

# Cyber-Physical Systems

Laura Nenzi

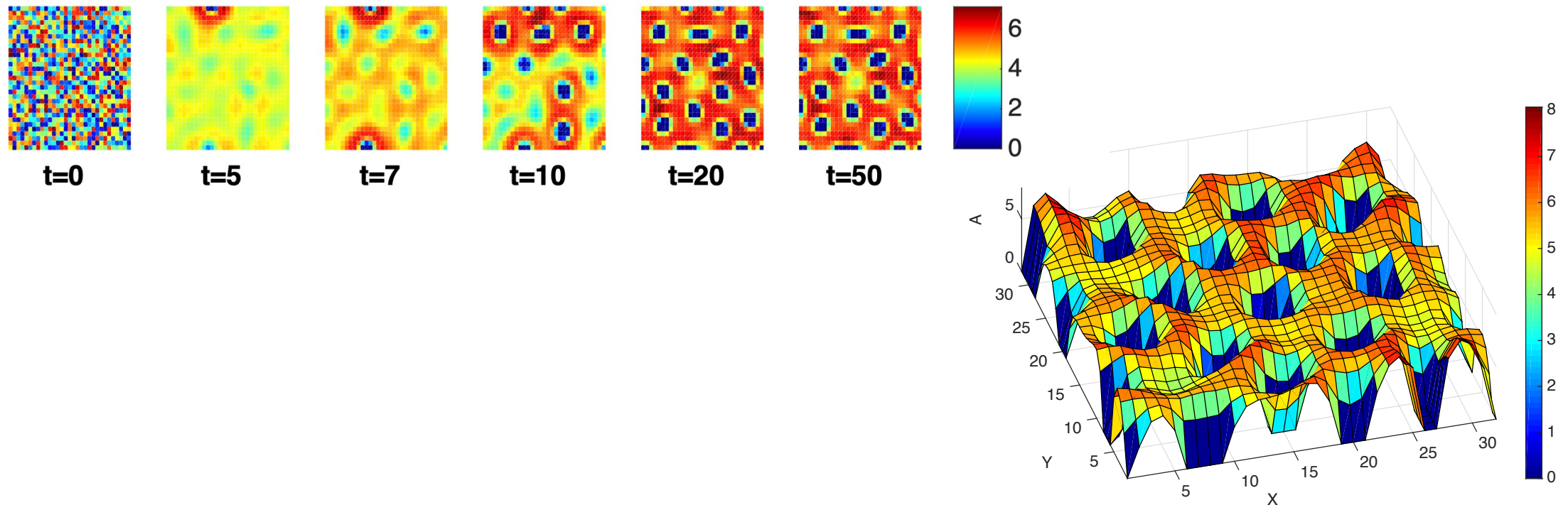
Università degli Studi di Trieste  
II Semestre 2020

Lecture 17 (II) STREL : Spatio-Temporal Reach and Escape Logic

# Static Space and Regular Grid

# The formation of Patterns

The production of skin pigments that generate spots in animal furs:

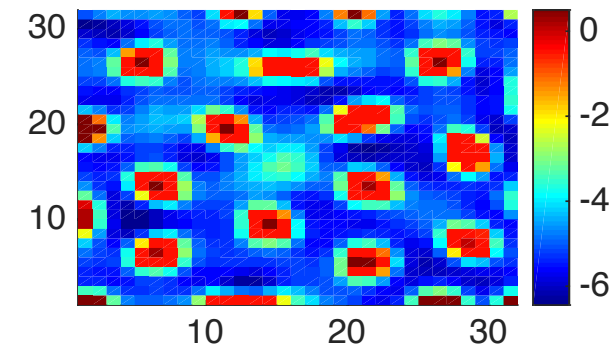
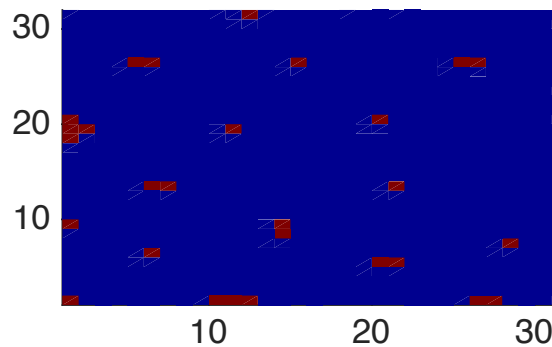
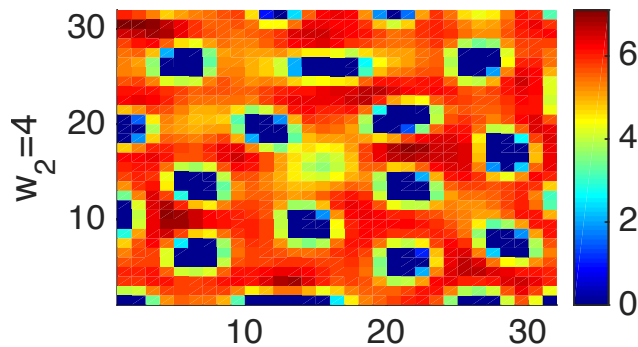
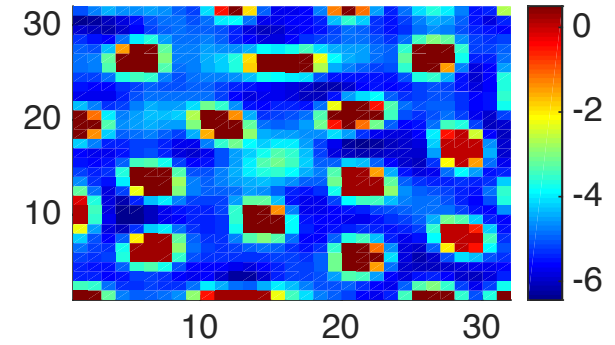
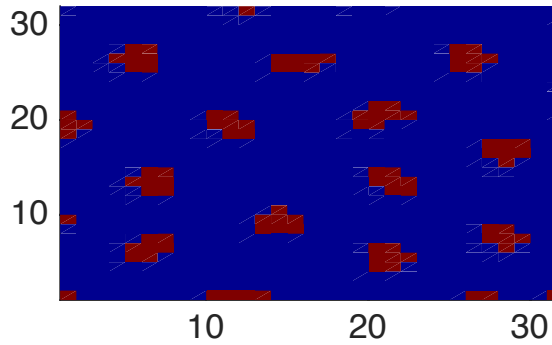
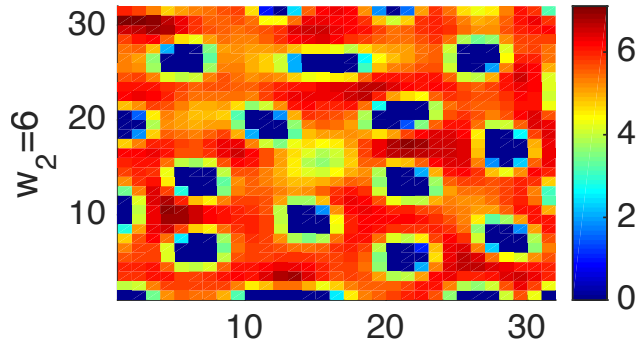


Space model: a  $K \times K$  grid treated as a graph,  $\text{cell}(i, j) \in L = \{1, \dots, K\} \times \{1, \dots, K\}$

Spatio-Temporal Trajectory:  $x: L \rightarrow \mathbb{T} \rightarrow \mathbb{R}^2$  s.t.  $x(\ell) = (x_A, x_B)$

# Spot formation property

$$\phi_{spot_{form}} = F_{[19,20]} G((A \leq 0.5) \odot_{[1,w_2]}^{hops} (A > 0.5))$$



