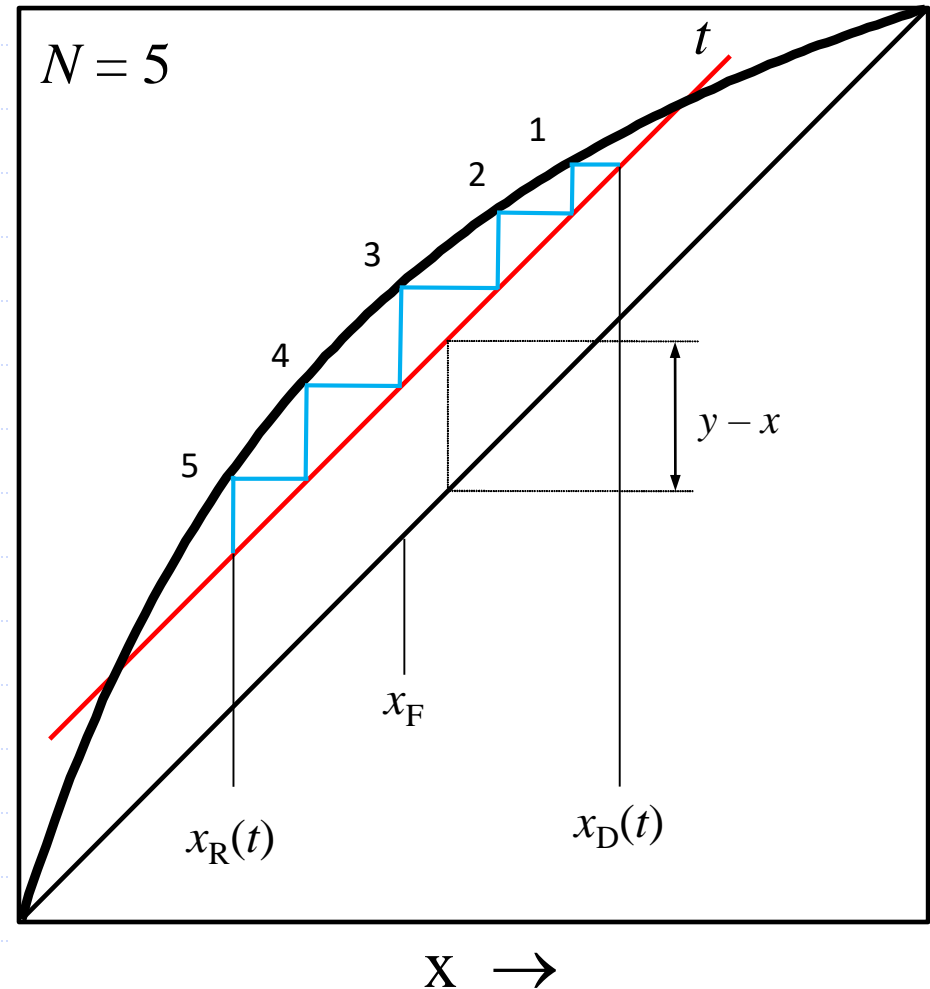


# Multistage Fully Batch operation (total reflux)

- ◆ At each time, the OL has a slope = 1 and its distance from  $y=x$  line is  $(y-x)$
- ◆ Fix an  $x_D(t)$  initial guess
- ◆ Step down the column and find the value  $x_R(t)$  compatible with the initial guess
  - The two compositions are correct if they satisfy the global balance too

$$D(x_D - z_F) = R(z_F - x_R)$$

- ◆ The OL moves in time getting closer to the diagonal

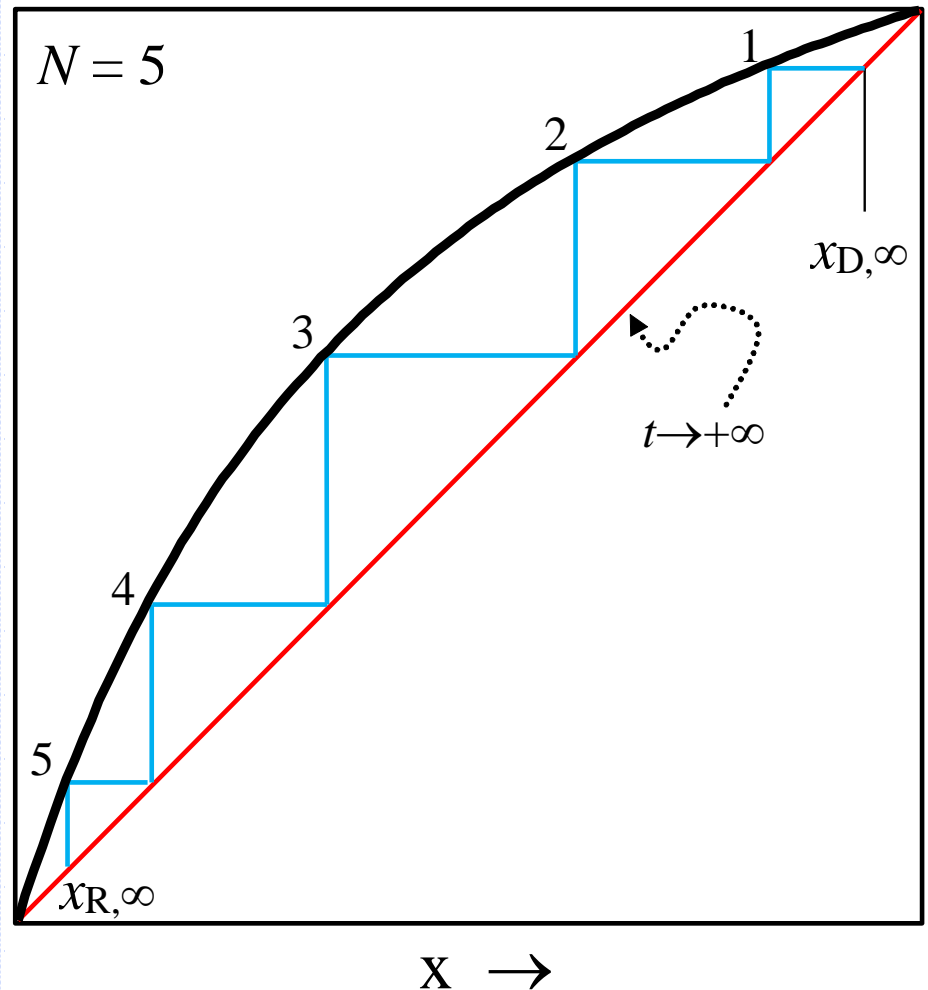


# Multistage Fully Batch operation (total reflux)

- ◆ After a long time (infinite time) the OL overlaps to the diagonal
- ◆ Compositions will have to satisfy the global balance

