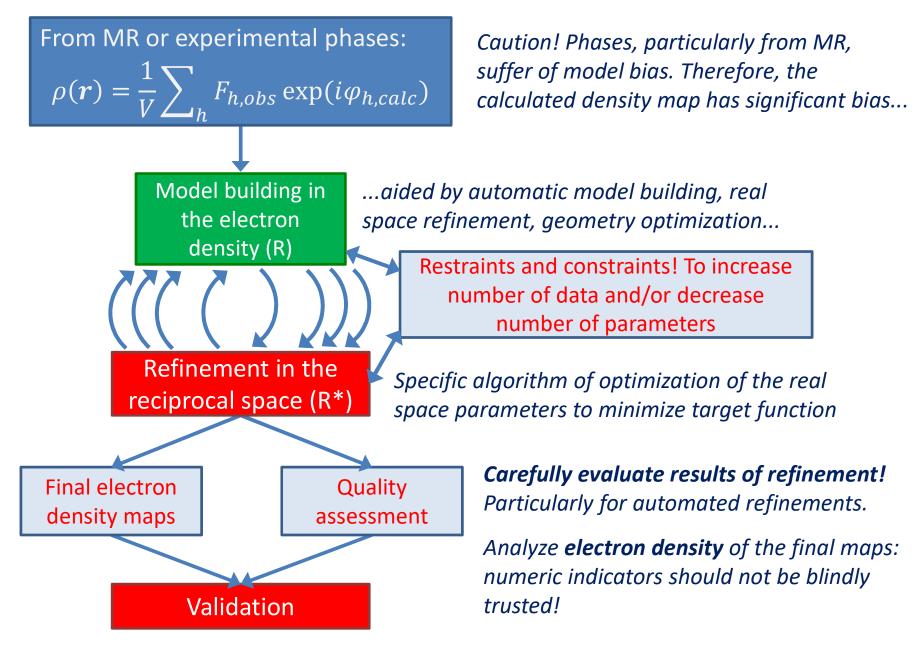
# Model Building and Refinement

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### From phasing to refinement

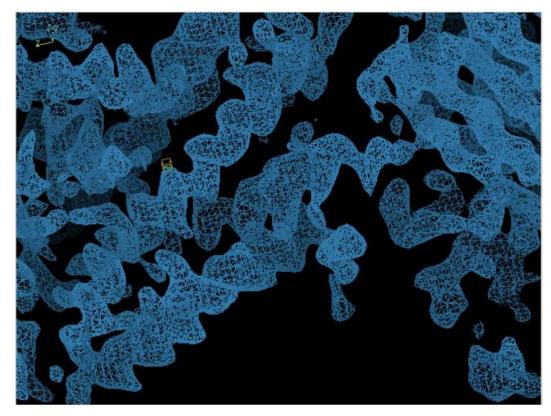


## Model building

MR phasing: model already available, except trimmed parts (loops, side chains of residues)

1. Trace  $C\alpha$  main chain

Experimental phasing: empty density, except for the heavy atom/anomalous scatterer

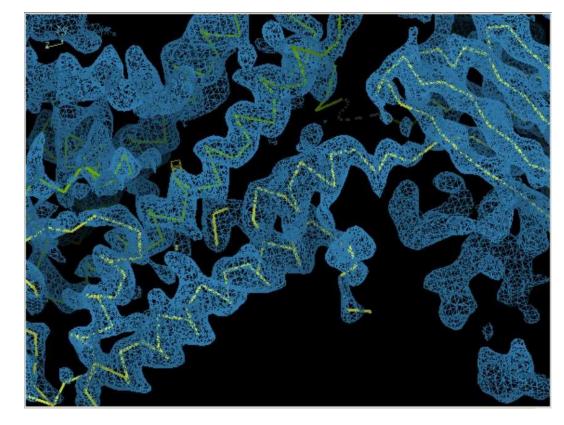


# Model building

MR phasing: model already available, except trimmed parts (loops, side chains of residues)

- 1. Trace  $C\alpha$  main chain
- Identify side chains of large residues (easier) and from those identify other residues according to sequence
- Introduce in the model cofactors and solvent molecules (when well defined)
- 4. Introduce ligands (<u>but it should</u> <u>be verified!!</u>)

Each step should be followed by Fourier space refinement. Experimental phasing: empty density, except for the heavy atom/anomalous scatterer



Automatic software for model building are available.