$x_A(50, l)$

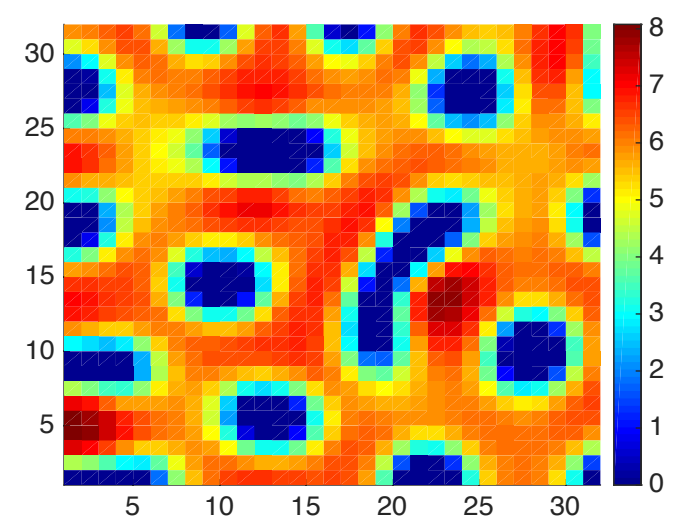
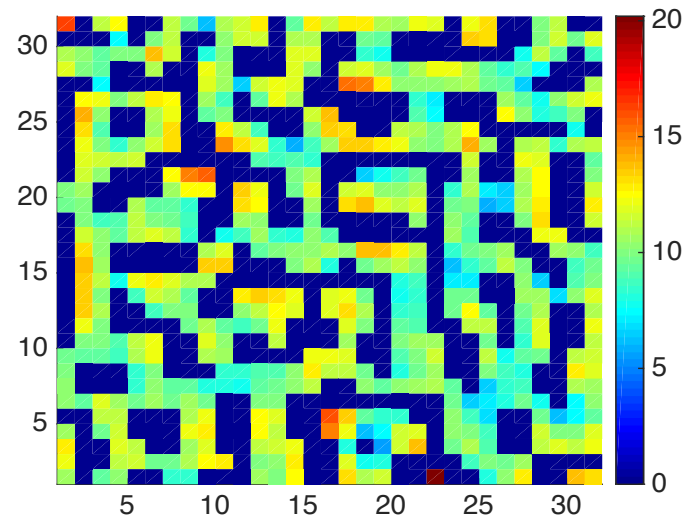
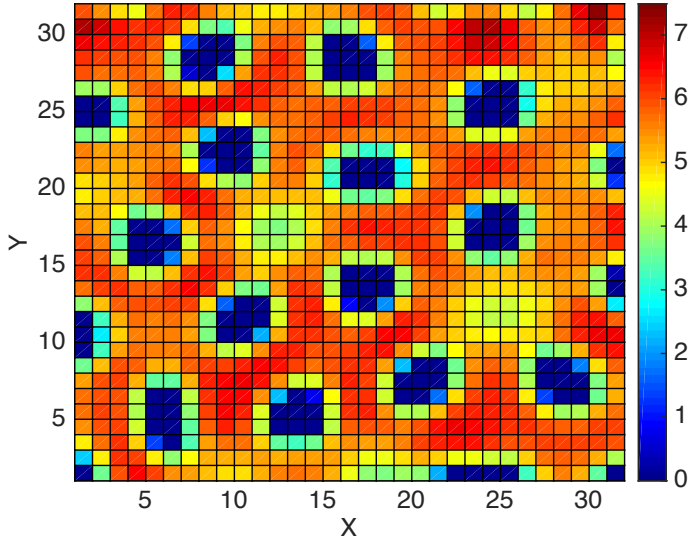
Boolean sat.

Quantitative sat.



# The formation of Patterns

$$\phi_{pattern} := \square^{hops} \diamond_{[0,15]}^{hops} \phi_{spot_{form}}$$

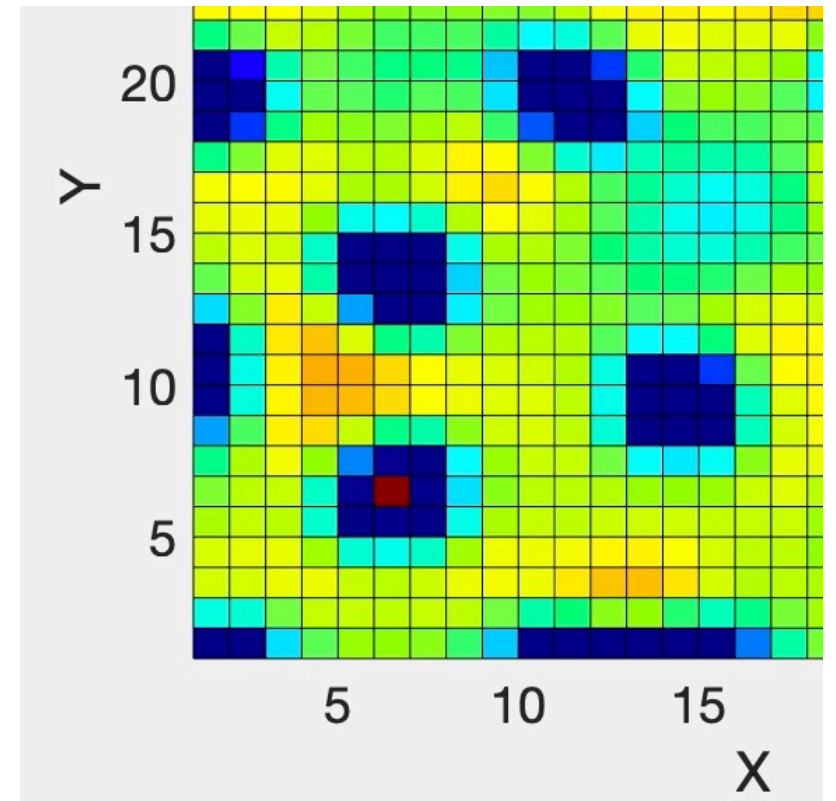


# Perturbation Property

$$\phi_{\text{pert}} := (x_A \geq 10) \wedge (\phi_{\text{absorb}} \odot_{[1,2]}^{\text{hops}} \phi_{\text{no\_effect}})$$

▶  $\phi_{\text{absorb}} = F_{[0,1]} G_{[0,10]} (x_A < 3)$ ;

▶  $\phi_{\text{noeffect}} := G_{[0,20]} (x_A < 3)$



# Static Space and Stochastic Systems

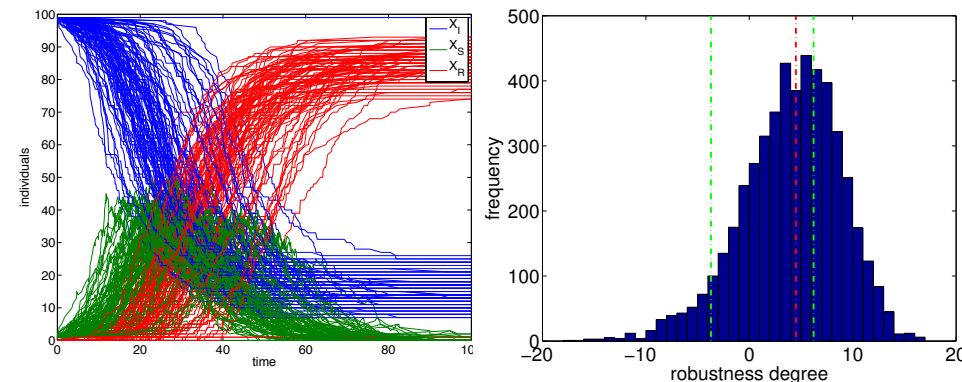
# Application to Stochastic Systems

STREL can be applied on stochastic systems considering methodologies as Statistical Model Checking (SMC)

Stochastic process  $\mathcal{M} = (\mathcal{T}, \mathcal{A}, \mu)$  where  $\mathcal{T}$  is a trajectory space and  $\mu$  is a probability measure on a  $\sigma$ -algebra of  $\mathcal{T}$ .

