

# Diffusion Imaging

102 THE ANATOMICAL RECORD (NEW ANAT.) 257:102-109, 1999

FEATURE ARTICLE

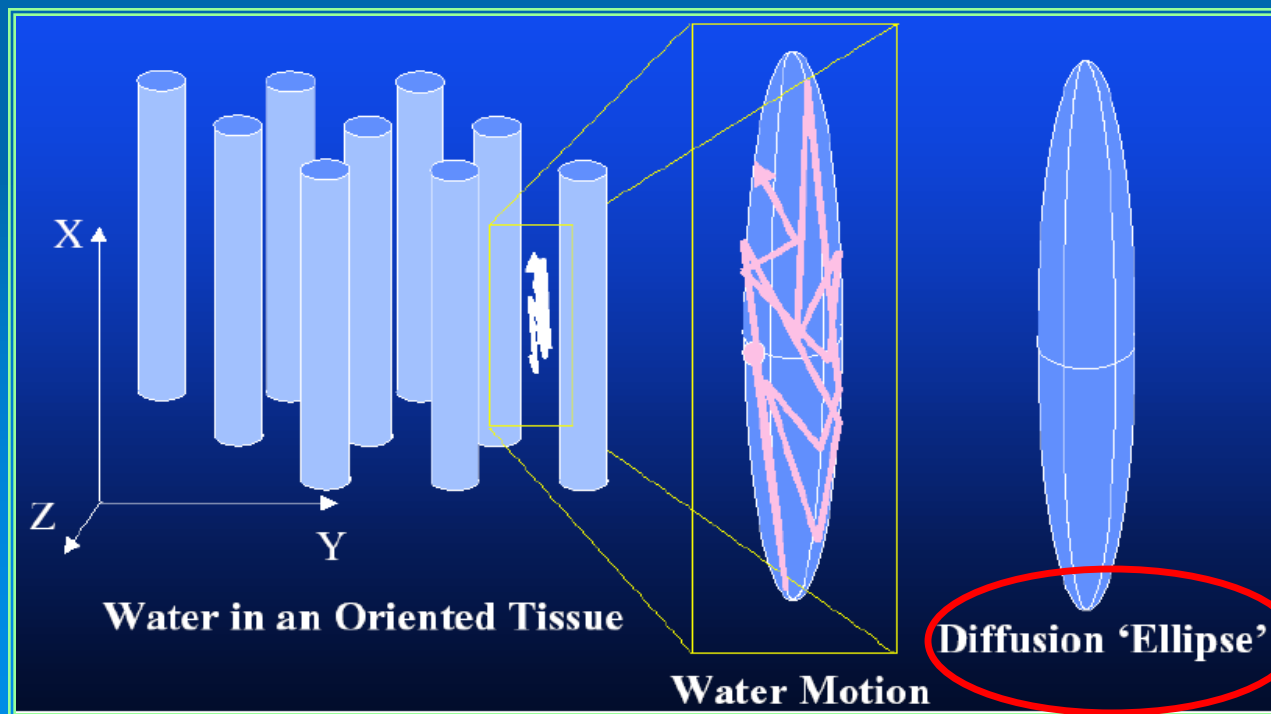
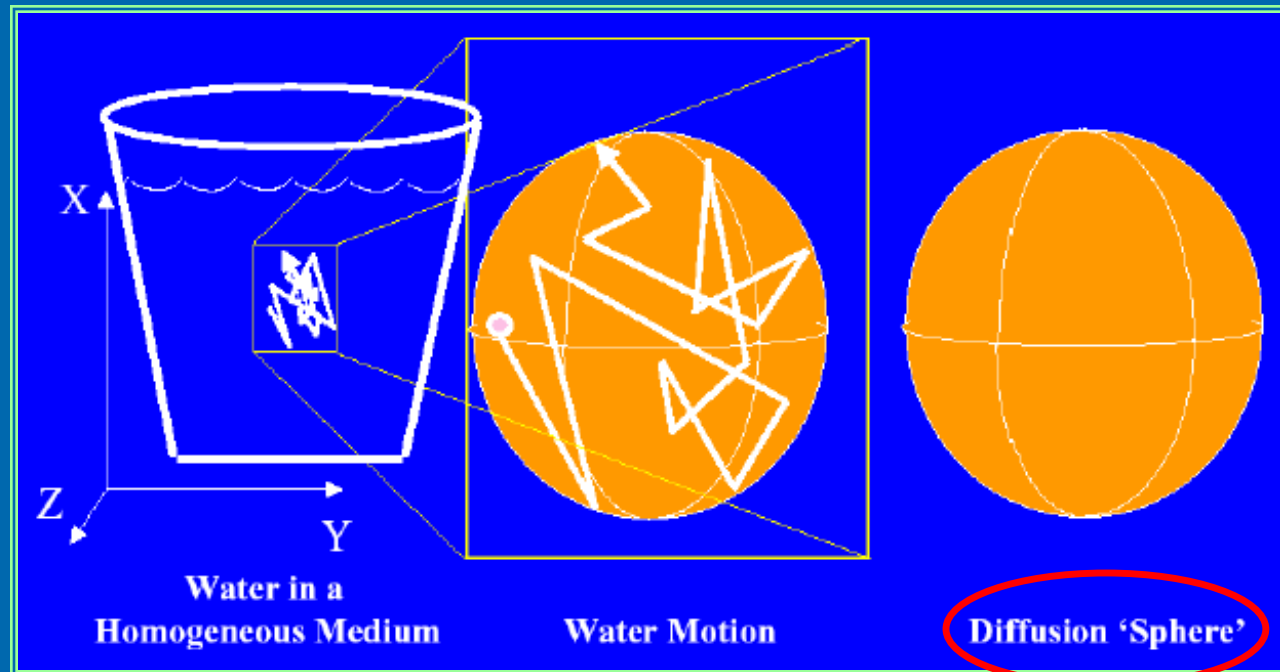
## Diffusion Magnetic Resonance Imaging: Its Principle and Applications

SUSUMU MORI\* AND PETER B. BARKER

Diffusion magnetic resonance imaging (MRI) is one of the most rapidly evolving techniques in the MRI field. This method exploits the random diffusional motion of water molecules, which has intriguing properties depending on the physiological and anatomical environment of the organisms studied. We explain the principles of this emerging technique and subsequently introduce some of its present applications to neuroimaging, namely detection of ischemic stroke and reconstruction of axonal bundles and myelin fibers. *Anat Rec (New Anat) 257:102-109, 1999.*

# Water diffusion:

- \* Thermal energy
- \* Brownian motion



Water in a inhomogeneous medium

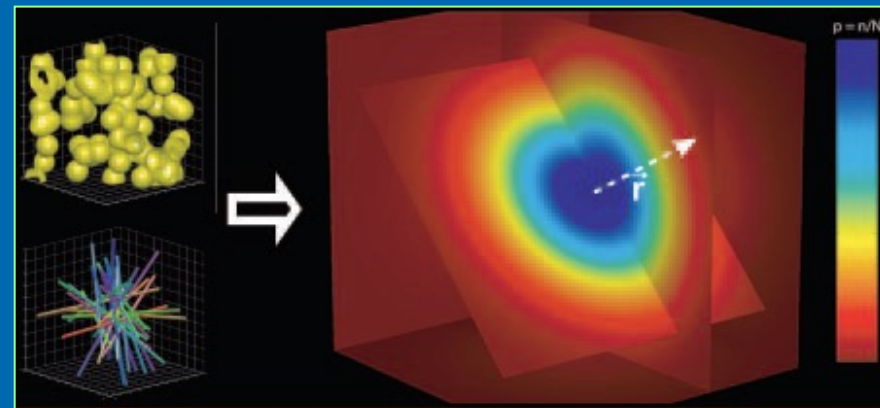
# 3D diffusion probability distributions

In a voxel that contains

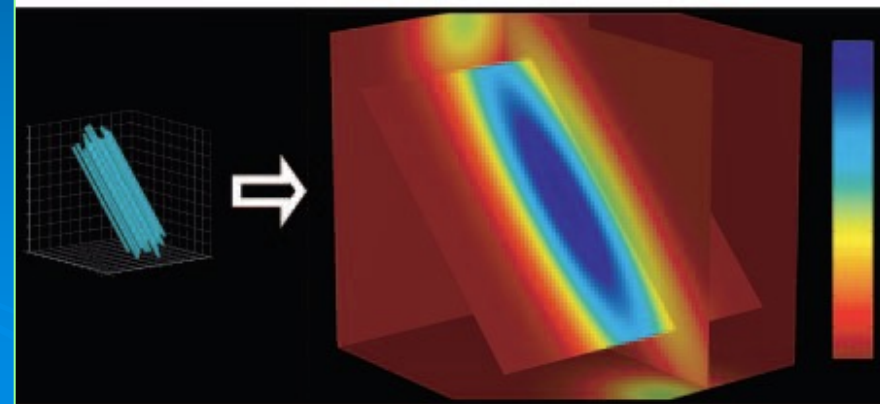
a) spherical cells or randomly oriented tubular structures, such as axons

b) all the axons are aligned in the same direction

- ✓ The displacement distribution is cigar shaped and aligned with the axons.



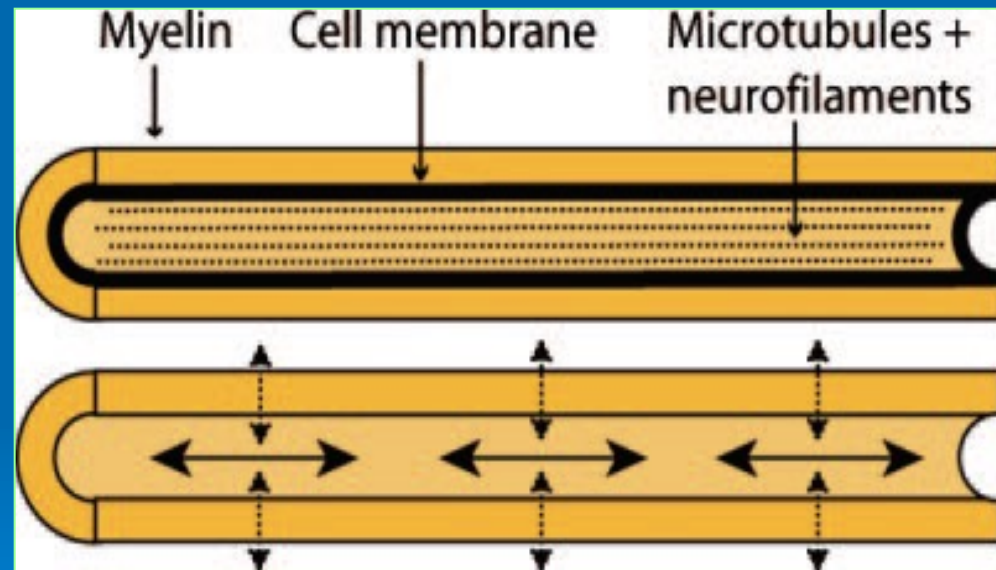
a.



b.

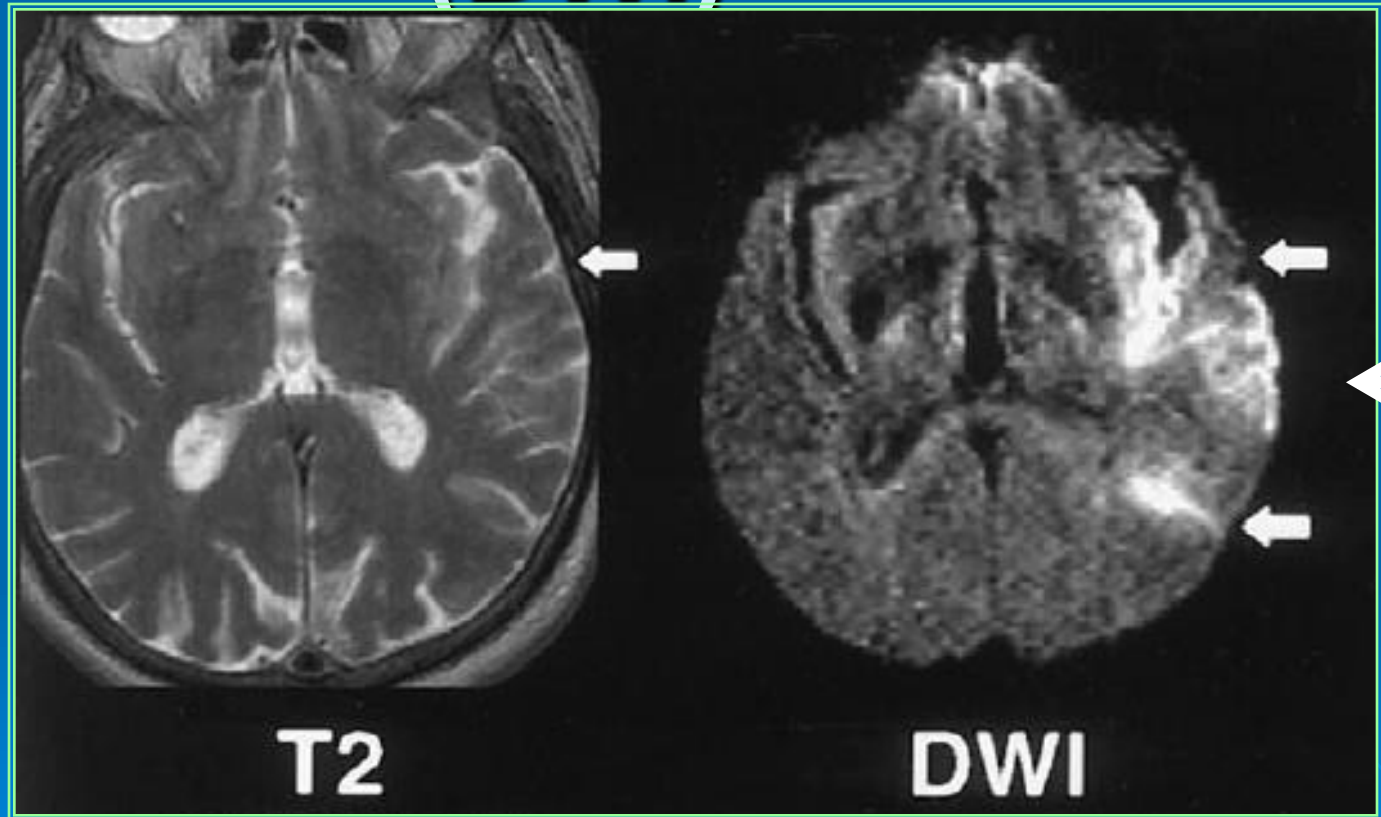
# Cellular elements and diffusion anisotropy