From bad phases and/or bad data, no good model can be built!!

#### Refinement in R\*

# Optimization of $N_P$ parameters against $N_D$ observations to minimize a target function.

**Observations**: measured diffraction intensities (R\*) + knowledge regarding protein structure (R)

**Parameters**: atom positions (x,y,z), atomic B-factors (isotropic or anisotropic), occupancy, scale factor, overall B-factor, bulk solvent correction, anisotropy correction... Continuously variable over the defined parameter space.

For each atom: at least 3 positional parameters and 1 B-factor (6 if anisotropy is taken into account).

Different parametrizations are possible and sometimes convenient.

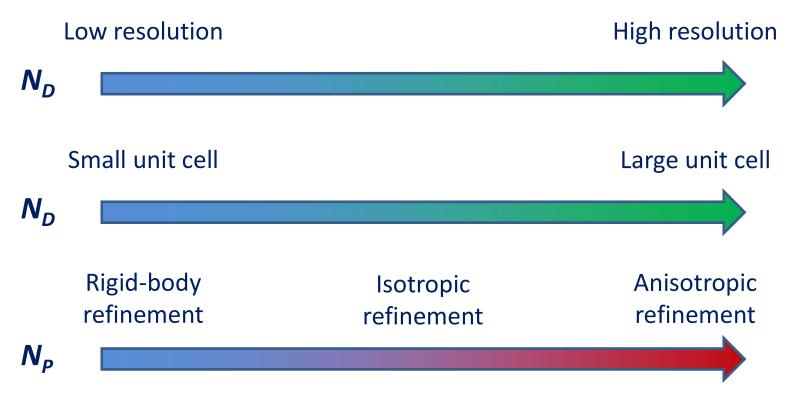
**Target function**: Changes in parameters don't have a simple effect on data fitting, as errors on a single atom interest many structure factors and their relation is not linear...

Problem: trapping in local minima.

To monitor refinement, linear residual value R

$$R = \frac{\sum_{h} |F_{obs} - F_{calc}|}{\sum_{h} F_{obs}}$$

#### Data and parameters

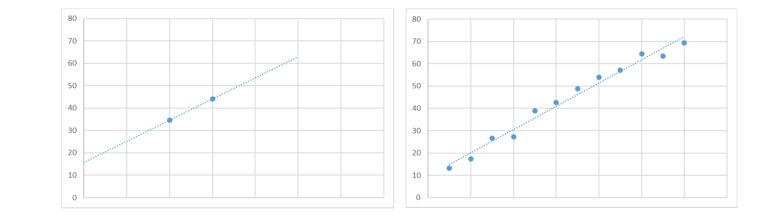


N<sub>P</sub>: For a 129 residue protein, each residue containing an average of 8 non-hydrogen atoms (+ solvent, ions, ligands...), each atom with 4 refinement parameters (in the isotropic case... otherwise 9!) = 4128 parameters + scaling parameters...

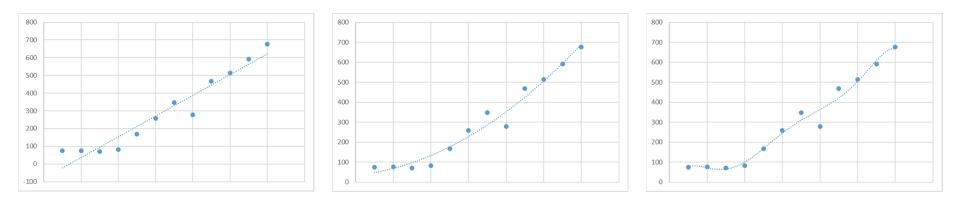
Hydrogen atoms are usually not refined with positional and atomic displacement parameters: their scattering contribution is not sufficient to justify the refinement. (However, hydrogen atoms are usually included in refinement in calculated postitions, because their contribution is important, particularly at high resolution.)

