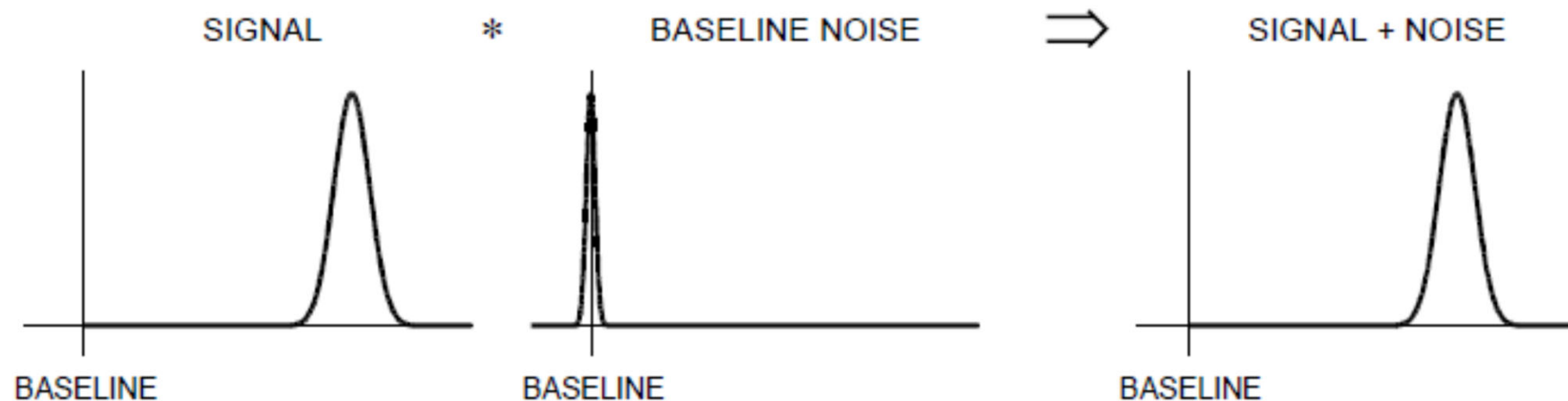


What determines Resolution?

Signal Variance \gg Baseline Variance



\Rightarrow Electronic (baseline) noise not important

Examples: • High-gain proportional chambers

• Scintillation Counters with High-Gain PMTs

e.g. 1 MeV γ -rays absorbed by NaI(Tl) crystal

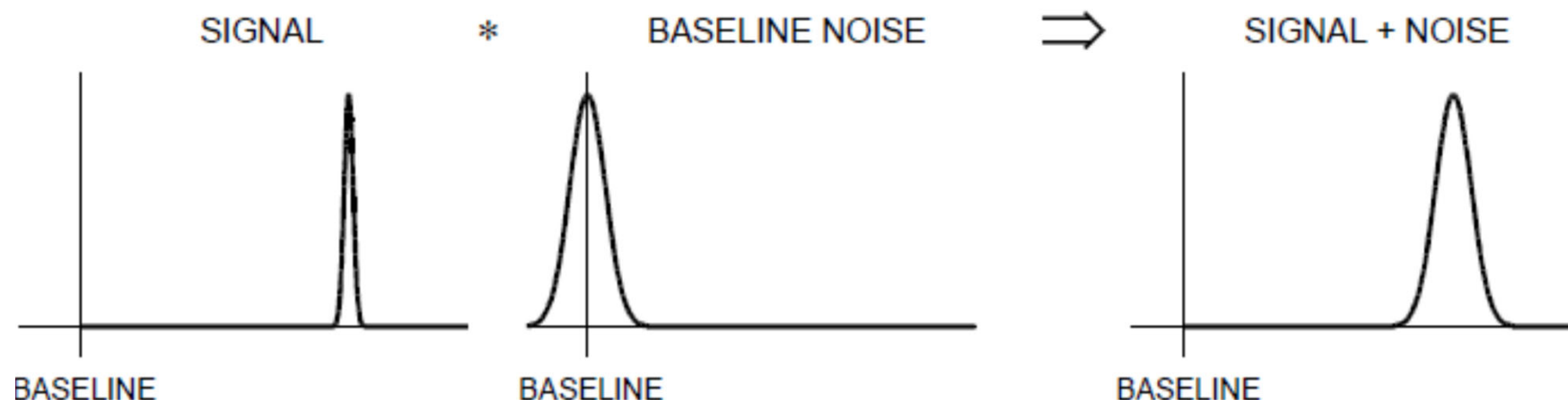
Number of photoelectrons: $N_{pe} \approx 8 \cdot 10^4 [\text{MeV}^{-1}] \times E_\gamma \times QE \approx 2.4 \cdot 10^4$

Variance typically: $\sigma_{pe} = N_{pe}^{1/2} \approx 160$ and $\sigma_{pe} / N_{pe} \approx 5 - 8\%$

Signal at PMT anode (assume Gain = 10^4): $Q_{sig} = G_{PMT} N_{pe} \approx 2.4 \cdot 10^8$ el and
 $\sigma_{sig} = G_{PMT} \sigma_{pe} \approx 1.2 \cdot 10^7$ el

whereas electronic noise easily $< 10^4$ el

Signal Variance \ll Baseline Variance



\Rightarrow Electronic (baseline) noise critical for resolution

- Examples:
- Gaseous ionization chambers (no internal gain)
 - Semiconductor detectors

e.g. in Si : Number of electron-hole pairs $N_{ep} = \frac{E_{dep}}{3.6 \text{ eV}}$

Variance $\sigma_{ep} = \sqrt{F \cdot N_{ep}}$ (where $F =$ Fano factor ≈ 0.1)

For 50 keV photons: $\sigma_{ep} \approx 40 \text{ el} \Rightarrow \sigma_{ep} / N_{ep} = 7.5 \cdot 10^{-4}$

Obtainable noise levels are 10 to 1000 el.

Baseline fluctuations can have many origins ...

pickup of external interference

artifacts due to imperfect electronics

... etc.,

but the (practical) fundamental limit is electronic noise.

1.10 Detection limits and resolution

In addition to signal fluctuations originating in the sensor, the minimum detection limit and energy resolution are subject to fluctuations introduced by the electronics. The gain can be controlled very precisely, but electronic noise introduces baseline fluctuations, which are superimposed on the signal and alter the peak amplitude. Figure 1.24 (left) shows a typical noise waveform. Both the amplitude and time distributions are random.

When superimposed on a signal, the noise alters both the amplitude and time dependence. Figure 1.24 (right) shows the noise waveform superimposed on a small signal. As can be seen, the noise level determines the minimum signal whose presence can be discerned.

