

# A2. INTEREST RATES

FINANCIAL MARKETS AND INSTITUTIONS

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# TOPICS



- WHY DO WE NEED IR AND HOW DO WE MEASURE THEM?
- WHAT ARE REAL IR AND WHY ARE THEY IMPORTANT?
- HOW DO WE USE IR TO MEASURE RETURNS AND RISKS?
- CAN WE PREDICT INTEREST RATES?

# MEASURES OF IR



# IR AND FINANCIAL CONTRACTS

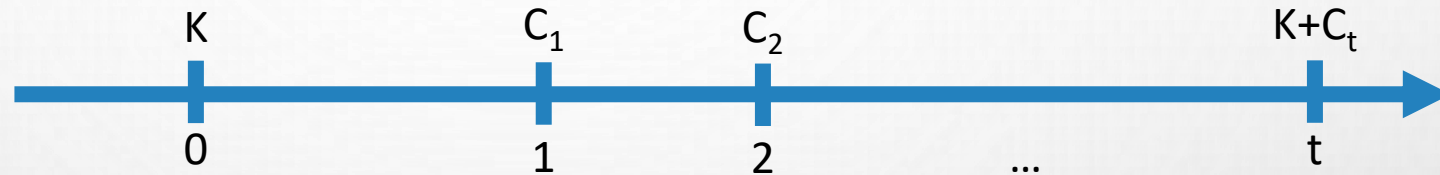
Balloon/simple loan:



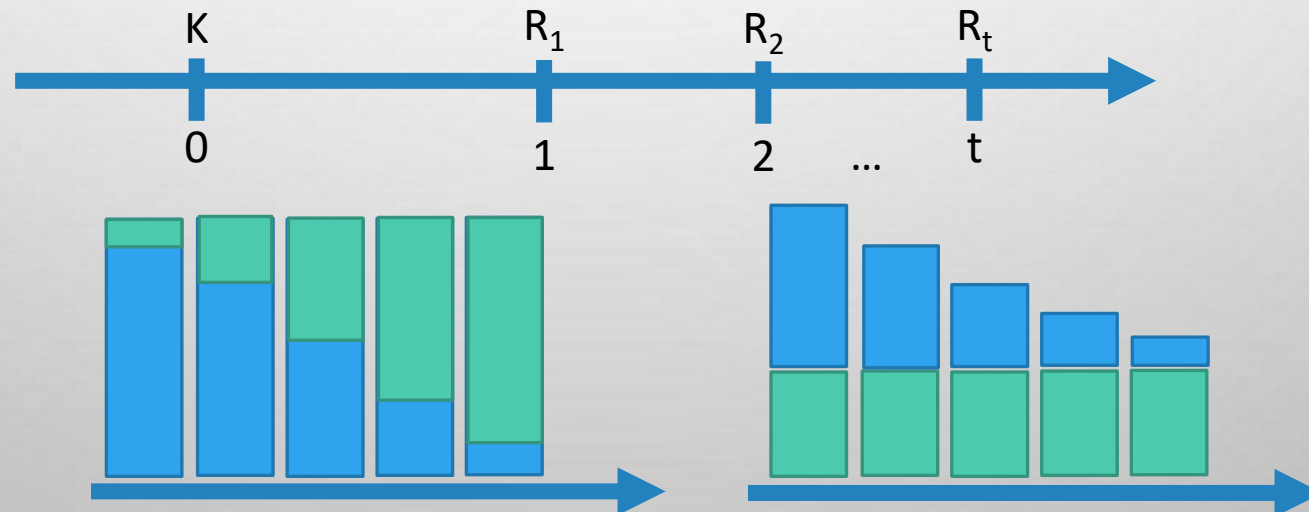
Discount bond (ZC):



Coupon bond:



Fully amortised loan:



Many variants: variable or adjustable IR, changing maturity, pre-amortization, ...



# MEASURES OF IR



*How to compare  
different debt  
instruments?*

## Yield to maturity (YTM)

- Strikes a balance across cashflows
- For simple loans only it equals the nominal rate

• ZC:

$$YTM = \sqrt[n]{\frac{FV}{CV}} - 1$$

- Coupon bonds (and others):

$$CV = \sum_{t=1}^n \frac{CF_t}{(1 + YTM)^t}$$

$$VA = \sum_{t=1}^n \frac{C_t}{(1 + YTM)^t} + \frac{FV}{(1 + YTM)^n}$$

- + YTM, - CV: an increase in IR lowers the current value (and v.v.)

# MEASURES OF IR

WHICH ONE IS MORE REWARDING? (OPEN EXCEL AND TRY THE FOLLOWING!)

1. SIMPLE LOAN: PROVIDING 104 IN 1 YEAR
2. DISCOUNT BOND: PRICE 98, MATURITY IN 6 MONTHS
3. COUPON BOND: PRICE 99, SEMIANNUAL COUPON 2%, MATURITY 2 YEARS
4. FULLY AMORTISED LOAN: PRICE 69, 3 YEARLY INSTALMENTS OF 25

# ISSUES WITH THE YTM



## YTM:

- Assumes holding period equals maturity
- Assumes reinvesting at the same rate
- **Nominal!**

- Risks and opportunity costs?
- Yields vary over time!
- **Real values matter more...**