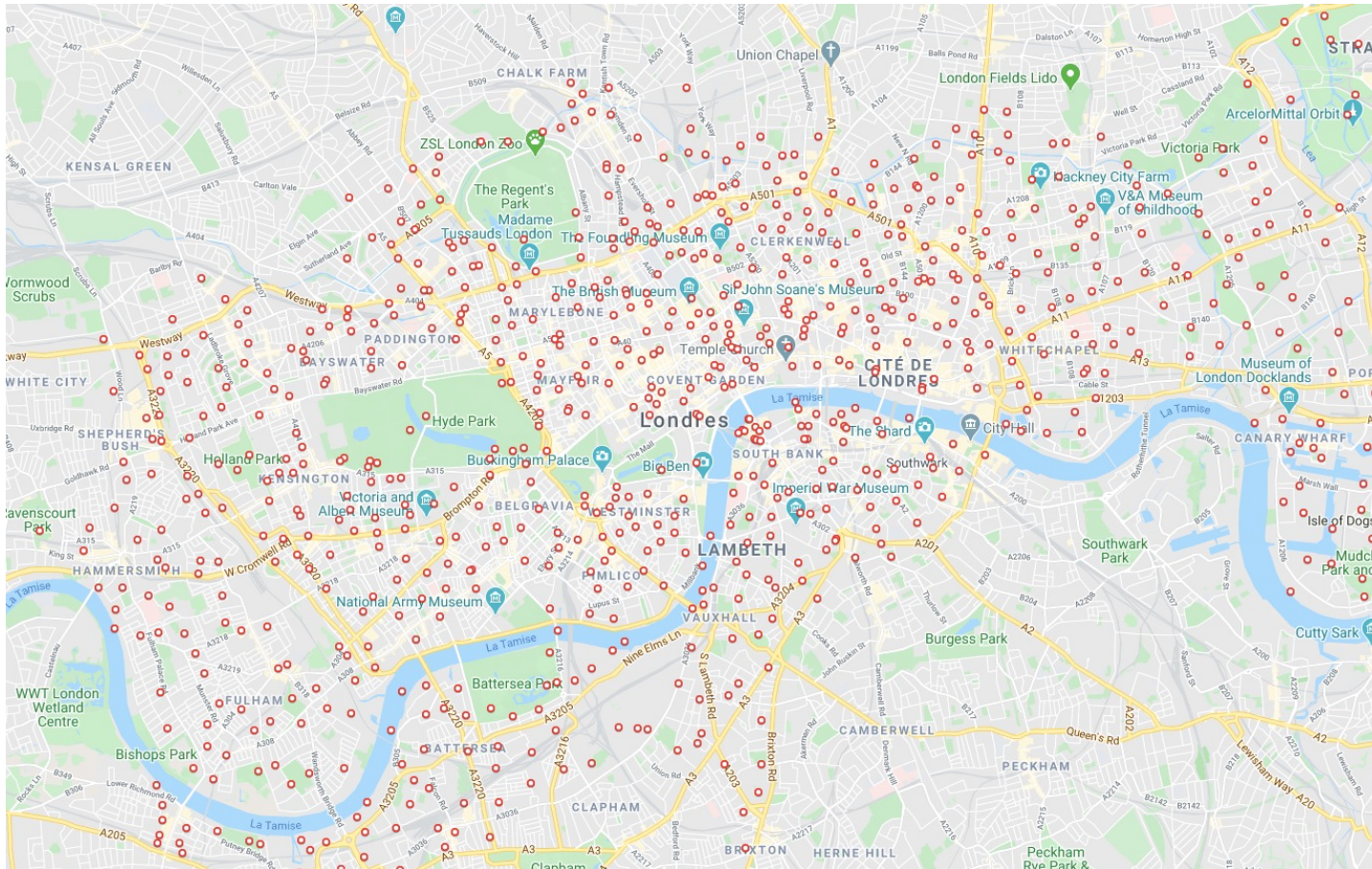
We approximate the satisfaction probability  $\mathcal{S}(\varphi, t)$ , i.e. the probability that a trajectory generated by the stochastic process  $\mathcal{M}$  satisfies the formula  $\varphi$ .

We can do something similar with the quantitative semantics computing the robustness distribution



# Bike Sharing Systems (BSS)

## London Santander Cycles Hire network



- 733 bike stations (each with 20-40 slots)
- a total population of 57,713 agents (users) picking up and returning bikes

We model it as a Population Continuous Time Markov Chain (PCTMC) with time-dependent rates, using historic journey and bike availability data.

Prediction for 40 minutes.

# Bike Sharing Systems (BSS)

Spatio-Temporal Trajectory:  $x: L \times \mathbb{T} \rightarrow \mathbb{Z}^2$  s.t.  $x(i, t) = (B_i(t), S_i(t))$

Space model

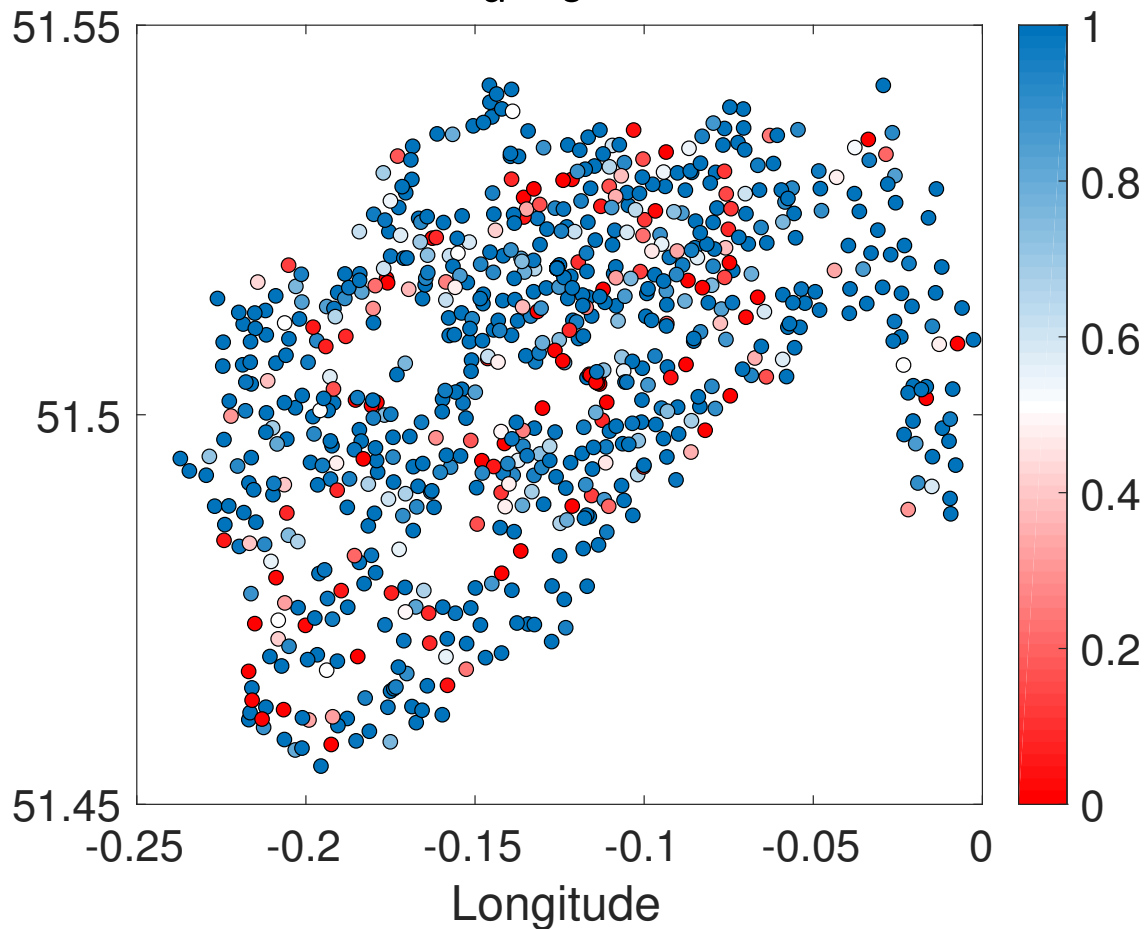
- Locations:  $L = \{\text{bike stations}\}$ ,
- Edges:  $(\ell_i, w, \ell_j) \in W$  iff  $w = \|\ell_i - \ell_j\| < 1 \text{ kilometer}$



