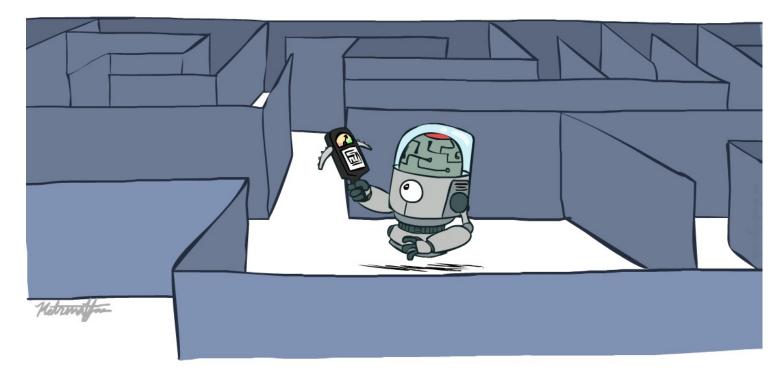
Introduction to Artificial Intelligence

Informed Search



Instructor: Laura Nenzi

University of Trieste, Italy

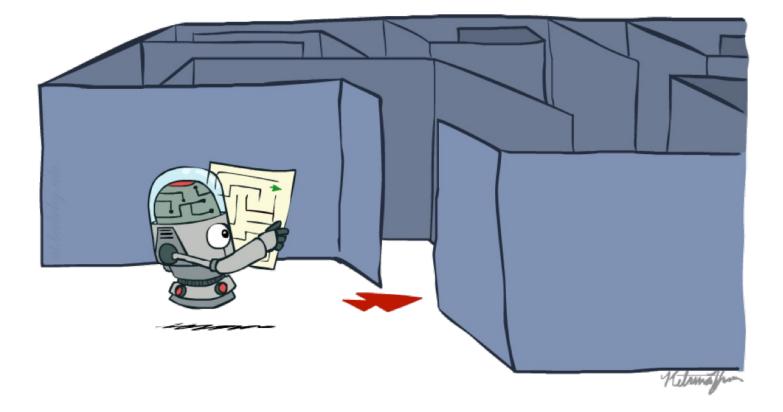
[slides adapted from Dan Klein, Pieter Abbeel, Stuart Russell, et al for CS188 Intro to AI at UC Berkeley. All materials available at http://ai.berkeley.edu.]

Today

- Informed Search
 - Heuristics
 - Greedy Search
 - A* Search



Recap: Search

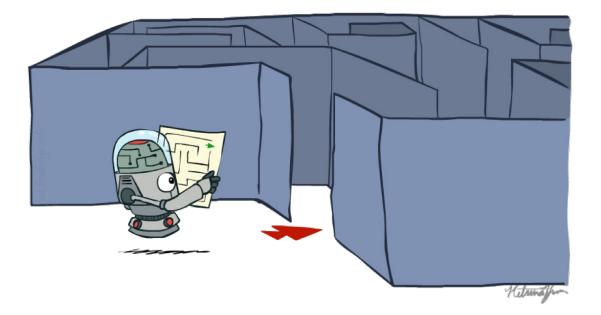


Recap: Search

- Search problem:
 - States (configurations of the world)
 - Actions and costs
 - Successor function (world dynamics)
 - Start state and goal test

Search tree:

- Nodes: represent plans for reaching states
- Plans have costs (sum of action costs)
- Search algorithm:
 - Systematically builds a search tree
 - Chooses an ordering of the fringe (unexplored nodes)
 - Optimal: finds least-cost plans



The One Queue

All these search algorithms are the same except for fringe strategies

- Conceptually, all fringes are priority queues (i.e. collections of nodes with attached priorities)
- Practically, for DFS and BFS, you can avoid the log(n) overhead from an actual priority queue, by using stacks and queues
- Can even code one implementation that takes a variable queuing object



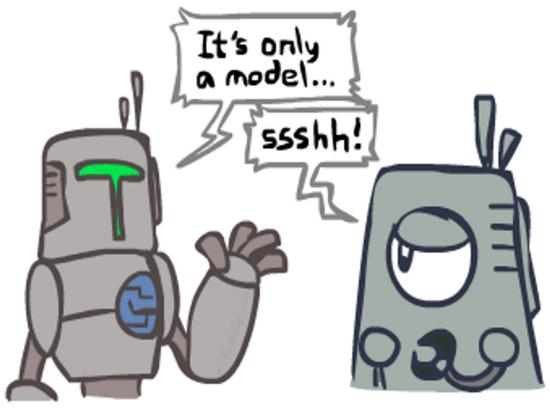
Search and Models

Search operates over models of the world

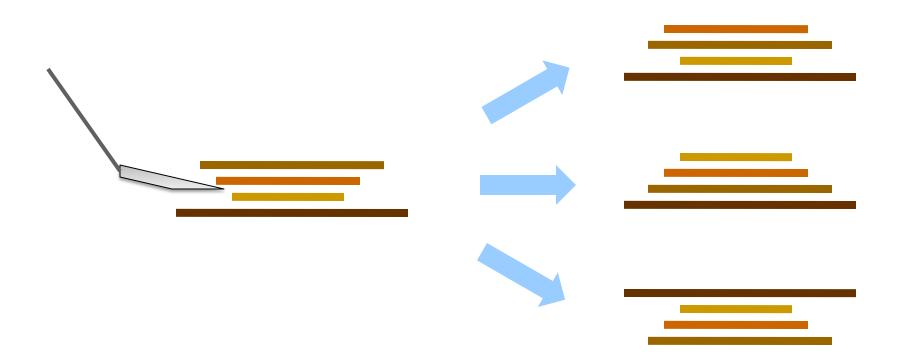
The agent doesn't actually try all the plans out in the real world!

