Tecniche di programmazione in chimica computazionale

Examples

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Dipole moment and center of charge in molecules

For any molecule/cluster the dipole moment $\vec{\mu}$:

$$\vec{\mu} = \sum_{\alpha} q_{\alpha} \vec{r}$$

with α running on the atoms, q_{α} are the charges on atoms (Mulliken, Lowdin etc.) and $\vec{r}$ are the atomic coordinates

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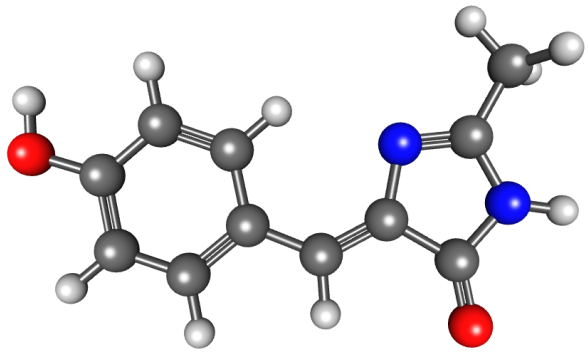
For charged systems, the center of charge $\vec{cc}$ is:

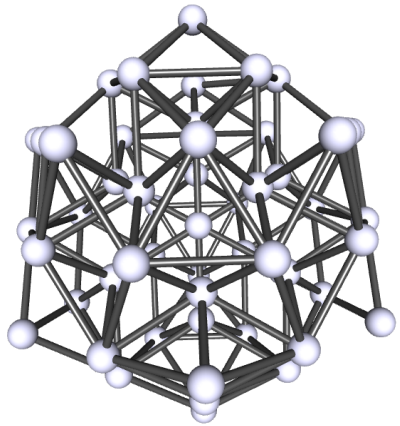
$$\vec{cc} = \frac{\sum_{\alpha} q_{\alpha} \vec{r}}{\sum_{\alpha} q_{\alpha}}$$

Dipole moment and center of charge in molecules

- Copy files from 2021/CC to your work space
- HBDI (chromophore of GFP)



- Ag_{55}^{5+}



Matrix diagonalization

- Square matrix **A** (*NxN*)

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- Example diag.f90

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- Example transpose.f90
- Transpose conjugated of a matrix: example tconjug.f90

Franck-Condon factors

Born-Oppenheimer approximation

$$
\begin{aligned}
\Psi_{e\nu}(q_e, q_N) &= \psi_e(q_e; q_N)\chi_\nu^e(q_N) \\
\mu_{e,\nu;e',\nu'} &= \int dq_N \chi_\nu^{e,*}(q_N) M_{ee'} \chi_{\nu'}^{e'}(q_N) \\
M_{ee'} &= \int dq_e \psi_e^*(q_e; q_N) \hat{\mu} \psi_{e'}(q_e; q_N)
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Electronic contribution to transition dipole moment not varying with q_N

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S^{e,e'}_{\nu,\nu'} &= \int dq_N \chi^{e,*}_\nu(q_N)\chi^{e'}_{\nu'}(q_N) \\
\mathrm{FC}^{e,e'}_{\nu,\nu'} &= |S^{e,e'}_{\nu,\nu'}|^2
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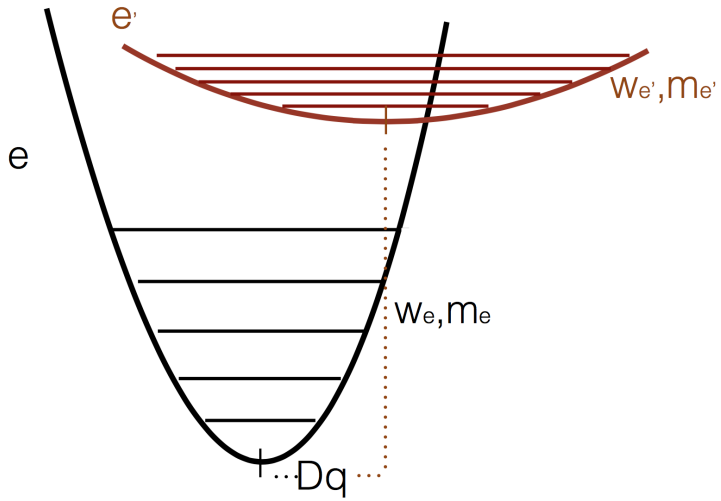
Franck-Condon factors