- Neuronal tissue consists of tightly packed and coherently aligned axons
  - surrounded by glial cells
  - Often organized in bundles
- The movements of water molecules are hindered in a direction perpendicular to the axonal orientation



*Hagmann P. et al  
RadioGraphics 2006; 26:S205–S223*

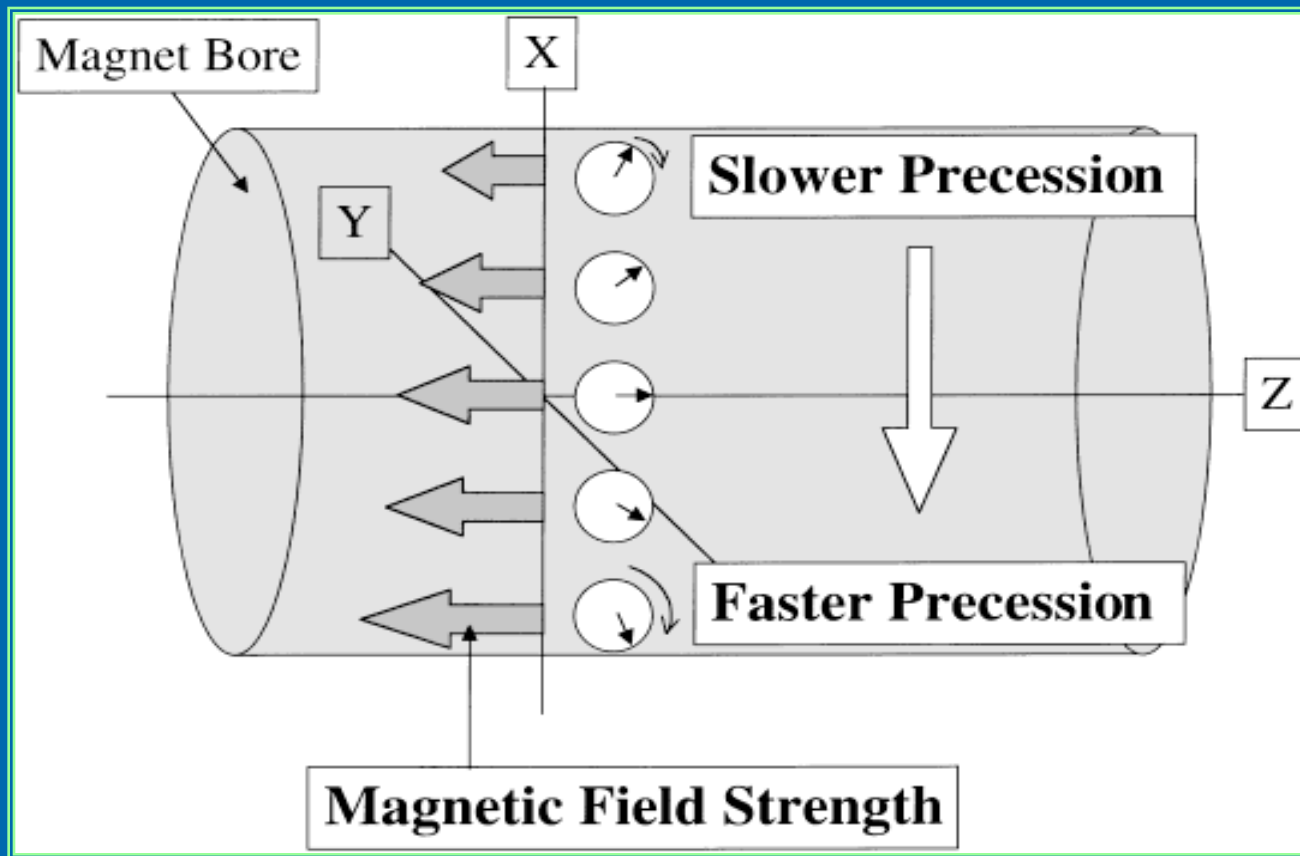
# Diffusion weighted imaging (DWI)



Ischemic  
stroke early  
diagnosis

Diffusion weighting enables one to distinguish between rapid diffusion of protons (unrestricted diffusion) and slow diffusion of protons (restricted diffusion)

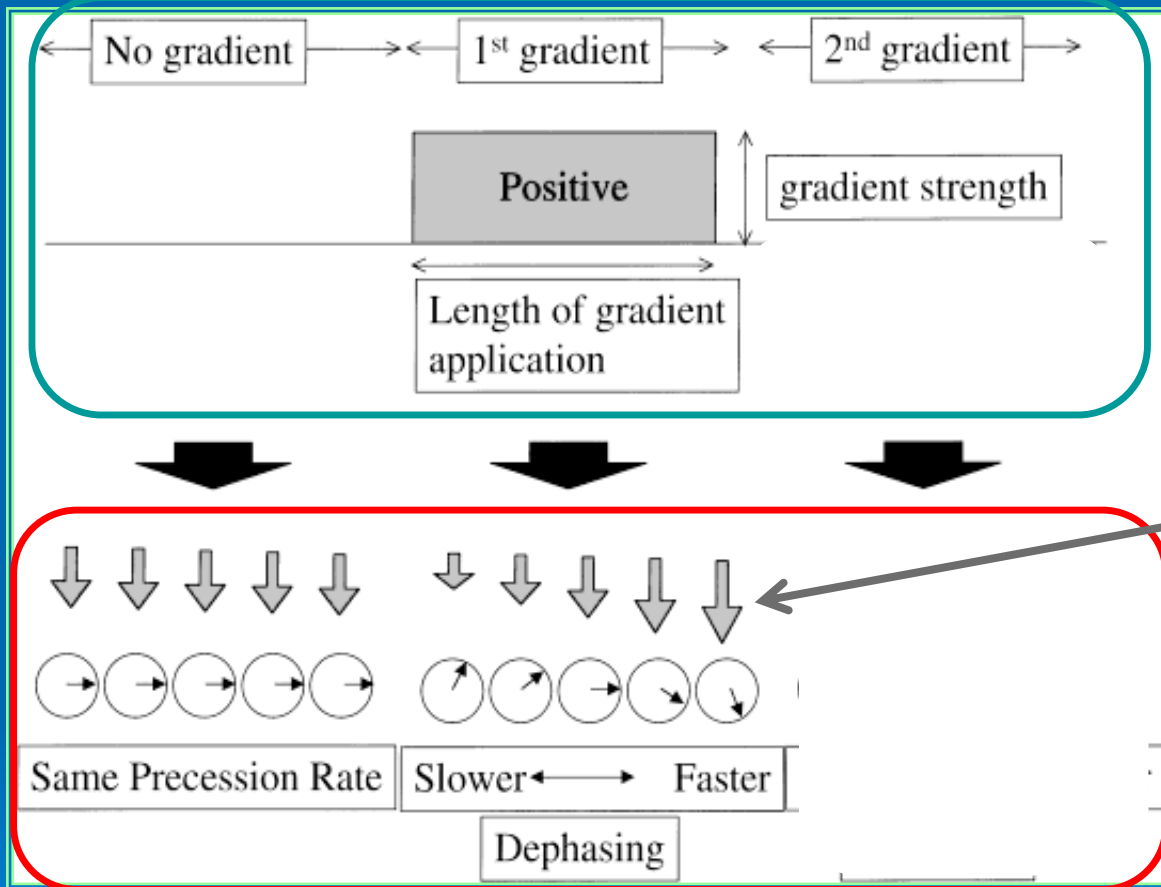
# Gradients and spin phase



## *An example of an x-gradient*

- Gradient units introduce linear magnetic field inhomogeneity
- Due to gradients, the Larmor frequency vary in the sample depending on the position of the protons

# Gradients and phase

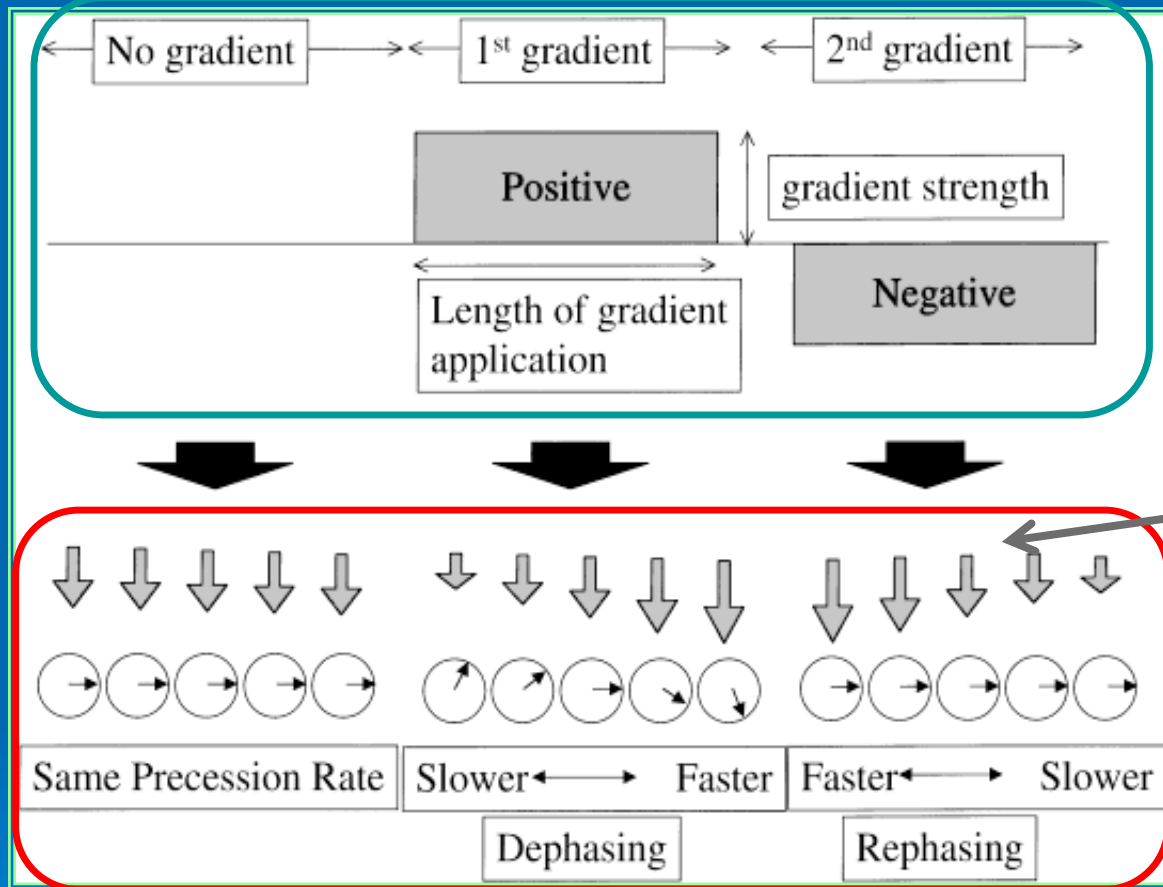


Gradient diagram (upper row) and signal phases (lower row) under application of a gradient.

The length of gray arrows indicates the strength of the magnetic field that is non-uniform during the application of the gradients.

- After the 1<sup>st</sup> gradient application, signals lose their uniform phase because each proton starts to precess at different rates depending on its position in space

# Gradients and phase



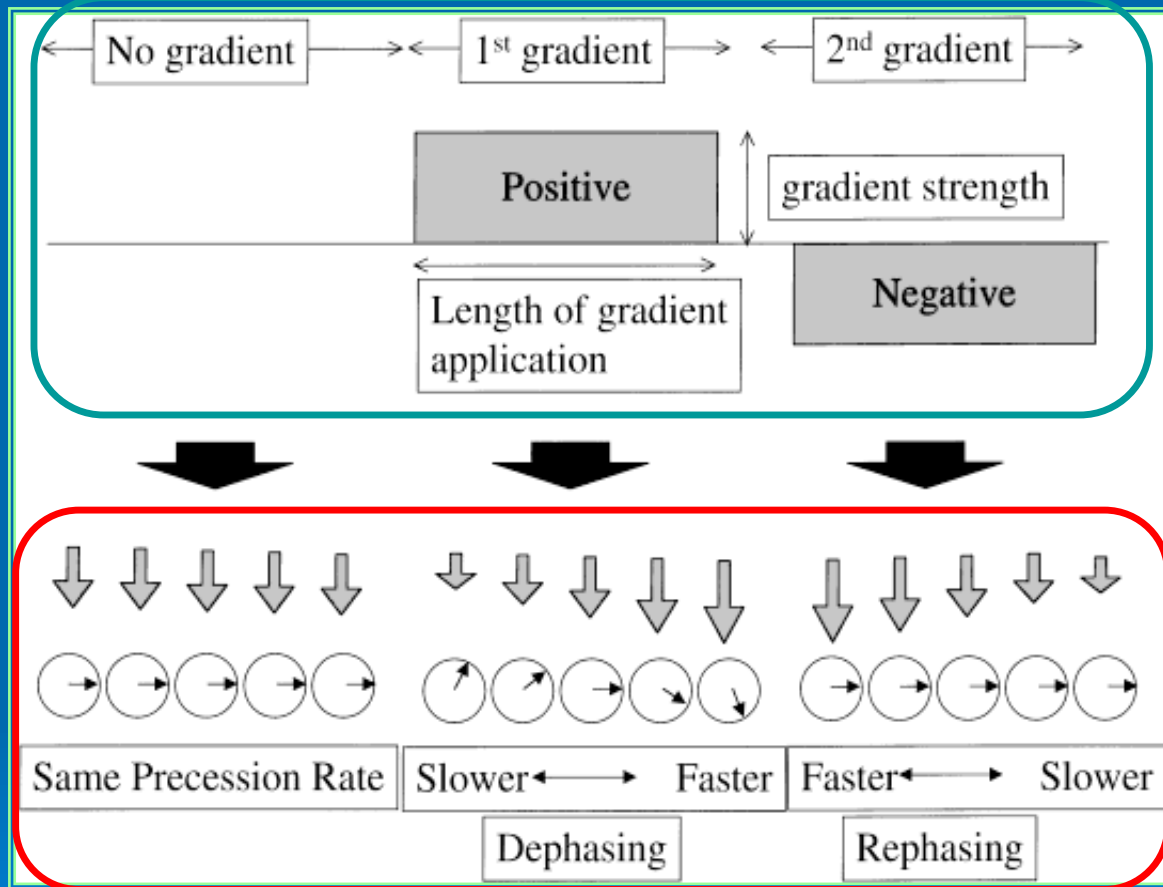
Gradient diagram (upper row) and signal phases (lower row) under application of a gradient.