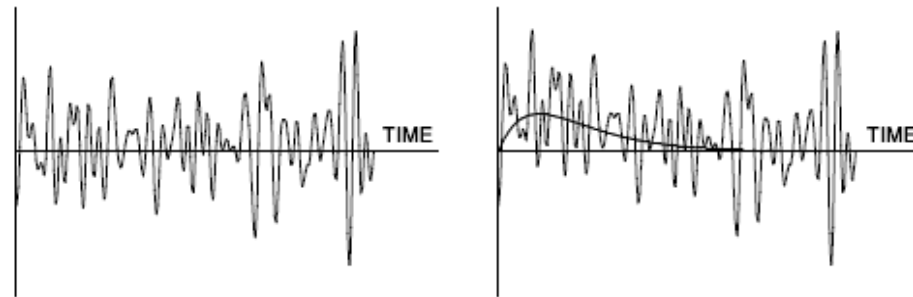
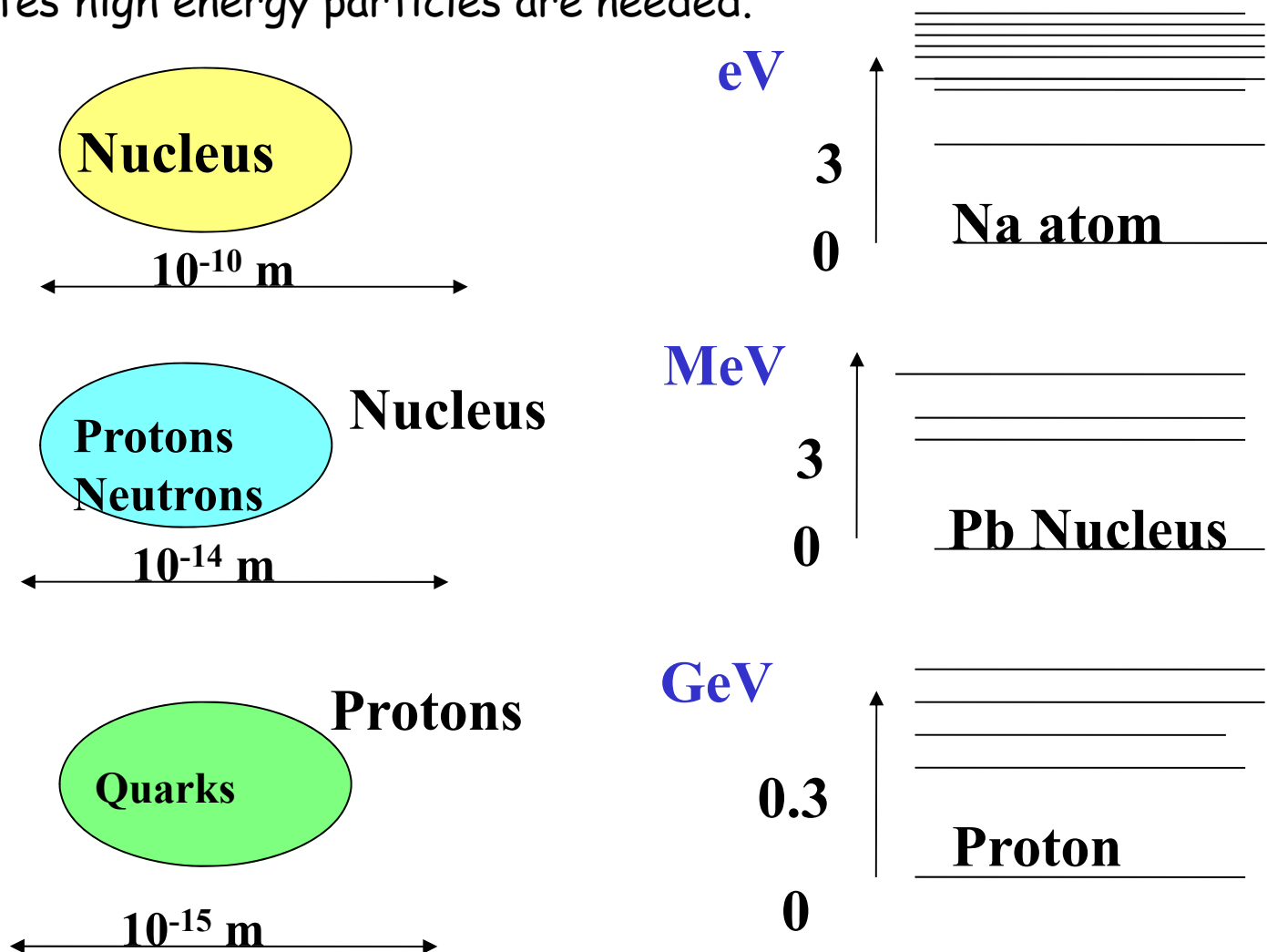


FIG. 1.24. Waveforms of random noise (left) and signal + noise (right), where the peak signal is equal to the rms noise level ($S/N = 1$). The noiseless signal is shown for comparison.

Spectroscopy:

- Experiments to determine the decay products of excited states and their interaction
- The excitation energies of a system increase as size decrease. To produce these excited states high energy particles are needed.

Absolute energies may vary a lot
But resolution usually still a critical issue



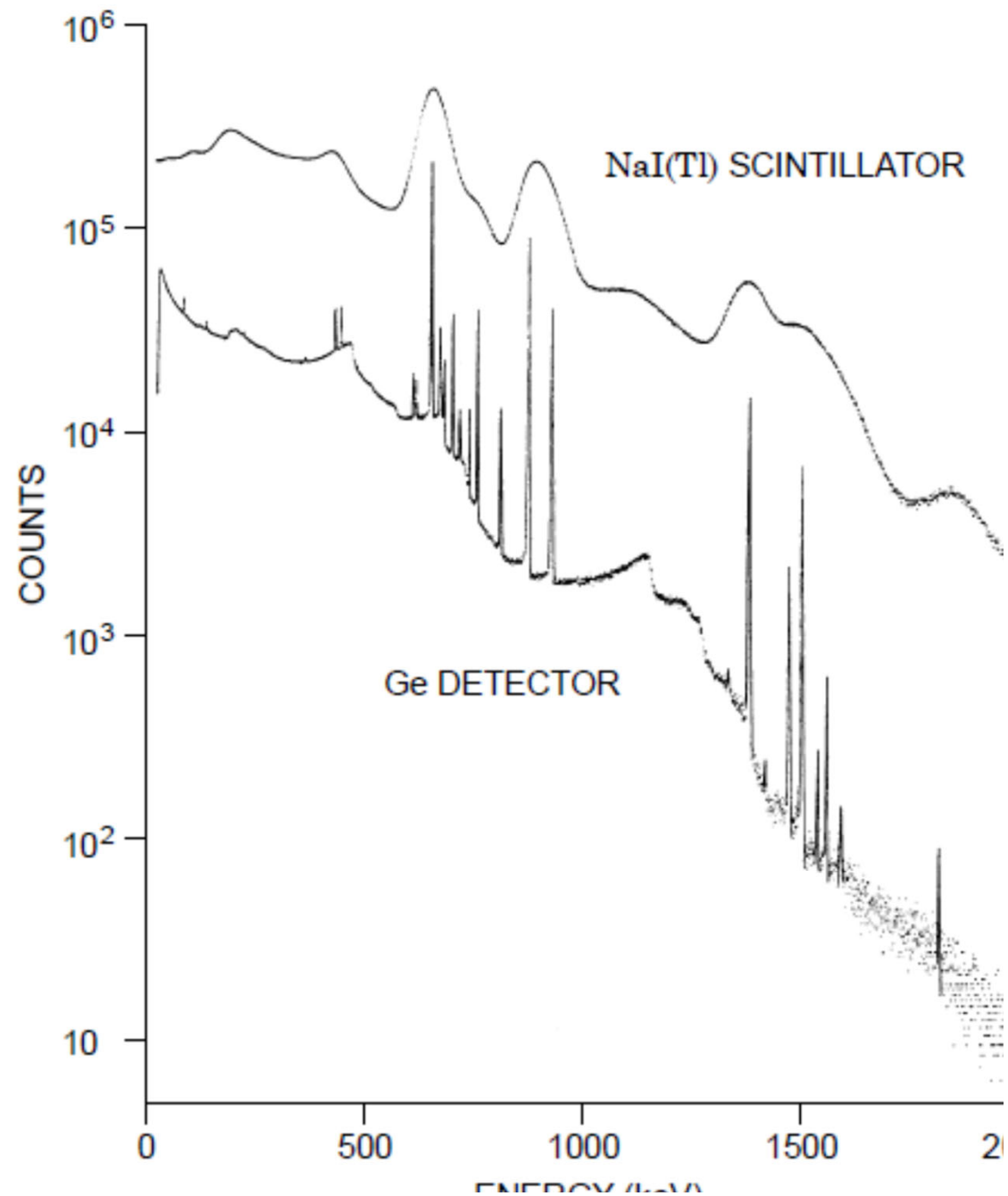
Resolution and Electronic Noise

Resolution: the ability to distinguish signal levels

Why?