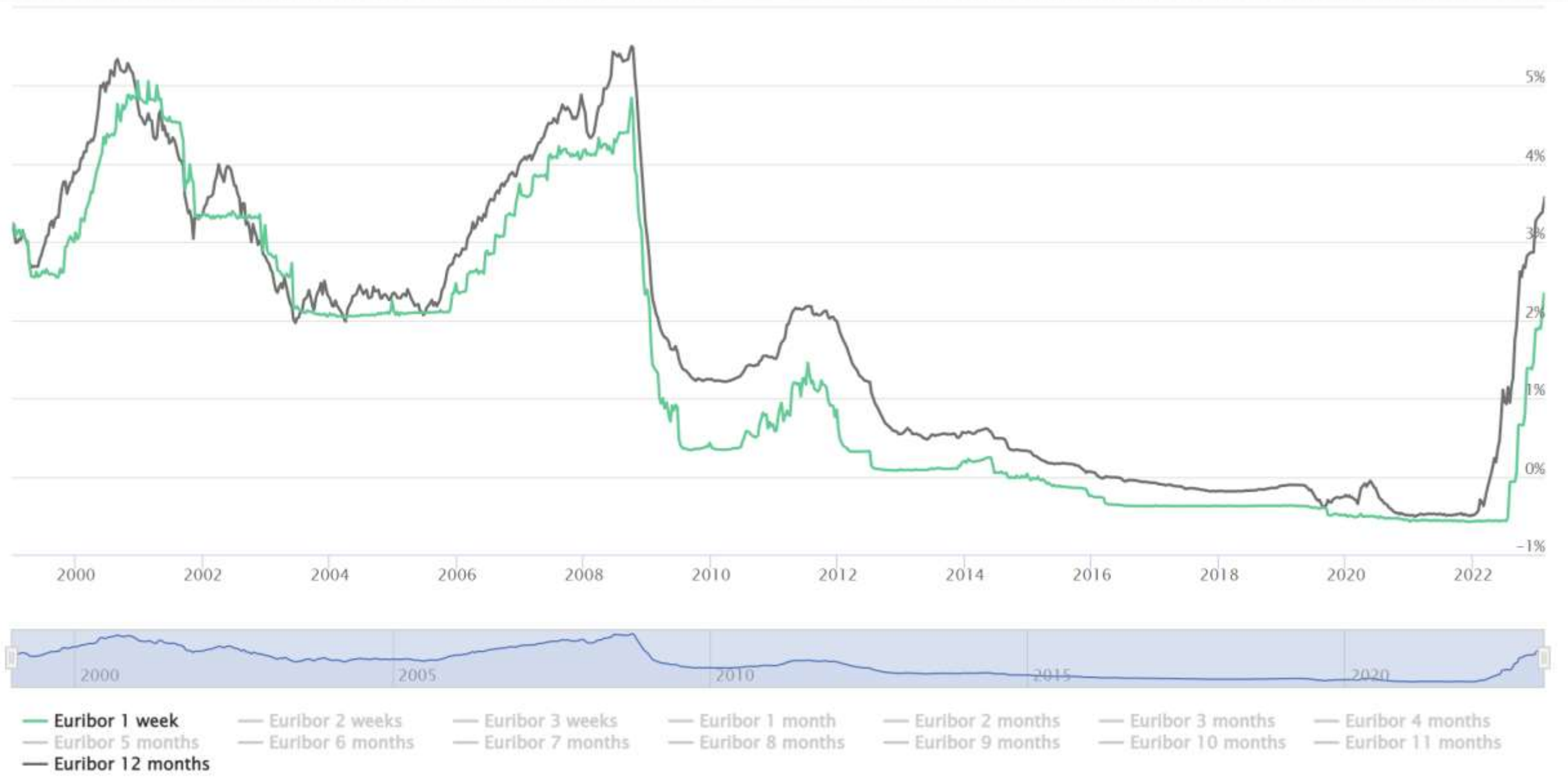
Ex-ante real IR consider the expected change in price levels (effective IR) :

$$i_n = i_r + \pi^e [+i_r \cdot \pi^e]$$

Ex-post real IR consider effective inflazione (but when the transaction is over!)

Then, tax issues may have impacts (charges on interest income, discounts on interest expense)