The length of gray arrows indicates the strength of the magnetic field that is non-uniform during the application of the gradients.

- After the 2<sup>nd</sup> gradient application of opposite magnitude, the system restores uniform phase.



# Gradients and phase

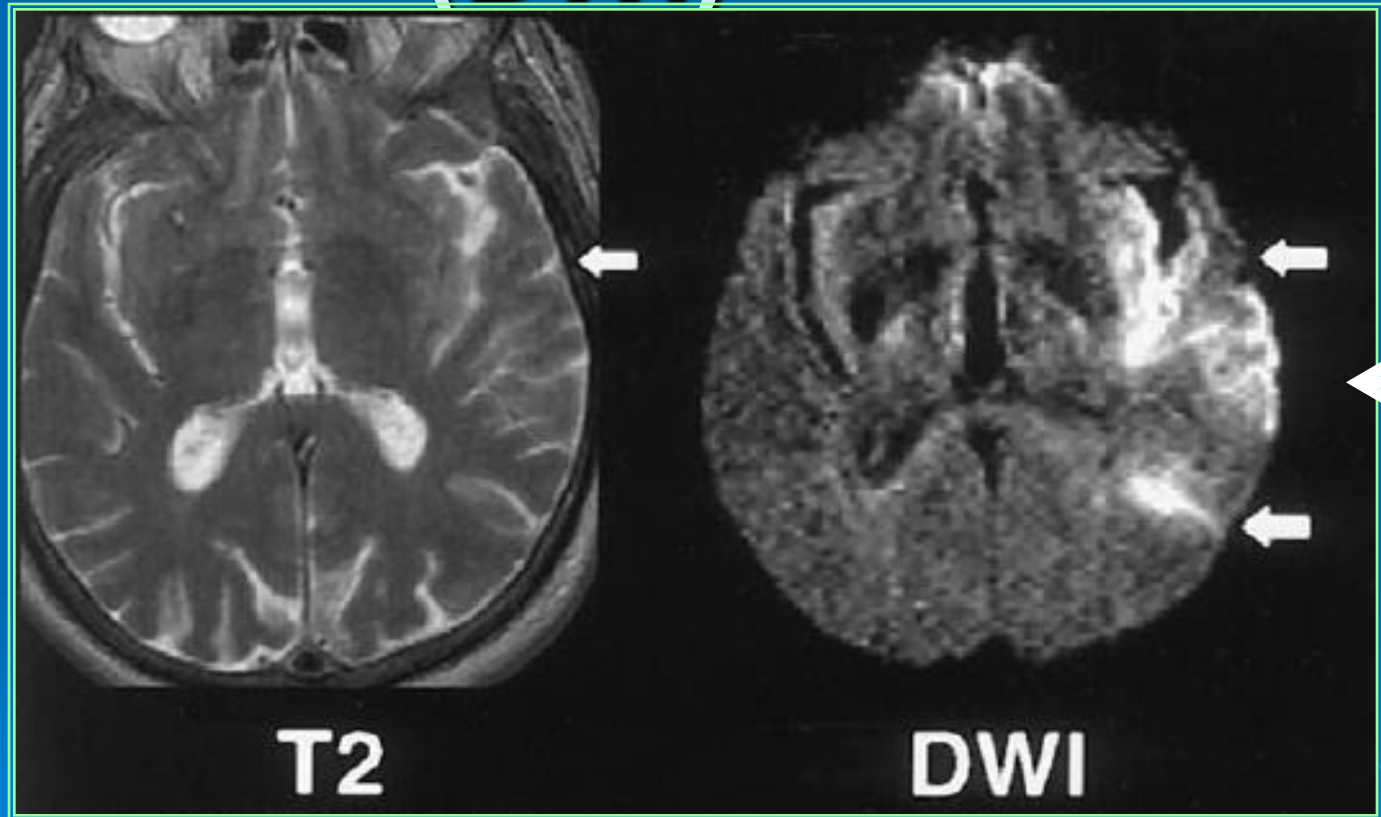


The rephasing is complete only when spins do not move by Brownian motion during the time in between the two applications of the gradient

Less complete the rephasing: More signal loss

- After the 2<sup>nd</sup> gradient application of opposite magnitude, the system restores uniform phase.

# Diffusion weighted imaging (DWI)



Ischemic stroke early diagnosis

Diffusion weighting enables one to distinguish between rapid diffusion of protons (unrestricted diffusion) and slow diffusion of protons (restricted diffusion)

# Diffusion gradients

The diffusional signal loss by the gradient application obeys the following equation

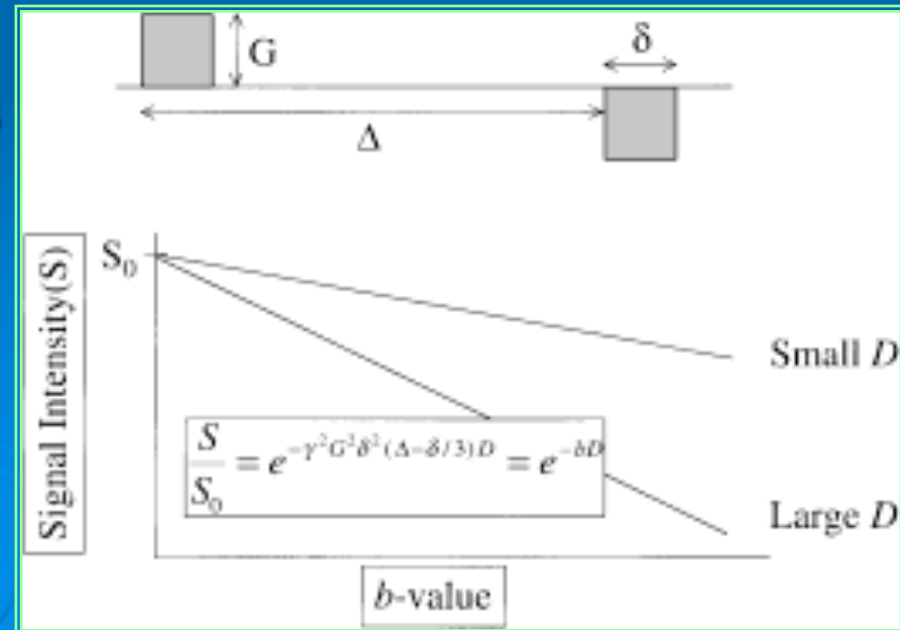
$$\frac{S}{S_0} = e^{-bD}$$

where  $S_0$  is the signal intensity without the diffusion weighting (no gradient application) and  $S$  is the signal with the gradient application.

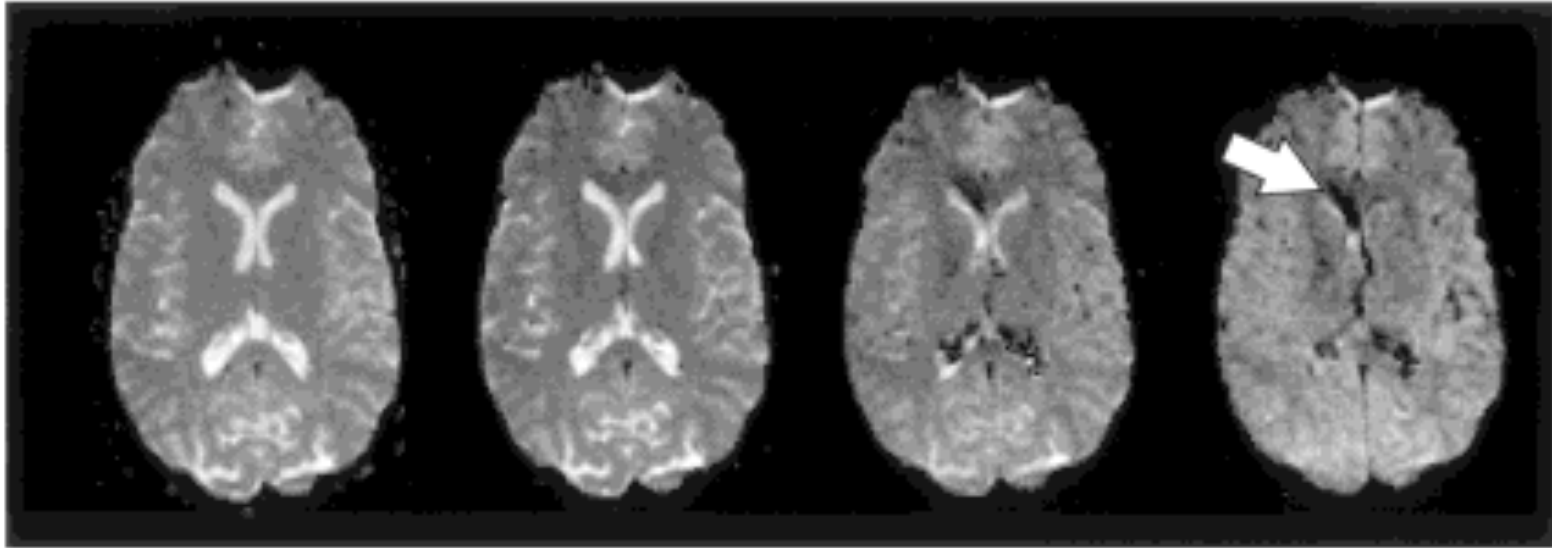
- $D$  is the diffusion constant
  - tissue dependent
- $b$  depends from the gradients
  - Operator dependent

Relationship between gradient application, signal loss, and diffusion constant ( $D$ ).

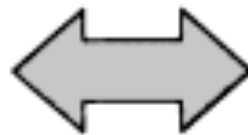
When  $b$  value is plotted against the log of the signal decay, the slope represents the diffusion constant.



# Diffusion Weighted Images



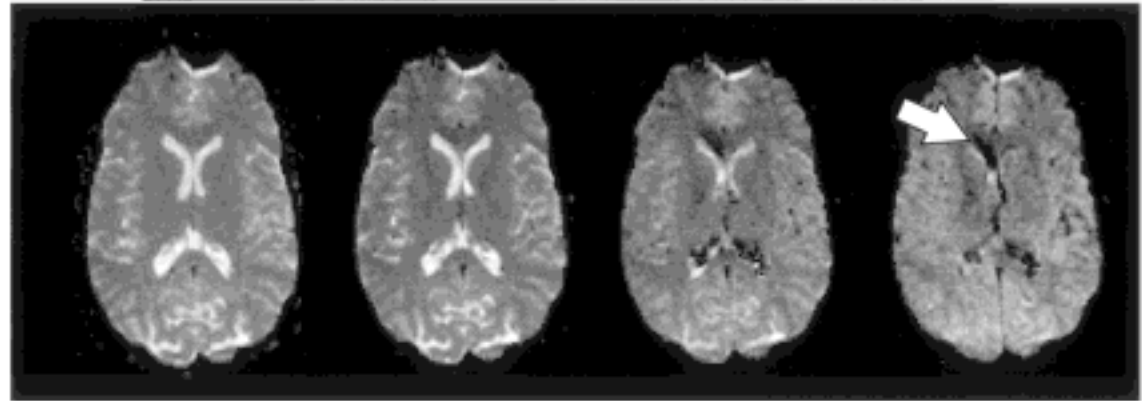
Small  $b$ -value  
(less dif.-weight)



Large  $b$ -value  
(more dif.-weight)

**More diffusion weight less signal from CSF**

## Diffusion Weighted Images

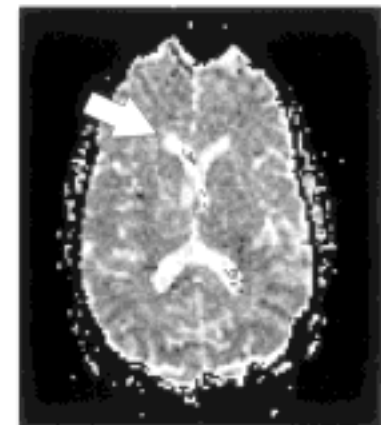


Small  $b$ -value  
(less dif.-weight)



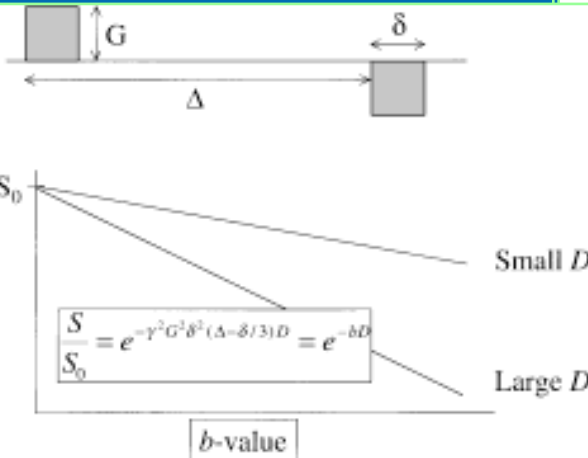
Large  $b$ -value  
(more dif.-weight)