Recognize structure in amplitude spectra

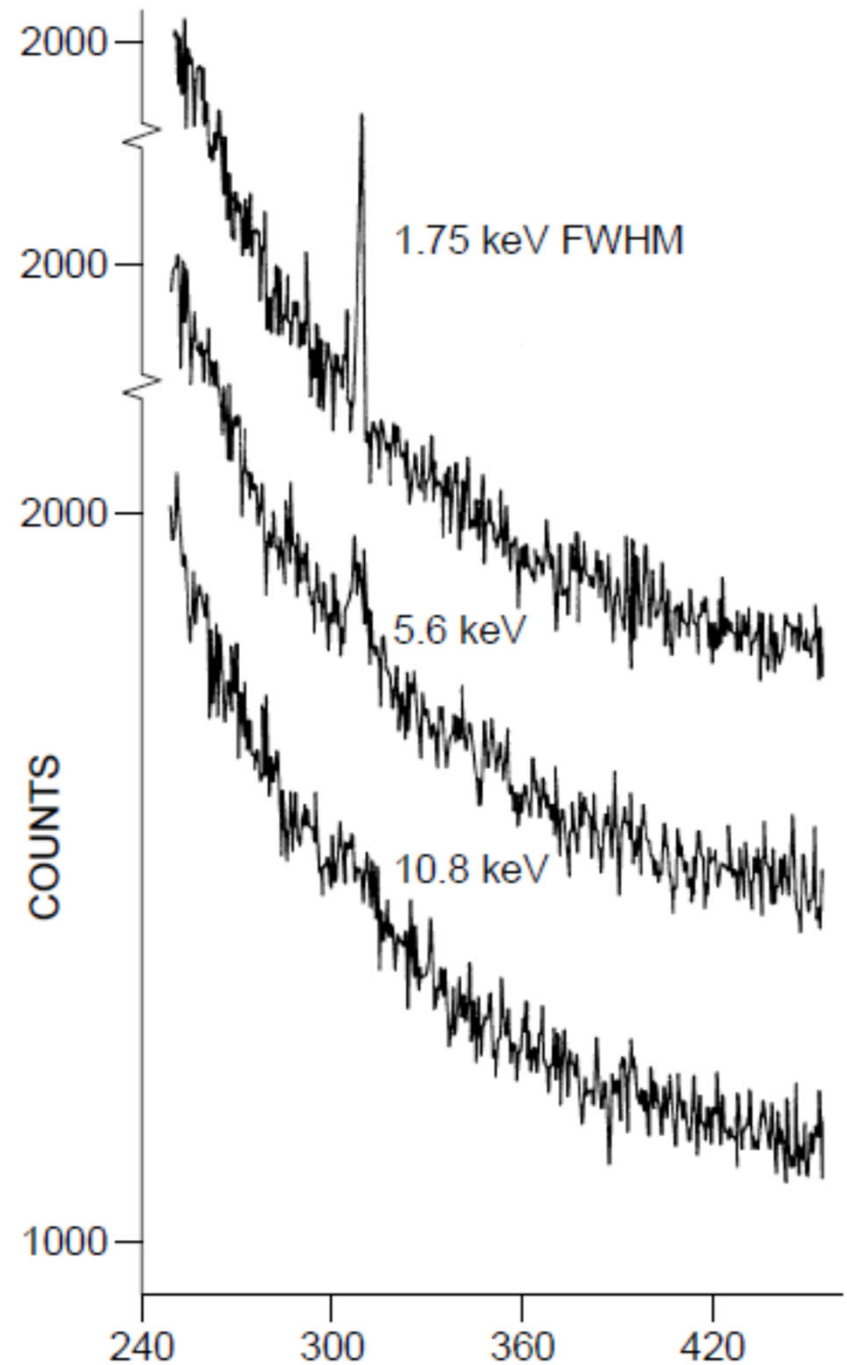
Comparison between NaI(Tl) and Ge detectors



b) Improve sensitivity

Signal to background ratio improves with better resolution

(signal counts in fewer bins compete with fewer background counts)



li di Frascati of INFN, wh
 text year. The experiment,
 ram, has some special f
 hypernuclear physics experi
 will operate at a e^+e^- collide
 What follows will describe it

structure of Λ -hypernuclei

A Λ -hypernucleus ${}^A_\Lambda Z$ is a b
 rons and a Λ hyperon. Th
 made by the $(A-1)$ nucleons:
 the nucleus ${}^{(A-1)}Z$ and the
 the Λ hyperon, carrying th
 indistinguishable baryon an
 imposed by the Pauli principl
 im states already filled up v
 hyperon, embedded in a
 explore nuclear structure.

The binding energy B_Λ of
 its ground state is defined

$$B_\Lambda = M$$

here M_{core} is the mass (in M
 the mass of the Λ particle an
 Z , experimentally measur
 ope of about 1 MeV/(unit
 r the heavy hypernuclei. Th
 which the Λ particle is con
 qual to the nuclear radius an
 the 55 MeV typical value c

This is consistent with a Λ -
 nucleon-one. Indeed
 teraction, the zero isospin

vector mesons like the π or the ρ with a nucleon and
 determines the lack of strong tensor components in the interaction.
 The relative weakness of the Λ -nucleon interaction entails that the
 shell structure is not disrupted by the insertion of the Λ in the
 nucleus and the lack of Pauli effects allows all the nuclear single
 particle states to be populated by the Λ . In Figure 2, the so called
 "egre table" of the hypernuclei shows the 35 hypernuclei known
 present.

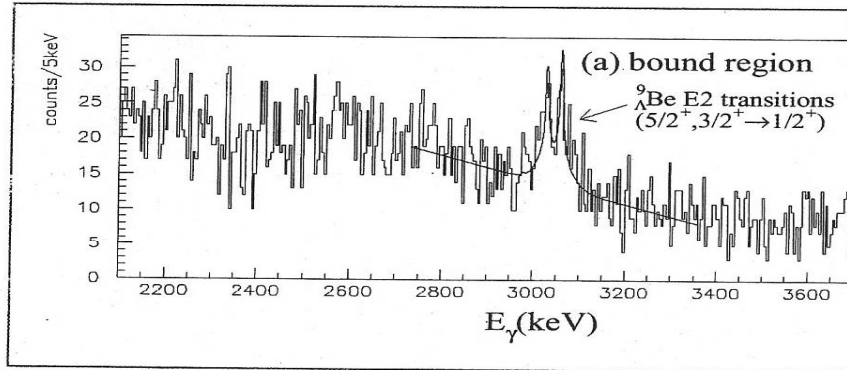
Experiments of hypernucleus production by "strangeness
 change" and "associated production" processes can produce
 hypernuclei in which the Λ populates different single particle
 states. The latter technique is particularly suitable for populating
 ν lying Λ states, thanks to the high recoil momentum trans-
 ferred to the Λ particle in the reaction.