$$D(x_{D,\infty} - x_F) = R(x_F - x_{R,\infty})$$

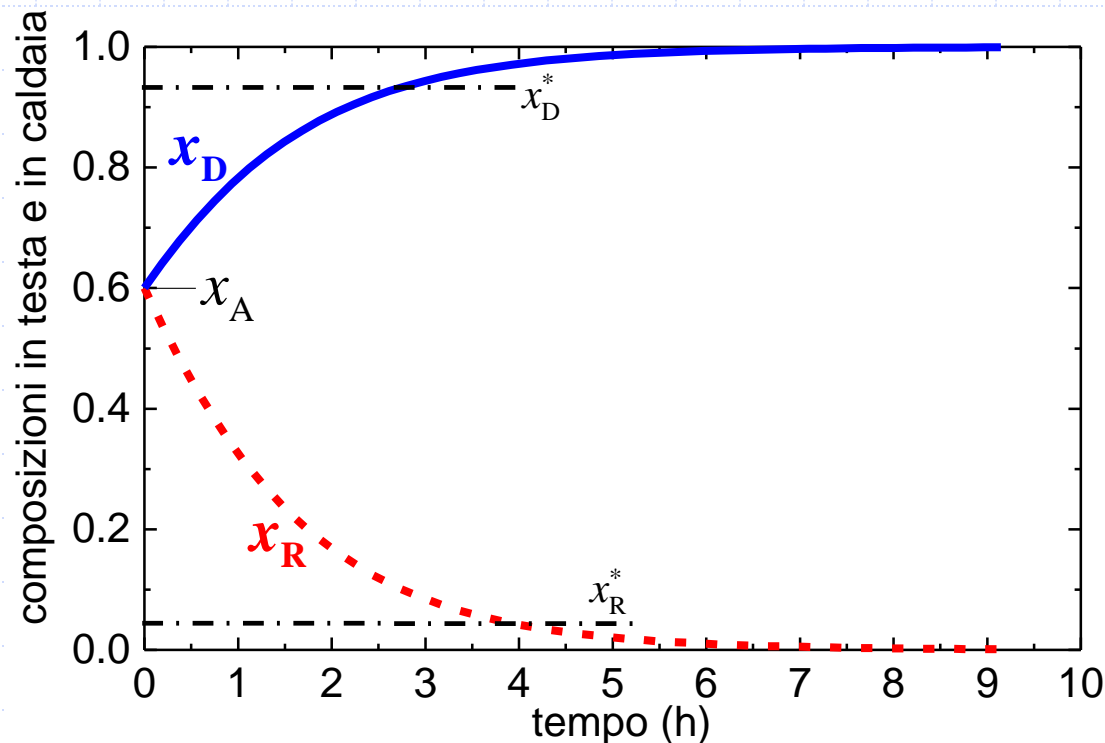
- ◆ Desired purity  $x_{D,\text{spec}}$  and  $x_{R,\text{spec}}$  will always be less than the maximum ones,
  - reachable at stationary regime only (i.e. at  $t \rightarrow \infty$ )



# Multistage Fully Batch operation (total reflux)

## ◆ Typical concentration profiles

- If, for a fixed  $z_F$  D and F are correctly chosen and the column has a sufficiently high number of stages,
- it is possible to get both products at high purity



# Multistage Fully Batch operation (total reflux)

- ◆ The heat required for a given separation is:

$$Q_r = \lambda \int_0^{t_F} \dot{V} dt = \lambda D \int_{z_A}^{x_{D,spec}} \frac{dx_D}{y-x}$$

- ◆ And the time  $t_F$  to reach the product specifications is:

$$t_F = \frac{Q_r}{\lambda_{st} W_{st}}$$

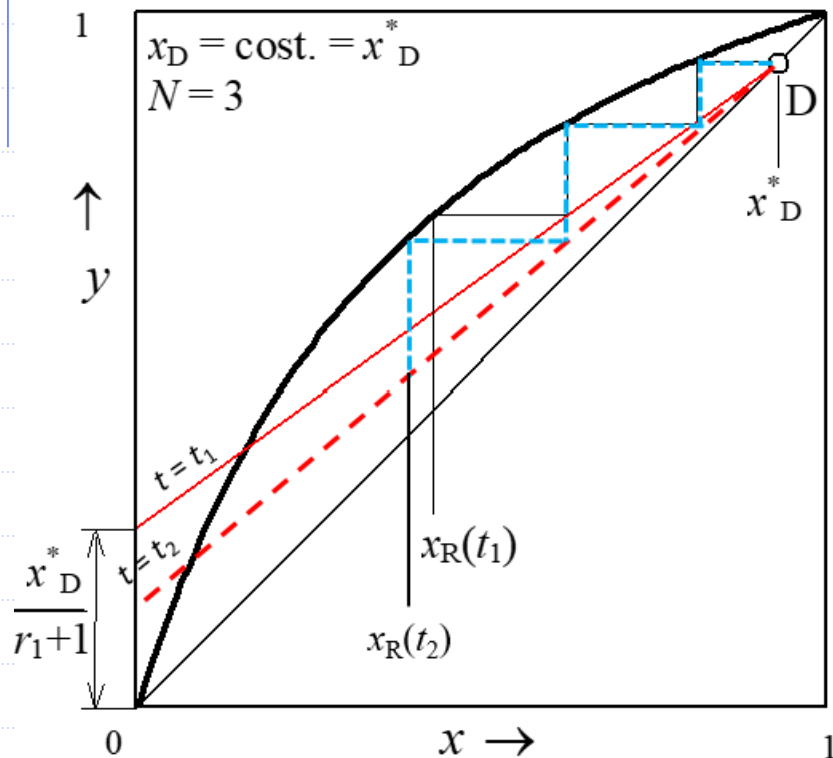
- ◆ The value of the integral does not depend on the vapor flow rate.
  - $Q_R$  is a function of the required separation ( $x_{D,spec} - x_{R,spec}$ ),
  - Vapor consumption is independent on how the separation is operated
  - This means that no control is necessary: it should only be run at total reflux.