## ADC Image

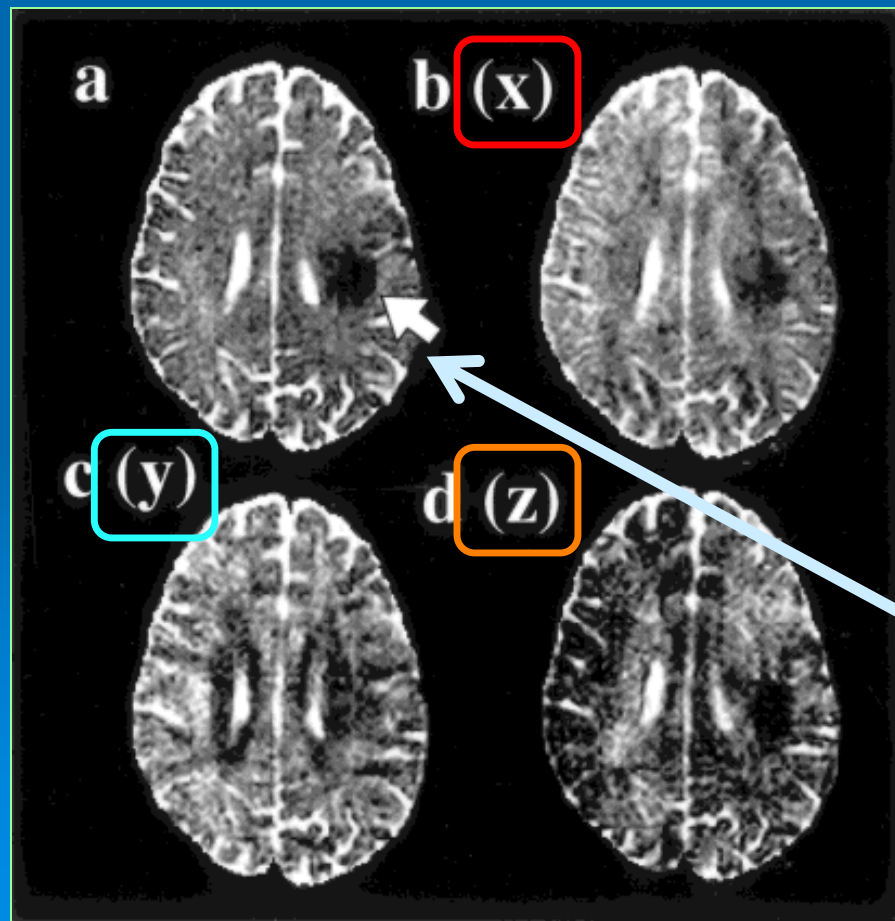


Calculate  $D$  for each pixel  
(slope of the signal decay)

➤ The **apparent diffusion constant (ADC) image** is calculated from a series of diffusion-weighted images with different  $b$ -values



# ADC maps and gradient directions

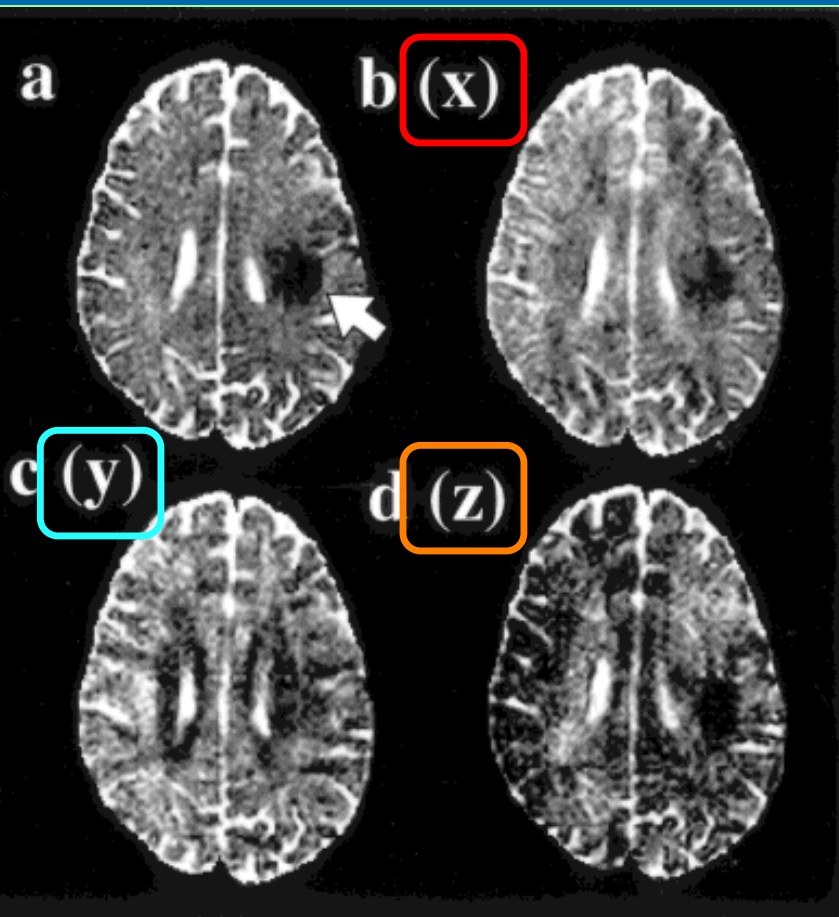


➤ The contrast in the ADC map of brains varies depending on the direction of the diffusion gradients

- MRI can measure molecular diffusion along any axis by using 3 independent gradients that are orthogonal each other

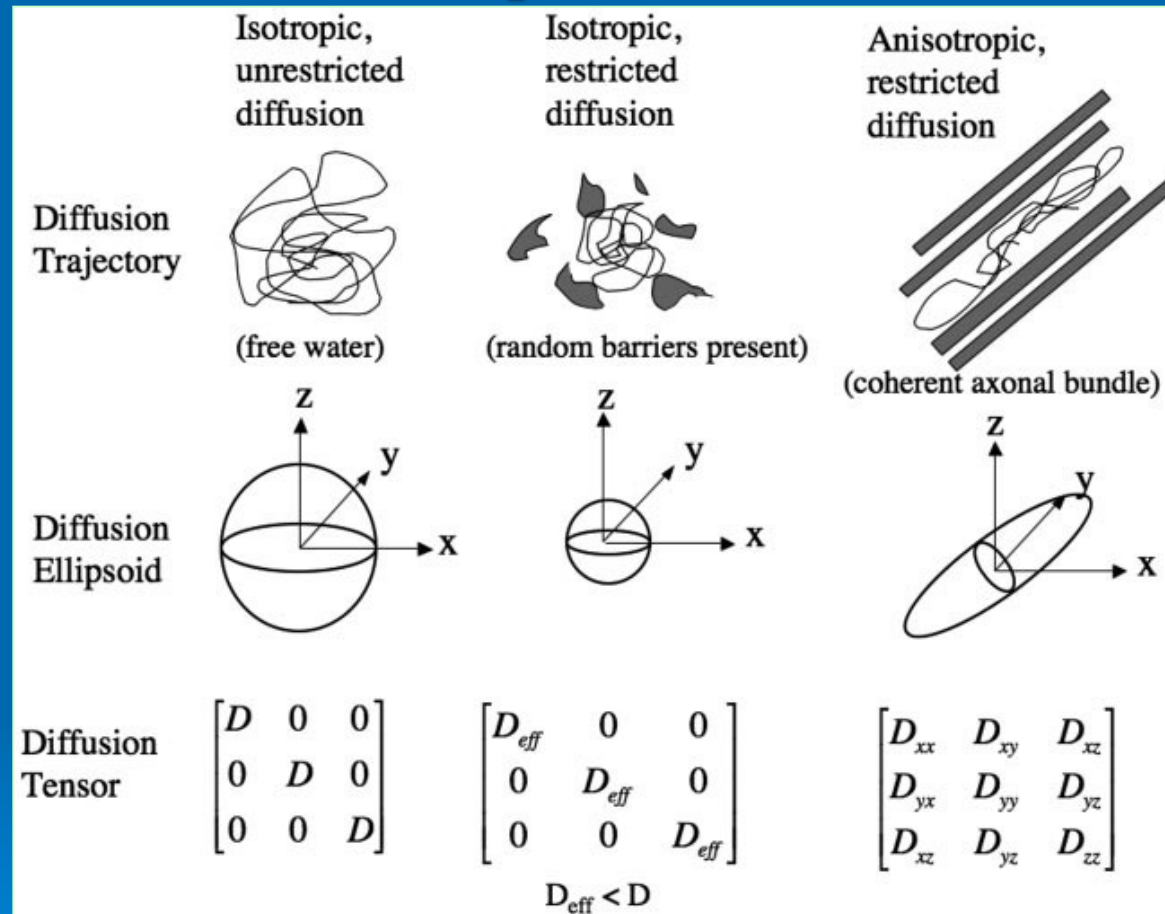
- The image shown in (a) is an image which is obtained by adding 3 ADC images recorded using **x,y,z**-gradients

# ADC maps and gradient directions



- ADC images of a human brain with stroke.
- The orientation dependent contrast is so great, that the location of ischemia, compared to artifactual signals, can no longer be easily differentiated

# Anisotropic Diffusion



The anisotropic diffusion can not be described by a single parameter

- $D$  is a scalar
- The mathematical tool necessary is called *tensor*



# Diffusion Tensor Imaging DTI

## PHYSICS REVIEW

P. Mukherjee  
J.I. Berman  
S.W. Chung  
C.P. Hess  
R.G. Henry

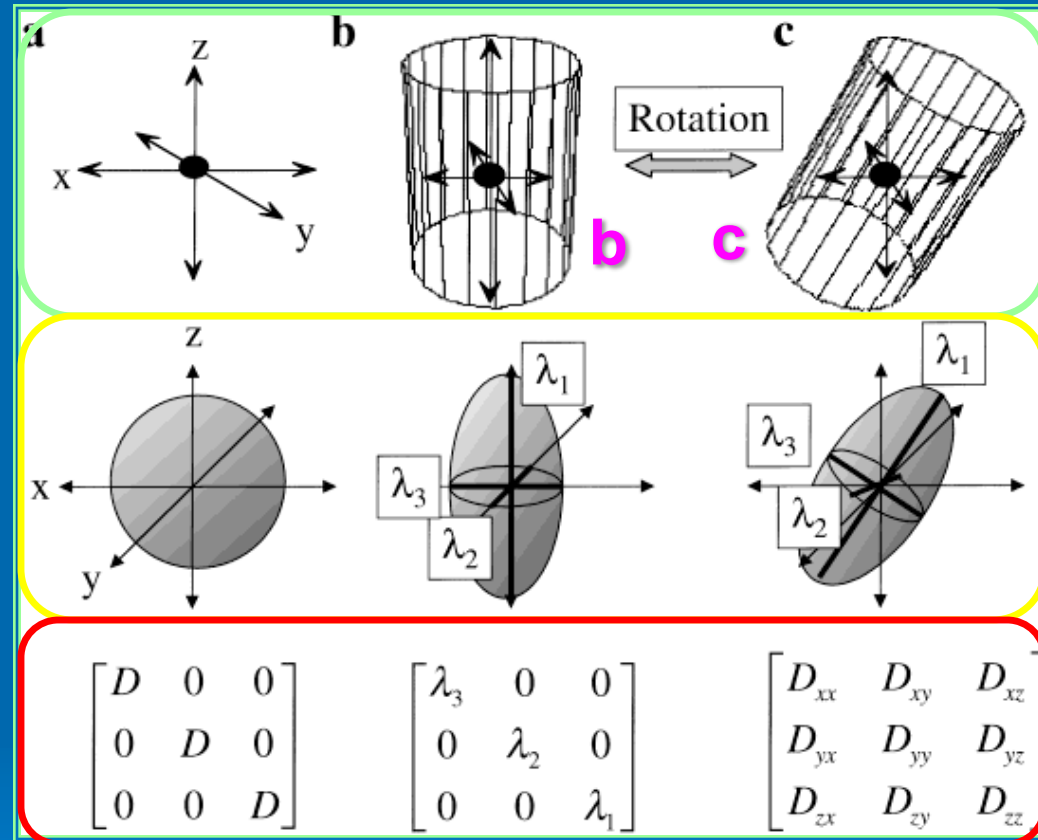
## Diffusion Tensor MR Imaging and Fiber Tractography: Theoretic Underpinnings

**SUMMARY:** In this article, the underlying theory of clinical diffusion MR imaging, including diffusion tensor imaging (DTI) and fiber tractography, is reviewed. First, a brief explanation of the basic physics of diffusion-weighted imaging (DWI) and apparent diffusion coefficient (ADC) mapping is provided. This is followed by an overview of the additional information that can be derived from the diffusion tensor, including diffusion anisotropy, color-encoded fiber orientation maps, and 3D fiber tractography. This article provides the requisite background for the second article in this 2-part review to appear next month, which covers the major technical factors that affect image quality in diffusion MR imaging, including the acquisition sequence, magnet field strength, gradient amplitude and slew rate, and multichannel radio-frequency coils and parallel imaging. The emphasis is on optimizing these factors for state-of-the-art DWI and DTI based on the best available evidence in the literature.