A beautiful representation of this process is given in Figure 3,
 where the excitation spectrum of ${}^{89}_\Lambda Y$, obtained by the "associated
 production" reaction ${}^{89}Y(\pi^+, K^+) {}^{89}_\Lambda Y$ at the KEK laboratory in
 Japan, is shown. The spectrum demonstrates how, starting from
 a neutron in the $g_{9/2}$ state, it is possible to accommodate a Λ particle
 in the hypernuclear states f, d, p and even in the ground state s .

These measurements constitute the spectacular confirmation,
 at a textbook level, of the validity of the independent particle
 model or shell model of the nucleus. In non-strange nuclei, the
 observation of single particle states is only possible for the states
 the most external nucleon orbits. In fact, due to the Pauli princi-
 ple and pairing interactions, deeply bound nucleon single
 particle states are so fragmented as to be essentially unobservable.
 The present experimental data on hypernuclear binding energies
 and detailed spectroscopic features are limited in quantity and

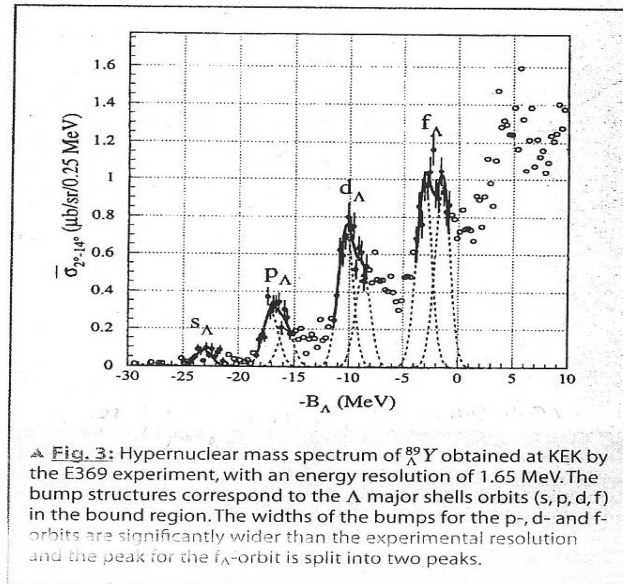
tion of the YN interaction.

Figure 4 reports a recent measurement of the splitting of the
 $5/2^+ - 3/2^+$ doublet in ${}^9_\Lambda Be$ by the BNL-AGS E930 experiment [4],
 measuring γ rays emitted in the nuclear transitions with the new
 germanium detector array Hyperball. This new technique allowed
 the energy resolution on low lying hypernuclear levels to be
 improved from a few MeV to a few keV, even if the count rate
 resulting is still quite low, ~ 200 γ 's per month of data taking. The
 spacing of the two levels was measured to be 31 ± 2 keV, incompat-
 ible with the prediction of the meson exchange models.



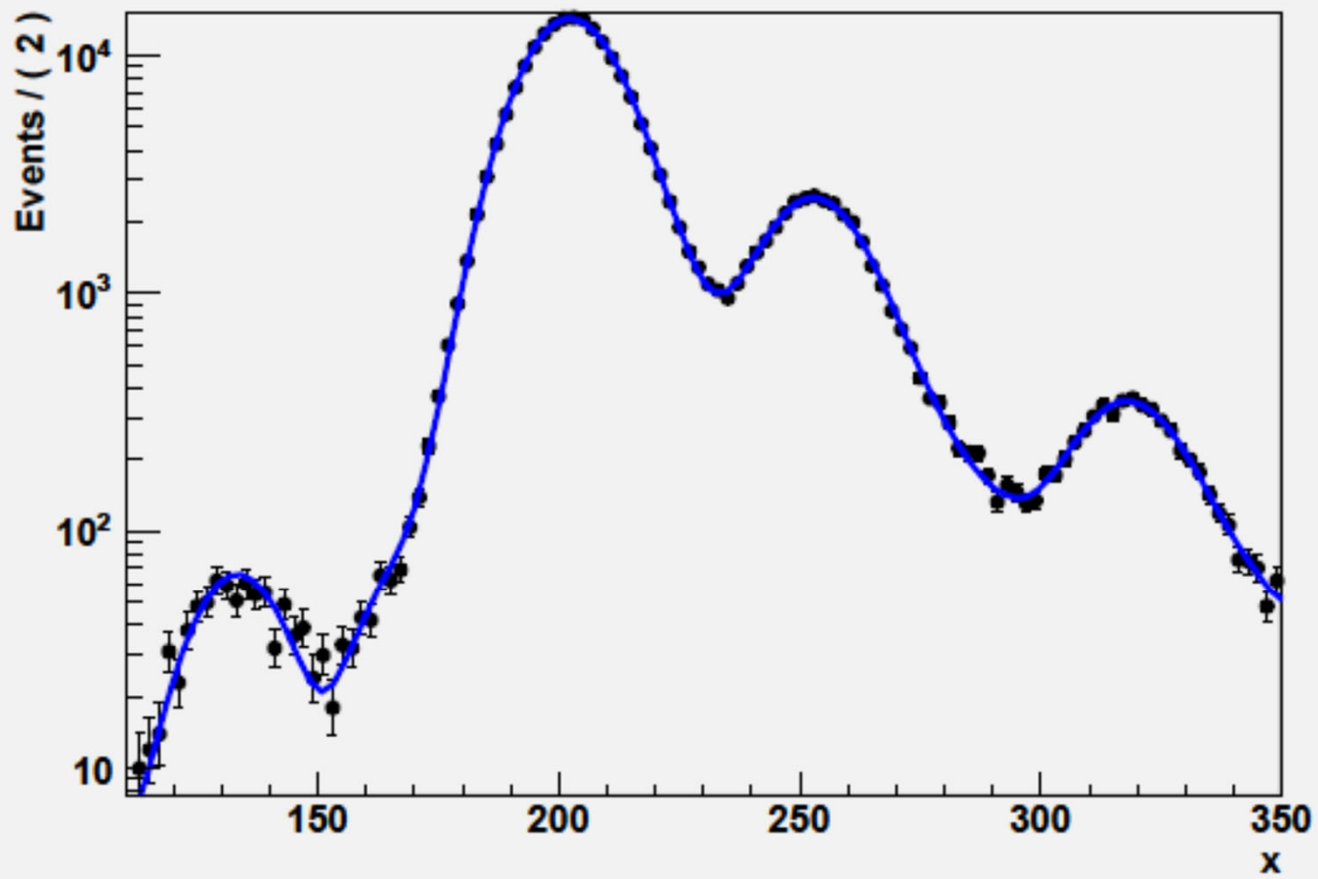
◀ Fig. 4: Energy resolution of the splitting of the $5/2^+ - 3/2^+$ doublet in ${}^9_\Lambda Be$ obtained by the BNL-AGS E930 experiment. The spacing of the two levels was measured to be 31 ± 2 keV, incompatible with the prediction of the meson exchange models.