- Harmonic oscillator



Franck-Condon factors

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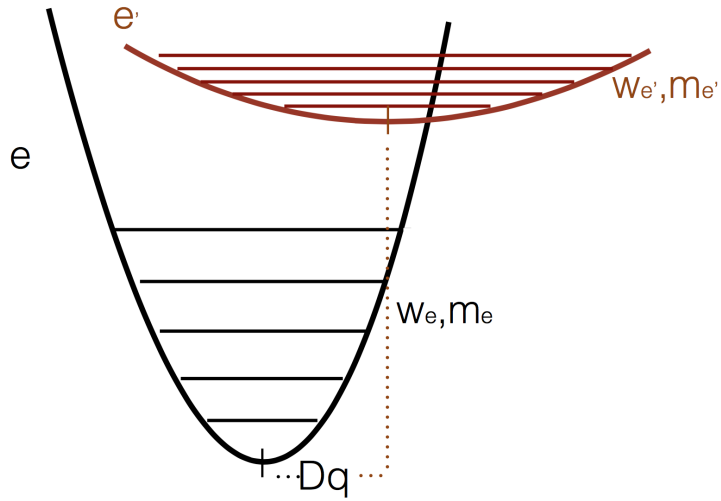

- Harmonic eigenfunctions

$$\chi_0^e(q_N) = \left(\frac{m_e\omega_e}{\pi}\right)^{1/4} \exp[-(m_e\omega_e)q_N^2/2]$$

$$\chi_1^e(q_N) = \sqrt{2}\left(\frac{m_e\omega_e}{\pi}\right)^{1/4} \left(\sqrt{m_e\omega_e}q_N\right) \exp[-(m_e\omega_e)q_N^2/2]$$

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Franck-Condon factors

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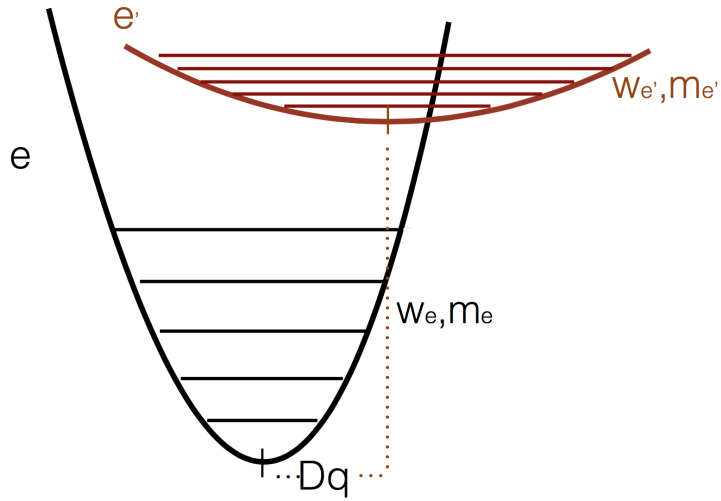