# Availability of Bikes

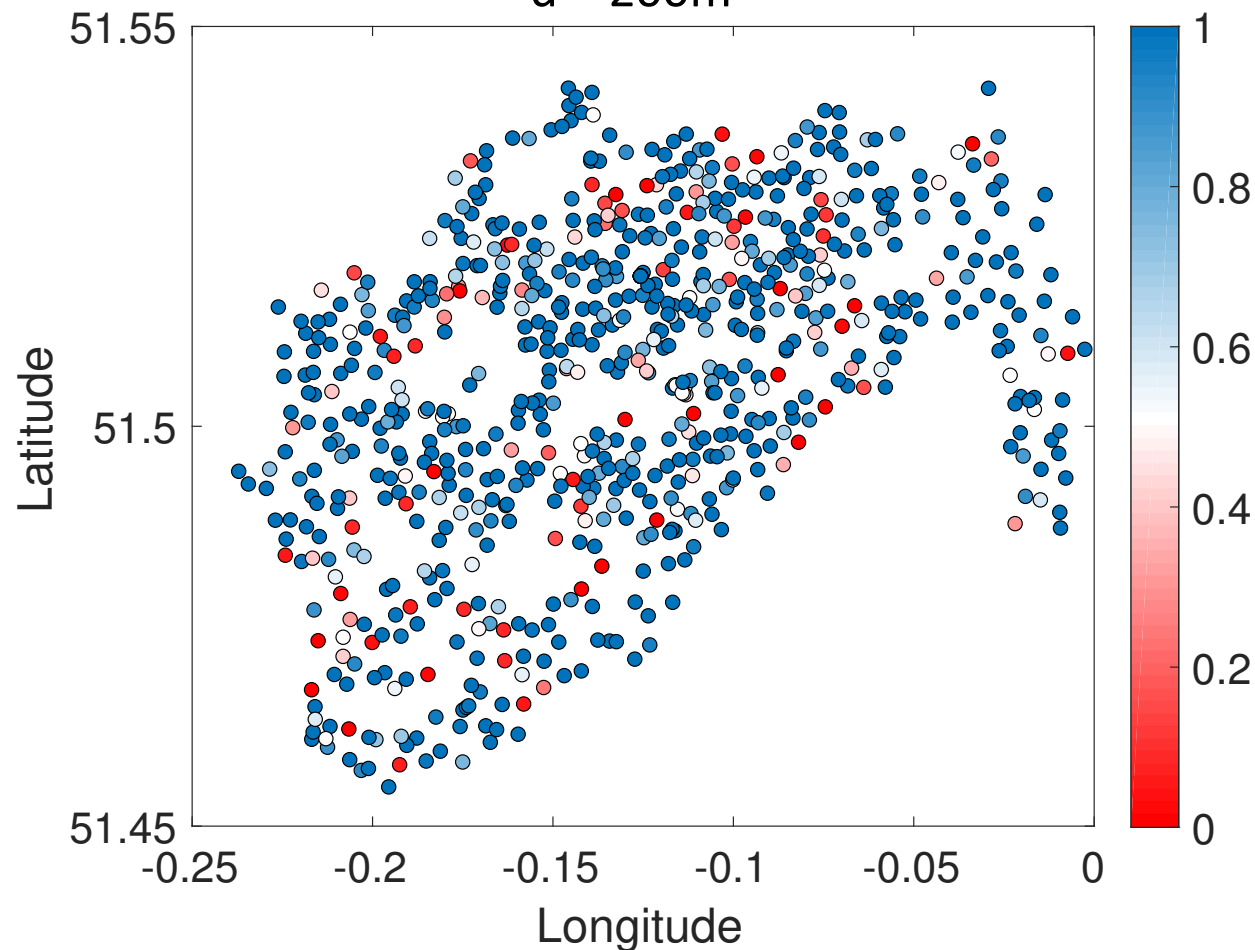
$$\phi_1 = G \left\{ \diamond_{[0,d]}^{weight} (B > 0) \wedge \diamond_{[0,d]}^{weight} (S > 0) \right\}$$

d = 0



std in  $[0, 0.0158]$ , mean std = 0.0053.

d = 200m

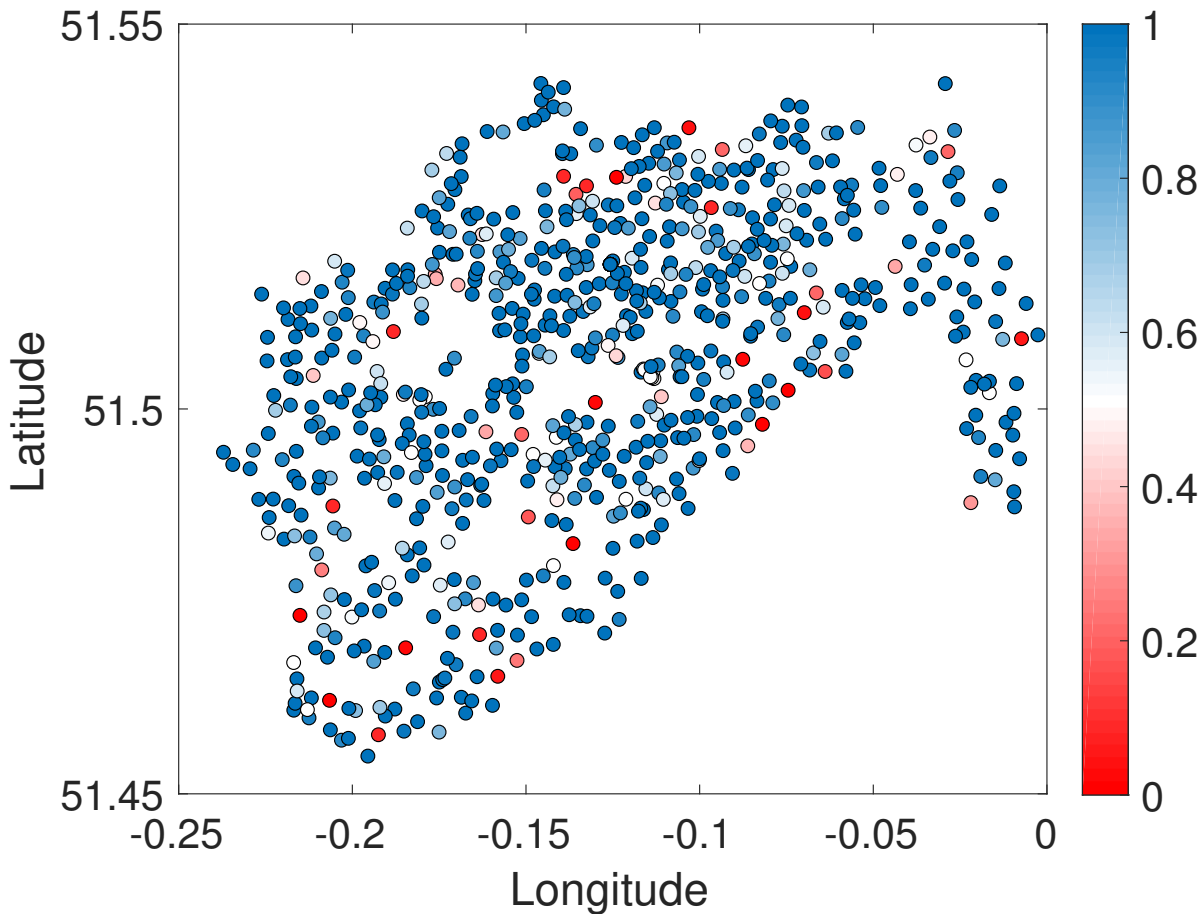


std in  $[0, 0.0158]$ , mean std = 0.0039.