Planning is all "in simulation"

Your search is only as good as your models...



Example: Pancake Problem



Cost: Number of pancakes flipped

Example: Pancake Problem

BOUNDS FOR SORTING BY PREFIX REVERSAL

William H. GATES

Microsoft, Albuquerque, New Mexico

Christos H. PAPADIMITRIOU*†

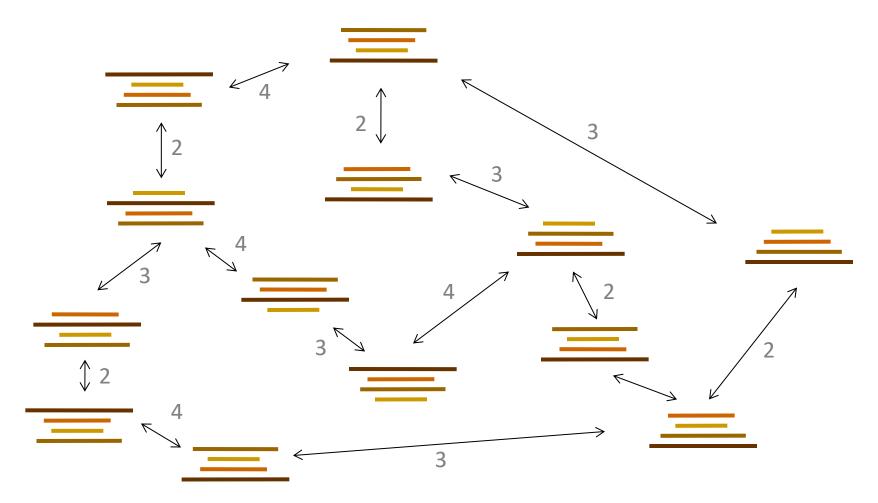
Department of Electrical Engineering, University of California, Berkeley, CA 94720, U.S.A.

Received 18 January 1978 Revised 28 August 1978

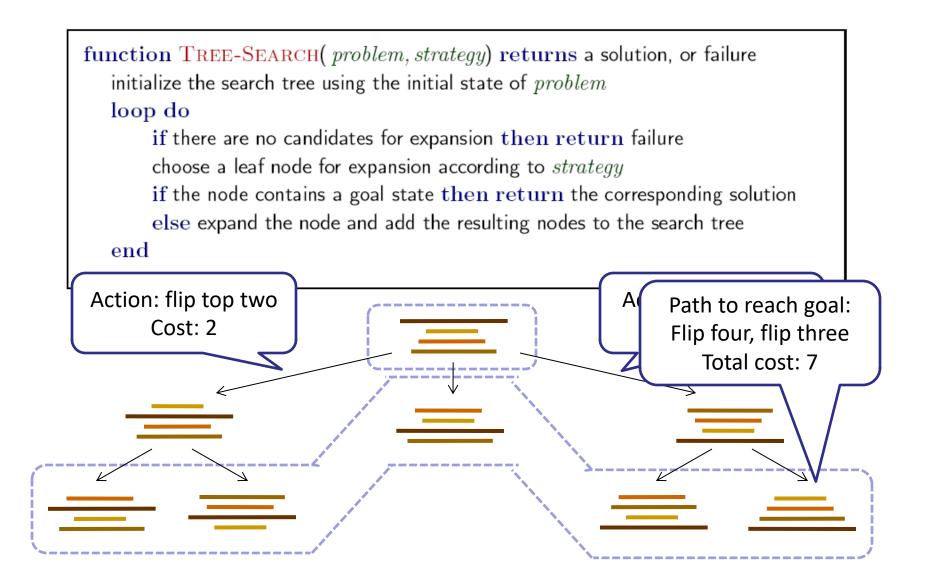
For a permutation σ of the integers from 1 to *n*, let $f(\sigma)$ be the smallest number of prefix reversals that will transform σ to the identity permutation, and let f(n) be the largest such $f(\sigma)$ for all σ in (the symmetric group) S_n . We show that $f(n) \leq (5n+5)/3$, and that $f(n) \geq 17n/16$ for *n* a multiple of 16. If, furthermore, each integer is required to participate in an even number of reversed prefixes, the corresponding function g(n) is shown to obey $3n/2 - 1 \leq g(n) \leq 2n + 3$.