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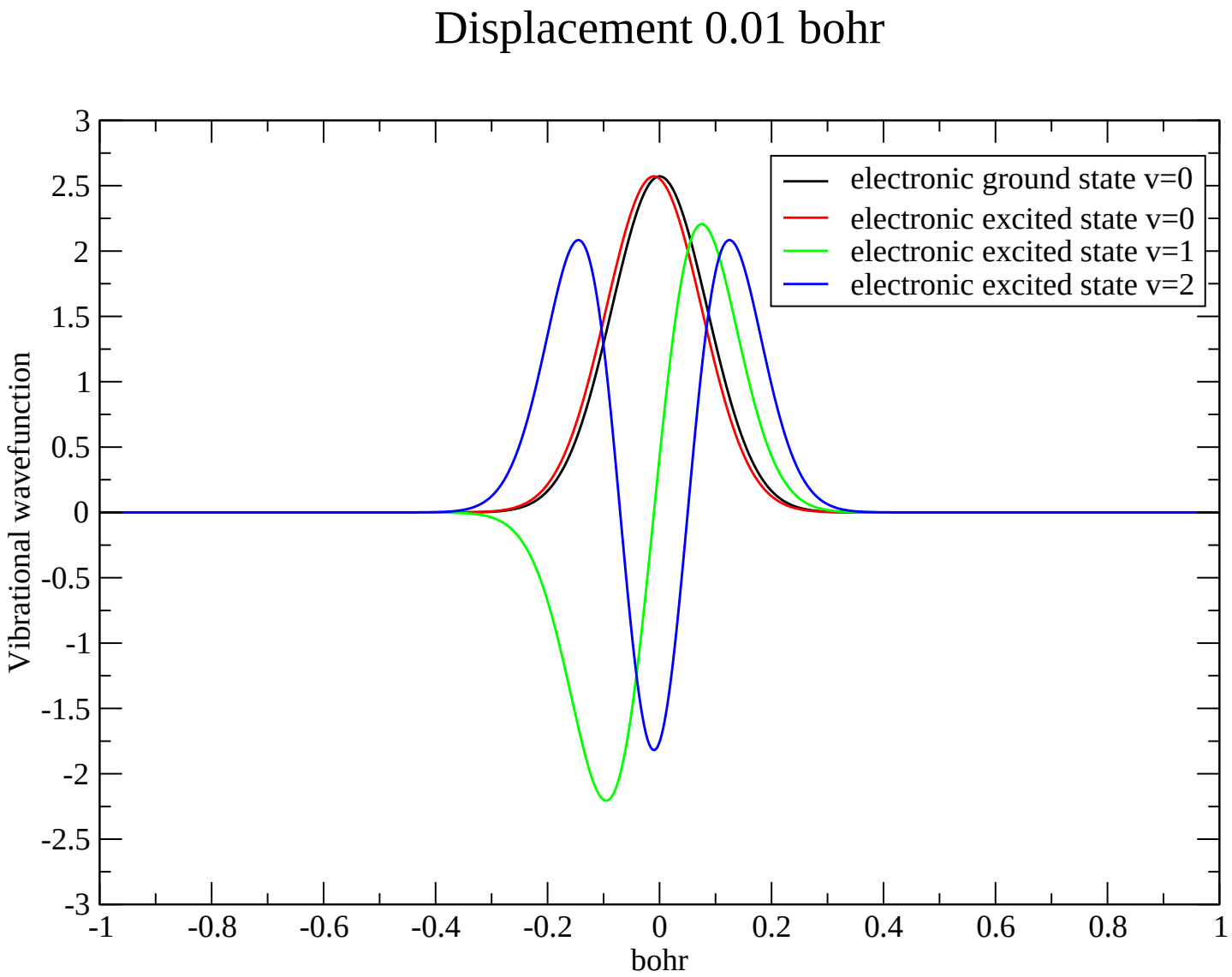
- Given the same frequencies and reduced masses, how the FC factor changes with the displacement Δq (for a chosen ν)?