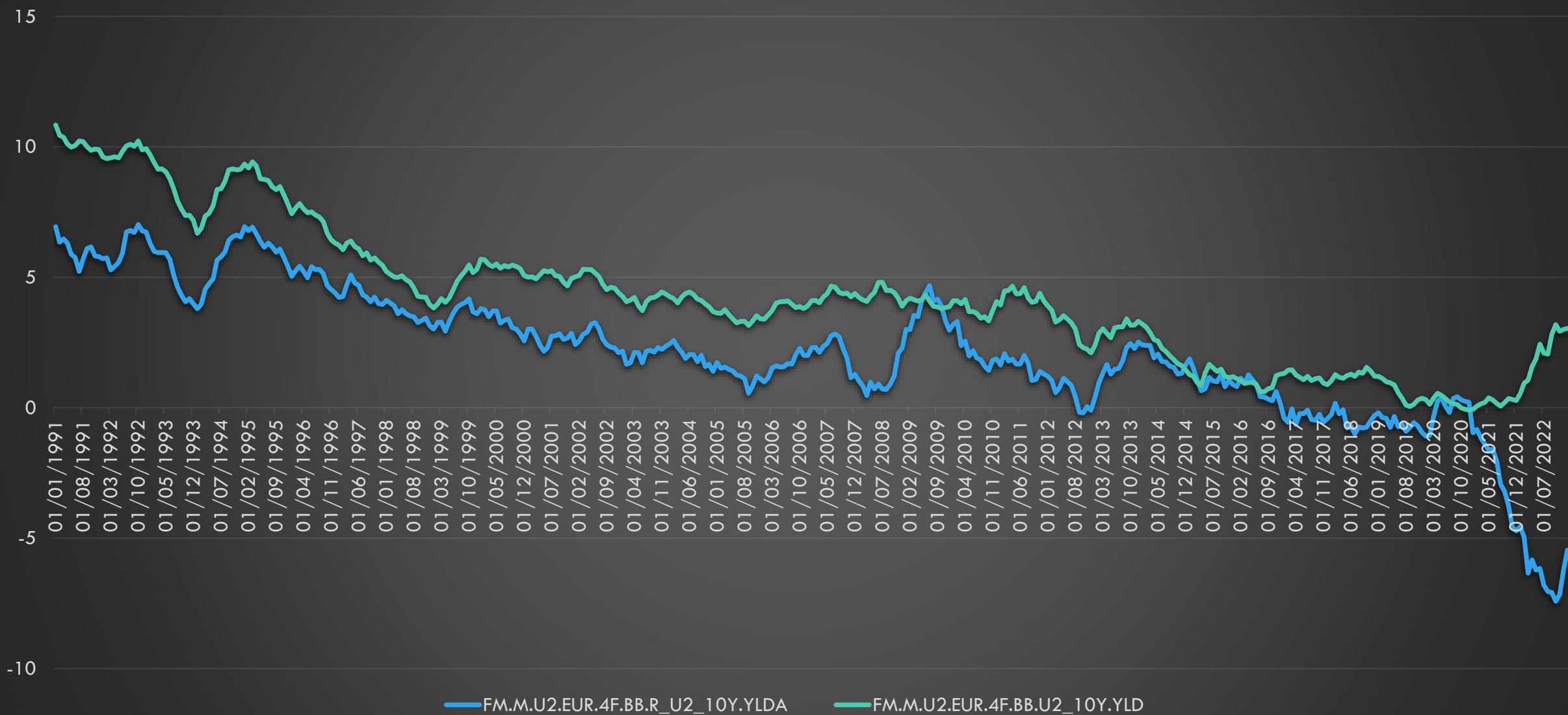
# ISSUES WITH THE YTM





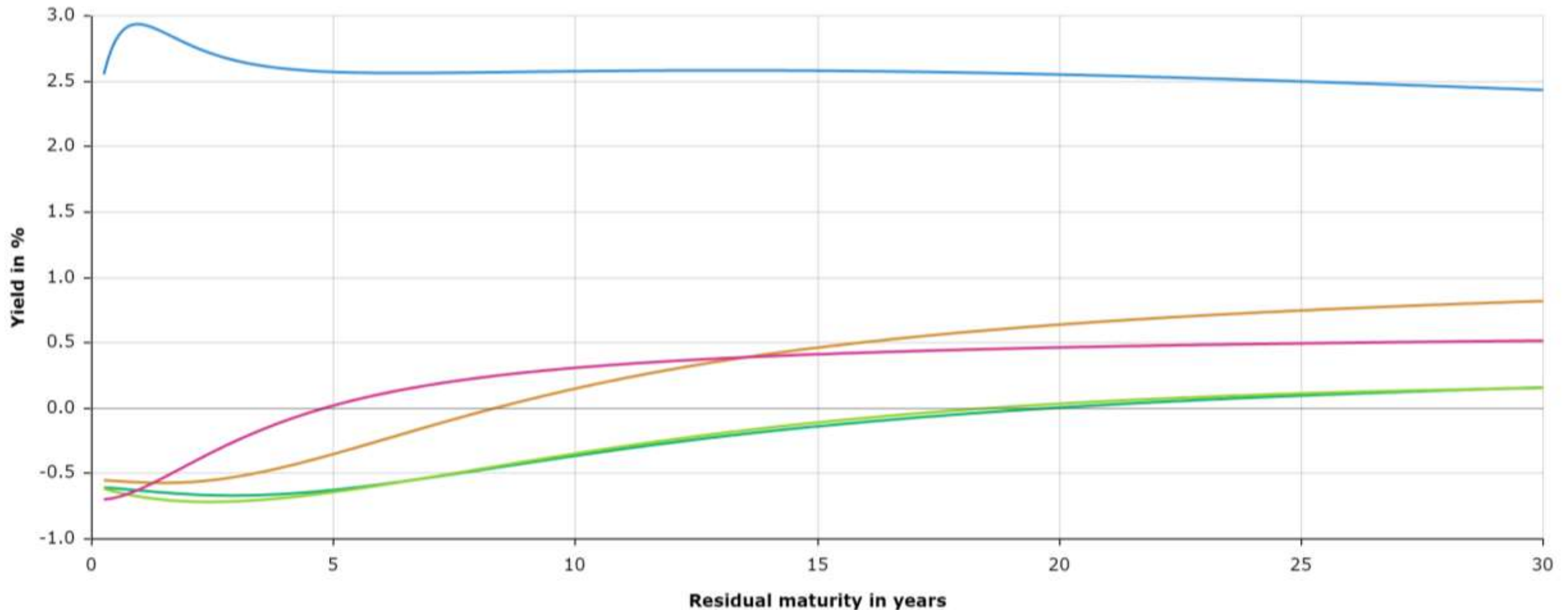
# ISSUES WITH THE YTM

## REAL vs NOMINAL 10y EZ GOV BONDS



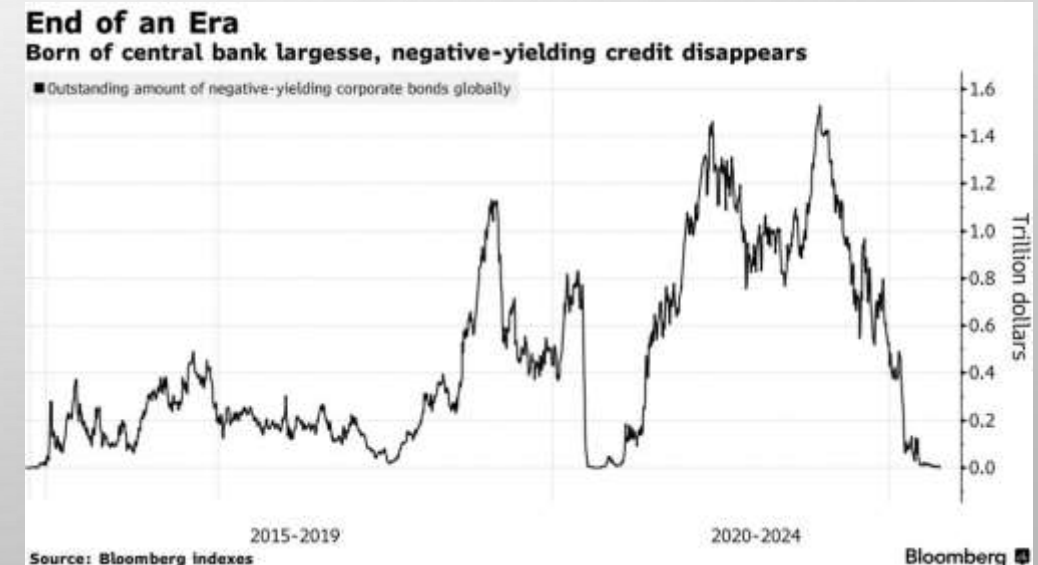
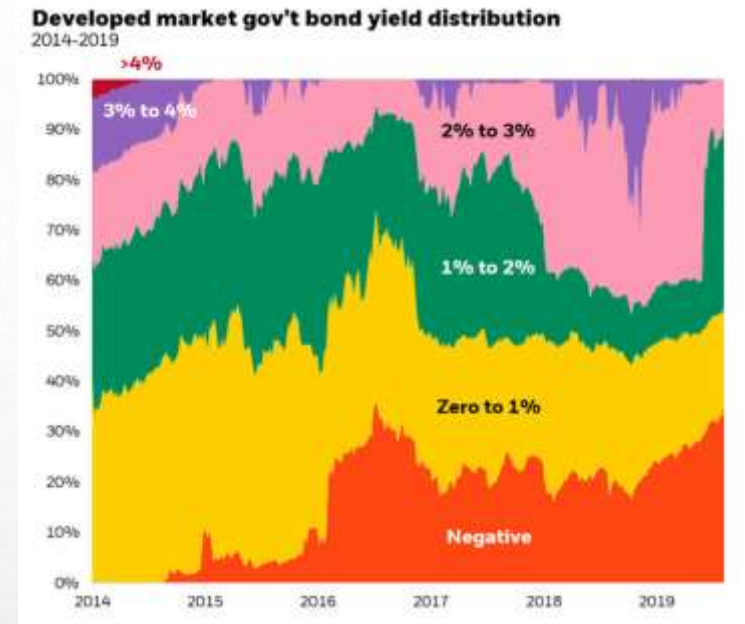
# ISSUES WITH THE YTM

*EZ GOV bonds yield by maturity - ECB*



# NEGATIVE RATES?

- «Paying for lending? Nobody can be that stupid...»
  - CB: BCE -0.2% on deposits from 9/2014 (also DEN, SWE, CH)
  - GOV: DE, NED, SWE, DEN, CH, AUT, ... some (FIN, DE) from issue (2/2015)
  - Firms: Nestlé experienced it on 4y € bonds (2/2015)
  - Retail: Jyske Bank sold 10y mortgages at -0,5% (8/2019)
- «But for borrowers this is great!»
  - Lenders less likely to lend, credit institutions at a loss
  - Search for higher yields → riskier! (Zombie firms)
  - Trading/currency wars?
- Any sense?
  - Real IR negative rarely and for little time (but today...?)
  - Cash reserves and access to payment systems costs (or is worth something)
  - Access to central bank operations requires bonds
  - Taxes are levied on nominal returns
  - Nominal and real IR are rooted on expectations...



# IR AND PERFORMANCE

- **Rate of return:** payments to the owner of a security plus the relative change in value
- IR and RoR differ because of capital gains:

$$RoR = \frac{C + P_{t+1} - P_t}{P_t} = \frac{C}{P_t} + \frac{P_{t+1} - P_t}{P_t} = i_c + g$$



- If holding period equals time to maturity, return equals YTM only for ZCs: reinvestment risk (if holding period is longer, even more reinvestment risk)
- The bigger the time to maturity, the bigger the effect on capital gains due to changes in IR: interest-rate risk
- Inverse relationship between IR and capital gains
- Even if unrealised, capital gains represent an opportunity cost



# IR AND RISKS: DURATION



*How to compare IR  
risks in debt instruments  
with different features?*

- Closer maturities and larger coupons lead to smaller losses if IR change
- BUT, bonds with similar maturities have also other risks (f.i. IT/DE spread), or even if maturities are different they may incur similar risks
- **How to compare them?** Weighting the time to maturity of each CF (*effective maturity, or duration*)
- **ZC** are simple: one flow, then DUR equals the TTM
- Other instruments can be considered as portfolios of ZC (since *duration* is additive):

$$DUR = \frac{\sum_{t=1}^n \frac{FC_t}{(1+i)^t} \cdot t}{\sum_{t=1}^n \frac{FC_t}{(1+i)^t}}$$

+ maturity, - cashflows, + interest = + duration

- And finally, *duration* proxies **interest rate risks**:

$$\% \Delta P = \frac{(P_{t+1} - P_t)}{P_t} = -DUR \cdot \frac{\Delta i}{(1+i)}$$