AJNR Am J Neuroradiol 29:632–41 | Apr 2008 | [www.ajnr.org](http://www.ajnr.org)

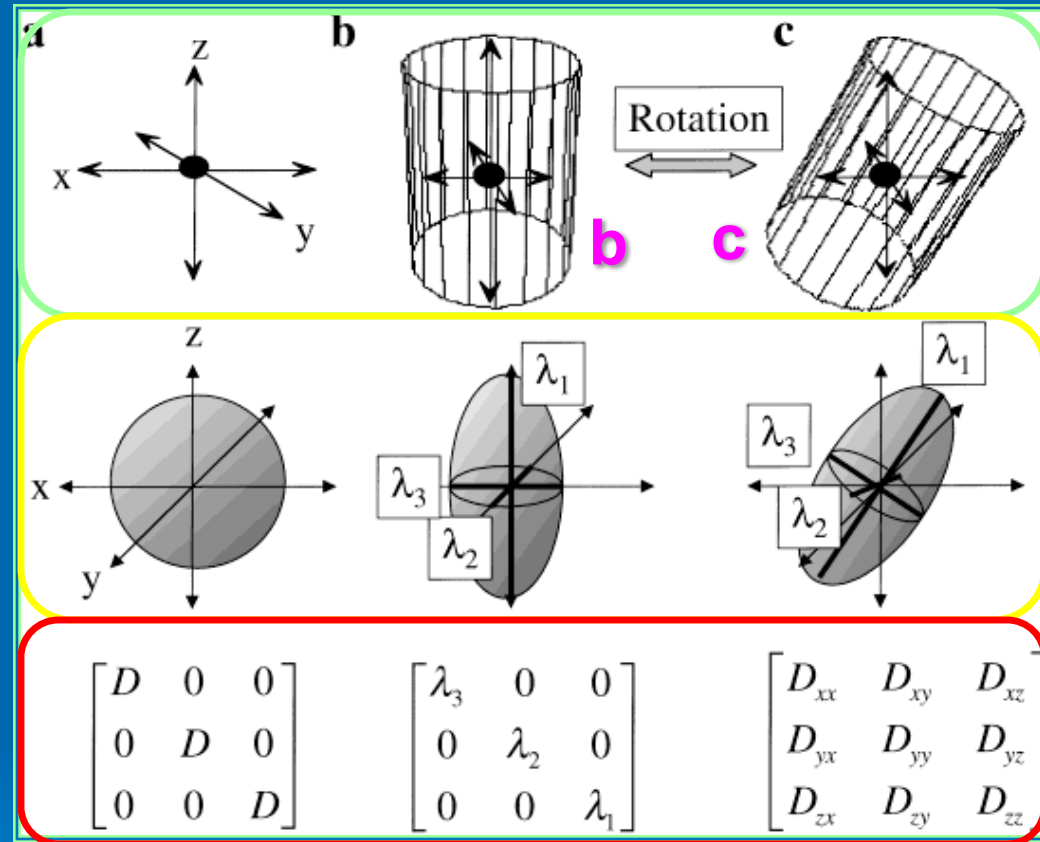
# Diffusion tensor

- Relationship between **anisotropic diffusion**, **diffusion ellipsoids**, and **diffusion tensor**
- In isotropic environment the diffusion ellipsoid is spherical
  - 1 diffusion constant, **D**
- In anisotropic environment water diffusion has directionality
  - e.g. cylindrical (**b,c**),
- The diffusion ellipsoid of water in a cylinder is elongated and has **3 principal axes**,  $\lambda_1, \lambda_2, \lambda_3$



# Diffusion tensor

- Relationship between **anisotropic diffusion**, **diffusion ellipsoids**, and **diffusion tensor**
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- To fully characterize such a system a 3x3 tensor is used
- values of the 9 elements depend on the orientation of the principal axes

# Diffusion tensor

The diffusional signal loss by the gradient application obeys the following equation

$$\frac{S}{S_0} = e^{-bD}$$

In the presence of anisotropy, the tensor  $\underline{D}$  fully describes molecular mobility along each direction and correlation between these directions

$$\underline{D} = \begin{matrix} D_{xx} & D_{xy} & D_{xz} \\ D_{yx} & D_{yy} & D_{yz} \\ D_{zx} & D_{zy} & D_{zz} \end{matrix}$$

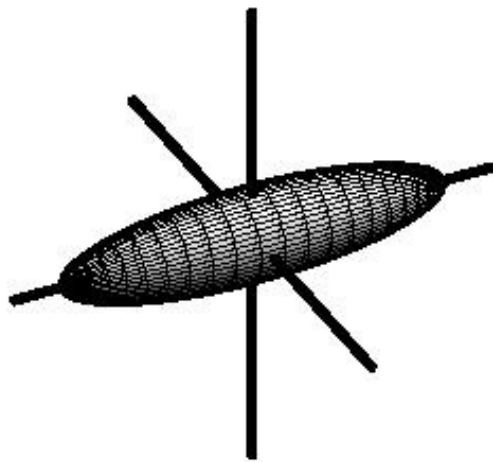
The diffusion tensor is symmetric:

$D_{ij} = D_{ji}$ , with  $i, j = x, y, z$   
9 elements but 6 independent values !

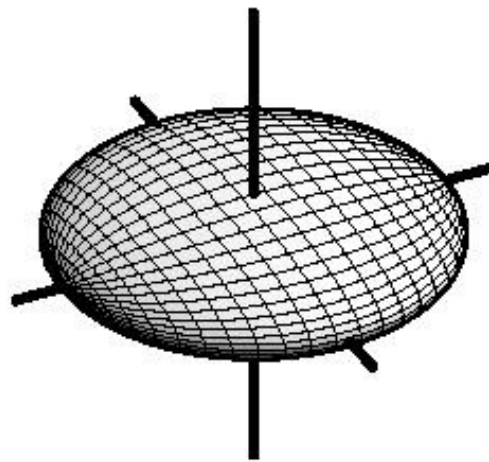
# Graphical description

The Diffusion Tensor has 3 real eigenvalues

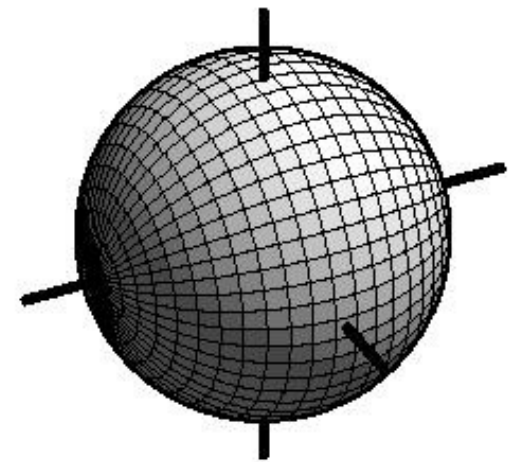
A good graphical description is given by a morphed sphere that reduces to an ellipsoid with the main axis parallel to the direction of the observed fibre



(a) Linear anisotropic diffusion

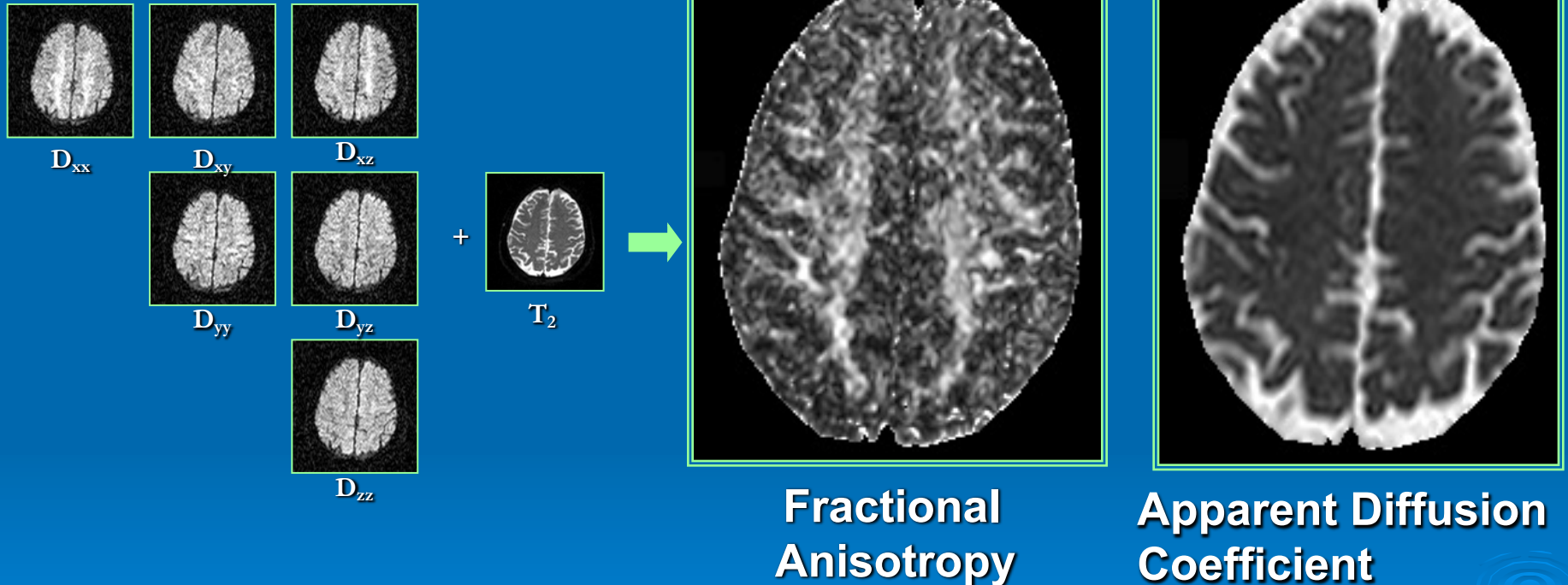


(b) Planar anisotropic diffusion



(c) Isotropic diffusion

# DTI parameters



## Fractional Anisotropy (FA):

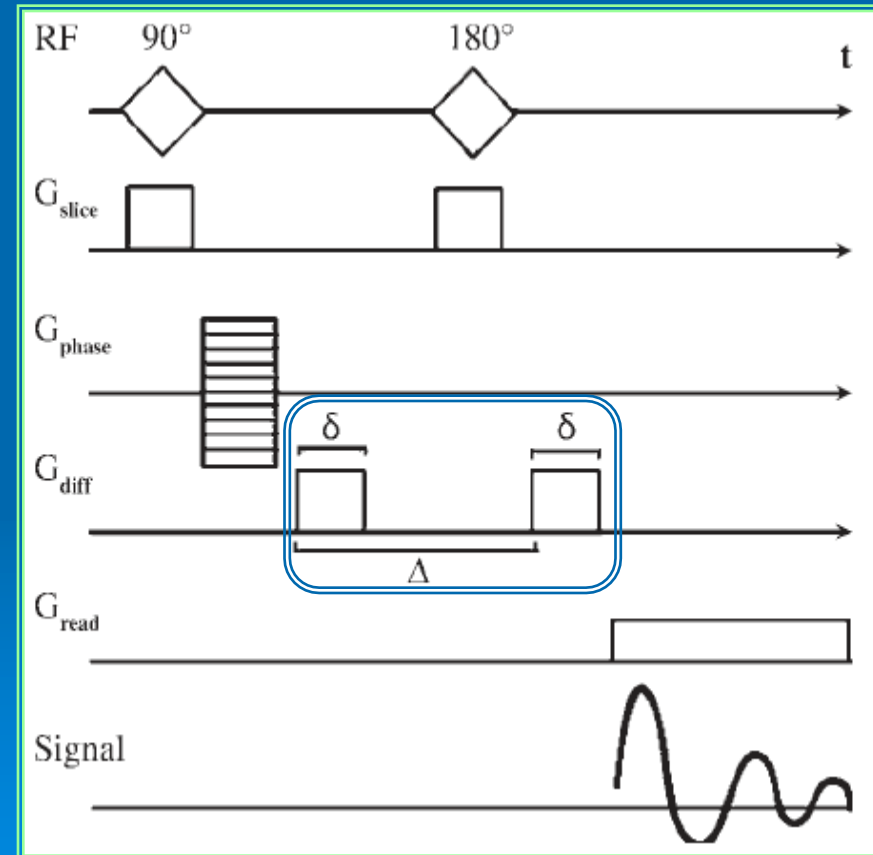
✓ between 0 e 1

- isotropic diffusion  $FA=0$
- monodirectional diffusion  $FA=1$

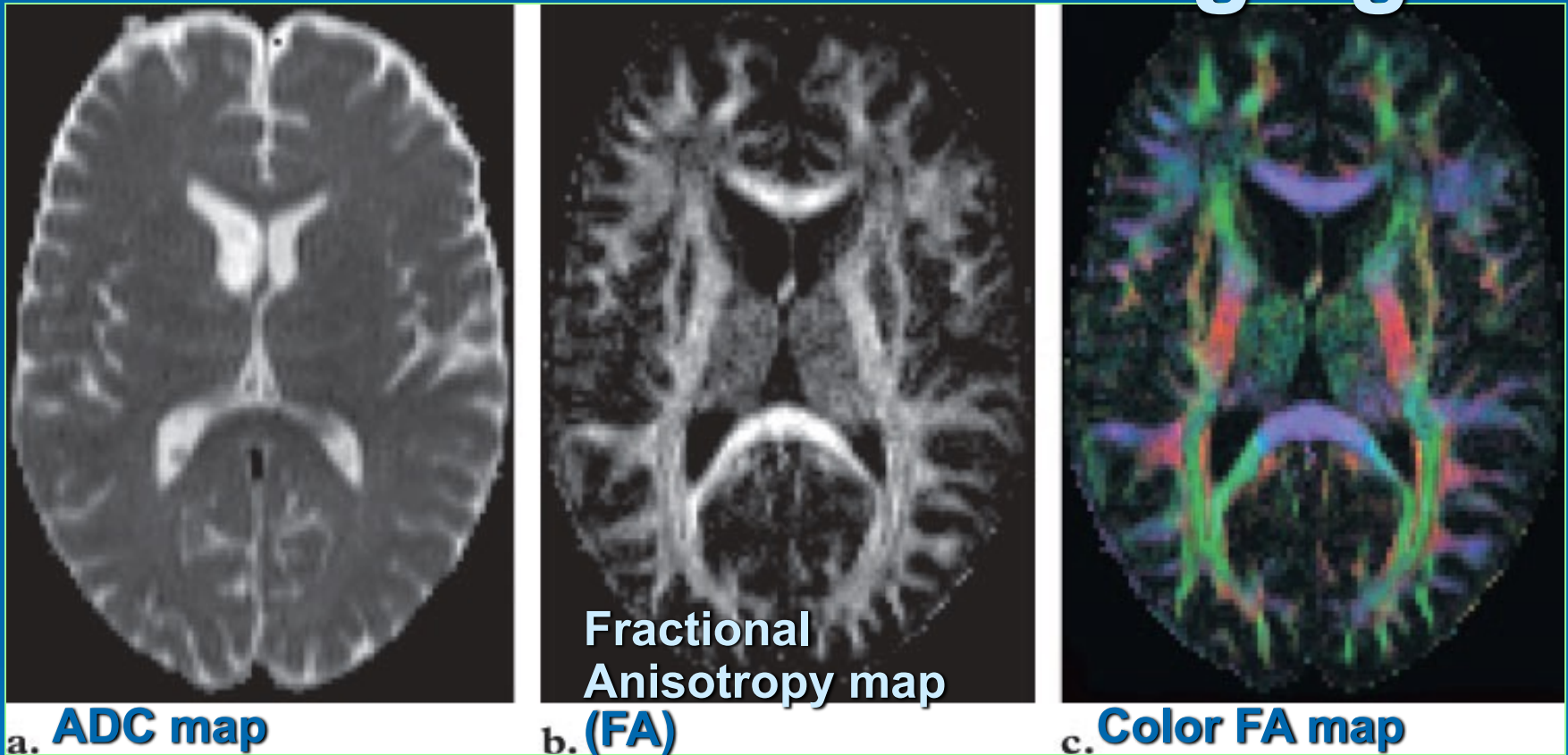
# Diffusion weighted image acquisition

To calculate the diffusion tensor

- 6 diffusion weighted images
- a reference image
  - without diffusion gradient
- In order to obtain better results a larger number of diffusion weighted images are acquired
  - 15, 32 gradient encoding directions or larger



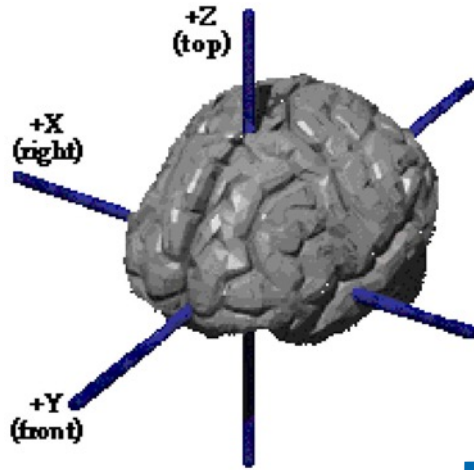
# Diffusion Tensor Imaging



- **ADC map: no information about direction**
- **FA map: information about the degree of anisotropy**
- **Color FA map: direction of the principal component**
  - red, blue, and green representing diffusion along x, y, and z-axes, resp.