# Availability of Bikes

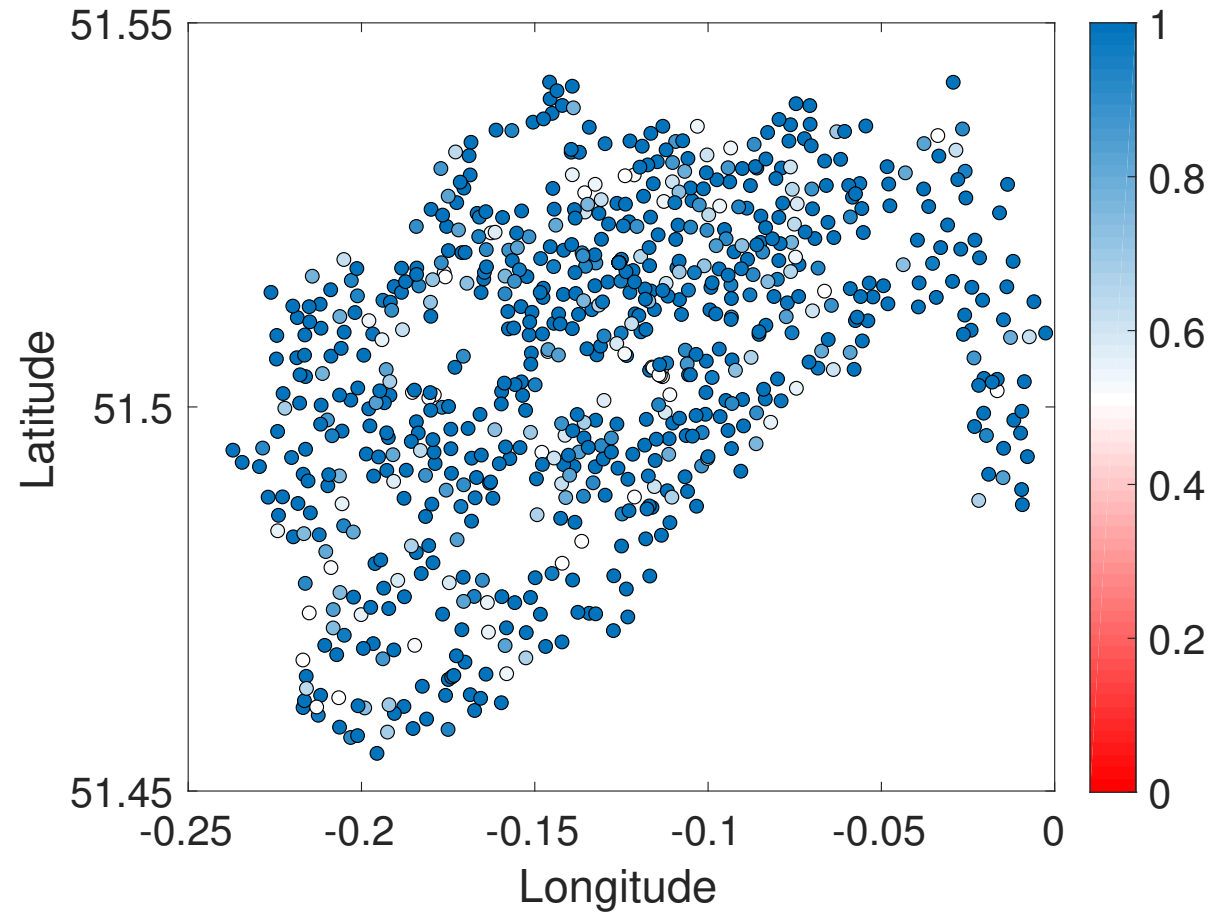
$$\phi_1 = G \left\{ \diamond_{[0,d]}^{weight} (B > 0) \wedge \diamond_{[0,d]}^{weight} (S > 0) \right\}$$

d = 300 m



std in  $[0, 0.0151]$  , mean std = 0.0015.

d = 600m



std in  $[0, 0.0142]$  , mean std = 0.0002.





# Bike Sharing Systems (BSS)

$$\psi_1 = G \left\{ \diamond_{[0,d]}^{weight} (F_{[t_w,t_w]} B > 0) \wedge \diamond_{[0,d]}^{weight} (F_{[t_w,t_w]} S > 0) \right\}$$

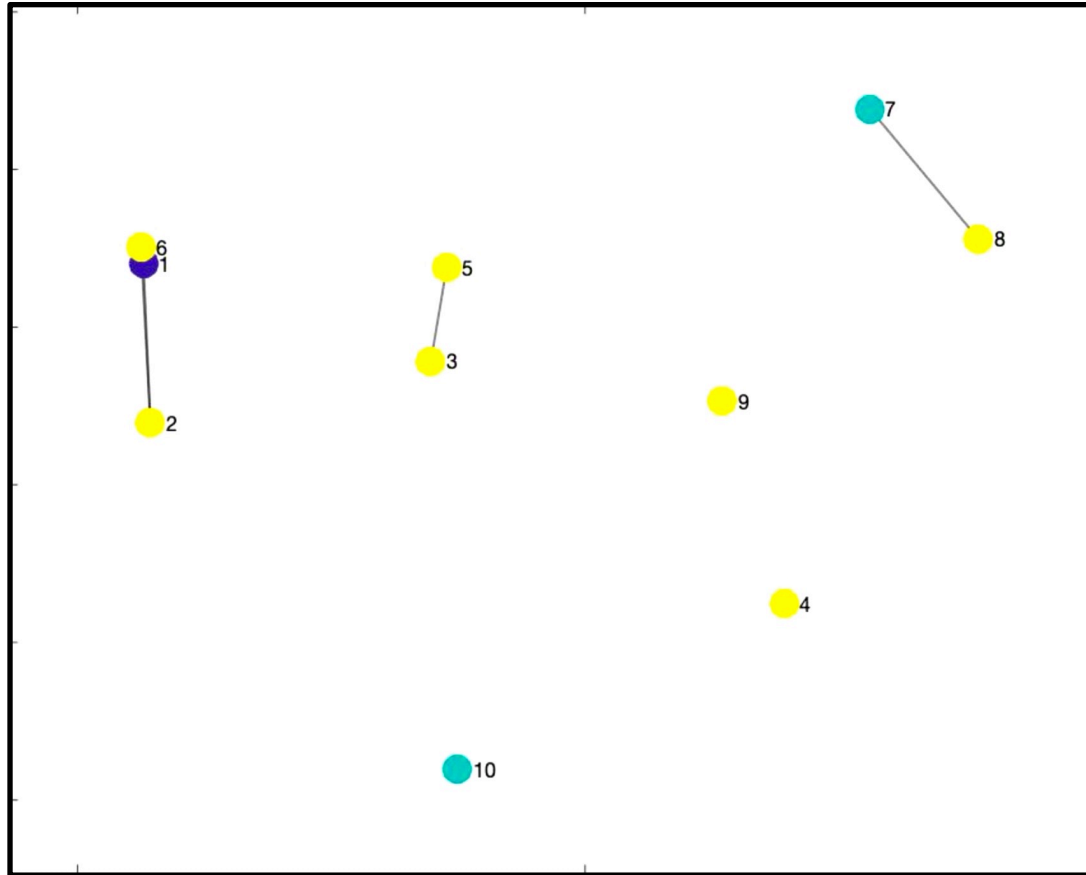
Average walking speed of 6.0 km/h, e.g.  $d = 0.5$  km  $\rightarrow t_w = 6$  minutes