"Pseudo" Br_2 results



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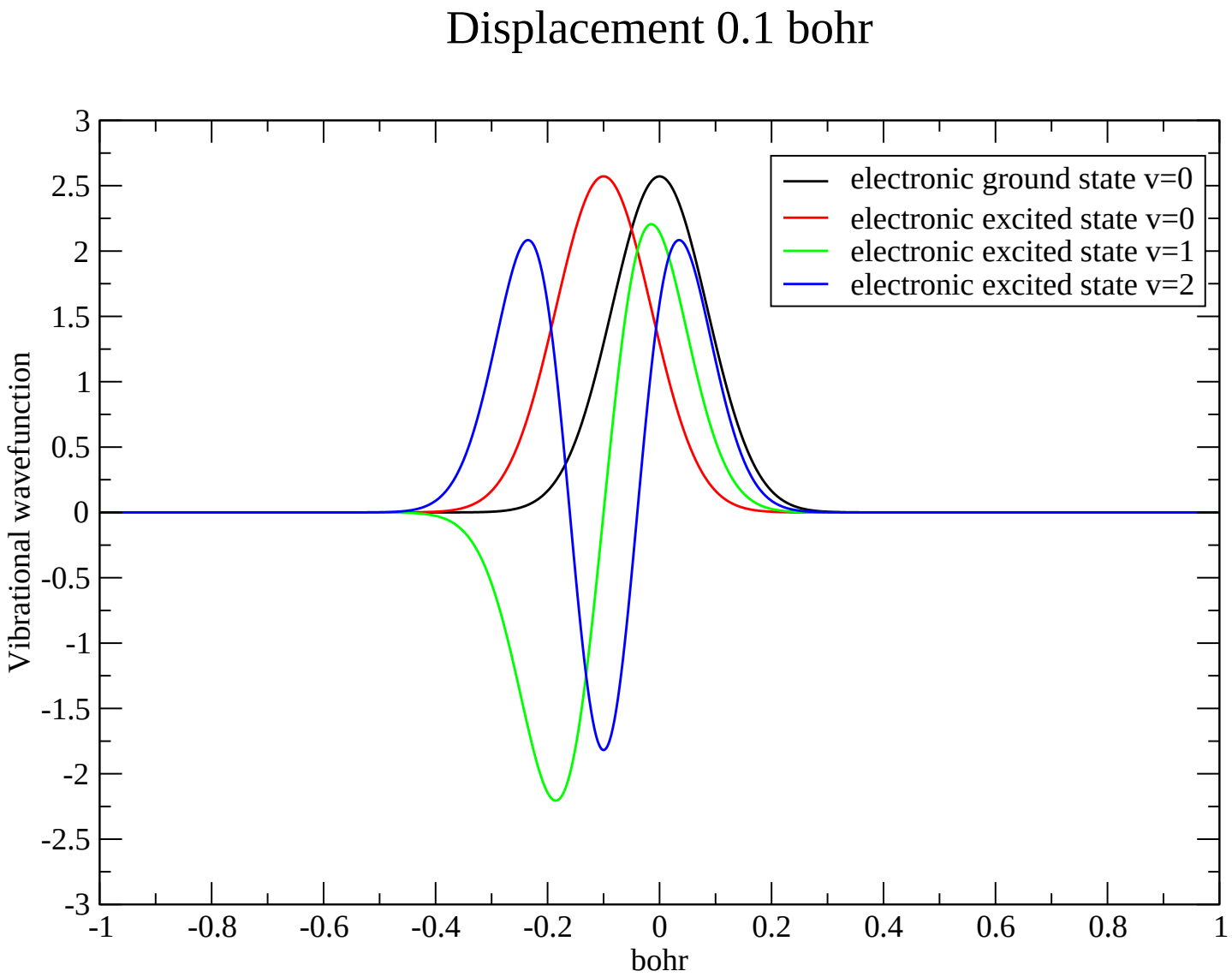