#### Data-to-parameter ratio $(N_D/N_P)$





2. The number of parameters should not be increased (even when the number of observations allows it) arbitrarly: the introduction of additional parameters should be justified by chemical reasons and by inspecting the electron density map.



#### **Restraints and constraints**

**Constraints**: Relations between parameters that make some dependent from others

E.g. In rigid-body refinement, protein model is maintained rigid: atom positions are not refined independently, but all their geometric relations (distances, angles, dihedrals, planarity...) are kept constant, reducing the number of parameters in the refinement. <u>Geometric relations are kept as constraints</u>.

**Constraints** reduce the number of parameters to refine!

**Restraints**: Relations between parameters based on statistical analysis that yield expected values with a defined uncertainty

*E.g.* For the phenyl group, the planarity of the aromatic ring can be expected from chemical considerations. Atoms are not forced on the same plane, but deviations from the planarity are considered less probable occurrences.

**Restraints** increase the number of observations!

#### Restraints

Geometric restraints: bond distances, bond angles, planarity, chirality... Usually dihedral angles are not restrained but analyzed as diagnostic parameters, i.e. Ramachandran plot. Usually tighter on main chain, looser on side chains.

Antibumbing restraints: distances between non-bonding atoms must be larger than van der Waals radii.

**Non-Crystallographic Symmetry (NCS) restraints**: core residues of NCS-related protein chains are likely to have similar conformations, while surface residues have more variable conformations.

**B-factor restraints**: atoms of the same group are restrained to have similar B-factors (particularly in case anisotropy is accounted for)

Libraries of restraints are available in the main refinement software and are automatically applied to each specific residue according to the residue type (written in the .pdb coordinate file).

Libraries of restraints for ligands or unusual cofactors must be prepared.

#### **Target function**

*Least squares*:

$$Q_{LS} = \sum_{i=1}^{n} \frac{[X_{obs}(i) - X_{calc}(i, \boldsymbol{p})]^2}{\sigma_{obs}^2(i)}$$

with  $X_{obs}(i)$  observations, including diffraction data and additional knowledge and p parameters vector, i.e. a vector containing all parameters sequentially.

#### Maximum likelihood:

$$Q_{ML} = \sum_{i=1}^{n} \frac{[X_{obs}(i) - \langle X_{calc}(i, \boldsymbol{p}) \rangle]^2}{\sigma_{obs}^2(i) + \sigma_{calc}^2(i, \boldsymbol{p})}$$

with  $\langle X_{calc}(i, \mathbf{p}) \rangle$  expectation value of a Bayesian probability distribution, and including  $\sigma_{calc}^2(i, \mathbf{p})$  to estimate non-random error for the proposed model.

Good for high resolution data and complete and correct structural models. Considers Gaussian distribution for all errors on parameters.

Better suited when the model is incomplete and/or partially incorrect: this function takes into account the conditional probability of model against data.

#### **Refinement protocol**

Details of the refinement:

- Parametrization: xyz? TLS?
- Restrained or unrestrained?
- Isotropic or anisotropic B-factors?
- Minimization function: Least squares (LS)? Maximum Likelihood (ML)? Energy minimization (based on Molecular Dynamics methods, e.g. simulated annealing)?
- Optimization algorithm:
  - Gradient descent methods (full-matrix, sparse matrix, steepest descent...)
  - Stochastic algorithms (often with energy minimization)

TLS parametrization: uses translation-librationscrew parameters. Reduces number of parameters.