The results similar to the results of previous property

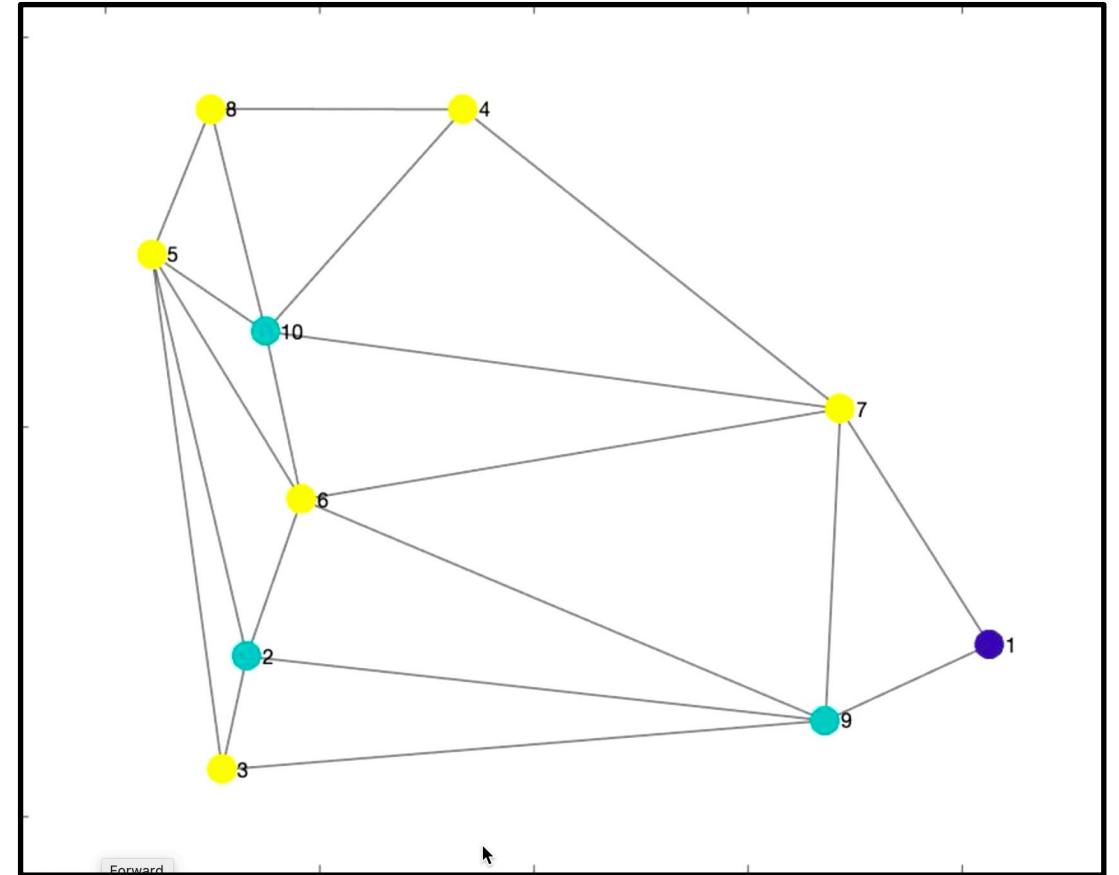
# Dynamic Space

# Mobile Ad-hoc sensor NETWORK (MANET)

Coordinator ● Router ● End-devices ●



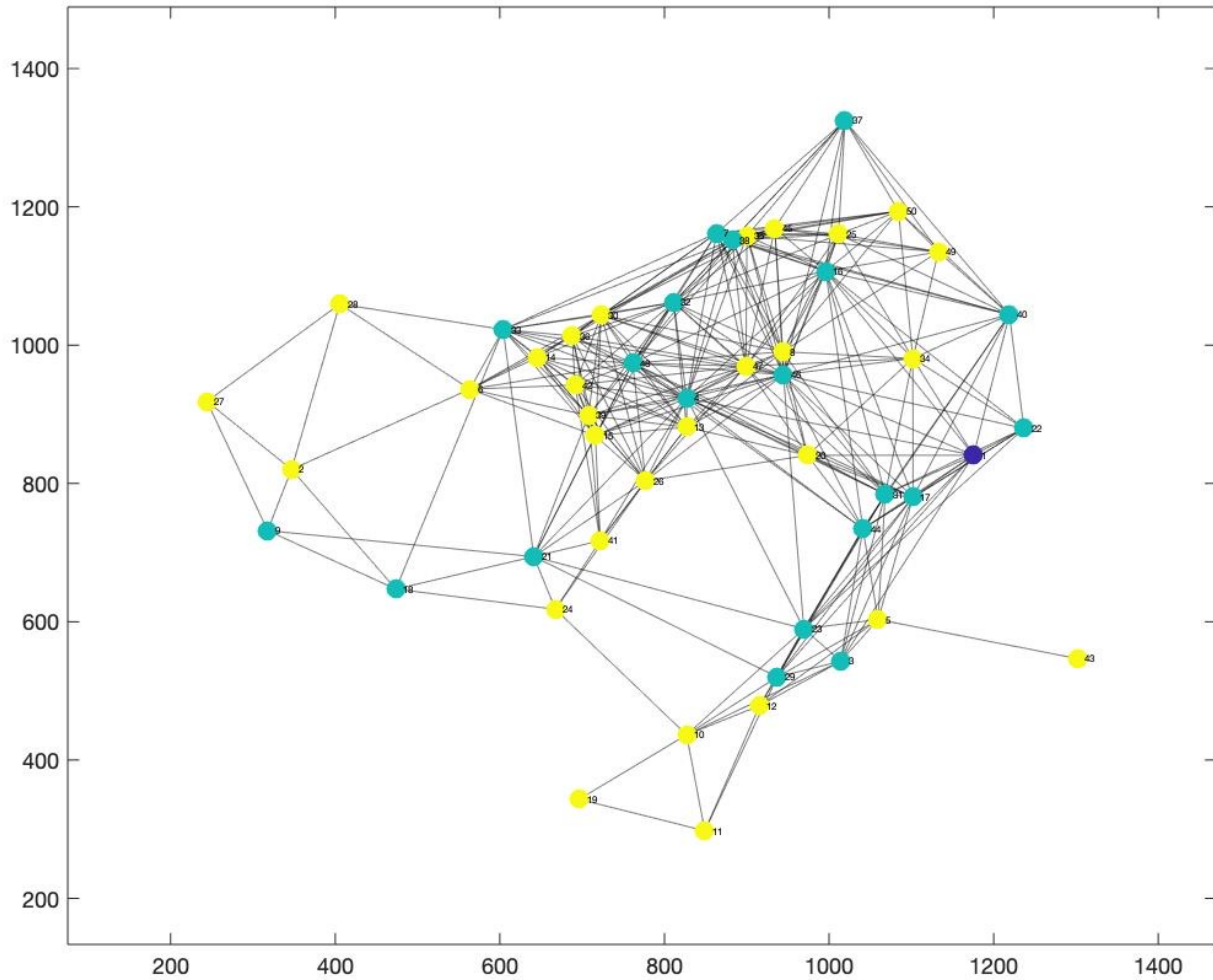
Connectivity Graph



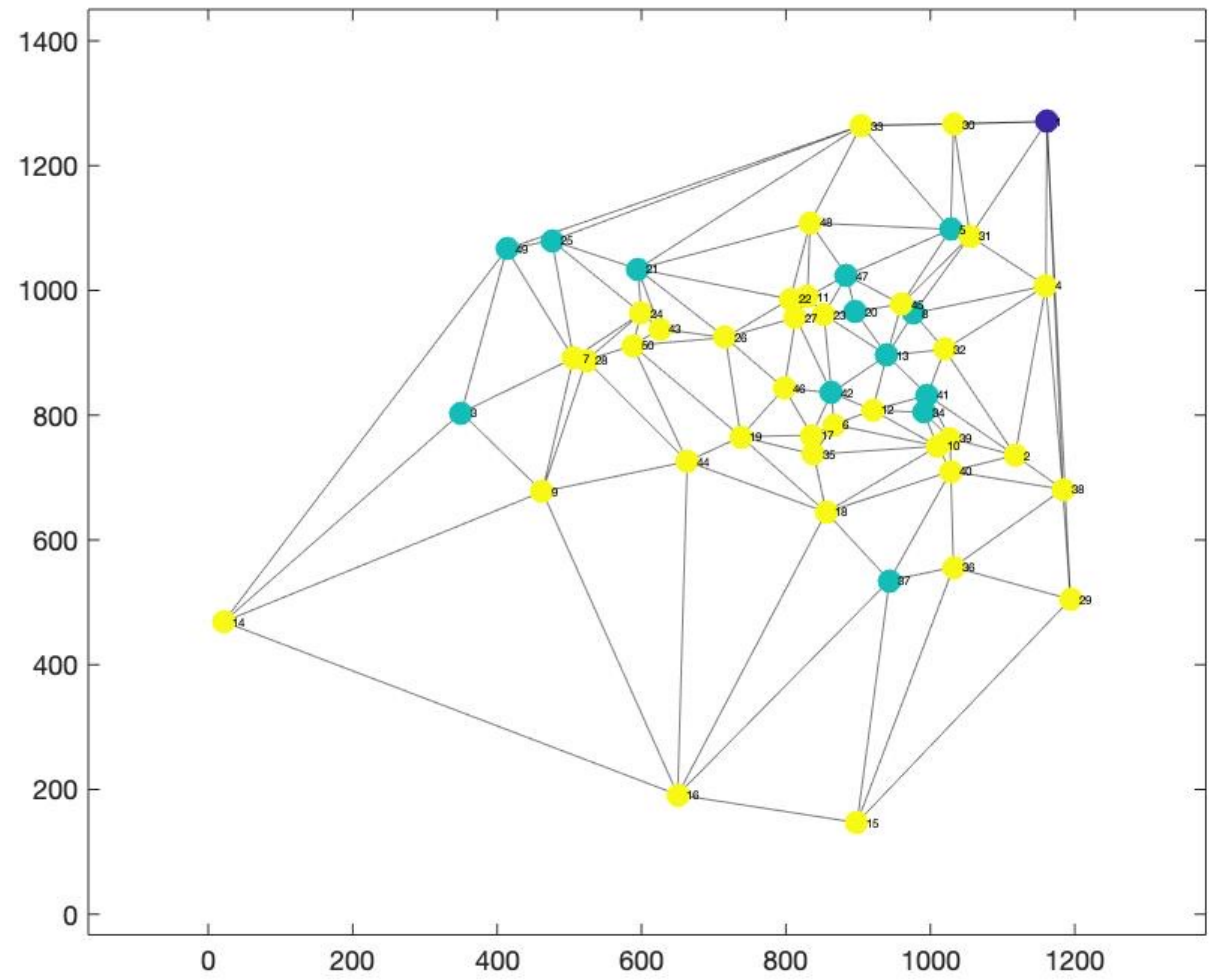
Proximity Graph

# Mobile Ad-hoc sensor NETWORK (MANET)

Coordinator ● Router ● End-devices ●



Connectivity Graph



Proximity Graph

# Mobile Ad-hoc sensor NETWORK (MANET)

Space model  $S(t)$

- Locations:  $L = \{devices\}$ ,
- Edges:  $(\ell_i, w, \ell_j) \in W$  iff  $w = \|\ell_i - \ell_j\| < \min(r_i, r_j)$