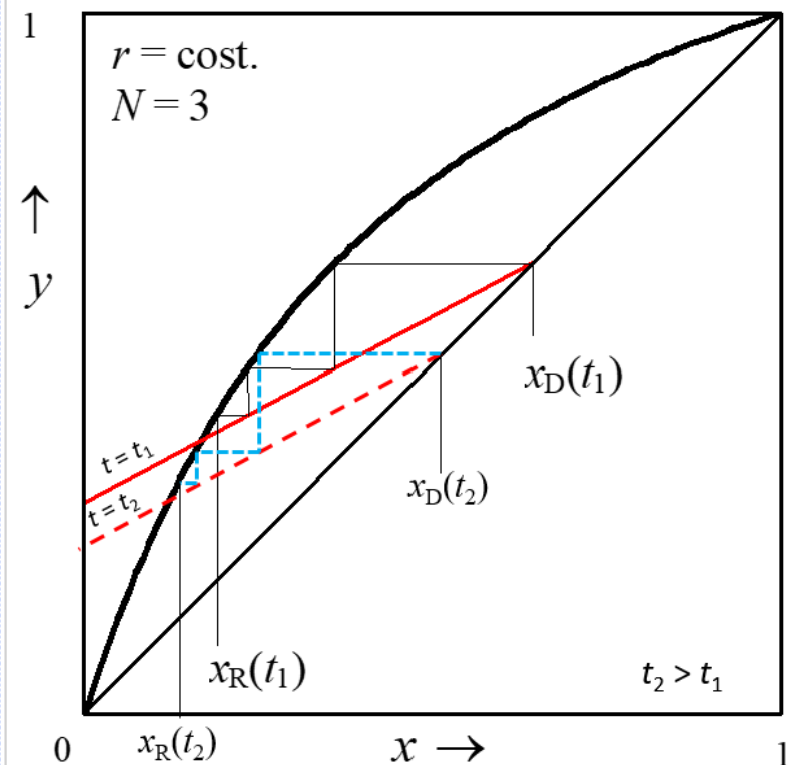


# Multistage Semi-Batch Distillation

- ◆ Multistage semi batch operation may be operated in two different conditions:
- ◆ Constant  $x_D$



## Constant L/D



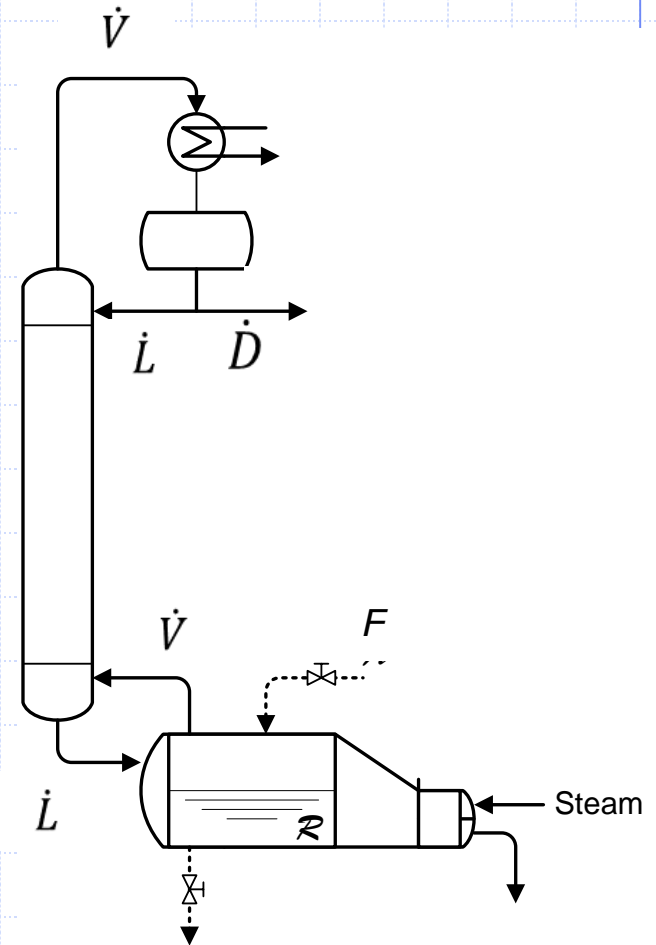
# Semi-batch distillation process

## ◆ Assumptions

- Adiabatic column
- Hold-up negligible in the column and in the condenser
- Hold-up in reboiler only
- Constant column efficiency during operation (time)
- Column at steady state at each time (quasi-stationary hypothesis)

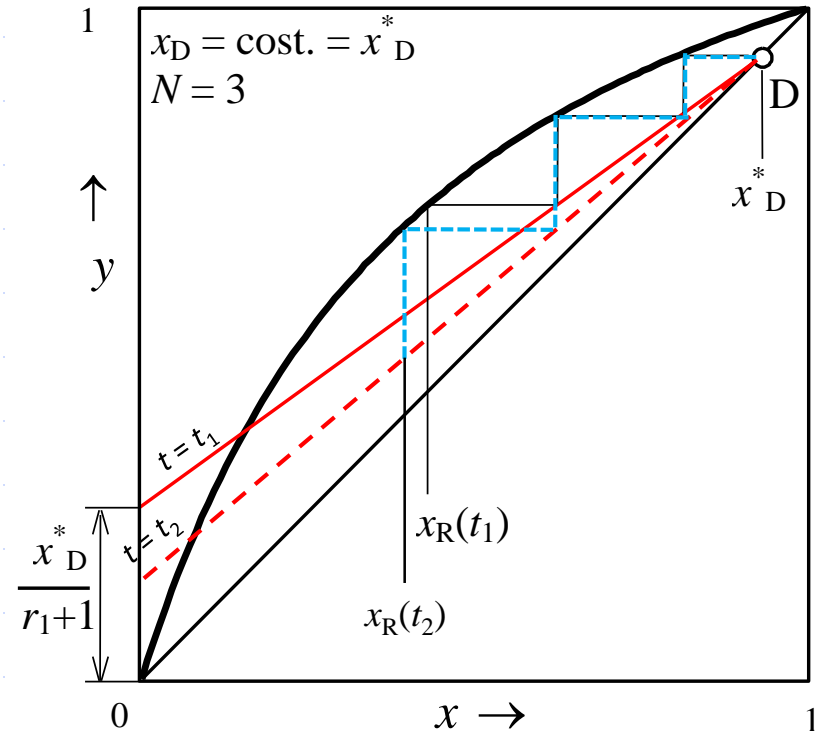
## ◆ In these conditions

- The column is a simple enrichment section only column
- With variable composition feed
- With constant feed flow rate