The improvement of the YN interaction models would need
 precise data on the free YN interaction, which are very difficult to

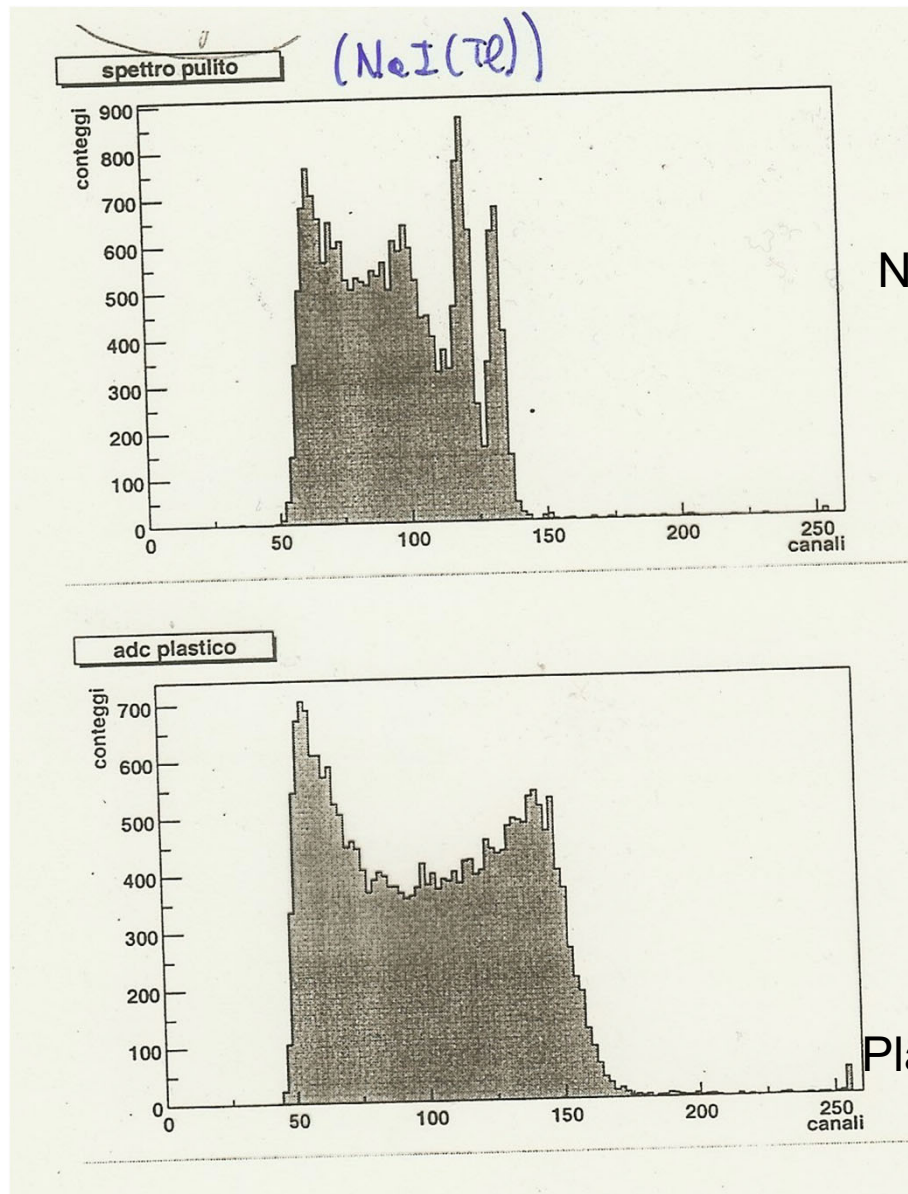


▲ Fig. 3: Hypernuclear mass spectrum of ${}^{89}_\Lambda Y$ obtained at KEK by the E369 experiment, with an energy resolution of 1.65 MeV. The bump structures correspond to the Λ major shells orbits (s, p, d, f) in the bound region. The widths of the bumps for the p, d - and f -orbits are significantly wider than the experimental resolution and the peak for the f_Λ -orbit is split into two peaks.

A RooPlot of "x"