Spatio-Temporal Trajectory:  $x: L \times \mathbb{T} \rightarrow \mathbb{Z} \times \mathbb{R}^2$  s.t.

$x(i, t) = (nodeType, battery, temperature)$

$nodeType = 1, 2, 3$  for coordinator, router, and end\_device

# Connectivity in a MANET

“an end device is either connected to the coordinator or can reach it via a chain of at most of 5 routers”

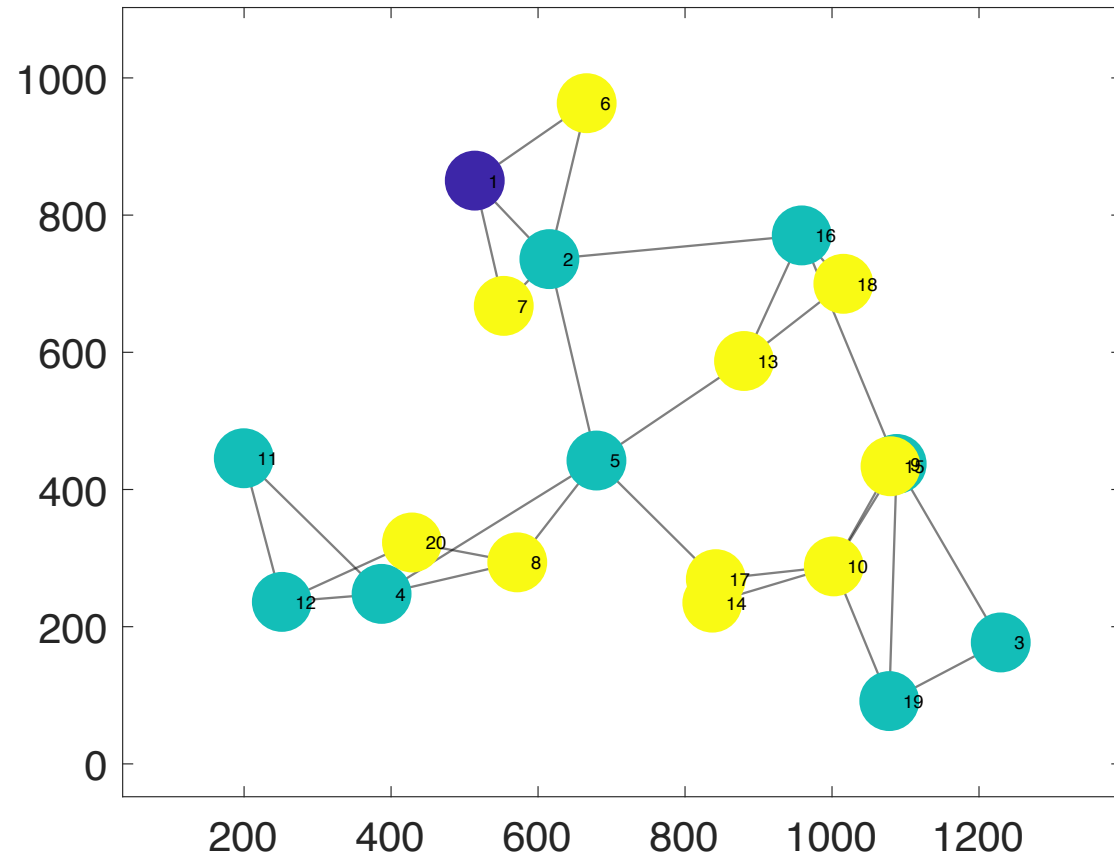
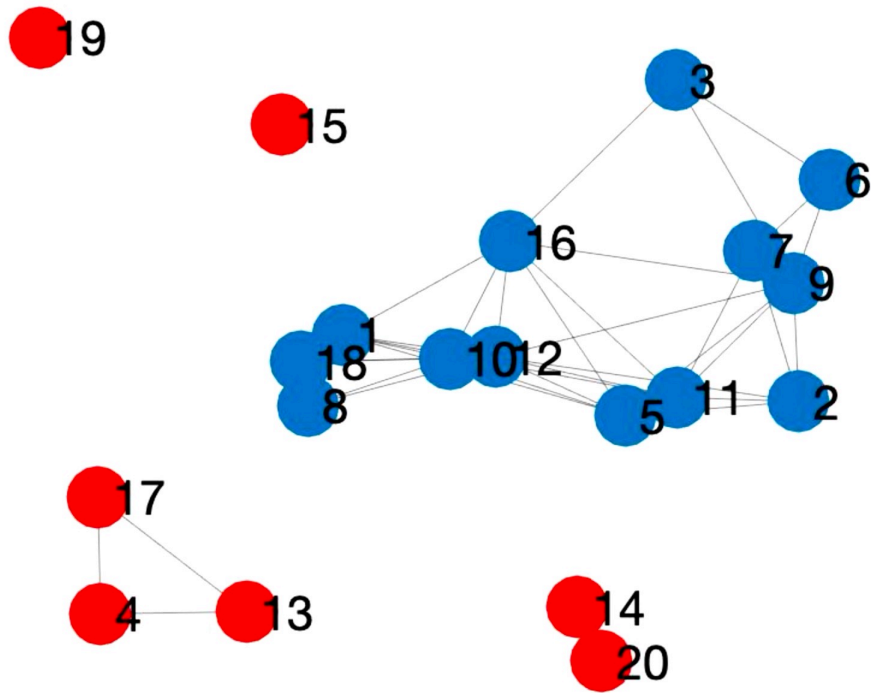
$$\phi_{connect} = device \mathcal{R}_{\leq 1}^{hops} (router \mathcal{R}_{\leq 5}^{hops} coord)$$

“broken connection is restored within h time units”

$$\phi_{connect\_restore} = G(\neg \phi_{connect} \rightarrow F_{[0,h]} \phi_{connect})$$