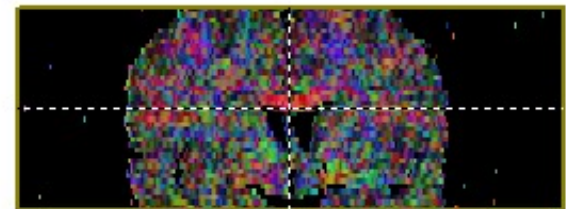
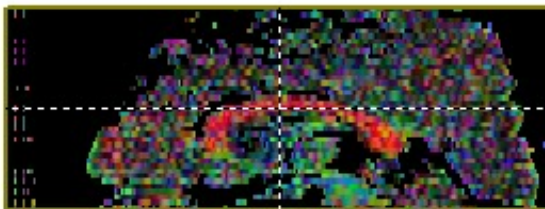
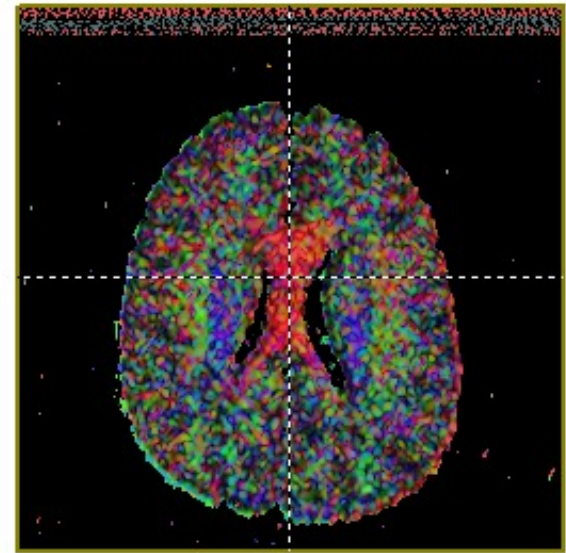
# Color – coded results



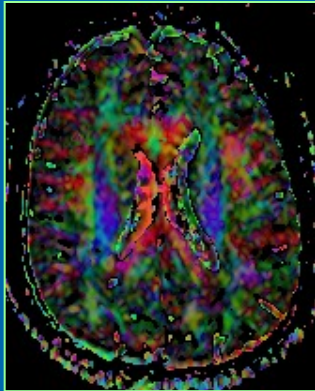
➤ **Red: x**

➤ **Green: y**

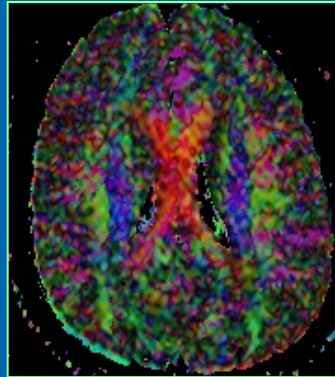
➤ **Blue: z**



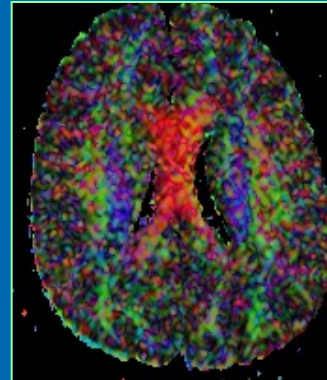
# Quality vs. Slice thickness



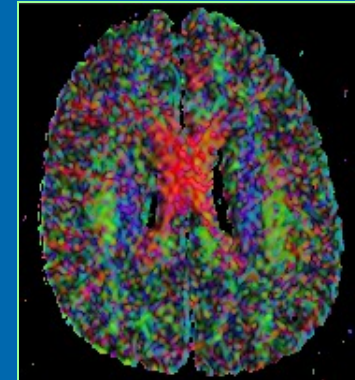
5 mm



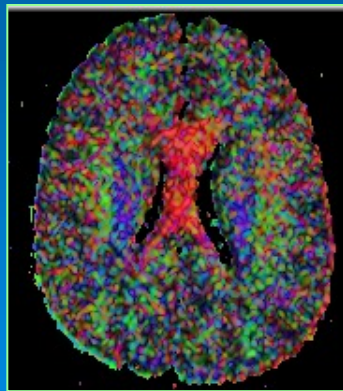
4 mm



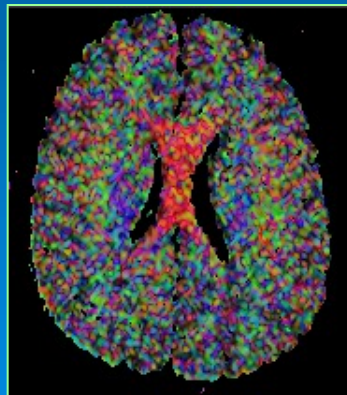
3 mm



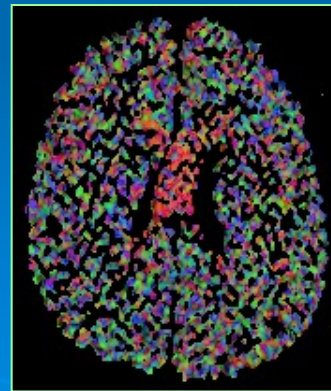
2.5 mm



2 mm



1.5 mm



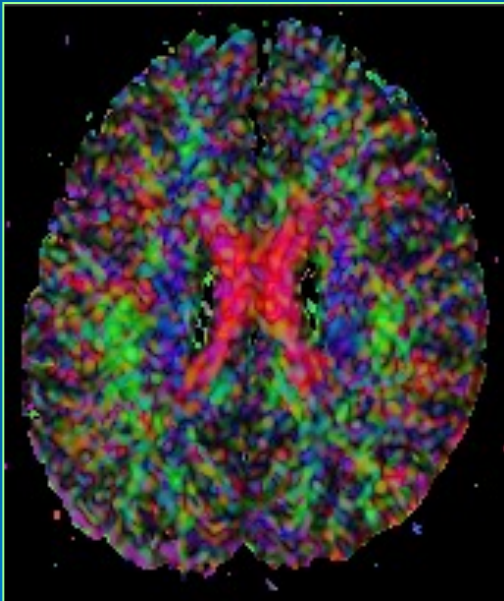
1 mm

- **Red: x**
- **Green: y**
- **Blue: z**

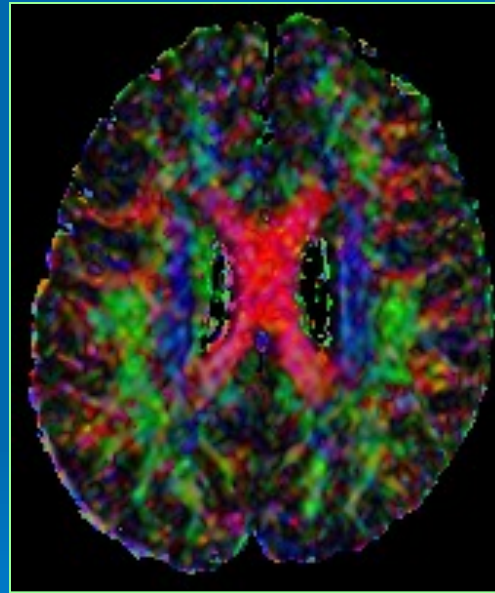
All slices are acquired along 6 directions