Example: Pancake Problem

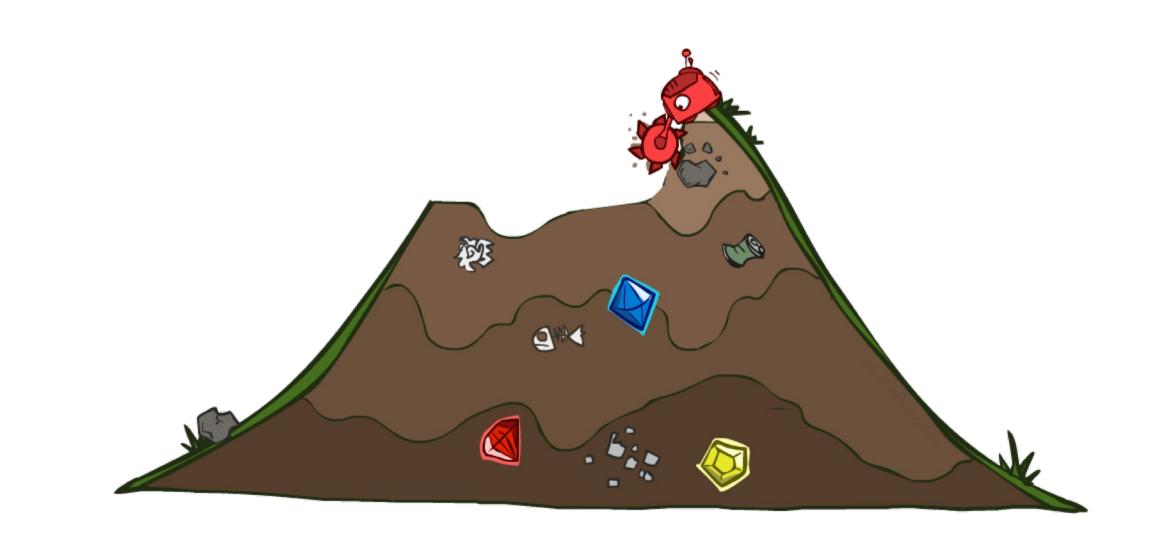
State space graph with costs as weights



General Tree Search



Uninformed Search

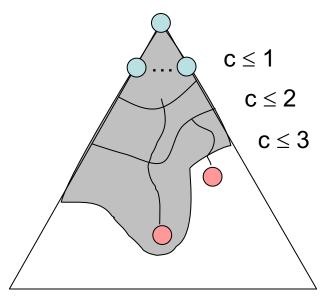


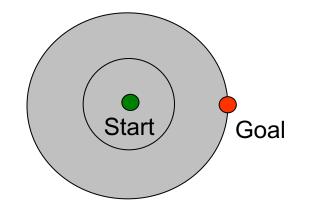
Uniform Cost Search

Strategy: expand lowest path cost

The good: UCS is complete and optimal!

- The bad:
 - Explores options in every "direction"
 - No information about goal location