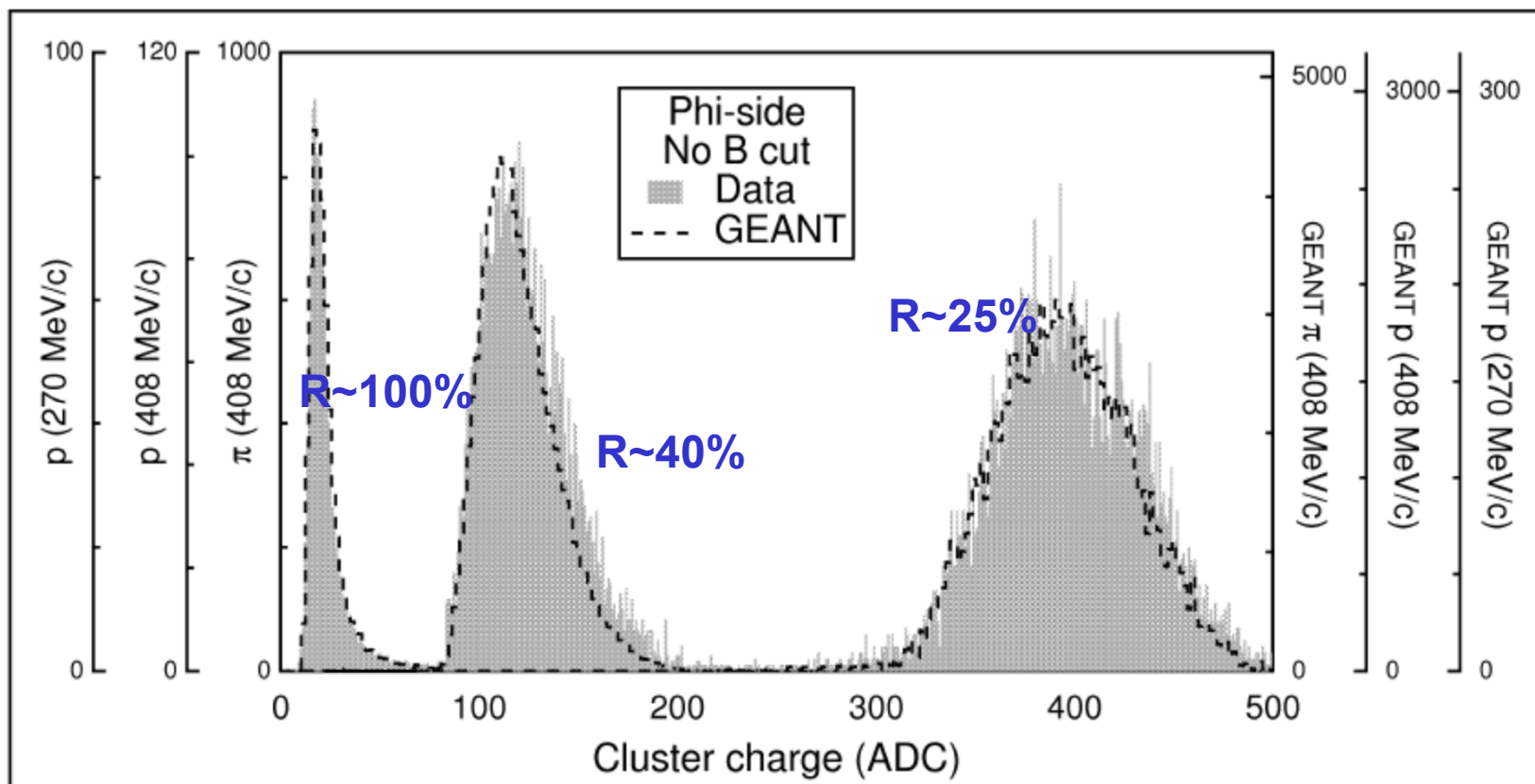
Response function

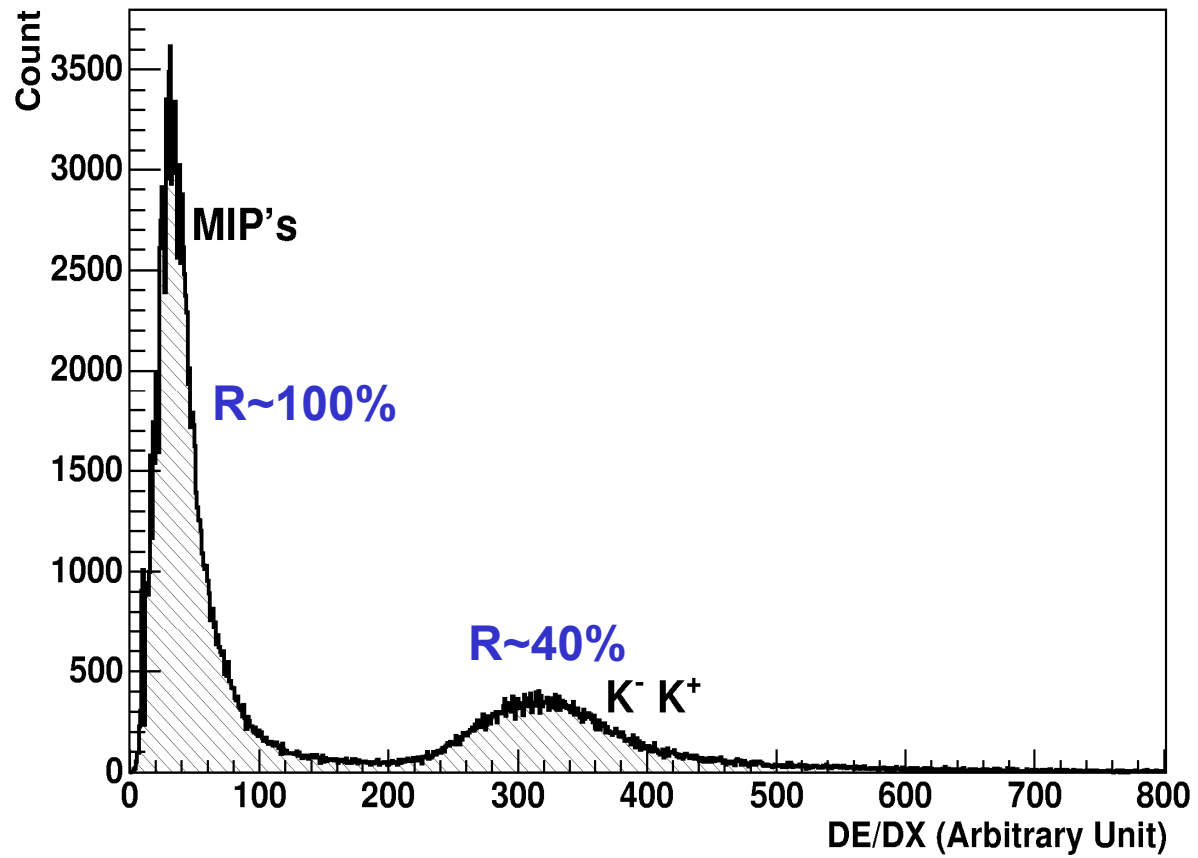


NaI(Tl) scintillator

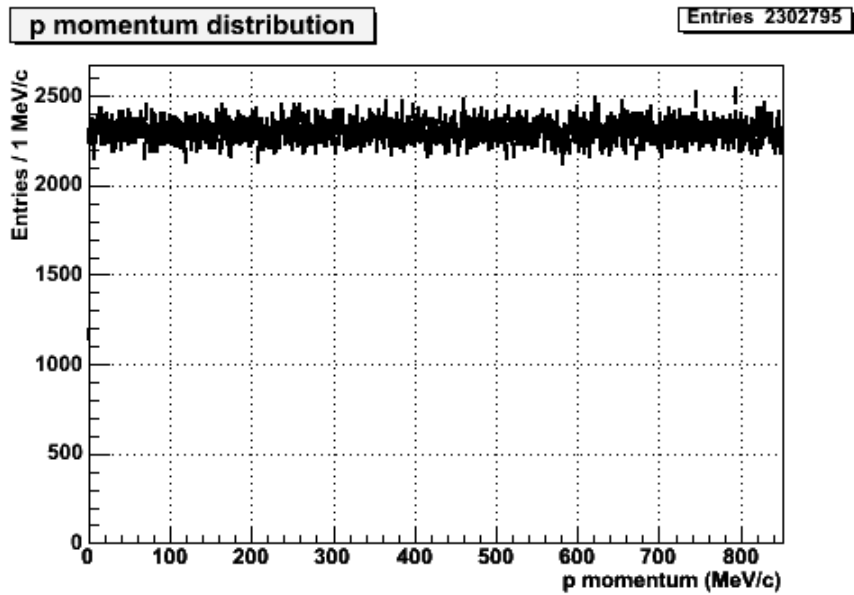
Plastic scintillator

There are actually 2
monoenergetic radiation
Sources...