# Quality vs. Directions number

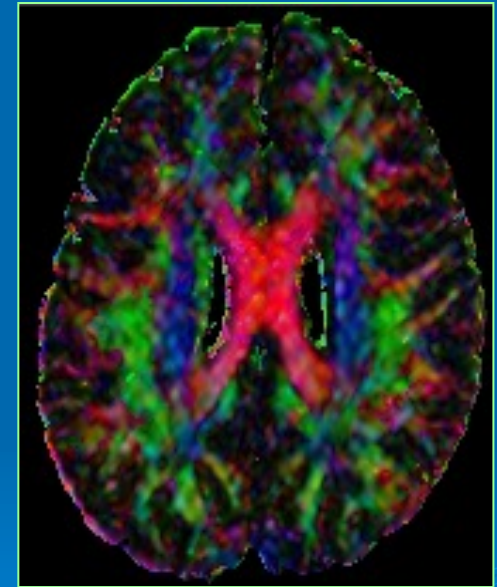
All slices are 2 mm thick



6 directions



15 directions



32 directions

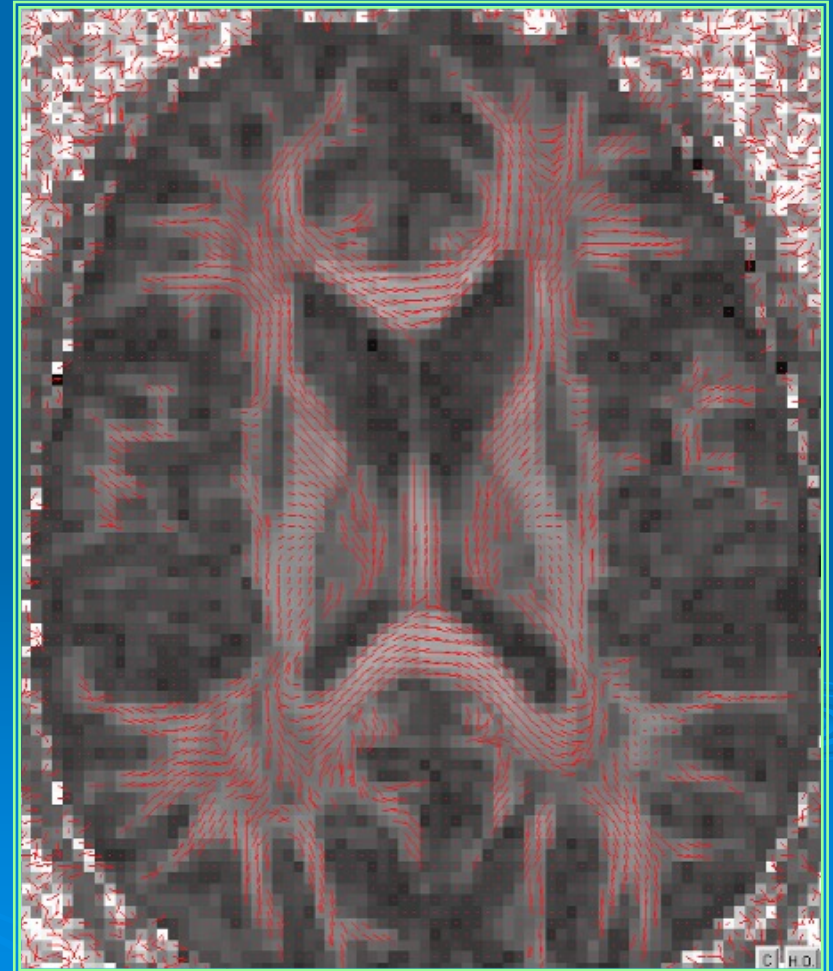
➤ Red: x

➤ Green: y

➤ Blue: z

# DTI-MRI summary

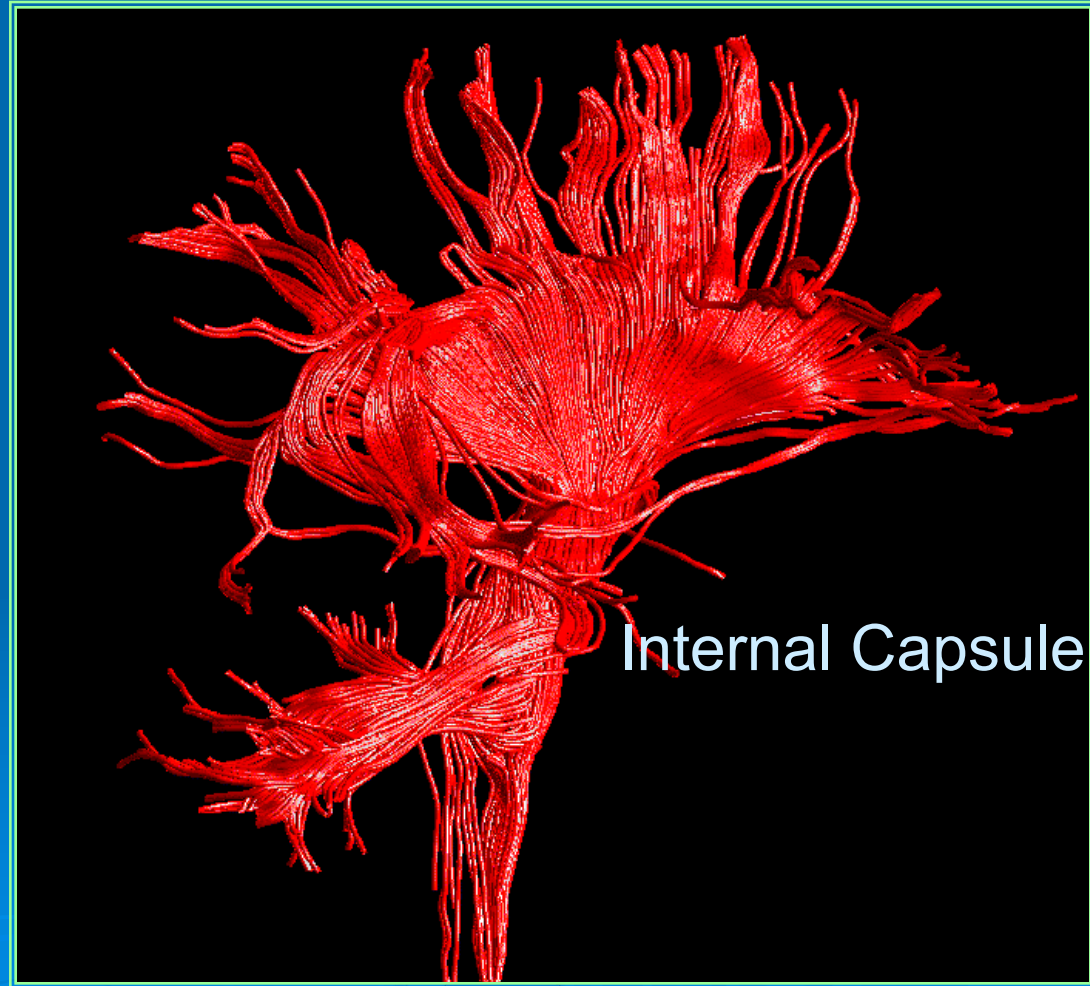
1. Image of diffuse fluid motion in brain
2. Construct “Tensor image”
  - extent of diffusion in each direction in each voxel in image
3. Diffusion along nerve sheaths defines nerve tracts
4. Create images of nerve connections/pathways



*Slides from Terry Peters*

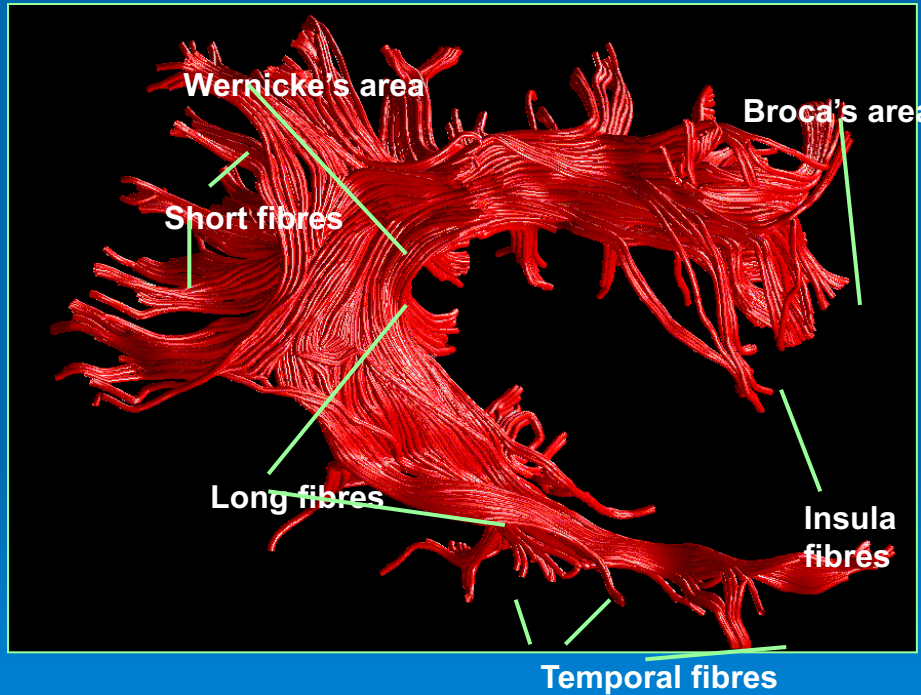
# Tractography

- Data analysed after scanning
- Identify “streamlines” of vectors
- Connect to form fibre tracts
- 14 min scan time



*Slides from Terry Peters*

# Tractography

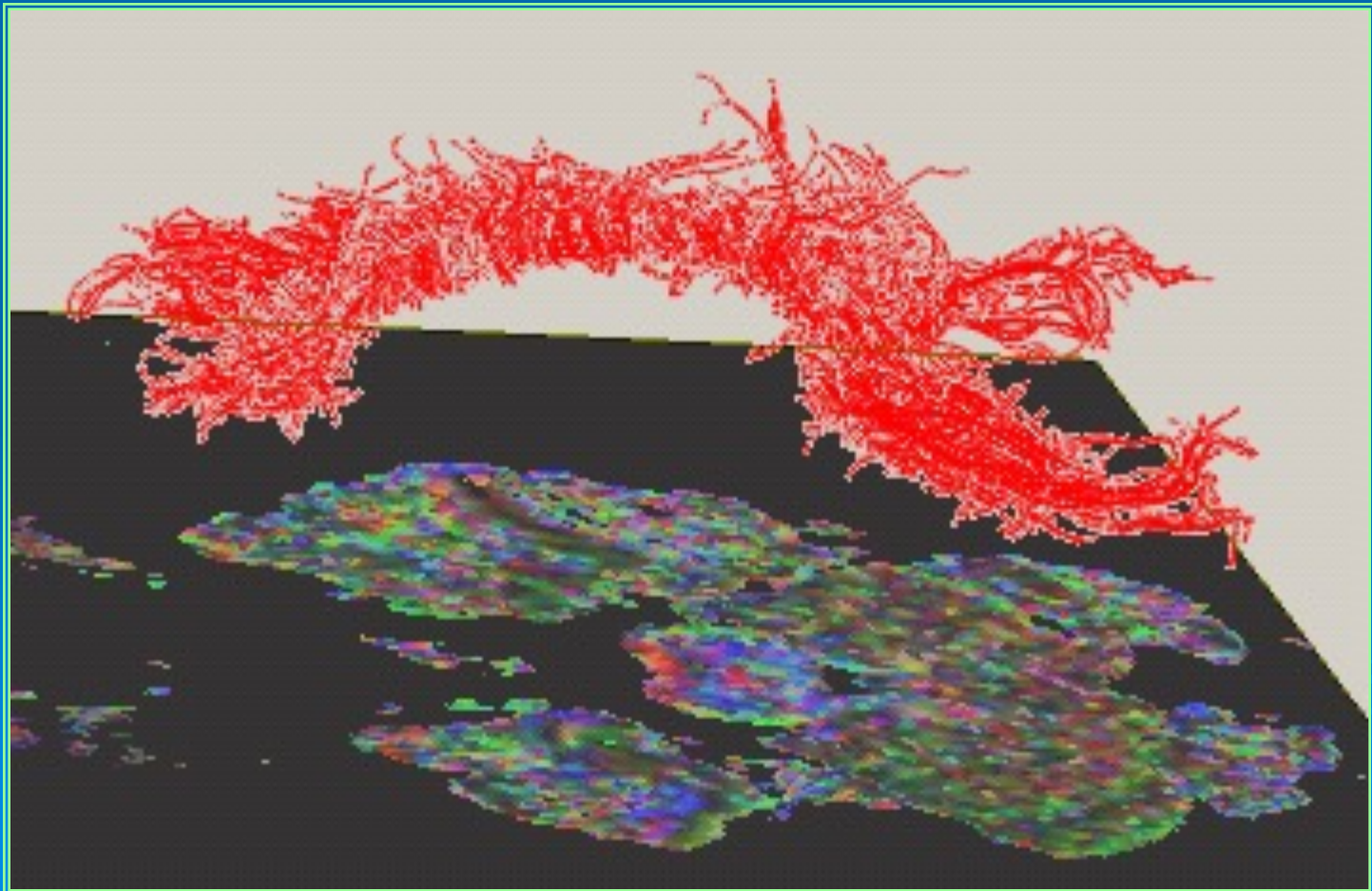


“just like Gray’s Anatomy”!

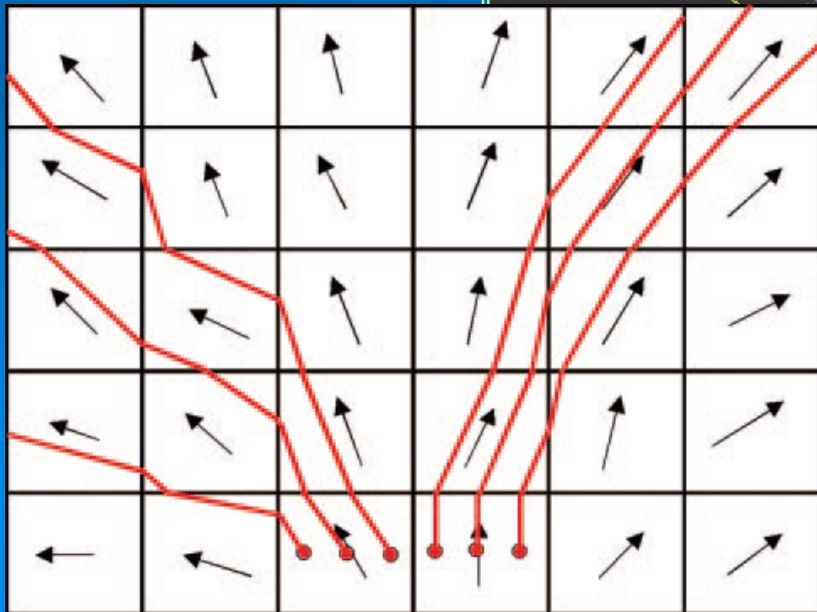
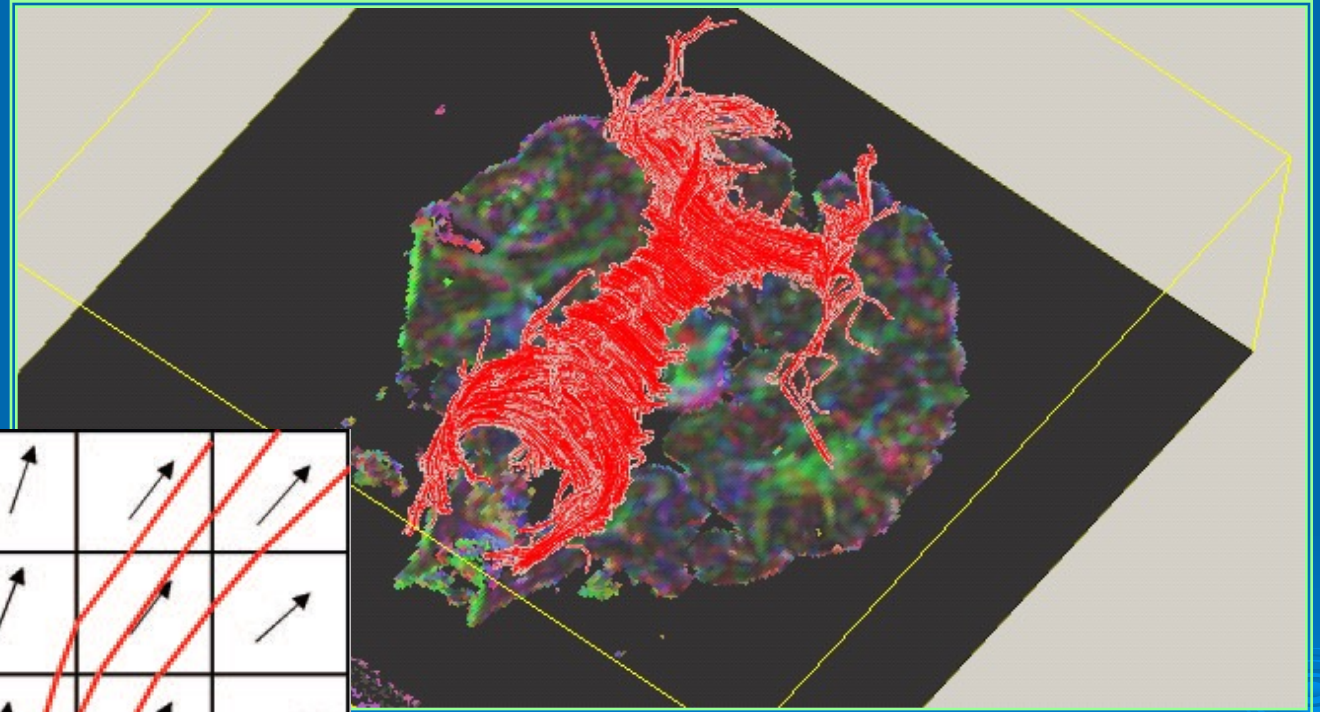
**Superior Longitudinal Fasciculus**