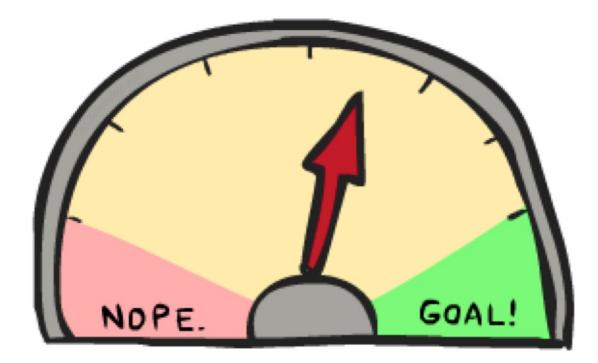
Video of Demo Contours UCS Empty



Video of Demo Contours UCS Pacman Small Maze

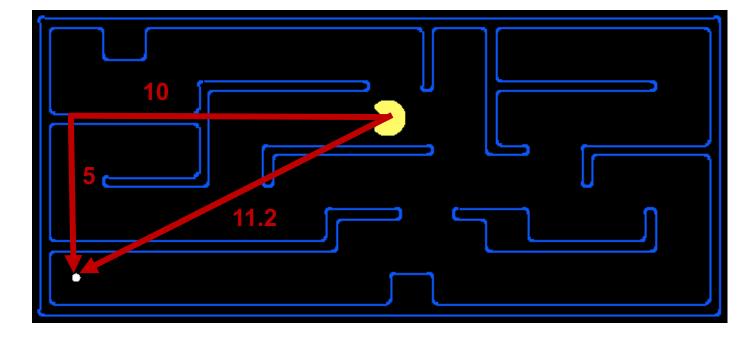


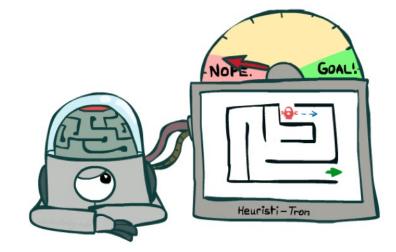
Informed Search

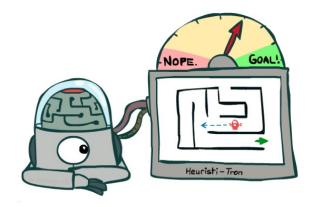


Search Heuristics

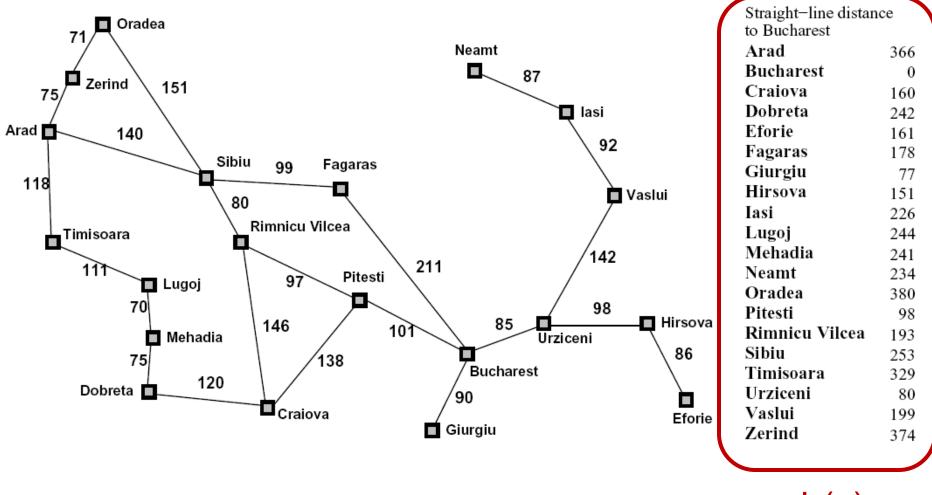
- An heuristic function h(n):
 - *Estimates* how close a state *n* is to a goal
 - Designed for a particular search problem
 - Examples: Manhattan distance, Euclidean distance for pathing







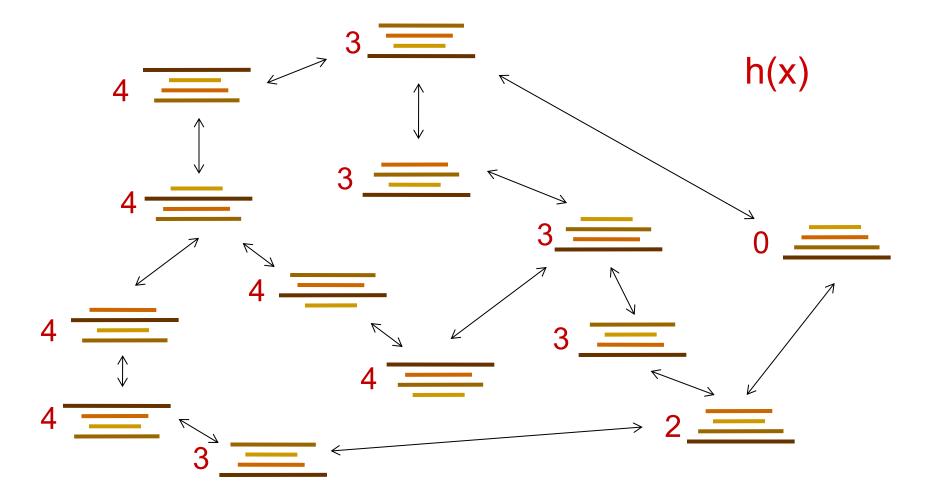
Example: Heuristic Function



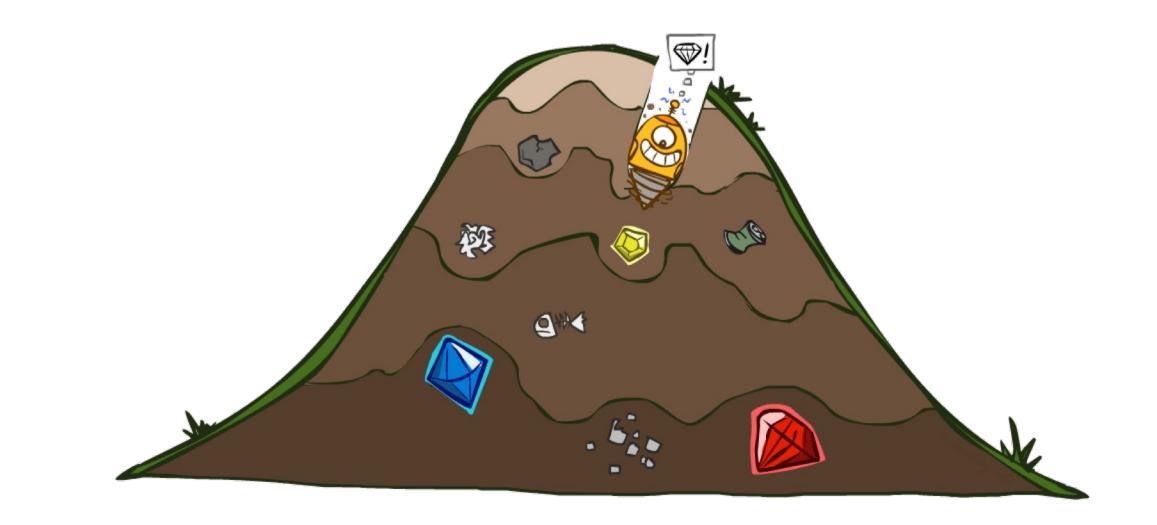
h(x)