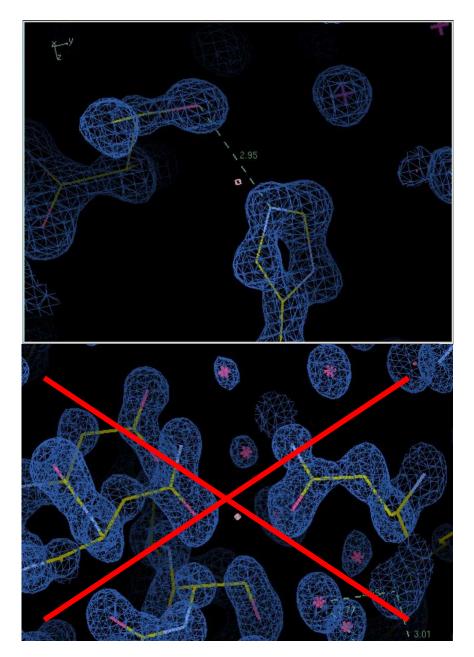
Unrestrained only for high resolution datasets!

Increase of number of parameters with anisotropic B-factors: check N<sub>P</sub>/N<sub>P</sub>!

LS: high resolution structures and reliable models. Energy refinement is an alternative to restrained refinement: minimum of energy function.

Compromize between rate of convergence (speed of calculation) and radius of convergence (dimension of parameter space covered)

### Side chain conformations



Side chain conformations should be adjusted in the electron density when visible.

Pay particular care in orientation of His, Gln and Asn side chains: orientations are particularly impotant when structures are used for docking/drug design.

To distinguish side chain orientation, analyze hydrogen bonding network.

In some cases it is necessary to distinguish two different conformations for some residues (part. on the surface).

The sum of occupancy of the two conformations should be equal to 1.

Multiple conformations should not be introduced in the model if not clearly identifiable from the maps!

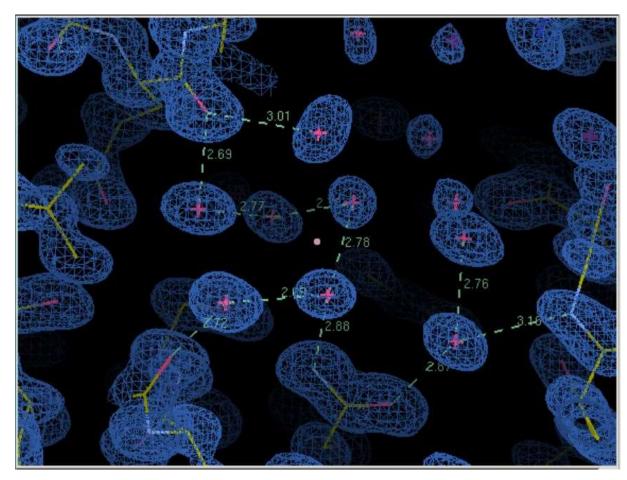
### Solvent molecules and ligands

**Solvent molecules**: they should be introduced only if clear electron density is visible in the map.

Analyze contacts: water molecules should be at hydrogen bonding distance from protein residues.

**Ions**: check charge of residues in contact with the ions; check distances and compare them with reported distances.

Difference in electron density between, e.g., K<sup>+</sup> and Cl<sup>-</sup> is not clear even at high resolution.



Ligands: The presence and conformation of ligands should be analyzed with particular care!! In this case, omit maps can be calculated to highlight unaccounted electron density.

# R<sub>free</sub> and R<sub>work</sub>

*Cross-validation*: a subset of the reflections is set aside during refinement and used to validate the model obtained.

The small percentage of removed reflections (usually  $\approx$  5% of all data) does not affect the density maps.

$$R_{free} = \frac{\sum_{\boldsymbol{h} \in free} |F_{obs} - kF_{calc}|}{\sum_{\boldsymbol{h} \in free} F_{obs}}$$

This value is compared to the R-value obtained on data used during refinement:

$$R_{work} = \frac{\sum_{h \notin free} |F_{obs} - kF_{calc}|}{\sum_{h \notin free} F_{obs}}$$
A high value of  $R_{free}$  compared to  
 $R_{work}$  is indicative of  
overparametrization of the  
refinement of the refined and  $R_{work}$  are too close, the refined model can be further improved. The expected difference between  $R_{work}$  and  $R_{free}$  depends on resolution.

Not all errors are highligthed by R-values: a careful inspection of the maps is still required!!