# IR AND RISKS

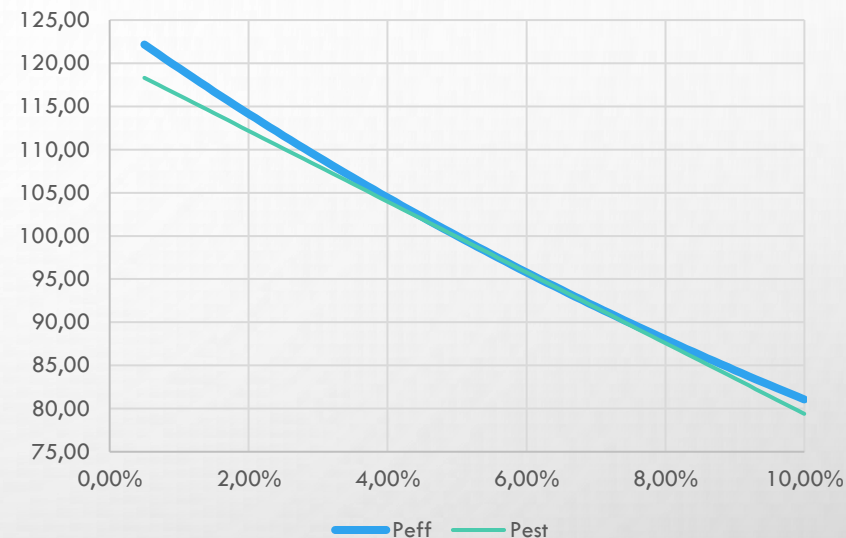
Go to **wooclap.com** and use the code **FMAI23**

Which of the following has the highest level of interest rate risk?

- ① Simple loan delivering 104 in 1 year 50% 11
- ② Discount bond priced 98 and due in 6 months 9% 2
- ③ Coupon bond price 99, with semiannual coupons at 2%, maturity 2 years 36% 8
- ④ Fully amortised loan: price 69, three yearly instalments of 25 5% 1

# ISSUES WITH DURATION

Linear proxy of a convex relationship between  $P$  and  $i$



Example: bond 5y annual coupon 6%

$P=95,79$  and  $MD=-4,28$

If  $\Delta i=1\%$ ,  $P_{eff}=91,80$  and  $P_{est}=91,69$

Duration as the 1st derivative... convexity as the 2nd!

$$CON = \frac{1}{P \cdot (1+i)^2} \cdot \sum_{t=1}^N \left[ \frac{CF_t}{(1+i)^t} \cdot (t^2 + t) \right]$$

# IR AND RISKS: DURATION

WHICH ONE IS RISKIER IN TERMS OF INTEREST RATES? (OPEN EXCEL AND TRY THE FOLLOWING, ASSUMING A 3,8% MARKET RATE!)

1. SIMPLE LOAN: PROVIDING 104 IN 1 YEAR
2. DISCOUNT BOND: PRICE 98, MATURITY IN 6 MONTHS
3. COUPON BOND: PRICE 99, SEMIANNUAL COUPON 2%, MATURITY 2 YEARS
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# FORECASTING IR

Why do interest rates change?

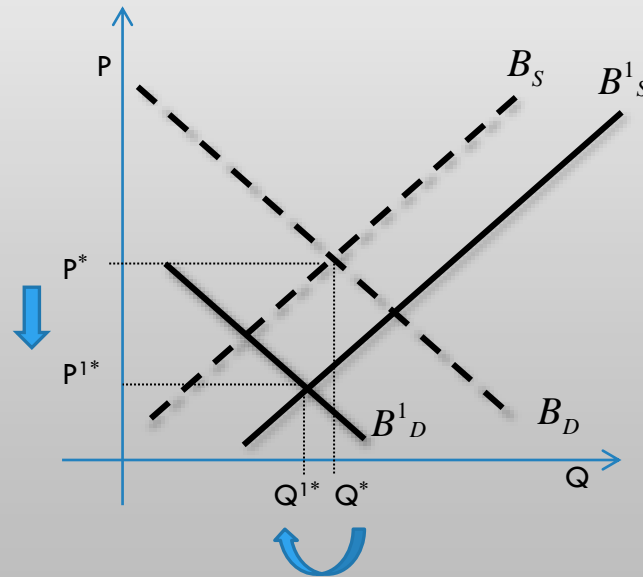
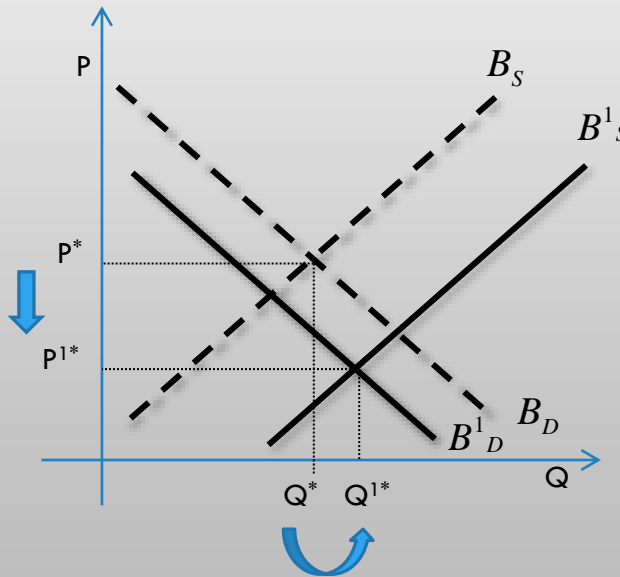
- Bonds' demand:
  - (+) Wealth owned by an individual
  - (+) Expected return relative to other assets
  - (-) Expected future interest rates
  - (-) Expected future inflation
  - (-) Risk (uncertain return) relative to other assets
  - (+) Liquidity relative to other assets
- Bonds' supply:
  - (+) Profitability of investments (more earnings)
  - (+) Expected inflation (cheaper borrowing)
  - (+) Government deficits (more public debt)