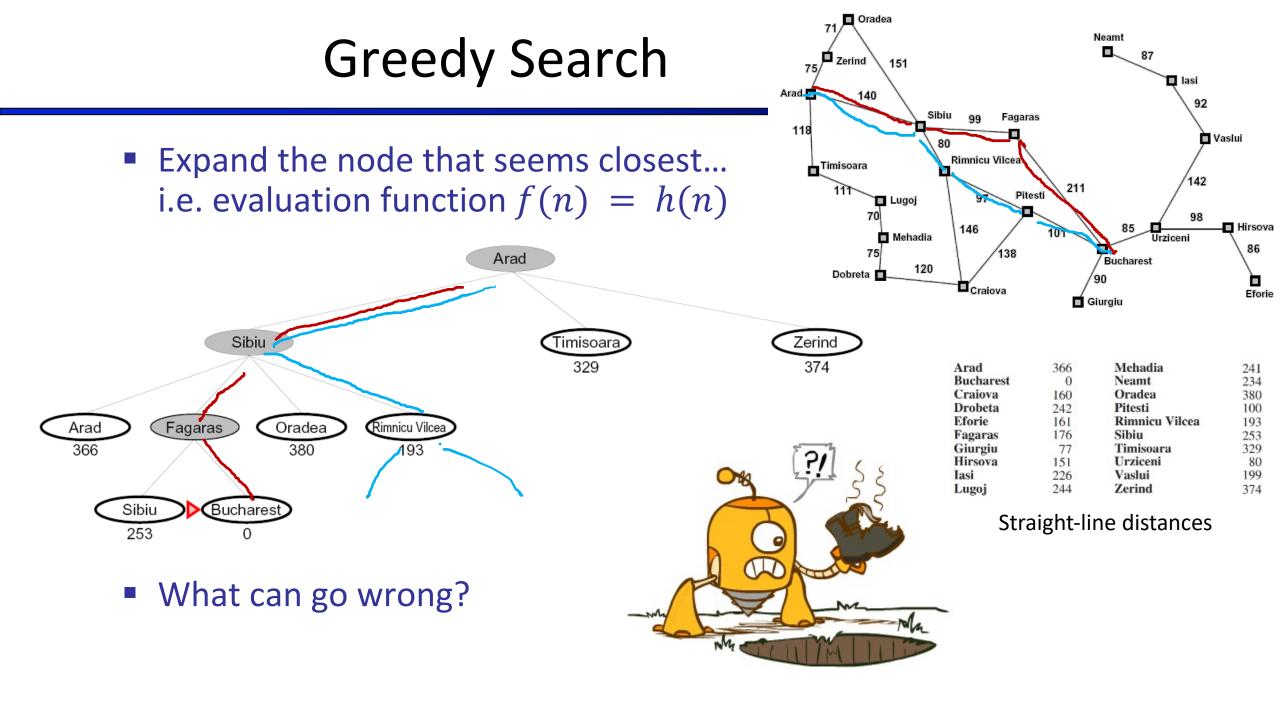
Example: Heuristic Function

Heuristic: the number of the largest pancake that is still out of place



Greedy Search

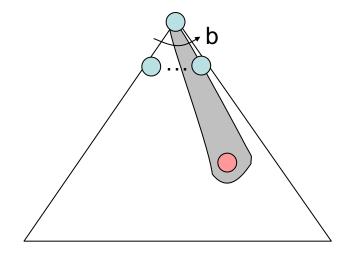


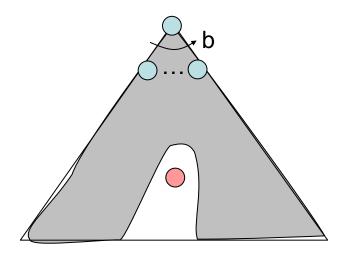


Greedy Search

- Strategy: expand a node that you think is closest to a goal state
 - Heuristic: estimate of distance to nearest goal for each state
- A common case:
 - Best-first takes you straight to the (wrong) goal

Worst-case: like a badly-guided DFS





Video of Demo Contours Greedy (Empty)



Video of Demo Contours Greedy (Pacman Small Maze)