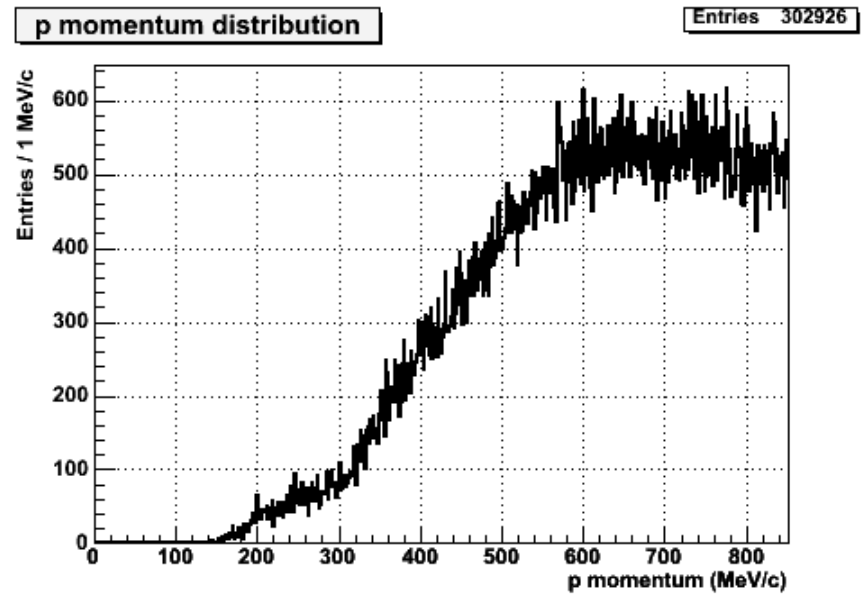




Acceptance effect on proton momentum distribution



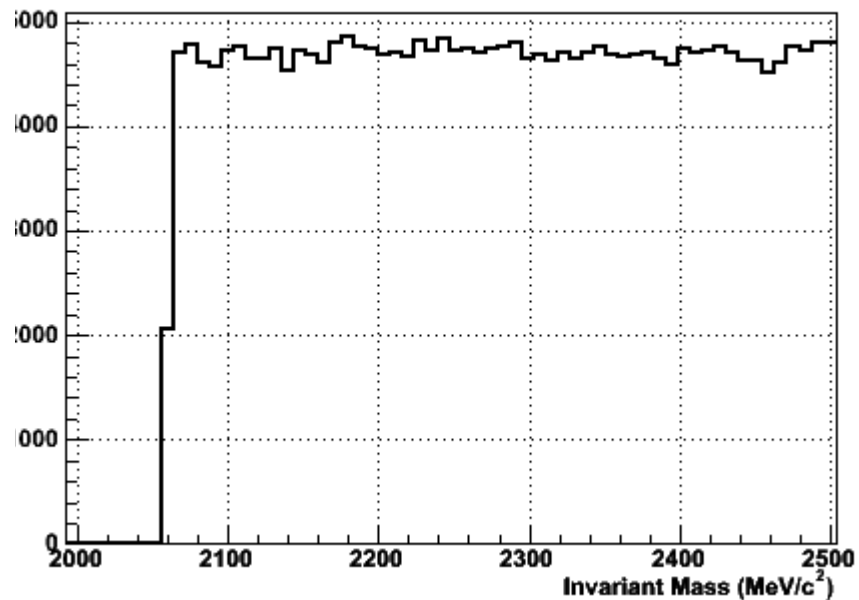
Original distribution



Reconstructed distribution

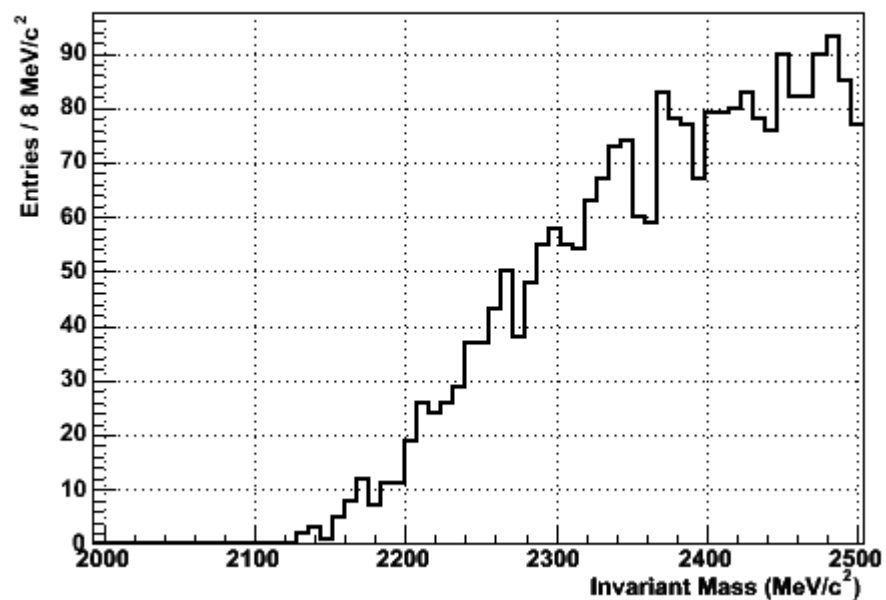
p and p invariant mass (coincidence π^+ , p, p)

Entries 588929



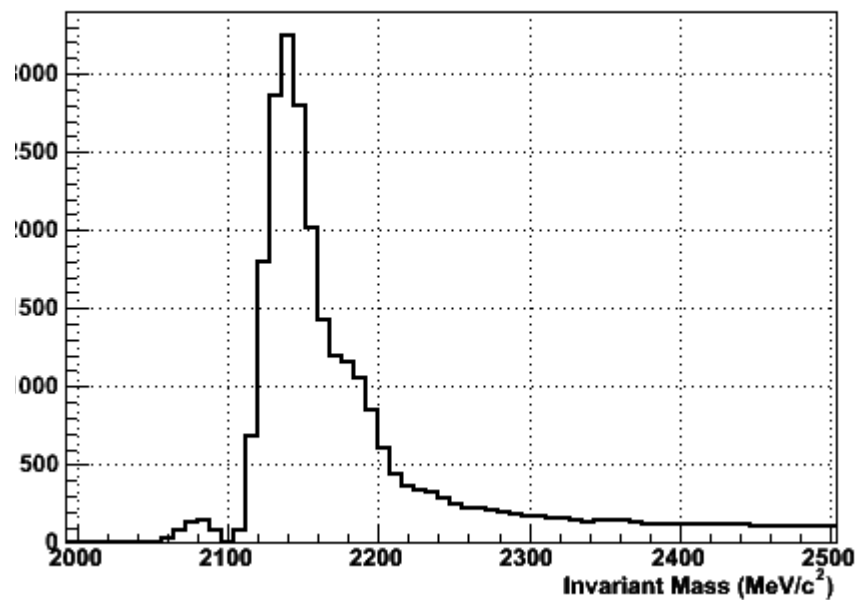
π^+ , p and p invariant mass (coincidence π^+ , p, p)

Entries 753



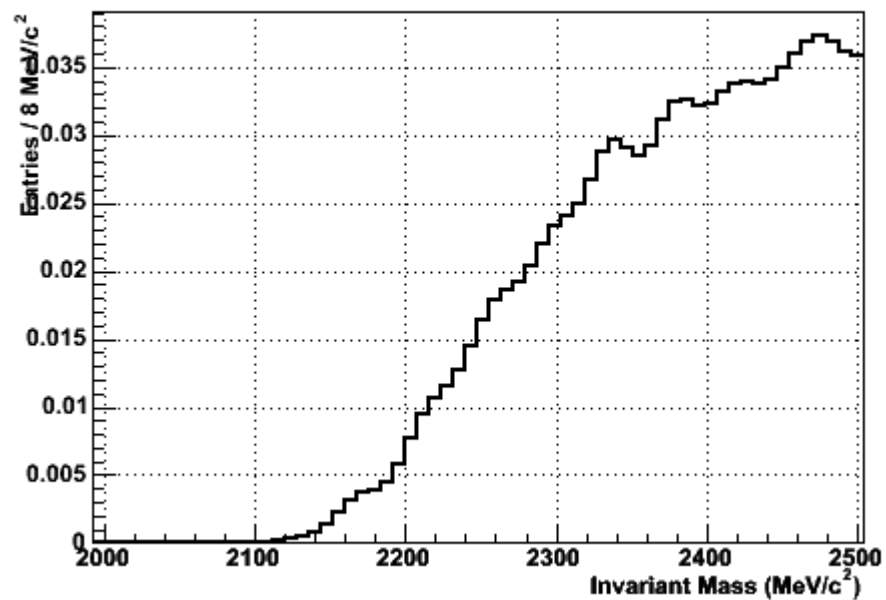
p and p invariant mass (coincidence π^+ , p, p)

Entries 589679



π^+ , p and p invariant mass (coincidence π^+ , p, p)

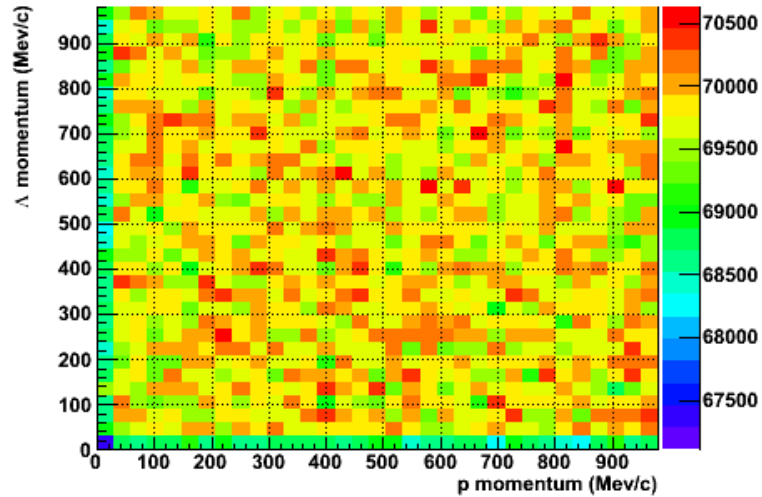
Entries 828



Λp acceptance

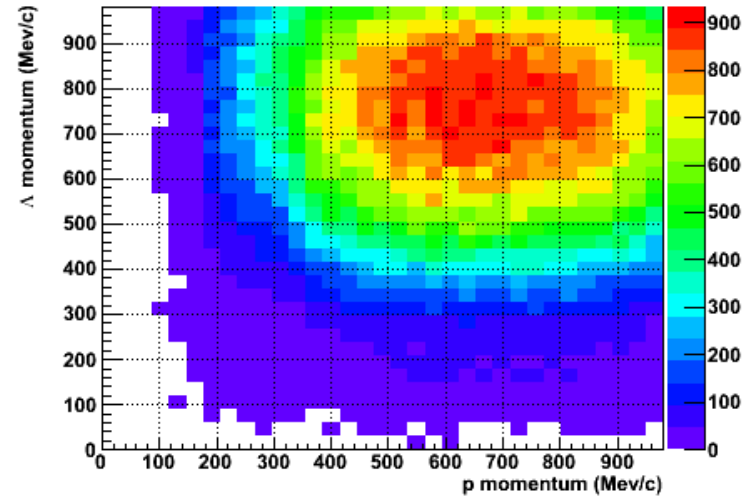
Λ momentum vs p momentum (coincidence π^- , p, p)

