

# 272SM: Introduction to Artificial Intelligence

## Homework Assignment: CSPs

Monday 27<sup>th</sup> March, 2023 - Thursday 25<sup>th</sup> May, 2023

### Instructions

Report your answers to the following exercises and submit them at any time before the exam. Submitting homework solutions is highly recommended; Correct solutions will be counted as bonus points towards the final grade.

### 1 Exercise 1: Formulating a CSP

Suppose you have a state-space search problem defined by the usual stuff:

- a set of states  $s$ ;
- an initial state  $s_0$ ;
- a set of actions  $A$  including the NoOp action that has no effect;
- a transition model  $\text{Result}(s, a)$ ;
- a set of goal states  $G$ .

Unfortunately, you have no search algorithms! All you have is a CSP solver. How could you reformulate this as a CSP? You may assume that you are given the maximum number of steps,  $T$  that any plan can have. Make sure that your formulation makes it easy to see what the plan is.

### 2 Exercise 2: Algorithmic map coloring - Performance analysis

Generate random instances of map-coloring problems as follows: scatter  $n$  points on the unit square; select a point  $X$  at random, connect  $X$  by a straight line to the nearest point  $Y$  such that  $X$  is not already connected to  $Y$  and the line crosses no other line; repeat the previous step until no more connections are possible. The points represent regions on the map and the lines connect neighbors. Now try to find  $k$ -colorings of each map, for both  $k=3$  and  $k=4$ , using min-conflicts, backtracking, backtracking with forward checking, and backtracking with arc consistency. Construct a table of average run times for each algorithm for values of  $n$  up to the largest you can manage. Comment on your results.

### 3 Exercise 3: Critical ratio

Using a CSP solver program and another program to generate random problem instances of CSPs, report on the time to solve the problem as a function of the ratio of the number of constraints to the number of variables.