A* Search



A* Search





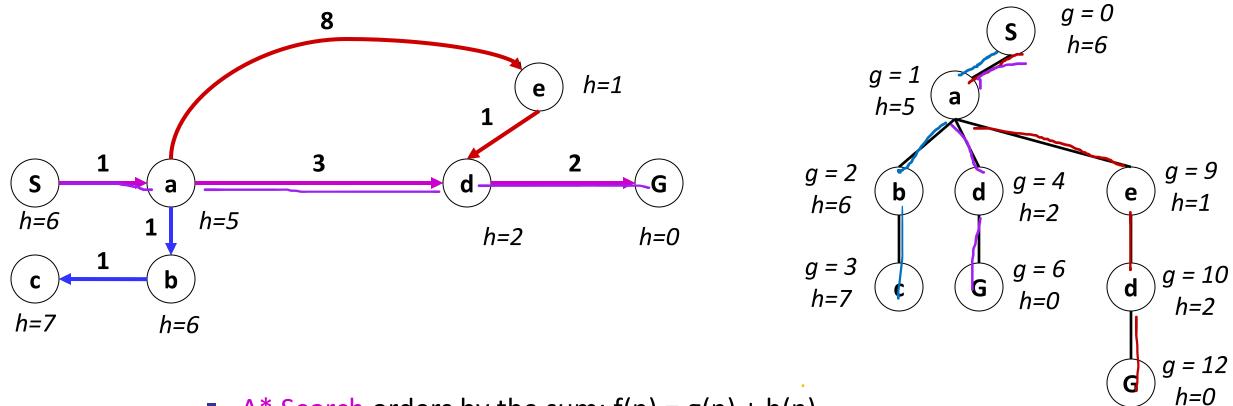
UCS

Greedy



Combining UCS and Greedy

- Uniform-cost orders by path cost, or backward cost g(n)
- Greedy orders by goal proximity, or *forward cost* h(n)

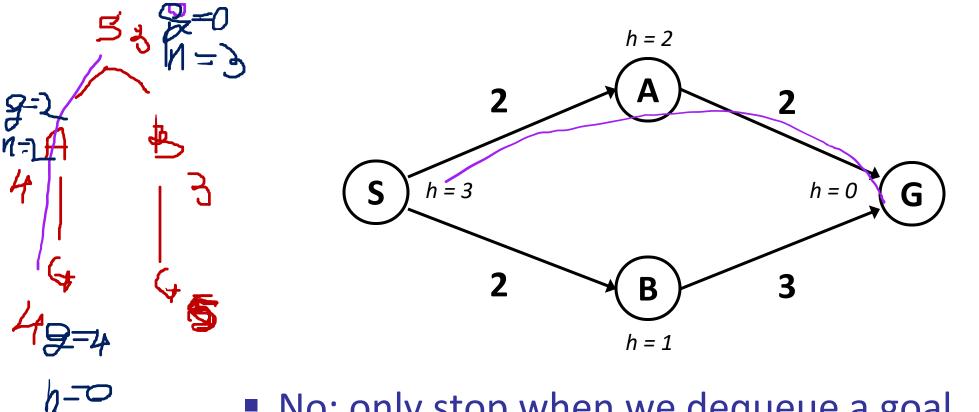


A* Search orders by the sum: f(n) = g(n) + h(n)

Example: Teg Grenager

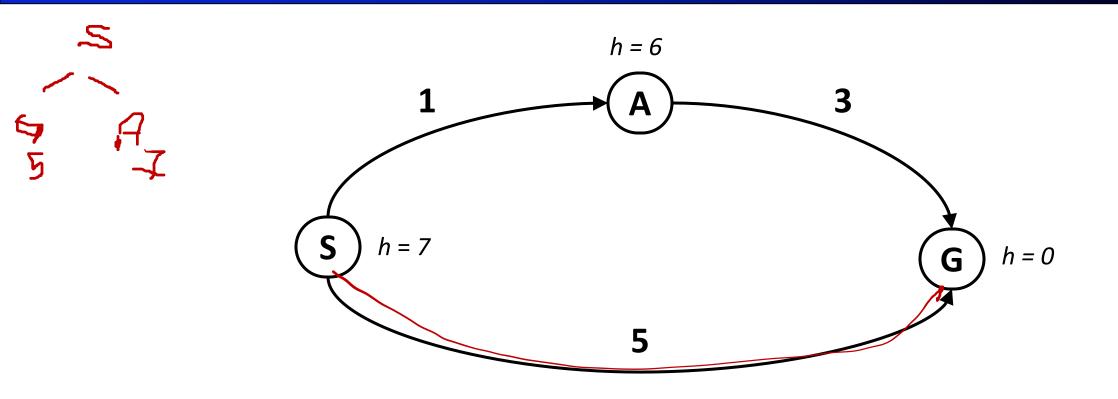
When should A* terminate?

Should we stop when we enqueue a goal?



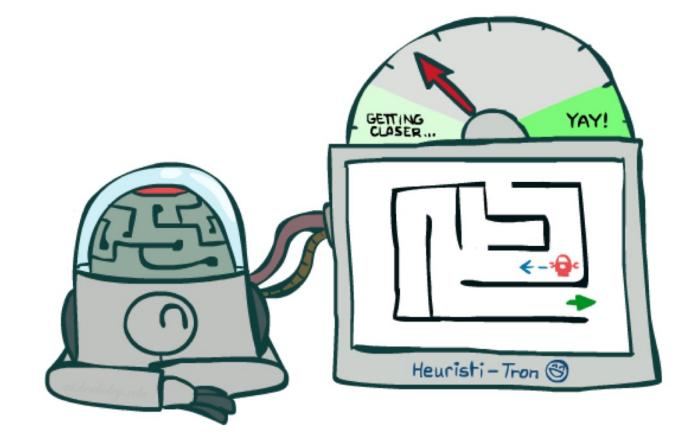
No: only stop when we dequeue a goal

Is A* Optimal?