# Semi-batch distillation process

- ◆ After startup, reflux flow rate  $L$  is varied so that  $x_D = x_{D,spec}$ 
  - At any time  $t_1$ , with fixed  $r$ , it is possible to find the composition in the reboiler at that time  $t_1$
  - Since light component is output from the top, its concentration in the reboiler goes down
  - To keep  $x_D$  at the desired value, it is necessary to push the separation and therefore raise the value of  $r$



# Constant $x_D$ operation

- ◆ The column is operated at constant  $x_D$ 
  - First value for  $r$  is such to fit exactly  $N$  stages between  $x_D$  and  $x_F$
  - Last value for  $r$  is such to fit exactly  $N$  stages between  $x_D$  and  $x_R$

- ◆ Energy balance and steam consumption

- Reflux ratio (instantaneous)

$$dQ_r = \lambda(r + 1)dD \longrightarrow Q_r = \lambda \int_0^{D, spec} (r + 1)dD$$

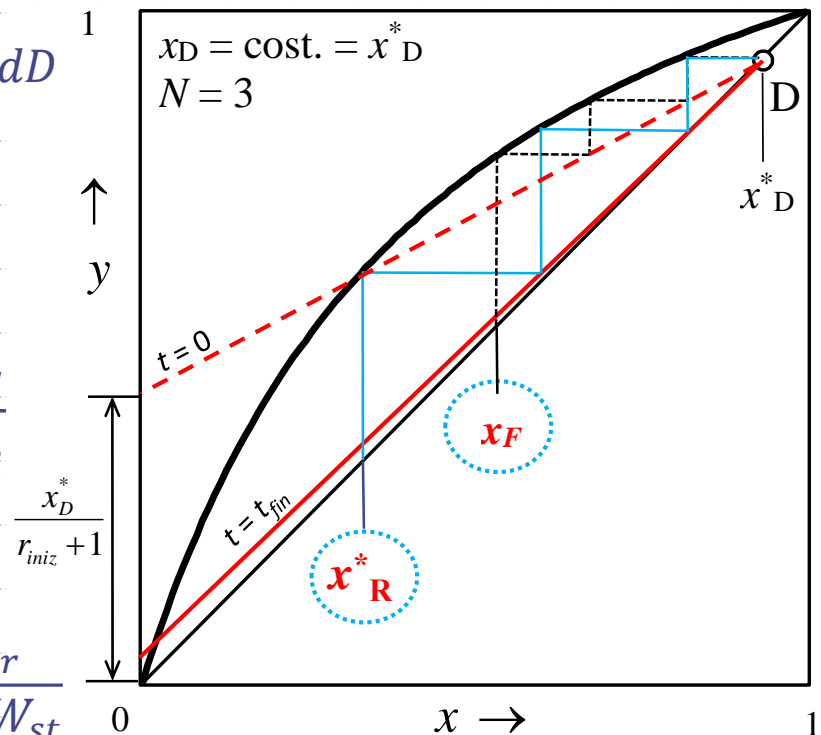
- It is necessary to know the function  $r(D)$ . Starting from Rayleigh eq.:

$$\ln \frac{R}{F} = \int_{z_F}^{x_R} \frac{dx_R}{x_D - x_R} \xrightarrow{x_D = \text{cost}} R = F \frac{x_D - x_F}{x_D - x_R}$$

- $r(x_R)$  is transformed in  $r(R)$ , and consequently one gets  $r(D)$ .

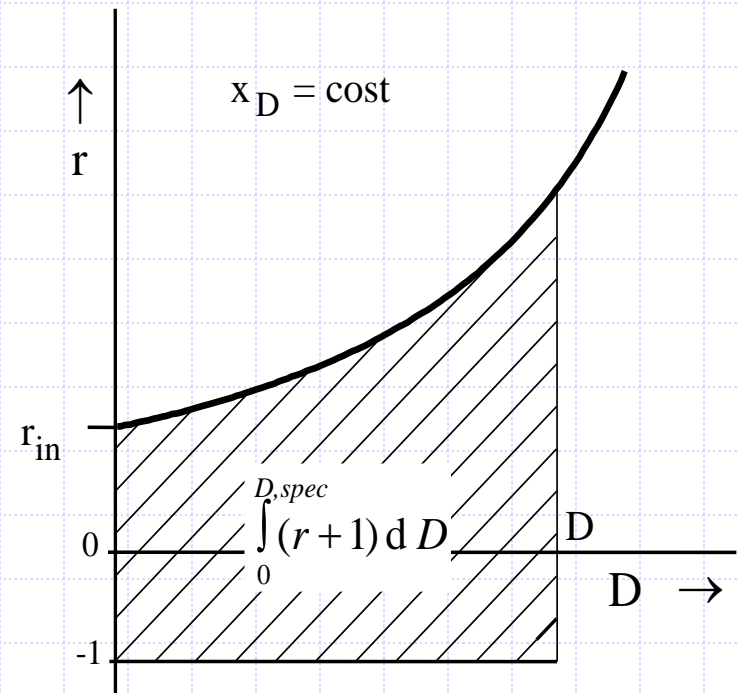
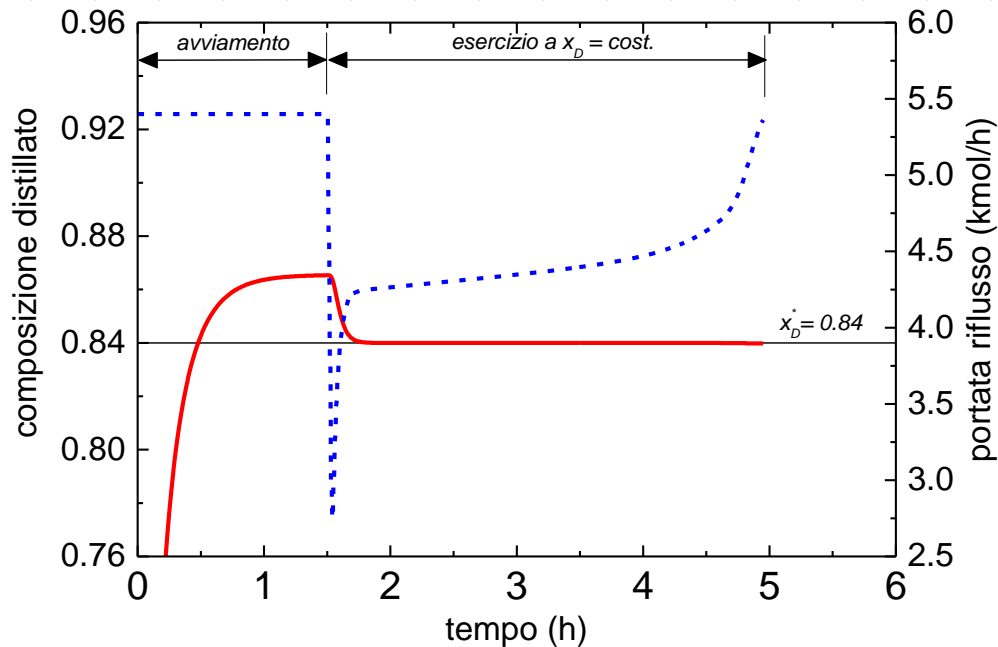
- The time of batch process is:  $t_F = \frac{Q_r}{\lambda_{st} W_{st}}$