Simulating real-time dynamics

- Light-matter interaction, simulating time-resolved spectroscopies

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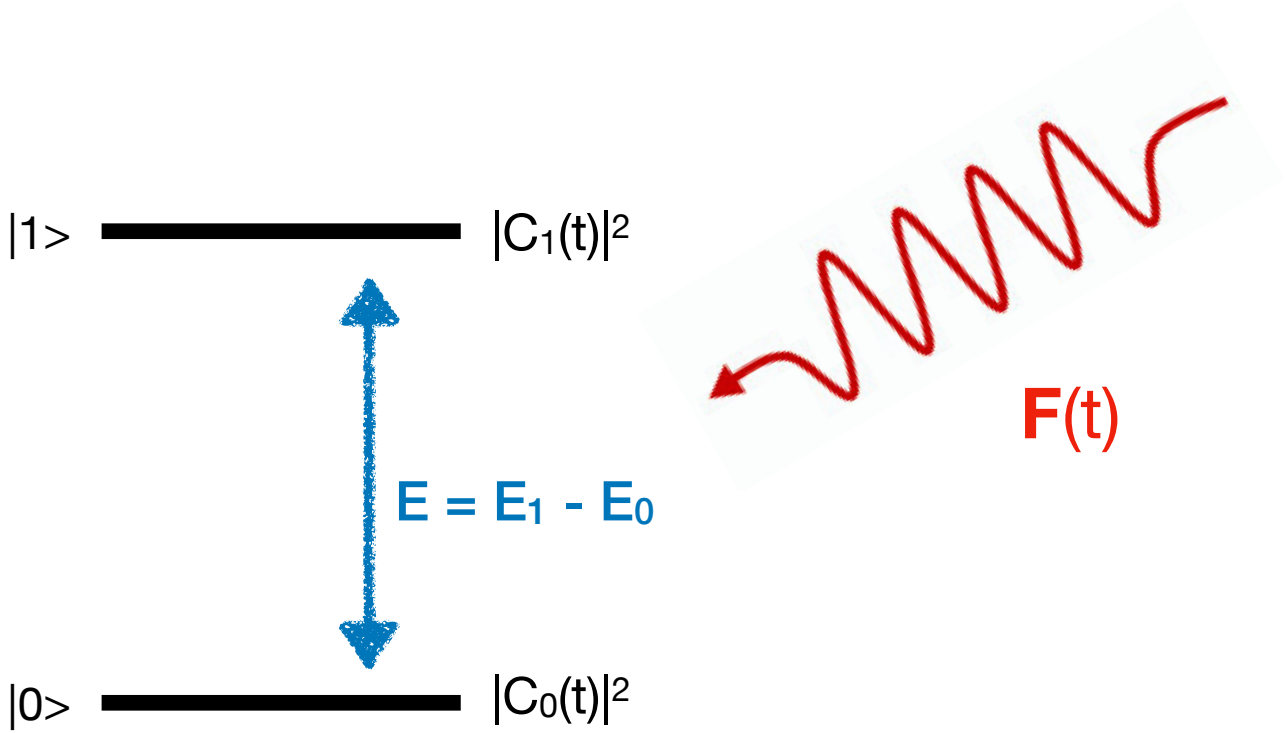
- Two-level system

$$|\Psi(t)\rangle = C_0(t)|0\rangle + C_1(t)|1\rangle$$



Simulating real-time dynamics

Time-dependent Schrödinger equation (TDSE)

$$
\begin{aligned}
i\frac{\partial|\Psi(t)\rangle}{\partial t} &= \hat{H}(t)|\Psi(t)\rangle \\
\hat{H}(t) &= \hat{H}_0 - \hat{\mu}\cdot\mathbf{F}(t) \\
i\frac{\partial C_0(t)}{\partial t} &= C_0(t)E_0 - \mathbf{F}(t)\left(\langle 0|\hat{\mu}|0\rangle + \langle 0|\hat{\mu}|1\rangle\right) \\
i\frac{\partial C_1(t)}{\partial t} &= C_1(t)E_1 - \mathbf{F}(t)\left(\langle 1|\hat{\mu}|1\rangle + \langle 1|\hat{\mu}|0\rangle\right) \\
\mathbf{F}(t) &= \mathbf{F}_{\max}\exp\left(-\frac{(t-t_{mid})^2}{2\sigma^2}\right)\sin(\omega t),
\end{aligned}
$$

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  - input: parameters for propagating TDSE
  - ci_ini.inp: initial populations
  - ci_energy.inp contains excitation energy E
  - ci_mut.inp contains dipoles and transition dipoles