Entries 7.876527e+07



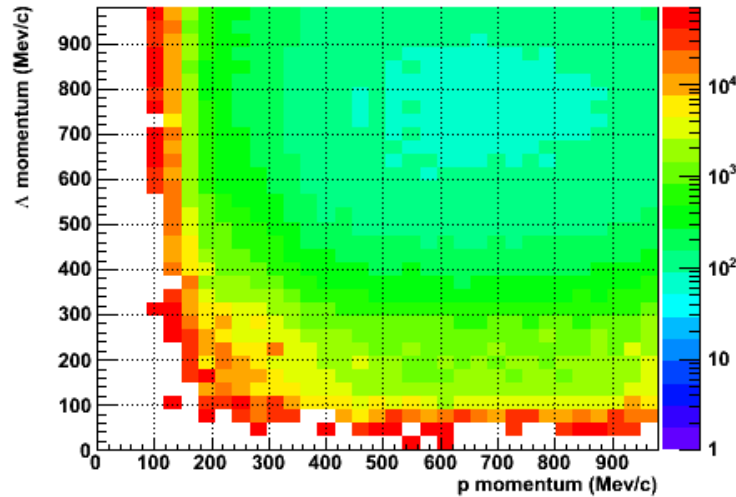
Λ momentum vs p momentum (coincidence π^- , p, p)

Entries 345297



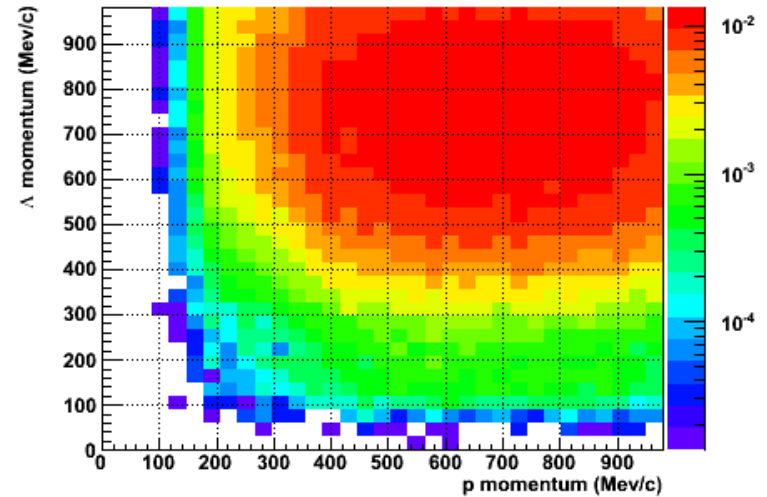
Λ momentum vs p momentum (coincidence π^- , p, p)

Entries 7.876527e+07

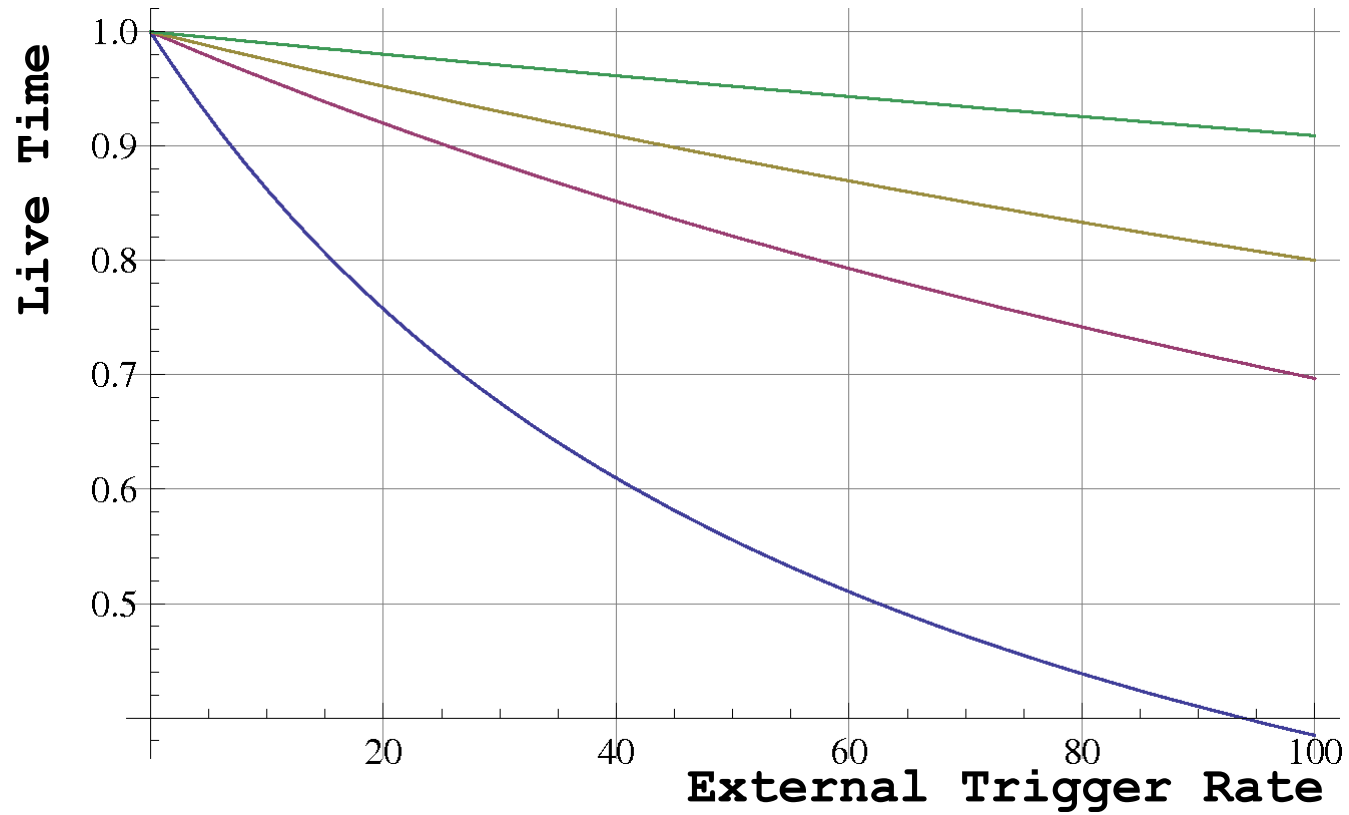


Λ momentum vs p momentum (coincidence π^- , p, p)

Entries 345297



Dead time measurements



$$\text{Live time} = 1 - T_{\text{dead}}/T$$