$$r = \frac{\dot{L}dt}{dD}$$



# Constant $x_D$ operation

- ◆ At the end of the operation, big steam consumption is required for small quantities of distillate
- ◆ It is possible to decide a maximum value of  $D$ 
  - Beyond which the operation is not economical any more
  - And column operation is very difficult since the raise of  $r$  is not linear in time



# Constant reflux operation

- ◆ After start up the reflux flow rate  $L$  is kept constant and therefore also  $D$  is constant:

$$Q_r = \lambda(r + 1)D$$

- ◆  $r$  is determined by a trial and error procedure.
  - Material balances must be satisfied in the form:

$$R = F \frac{x_{D,spec} - z_F}{z_F - x_{R,spec}}$$

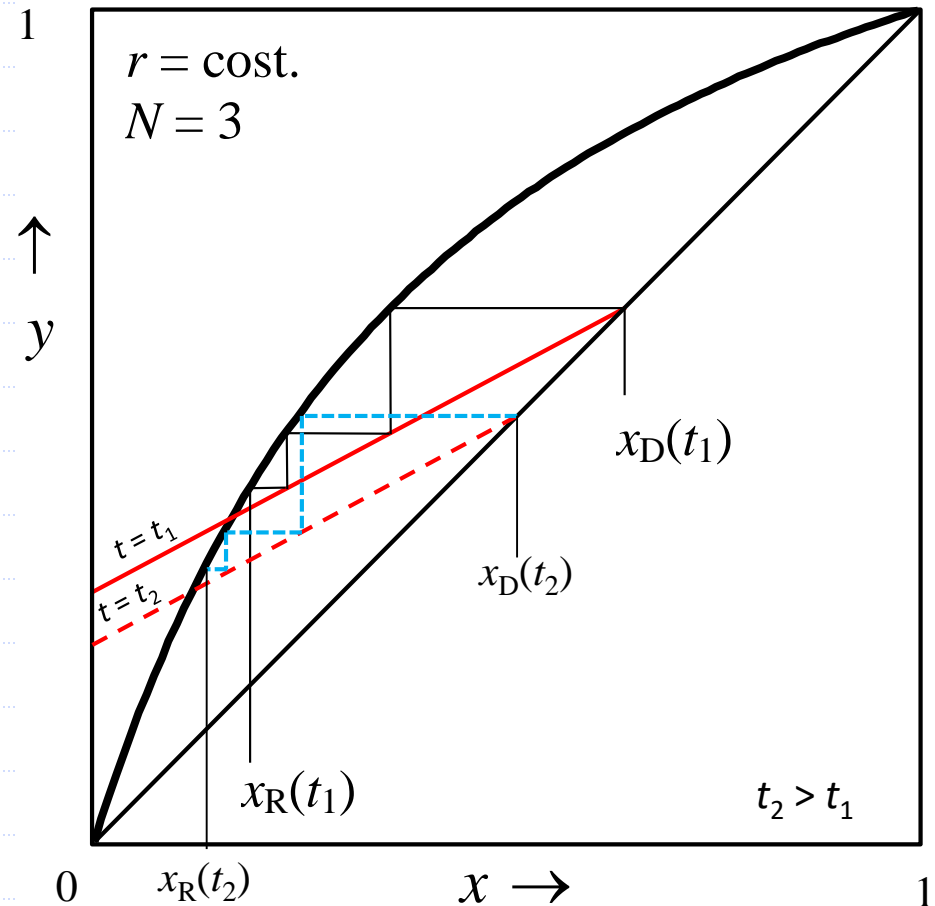
- And Rayleigh equation is:

$$\ln \frac{R}{F} = \int_{z_F}^{x_R} \frac{dx_R}{x_D - x_R}$$

Integration requires to know the function  $x_D(x_R)$ , to be obtained through a McCabe-Thiele construction.