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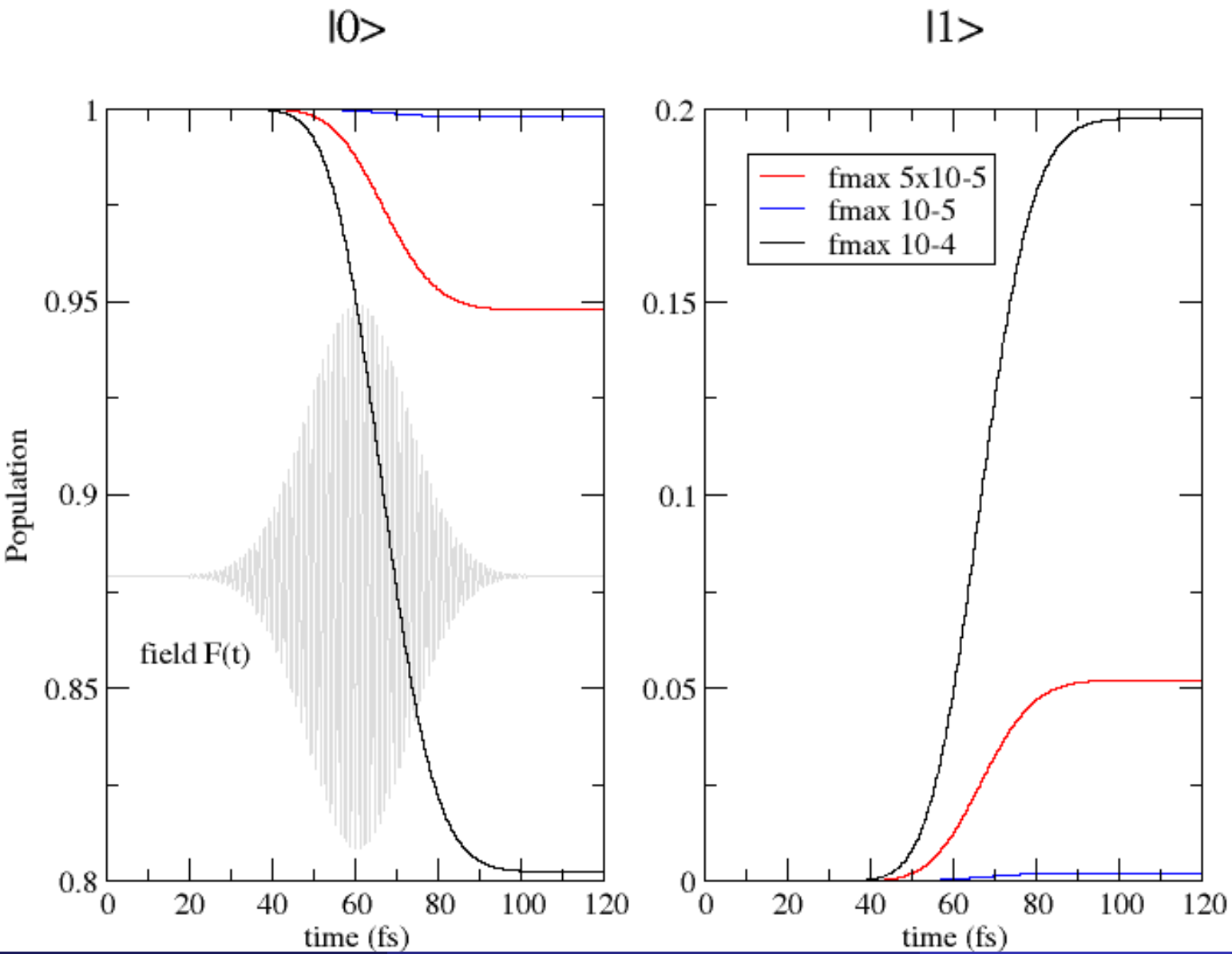
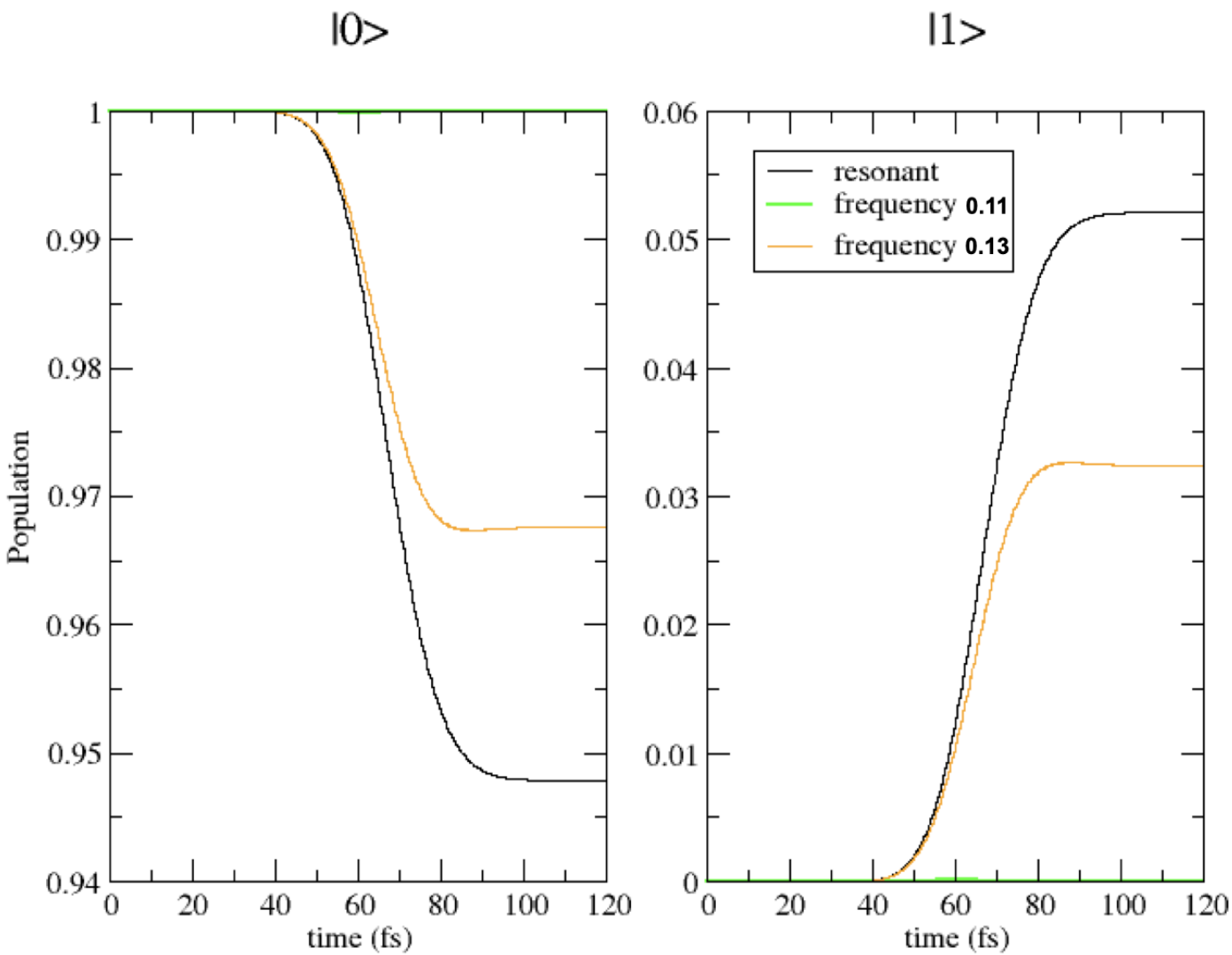
- To run the simulation, copy the files in your working directory, and type ./wavet.x < input > output
- Many files are produced, focus on c_t_1.dat
  - c_t_1.dat: time evolution of $|C_0(t)|^2$ and $|C_1(t)|^2$ *step time Population* $|0\rangle$, $|1\rangle$

Simulating real-time dynamics

1. Check the last value of $|0\rangle$ and $|1\rangle$ populations by changing the amplitude of the pulse (fmax = 10^{-4}, 5x10^{-5}, 10^{-5}, resonant frequency)
2. Check the last value of $|0\rangle$ and $|1\rangle$ populations by changing the frequency of the pulse (fmax= 5x10^{-5}, omega=0.11, 0.13 and resonant)

Simulating real-time dynamics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