# Boolean Satisfaction at each time step

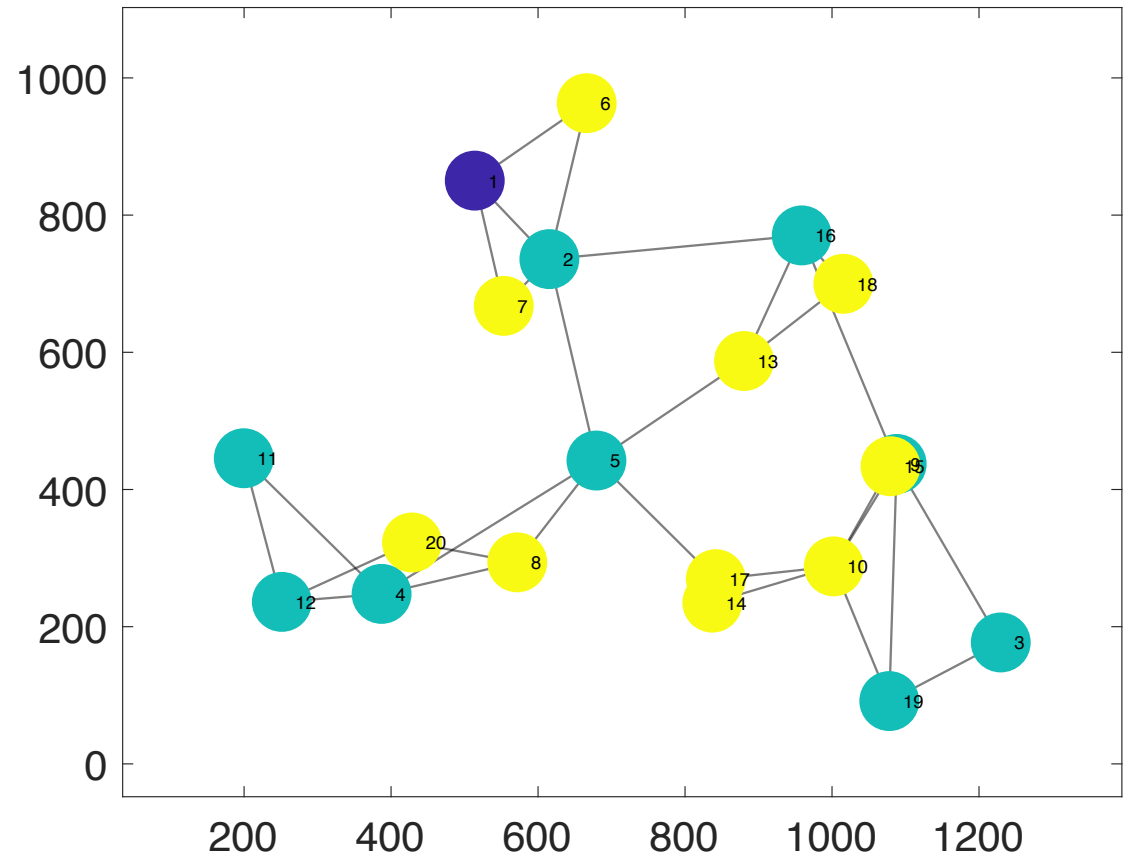
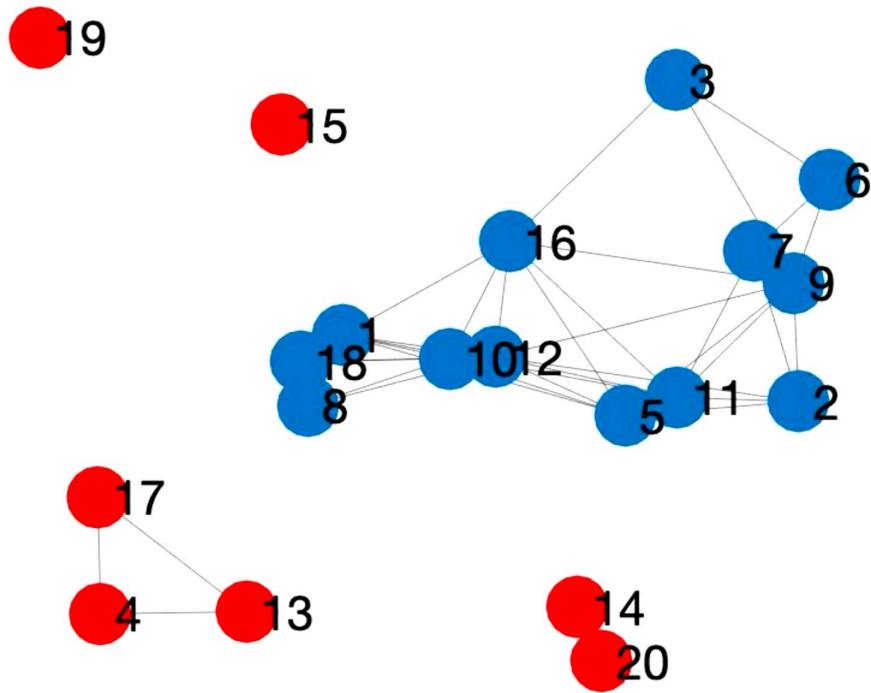
$$\phi_{connect} = device \mathcal{R}_{\leq 1}^{hops} (router \mathcal{R}_{< \infty}^{hops} coord)$$





# Boolean Satisfaction at each time step

$$\phi_{connect} = device \mathcal{R}_{\leq 1}^{hops} (router \mathcal{R}_{< \infty}^{hops} coord)$$



# Delivery in a MANET

“from a given location, we can find a path of (hops) length at least 5 such that all nodes along the path have a battery level greater than 0.5”

$$\psi_3 = \mathcal{E}_{[5, \infty]}^{hops} (\text{battery} > 0.5)$$

# Reliability in a MANET

“reliability in terms of battery levels, e.g. battery level above 0.5

$$\phi_{\text{reliable\_router}} = ((\text{battery} > 0.5) \wedge \text{router}) \mathcal{R}_{<\infty}^{\text{hops}} \text{coord}$$

$$\phi_{\text{reliable\_connect}} = \text{device} \mathcal{R}_{\leq 1}^{\text{hops}} (\phi_{\text{reliable\_router}})$$

# Moonlight: <https://github.com/MoonLightSuite/MoonLight/wiki>

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## Home

Simone edited this page on 1 Jul · 30 revisions

## MoonLight build passing codecov 39%

MoonLight is a light-weight Java-tool for monitoring temporal, spatial and spatio-temporal properties of distributed complex systems, as *Cyber-Physical Systems* and *Collective Adaptive Systems*.

It supports the specification of properties written with the *Reach and Escape Logic* (STREL). STREL is a linear-time temporal logic, in particular, it extends the *Signal Temporal Logic* (STL) with a number of spatial operators that permit to described complex spatial behaviors as being surround, reaching target locations, and escaping from specific regions.

MoonLight is implemented in Java, but it features also a [MATLAB](#) interface that allows the monitoring of spatio-temporal signals generated within the MATLAB framework. A [Python](#) Interface is under development.

## Getting Started

First, you need to download JAVA (version 8) and set the environmental variable

```
JAVA_HOME= path to JAVA home directory
```

Then you need to get or generate the executable for Python or MATLAB.

First, you need to clone our repository

```
$ git clone https://github.com/MoonLightSuite/MoonLight.git
```

or download it ([link](#)).

Then you need to compile it by executing the following Gradle tasks in the console

### Pages 5

- [Moonlight](#)
- [Script Syntax](#)
- [Matlab](#)
  - [Installation](#)
  - [Getting Started](#)
- [Python](#)
- [License](#)

### Clone this wiki locally

<https://github.com/MoonLightSuite/MoonLight/wiki>

```
1      (atomicExpression)
2      | ! Formula
3      | Formula & Formula
4      | Formula | Formula
5      | Formula => Formula
6      | Formula until [a b] Formula
7      | Formula since [a b] Formula
8      | eventually [a b] Formula
9      | globally [a b] Formula
10     | once [a b] Formula
11     | historically [a b] Formula
12     | escape(distanceExpression)[a b] Formula
13     | Formula reach (distanceExpression)[a b] Formula
14     | somewhere(distanceExpression) [a b] Formula
15     | everywhere (distanceExpression) [a b] Formula
16     | {Formula}
```