# Constant reflux operation

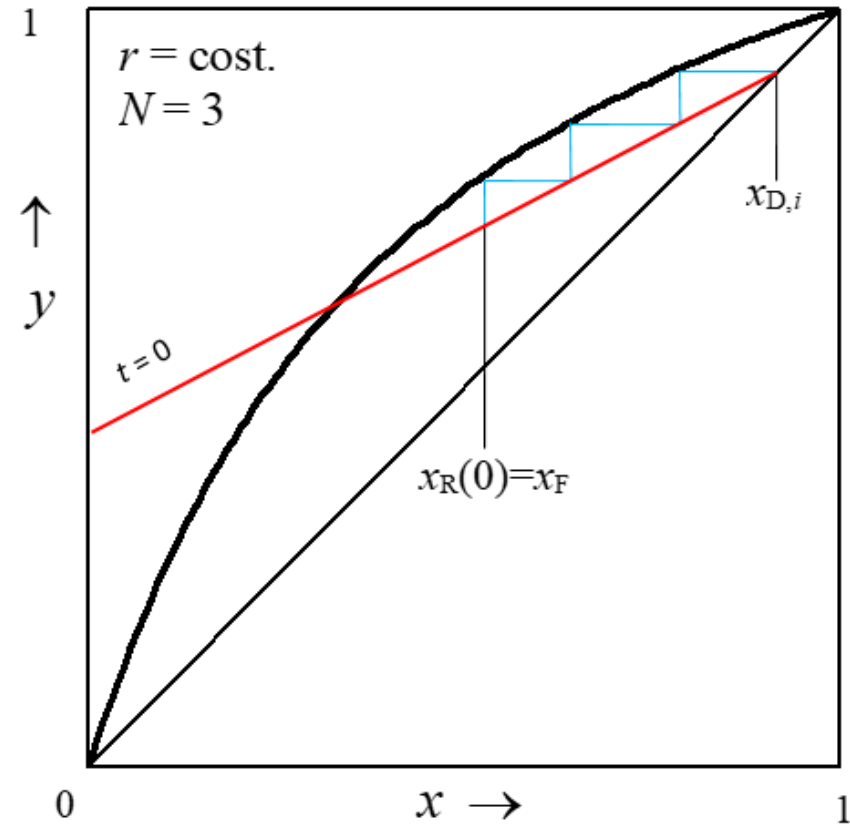
- ◆ An arbitrary value of  $r$  is chosen
  - between the instantaneous composition of the distillate and the residue
  - so that the exact number of stages fits in.
- ◆ Light component is extracted in the distillate,  $\rightarrow$  the concentration of the light component goes down in the reboiler ( $x_R$  falls in tempo)
- ◆ Since  $N$  is fixed  $\rightarrow$  if  $x_R$  goes down in time,  $x_D$  goes down too
- ◆ The OL moves downwards keeping the same slope
- ◆ Final composition of the distillate will be the average of the compositions in time





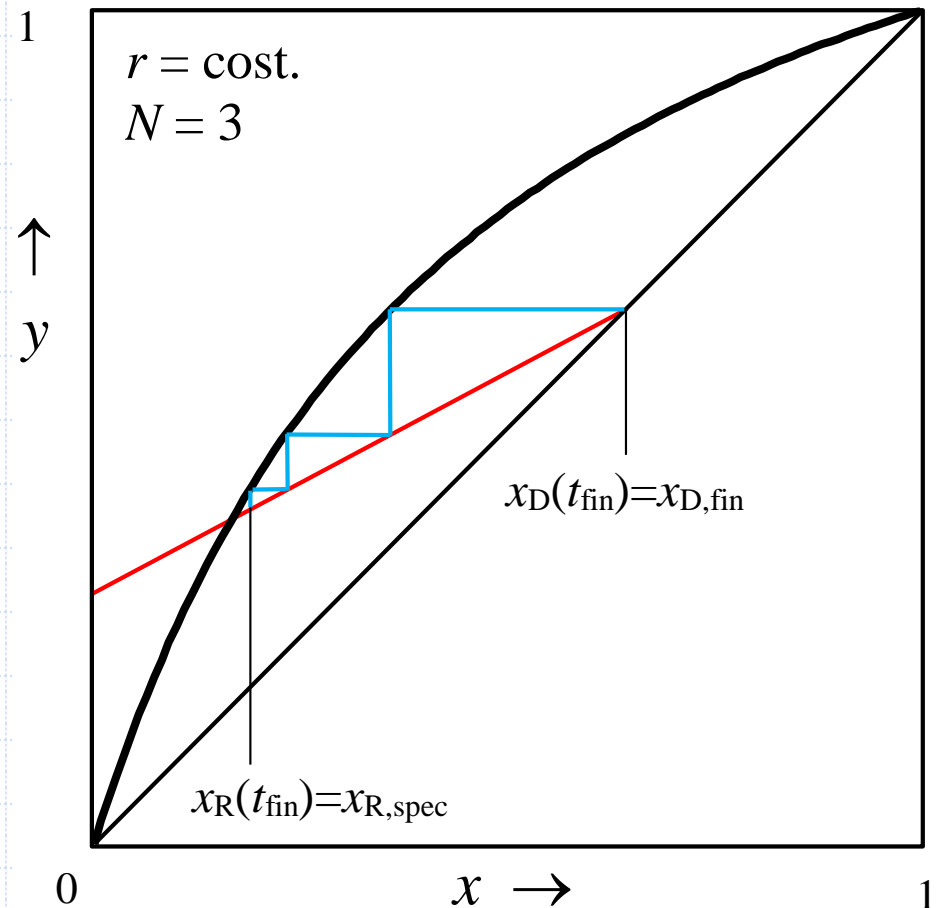
# Constant reflux operation

- ◆ Initial distillate composition  $x_{D,i}$  allows to get to the  $x_F$  composition of the feed to the reboiler with exactly  $N = 3$  stages