# FORECASTING IR

## Changes in IR due to inflation:

- An increase in expected inflation affects simultaneously demand (decrease of expected return) and supply (cheaper borrowing)
- IR will increase (prices fall)
- Effect on quantity is not readily predictable

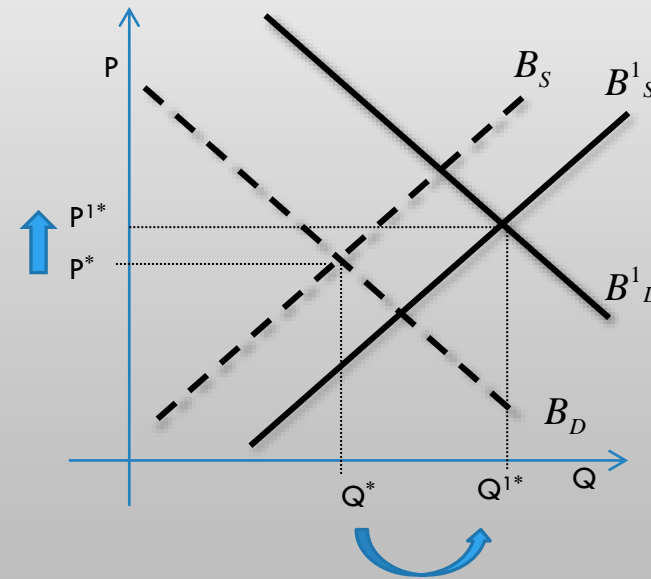
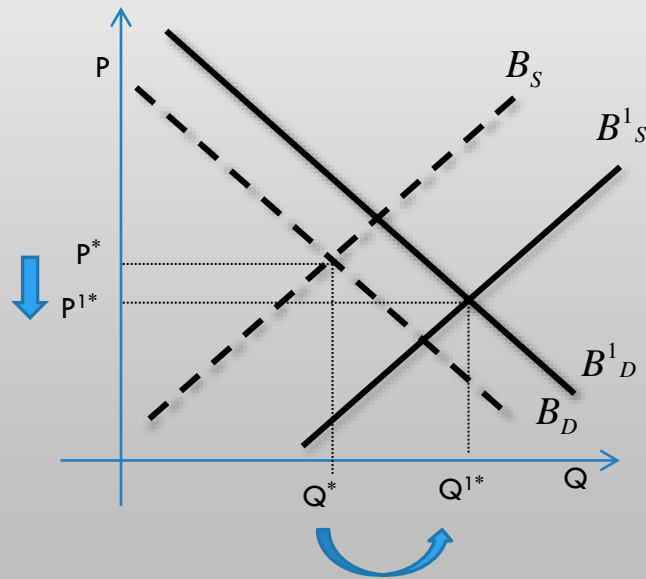




# FORECASTING IR

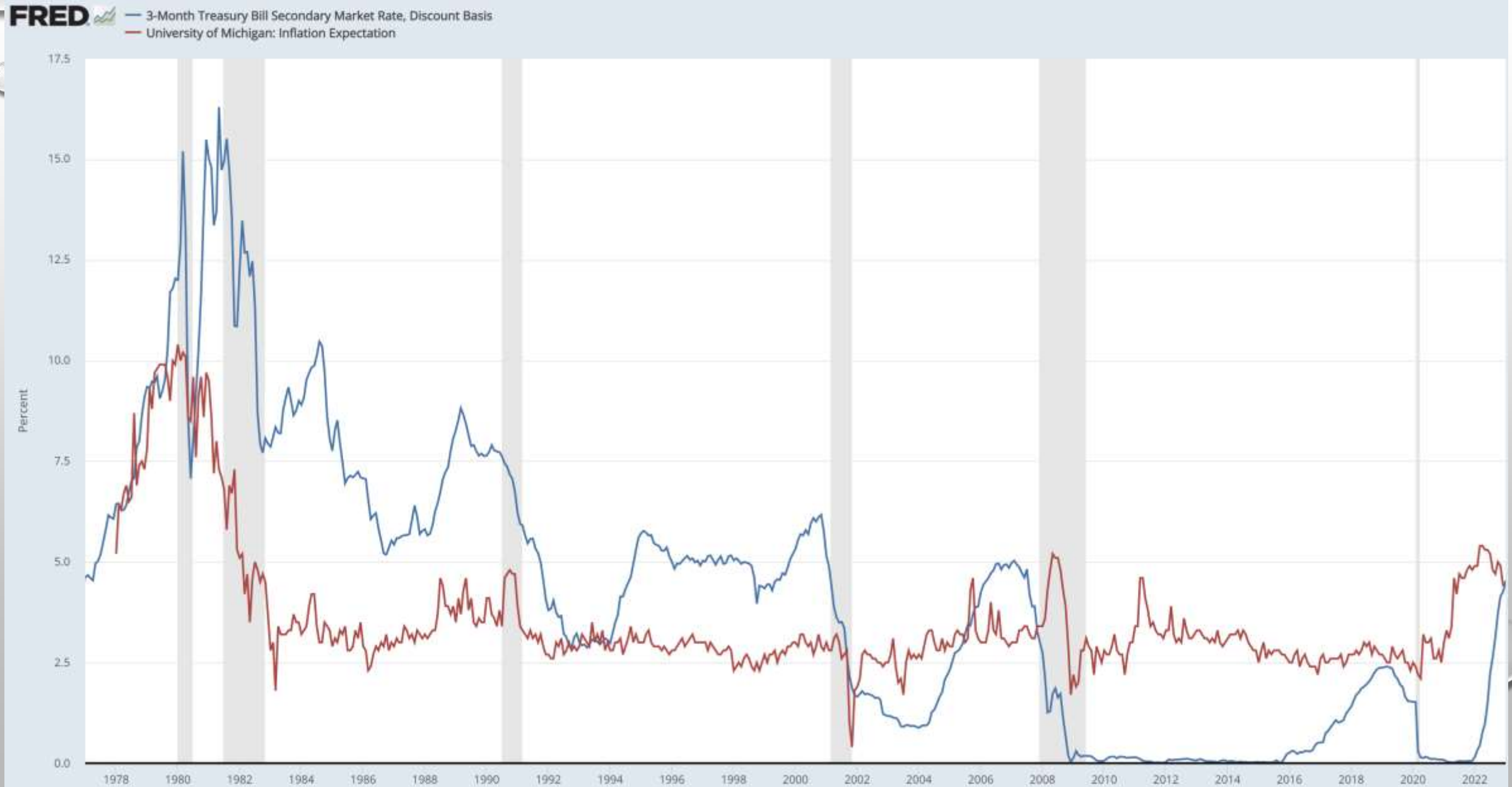
## Changes in IR due to business cycles:

- An economic expansion affects simultaneously demand (increase of wealth) and supply (greater expected returns on investments)
- Quantity will increase
- IR can increase or decrease (usually, increase – and decrease during recessions)



# FORECASTING IR

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# FORECASTING IR: DOES MONEY STEP IN?

WHEN CBS INCREASE THE MONEY SUPPLY, IR SHOULD DECLINE, BUT:

- IMMEDIATE **LIQUIDITY EFFECT** REDUCING IR
- ECONOMIC STIMULUS: MORE INCOME (**INCOME EFFECT**) AND IR, BUT IT TAKES TIME TO HAVE EFFECTS (WAGES, INVESTMENTS, ...)
- MORE INFLATION (**PRICE-LEVEL EFFECT**) AND IR, BUT IT TAKES TIME TO ADJUST PRICES OF GOODS AND SERVICES
- MORE EXPECTED INFLATION (**EXPECTED-INFLATION EFFECT**) AND IR, WITH SPEED OF EFFECTS DEPENDING ON PEOPLE'S SPEED OF ADJUSTING EXPECTATIONS
- RESULT:
  - IF THE LIQUIDITY EFFECT IS DOMINANT, SHARP REDUCTION IN IR, THEN RECOVERY UP TO A SMALLER FINAL VALUE
  - IF THE LIQUIDITY EFFECT IS INSUFFICIENT, SHARP REDUCTION IN IR, THEN RECOVERY UP TO A HIGHER FINAL VALUE
  - IF THE LIQUIDITY EFFECT IS MARGINAL, PEOPLE ADAPT THEIR EXPECTATIONS ON INFLATION AND THE REDUCTION IN IR DOES NOT TAKE PLACE, AND FINAL IR ARE HIGHER IMMEDIATELY

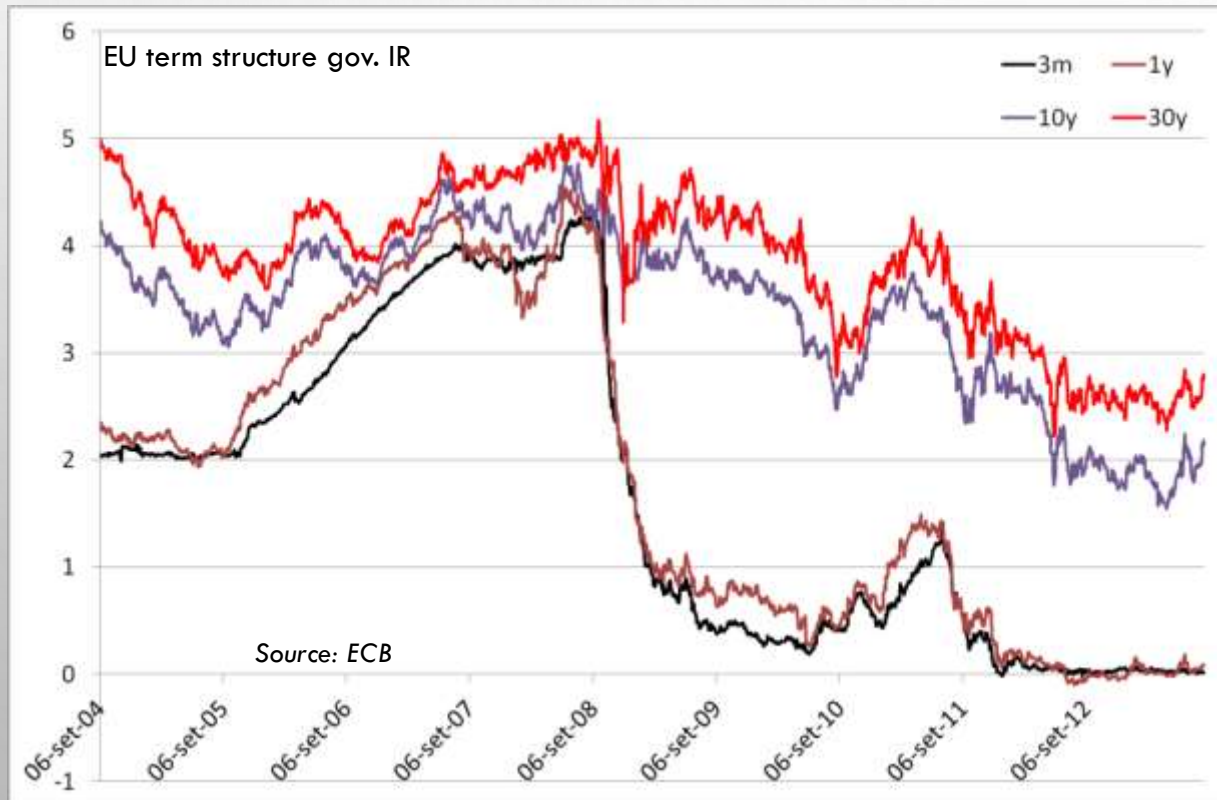




# THE YIELD CURVE

IR differ also based on bonds' maturity:

- Differences in IR can be plotted at different maturities to derive the **term structure of IR** (yield curve)
- Usually yield curves are upward-sloping, meaning that longer maturities are charged with higher IR
- Flat or even downward-sloping or inverted yield curves are rare



- Different maturities move similarly
- When short-term IR are high, inversion is more likely
- Inverted yield curves seem to anticipate recessions ('81, '91, 2000, '07), steep upward curves are associated with economic booms



# THE YIELD CURVE

Three theories for explaining the term structure of IR:

## Expectations theory

- If bonds at different maturities are perfect substitutes, their expected return must be equal
- $$(1 + i_{n,0})^n = (1 + i_{1,0})(1 + i_{1,1}^e) \cdot \dots \cdot (1 + i_{1,n-1}^e) \rightarrow i_{n,0} \approx \frac{i_{1,0} + i_{1,1}^e + \dots + i_{1,n-1}^e}{n}$$
- Predicts flat curves, whereas instead are usually upward-sloping (worked... until 1915)

## Market segmentation theory

- Bonds at different maturities are not substitutes and each has a specific market, as well as each investor has a preferred maturity
- Together with interest-rate risk aversion, explains why longer investments require a risk premium
- Does not explain why IR move together along time
- Does not explain why with high short-term IR inversion is more likely



# THE YIELD CURVE

## Liquidity premium theory

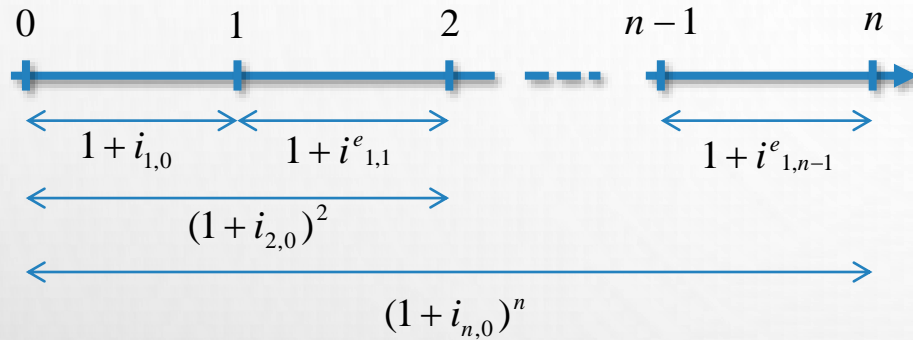
- Combines the other two in a comprehensive way
- Adds to expectations theory a liquidity premium for longer term bonds that is subject to market (demand, supply) conditions for that segment
- Bonds are substitutes as long as investors' preferences are compensated with a term (liquidity) premium that is always positive and grows as maturity gets longer
- $$i_{n,0} \approx \frac{i_{1,0} + i_{1,1}^e + \dots + i_{1,n-1}^e}{n} + l_{n,0}$$
- Explains inverted term structures: when future expectations on short-term IR are of a wide fall, so that their average is not balanced even by a positive liquidity premium (more likely when short-term rates are high)
- Support empirical evidence that:
  - Term structure is a predictor of business cycles and inflation
  - Term structure is less reliable for intermediate movements



# THE YIELD CURVE

## Forward and spot rates:

- Term structures allow to measure expected IR



- Expected future IR are forward rates, in contrast to spot rates
- Knowing spot IR we can derive market expectations

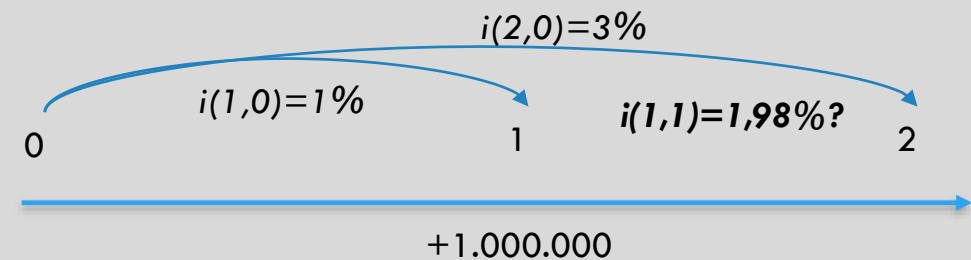
F.i.:  $i_{1,1}^e = \frac{(1 + i_{2,0})^2}{1 + i_{1,0}} - 1$       or, generalising:  $i_{1,k}^e = \frac{(1 + i_{k+1,0})^{k+1}}{(1 + i_{k,0})^k} - 1$

- Including liquidity premiums:

$$i_{1,k}^e = \frac{(1 + i_{k+1,0} - l_{k+1,0})^{k+1}}{(1 + i_{k,0} - l_{k,0})^k} - 1$$

## Can we gain from knowing the yield curve?

Imagine that, as a CFO, you know that you are going to receive 1 mln€ in 1 year. You also know that:  $i(1,0)=1\%$  and  $i(2,0)=3\%$  (biannual)



	0	1	2
Inflow		+ 1,000,000	
1. Loan	+990,099	-1,000,000	
2. Investment	-990,099		+1,019,802
NET RESULT	0	0	+1,019,802

# THE YIELD CURVE