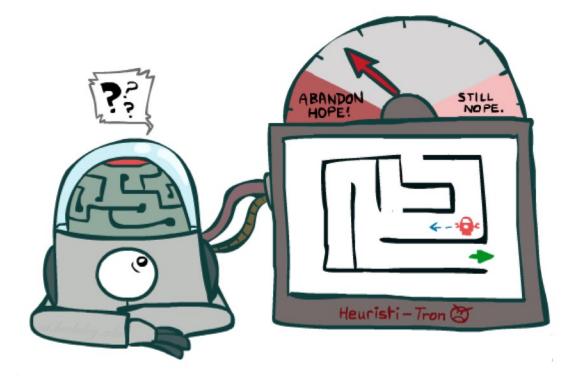


- What went wrong?
- Actual bad goal cost < estimated good goal cost</p>
- We need estimates to be less than actual costs!

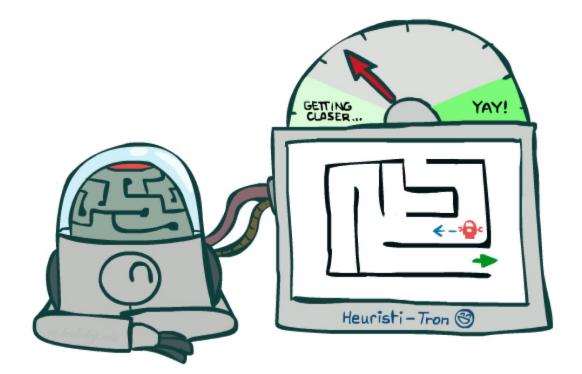
Admissible Heuristics



Idea: Admissibility



Inadmissible (pessimistic) heuristics break optimality by trapping good plans on the fringe



Admissible (optimistic) heuristics slow down bad plans but never outweigh true costs

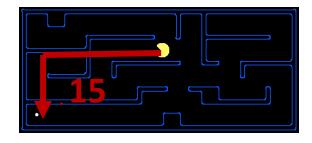
Admissible Heuristics

A heuristic *h* is *admissible* (optimistic) if:

 $0 \le h(n) \le h^*(n)$

where $h^*(n)$ is the true cost to a nearest goal

Examples:



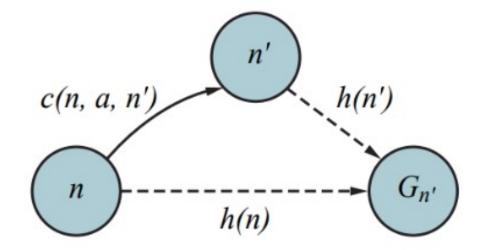


 Coming up with admissible heuristics is most of what's involved in using A* in practice.

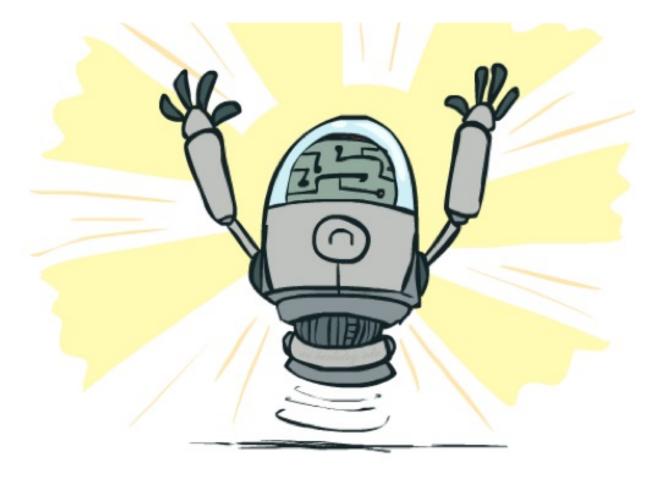
Consistent Heuristics

A heuristic h is consistent if, for every node n and every successor n' of n generated by an action a, we have:

$$h(n) \leq c(n, a, n') + h(n')$$



Optimality of A* Tree Search



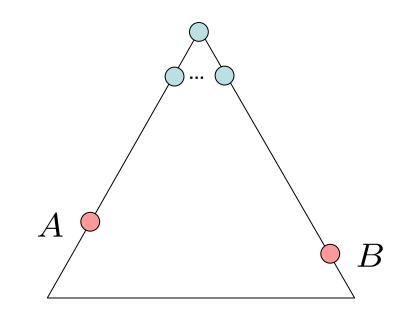
Optimality of A* Tree Search

Assume:

- A is an optimal goal node
- B is a suboptimal goal node
- h is admissible

Claim:

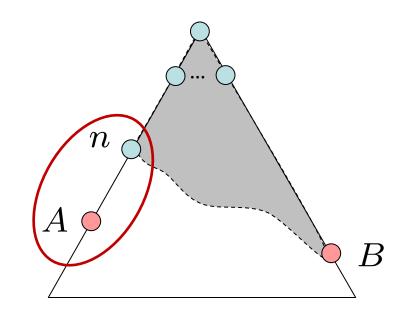
A will exit the fringe before B



Optimality of A* Tree Search: Blocking

Proof:

- Imagine B is on the fringe
- Some ancestor *n* of A is on the fringe, too (maybe A!)
- Claim: n will be expanded before B
 1. f(n) ≤ f(A)



Optimality of A* Tree Search: Blocking

B

1. $f(n) \leq f(A)$

- Definition of f-cost says: f(n) = g(n) + h(n) = (path cost to n) + (est. cost of n to A) f(A) = g(A) + h(A) = (path cost to A) + (est. cost of A to A)
- The admissible heuristic must underestimate the true cost h(A) = (est. cost of A to A) = 0
- So now, we have to compare:

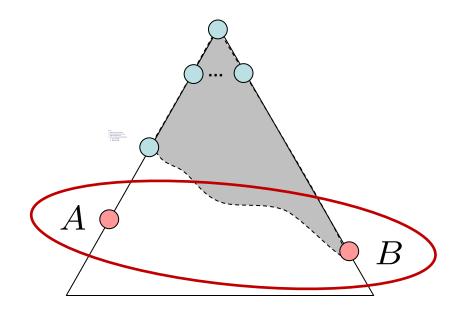
f(n) = g(n) + h(n)f(A) = g(A)

h(n) must be an underestimate of the true cost from n to A
 g(n) + h(n) ≤ g(A)
 f(n) ≤ f(A)

Optimality of A* Tree Search: Blocking

Proof:

- Imagine B is on the fringe
- Some ancestor *n* of A is on the fringe, too (maybe A!)
- Claim: n will be expanded before B
 - 1. $f(n) \le f(A)$ 2. $f(A) \le f(B)$



Optimality of A* Tree Search: Blocking

B

2. $f(A) \leq f(B)$

We know that:

f(A) = g(A) + h(A) = (path cost to A) + (est. cost of A to A)f(B) = g(B) + h(B) = (path cost to B) + (est. cost of B to B)

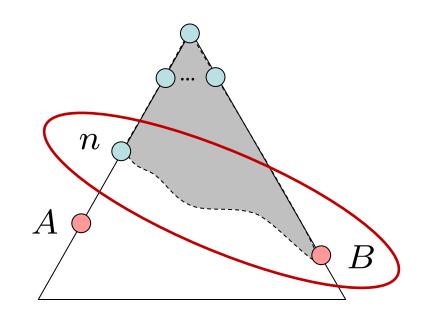
- The heuristic must underestimate the true cost:
 h(A) = h(B) = 0
- So now, we have to compare:
 f(A) = g(A)
 f(B) = g(B)
- We assumed that B is suboptimal! So

g(A) < g(B)f(A) < f(B)

Optimality of A* Tree Search: Blocking

Proof:

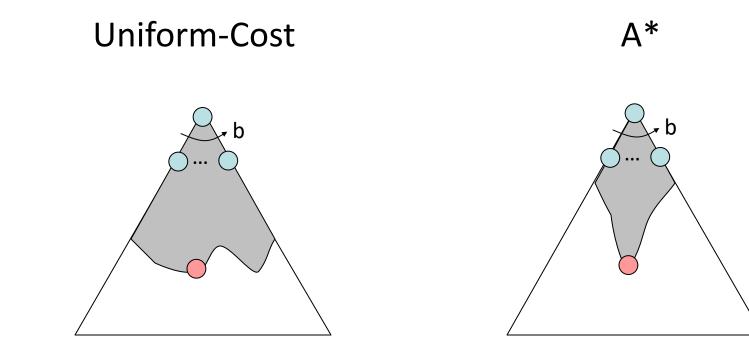
- Imagine B is on the fringe
- Some ancestor n of A is on the fringe, too (maybe A!)
- Claim: n will be expanded before B
 - 1. $f(n) \leq f(A)$
 - 2. f(A) < f(B)
 - 3. n expands before B —
- All ancestors of A expand before B
- A expands before B
- A* search is optimal



 $f(n) \le f(A) < f(B)$

Properties of A*

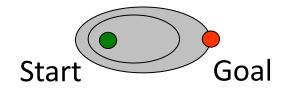
Properties of A*

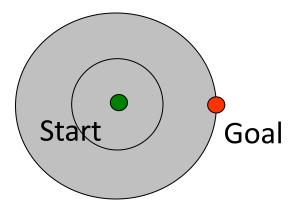


UCS vs A* Contours

 Uniform-cost expands equally in all "directions"

 A* expands mainly toward the goal, but does hedge its bets to ensure optimality





Video of Demo Contours (Empty) -- UCS



Video of Demo Contours (Empty) -- Greedy



Video of Demo Contours (Empty) – A*



Video of Demo Contours (Pacman Small Maze) – A*



Comparison



Greedy

Uniform Cost

A* Applications



A* Applications

- Video games
- Pathing / routing problems
- Resource planning problems
- Robot motion planning
- Language analysis



Video of Demo Pacman (Tiny Maze) – UCS / A*

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Video of Demo Empty Water Shallow/Deep – Guess Algorithm

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