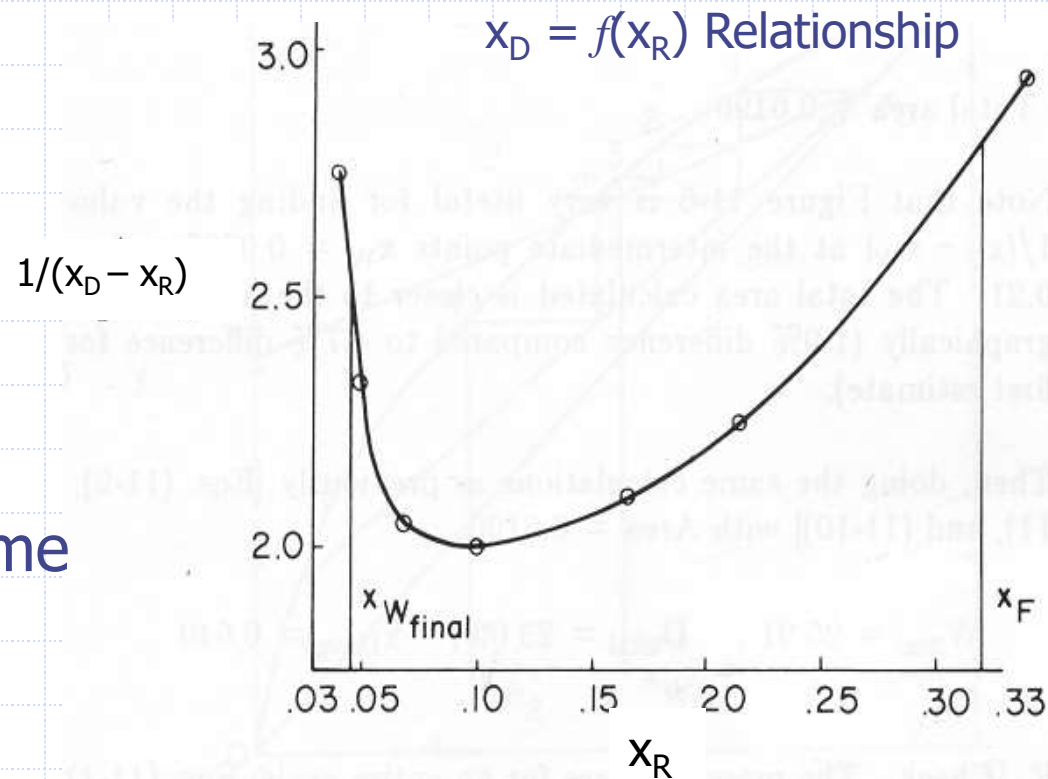
# Constant reflux operation

- ◆ Construction stops when bottom composition is equal to the specification ( $x_{R,spec}$ )



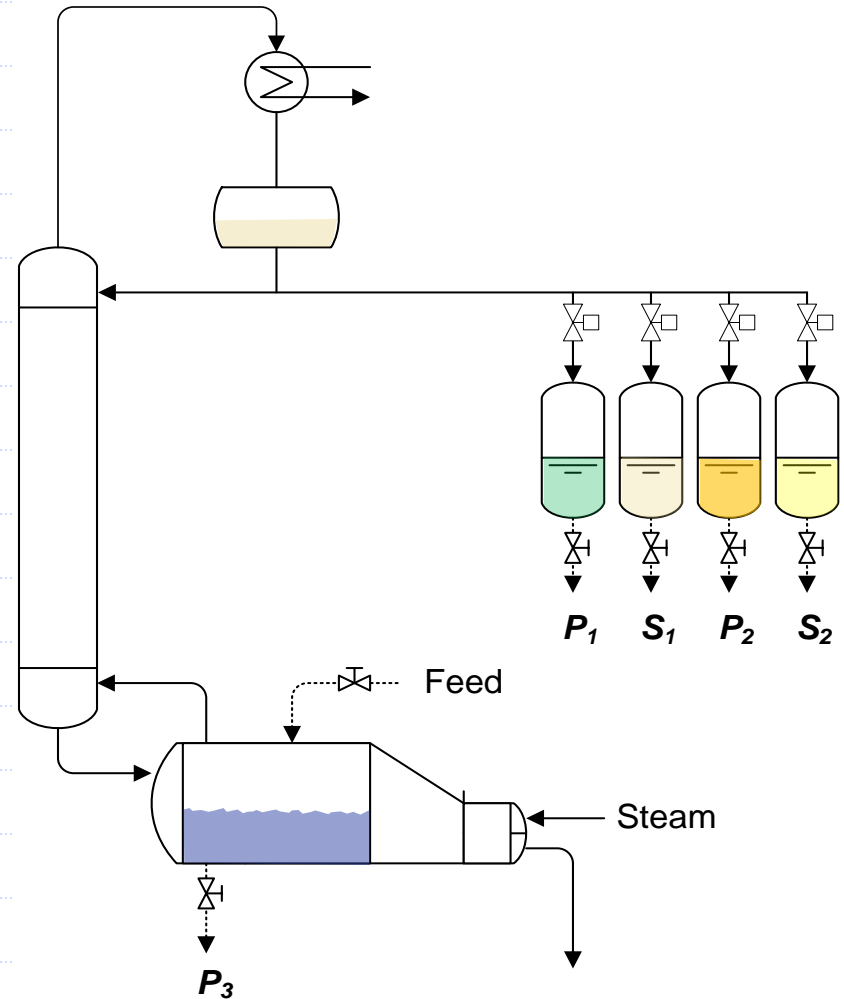
# Constant reflux operation

- ◆ For a given  $L/D$  and number of column stages, assume  $x_D$ 's, perform a McCabe-Thiele Analysis at each  $x_D$  stepping down to determine the corresponding  $x_R$ 's.
- ◆ Plot  $1/(x_D - x_R)$  vs.  $x_R$ .
- ◆ Graphically integrate
  - or do a polynomial curve fit between  $x_R = z_F$  and  $x_R = x_{R,final}$  and integrate.
  - Use Polymath or Excel for integration
- ◆ The correct value of  $r$  satisfies at the same time both Rayleigh equation and material balances



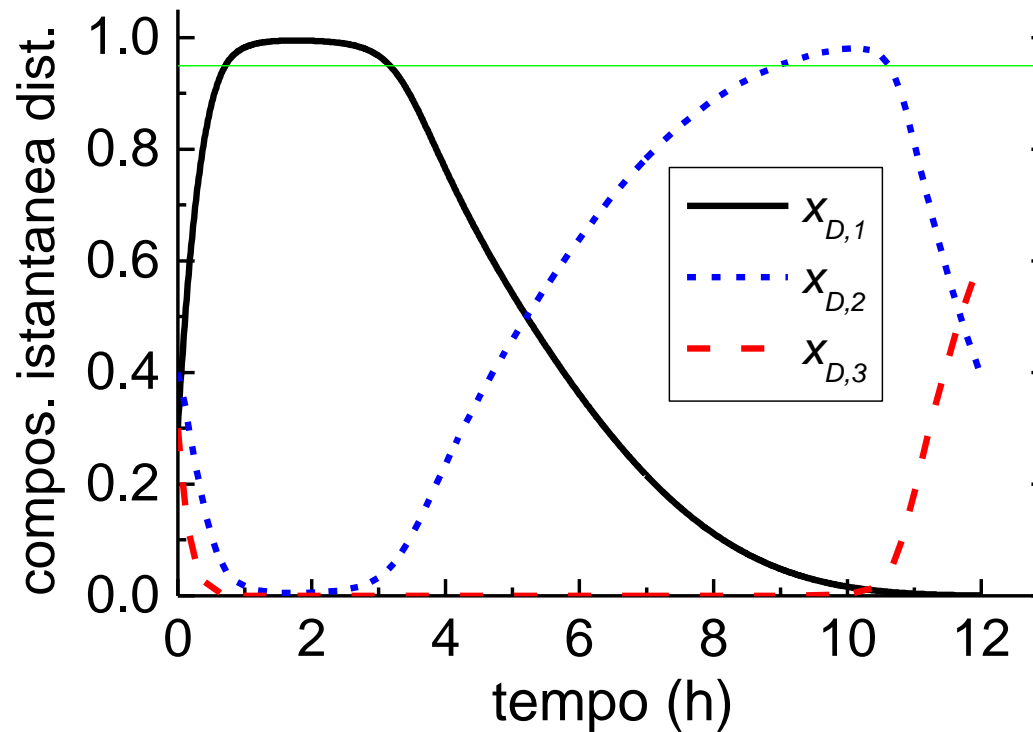
# Multicomponent batch distillation

- ◆ It is possible to treat multicomponent mixtures ( $N_c = 3$  in the example)
  - Different product cuts are obtained ( $P_1, P_2$  e  $P_3$ )
  - wastes (slop cuts) are obtained ( $S_1$  and sometimes  $S_2$ )
  - Heavier product is always obtained in the reboiler at the end of the batch.
- ◆ Tanks are needed
  - One for each cut;
  - slop cuts could be mixed and treated again in the same column
- ◆ One column is sufficient for obtaining all requested  $N_c$  cuts
  - A continuous operation would have required  $N_c - 1$  columns



# Multicomponent batch distillation

## ◆ Typical composition profiles



# Column Overall Efficiency

- ◆ For a column containing an  $N_{\text{actual}}$  number of stages, the overall efficiency can be determined from

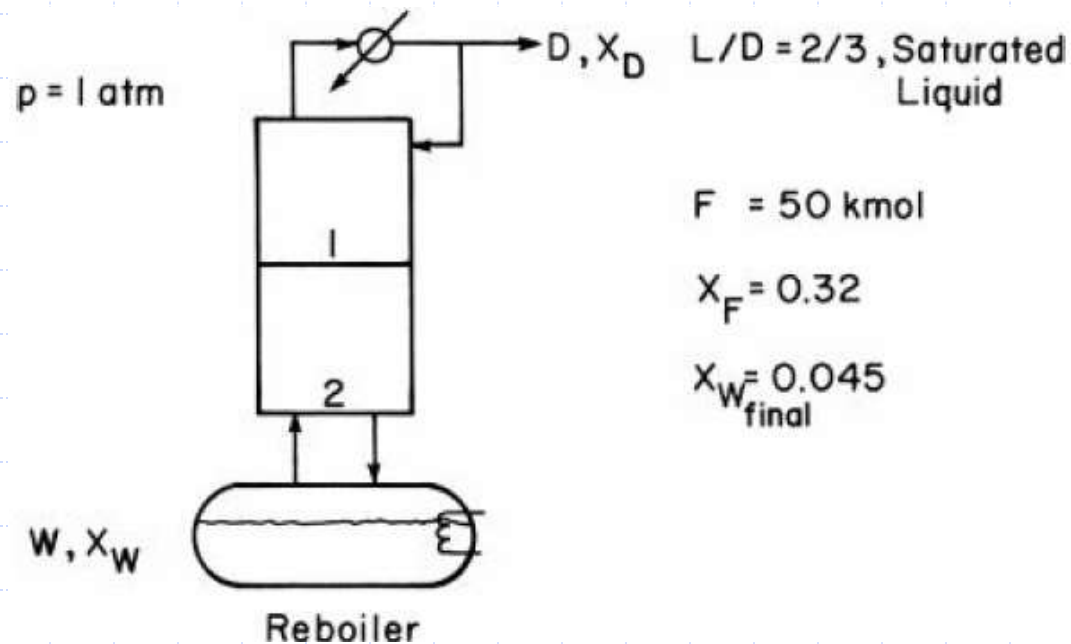
$$E_o = N_{\text{equil}} / N_{\text{actual}}$$

where  $N_{\text{equil}}$  is the theoretical  $N$  obtained from the McCabe Thiele analysis.

# Example: ethanol – water batch distillation

- ◆ We wish to batch distill 50 kmol of a 32 mol% ethanol, 68 mol% water feed. The system has a still pot plus two equilibrium stages and a total condenser. Reflux is returned as a saturated liquid, and we use  $L/D = 2/3$ . We desire a final still pot composition of 4.5 mol% ethanol.

Find the average distillate composition, the final charge in the still pot, and the amount of distillate collected.  
Pressure is 1 atm.



# Example: ethanol – water batch distillation

## ◆ Solution

- The McCabe-Thiele diagram for several arbitrary values of  $x_D$  is shown in Figure.

- The top operating line is

$$y = \frac{L}{V}x + \left(1 - \frac{L}{V}\right)x_D$$

- Where  $L/V = (2/3)/(5/3) = 2/5$

- The corresponding  $x_W$  and  $x_D$  values are used to calculate  $x_D - x_W$  and then  $1/(x_D - x_W)$  for each  $x_W$  value.

- These values are plotted in Figure. The area under the curve from  $x_F = 0.32$  to  $x_{W,final} = 0.045$  is 0.608 by graphical integration.

- From Eq.:  $W_{final} = F \exp^{-\text{Area}} = (50) \exp(-0.608) = 27.21$

- From Eq.:  $D_{total} = F - W_{final} = 22.79$

- From Eq.:

$$x_{D,avg} = \frac{F x_F - W_{final} x_{W,final}}{F - W_{final}} = 0.648$$

- The area can also be found by Simpson's rule.