- Dr. D Jones, NIH USA

# DTI: corpus callosum (1)

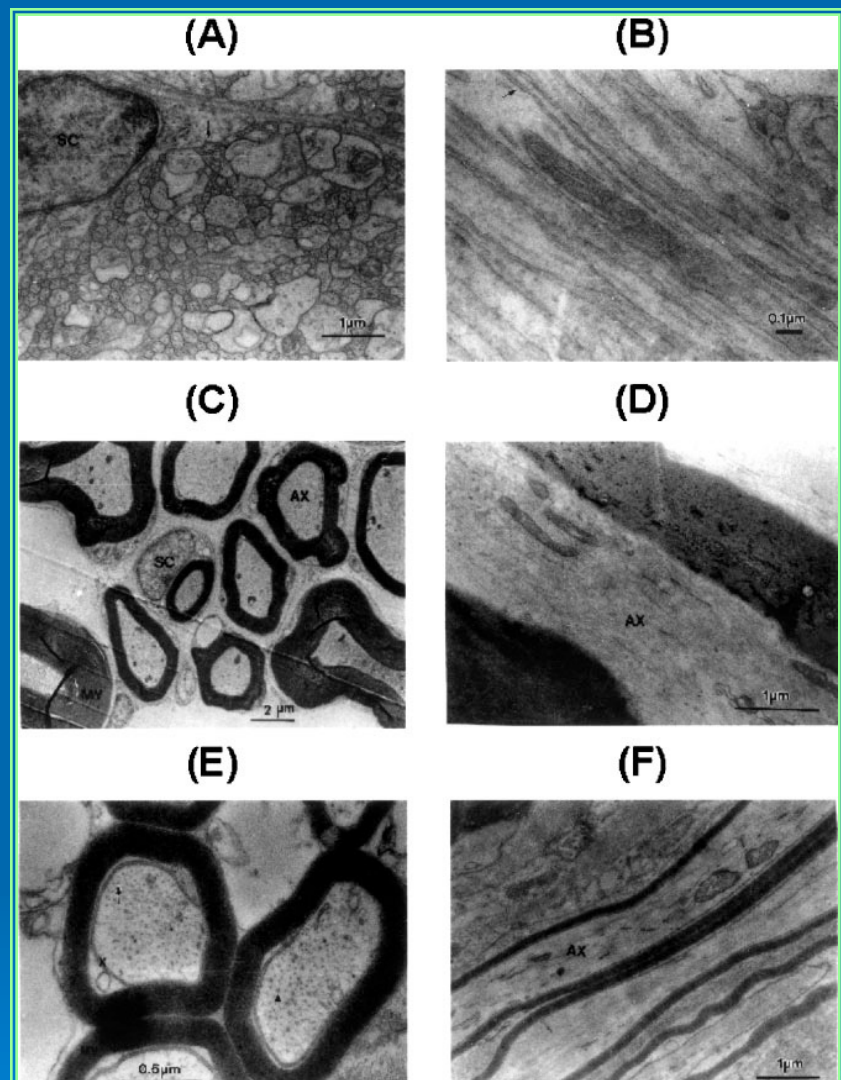


# DTI: corpus callosum (2)



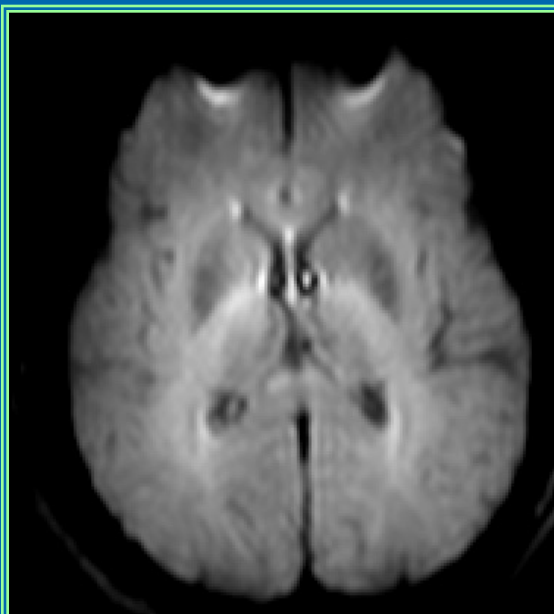


# Nerves geometry

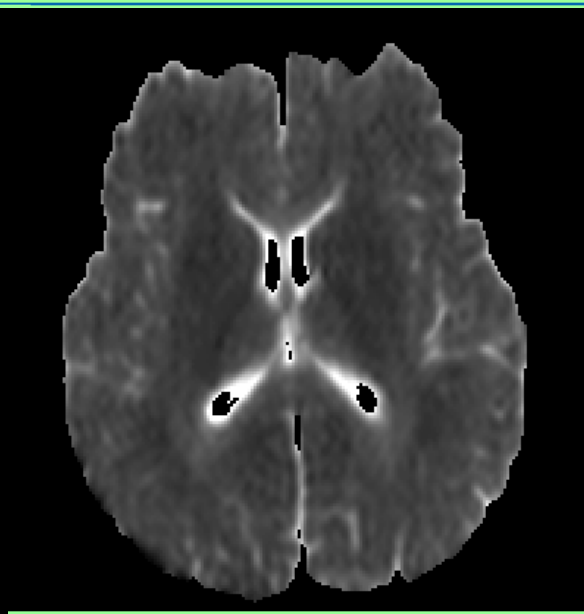


**Figure 6.** Electron micrographs of transverse (A, C, E) and longitudinal (B, D, F) sections from freshly excised non-myelinated olfactory (A, B), myelinated trigeminal (C, D), and myelinated optic (E, F) nerves of the garfish. *Olfactory nerve*: (A) The small ( $\sim 0.25 \mu\text{m}$  diameter), circular, relatively homogeneous non-myelinated axons (arrow) are packed together tightly. Microtubules (seen as small dots within the axons) and a Schwann cell nucleus (SC) are visible. (B) Axonal membranes (arrow) run diagonally across the micrograph. *Trigeminal nerve*: (C) The axons (AX) have diameters  $\sim 3\text{--}6 \mu\text{m}$  and appear to have good circular shapes which is indicative of a structurally sound nerve.

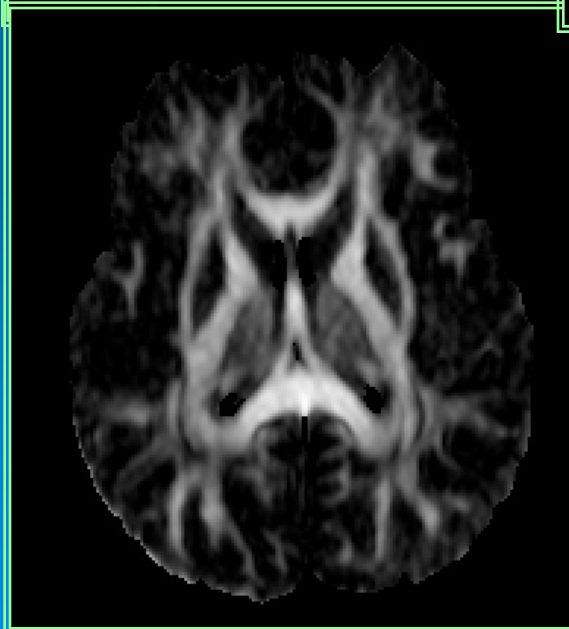
**T2**



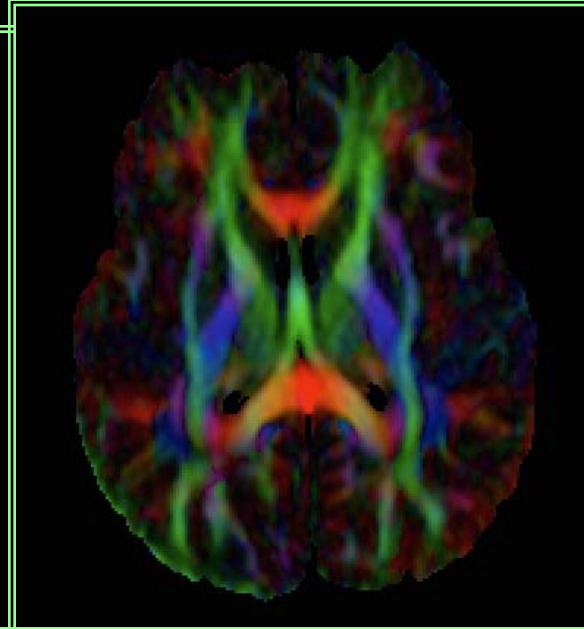
**ADC**



**FA**



**FA  
Color  
coded**



# Modeling diffusion

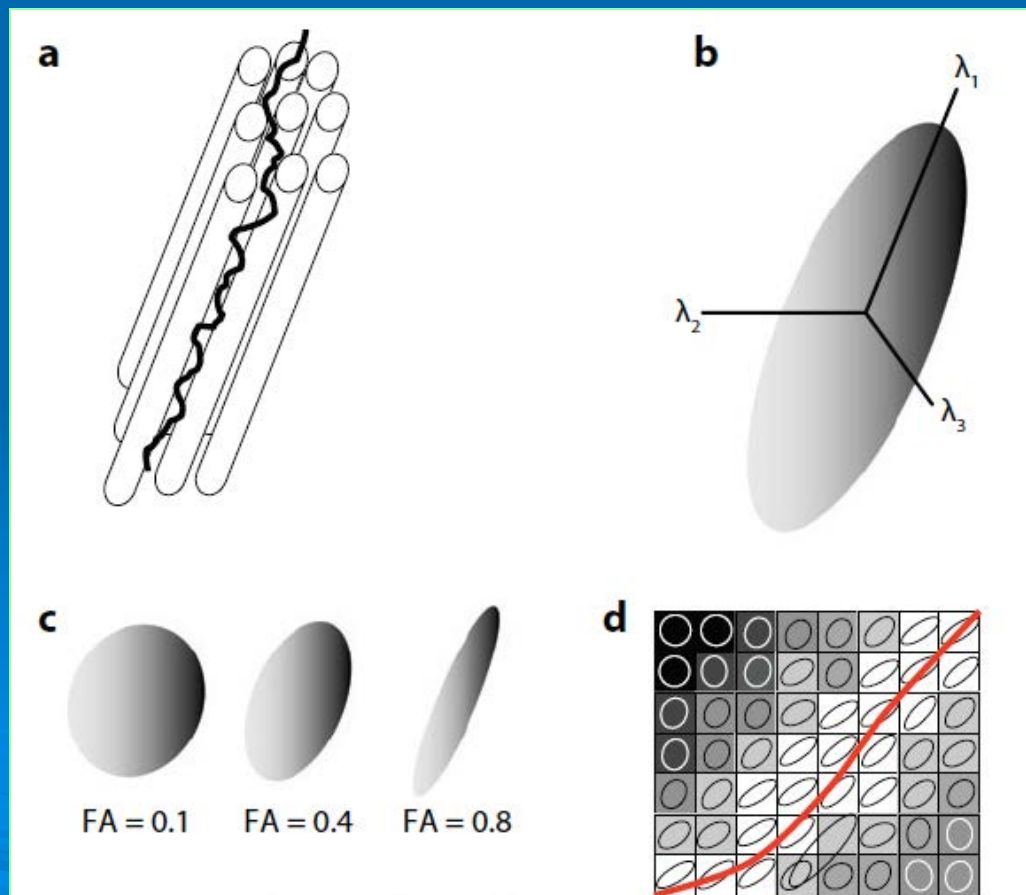
Using Diffusion Imaging to Study Human Connectional Anatomy

Heidi Johansen-Berg<sup>1</sup>  
and Matthew F.S. Rushworth<sup>1,2</sup>

a) Schematic to illustrate diffusion of a water molecule (black line) within a fiber bundle.

b) The diffusion tensor model: water diffusion at each voxel is modeled by a tensor

- ✓ characterized by its 3 principal eigenvectors and their associated eigenvalues ( $\lambda_1$ ,  $\lambda_2$ ,  $\lambda_3$ ).



# Modeling diffusion

Using Diffusion Imaging to Study Human Connectional Anatomy

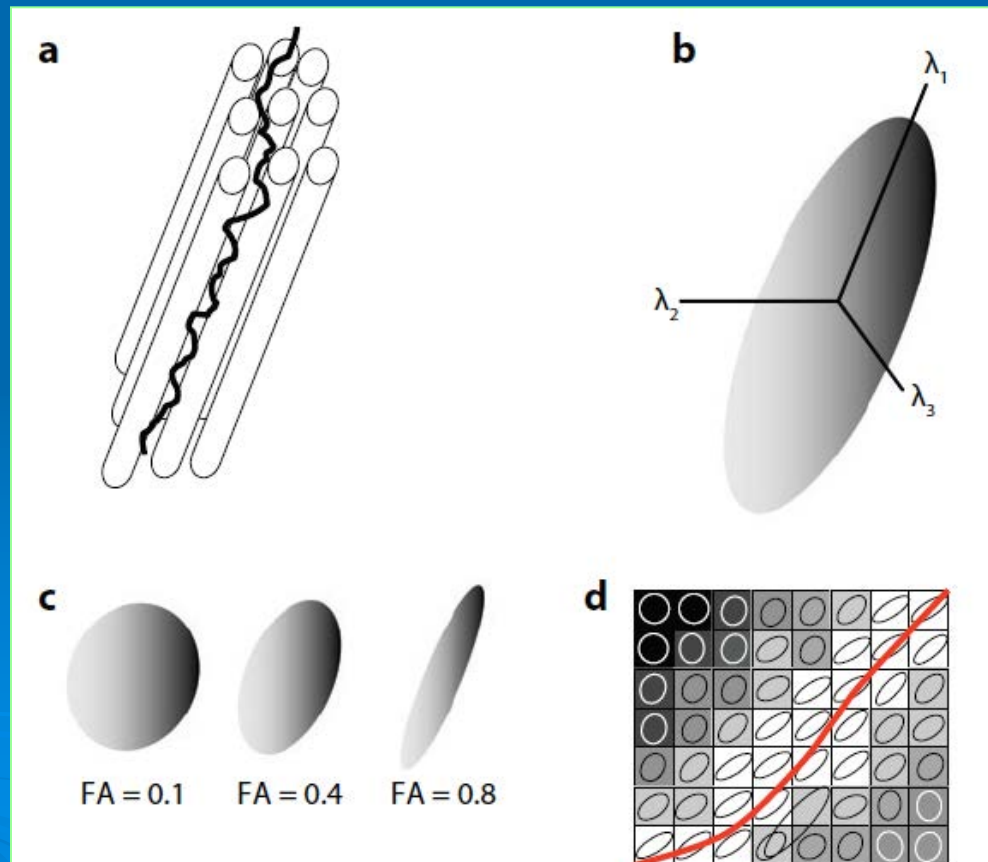
Heidi Johansen-Berg<sup>1</sup>  
and Matthew F.S. Rushworth<sup>1,2</sup>

c) Fractional anisotropy (FA) is calculated from the tensor fit and ranges between 0 and 1

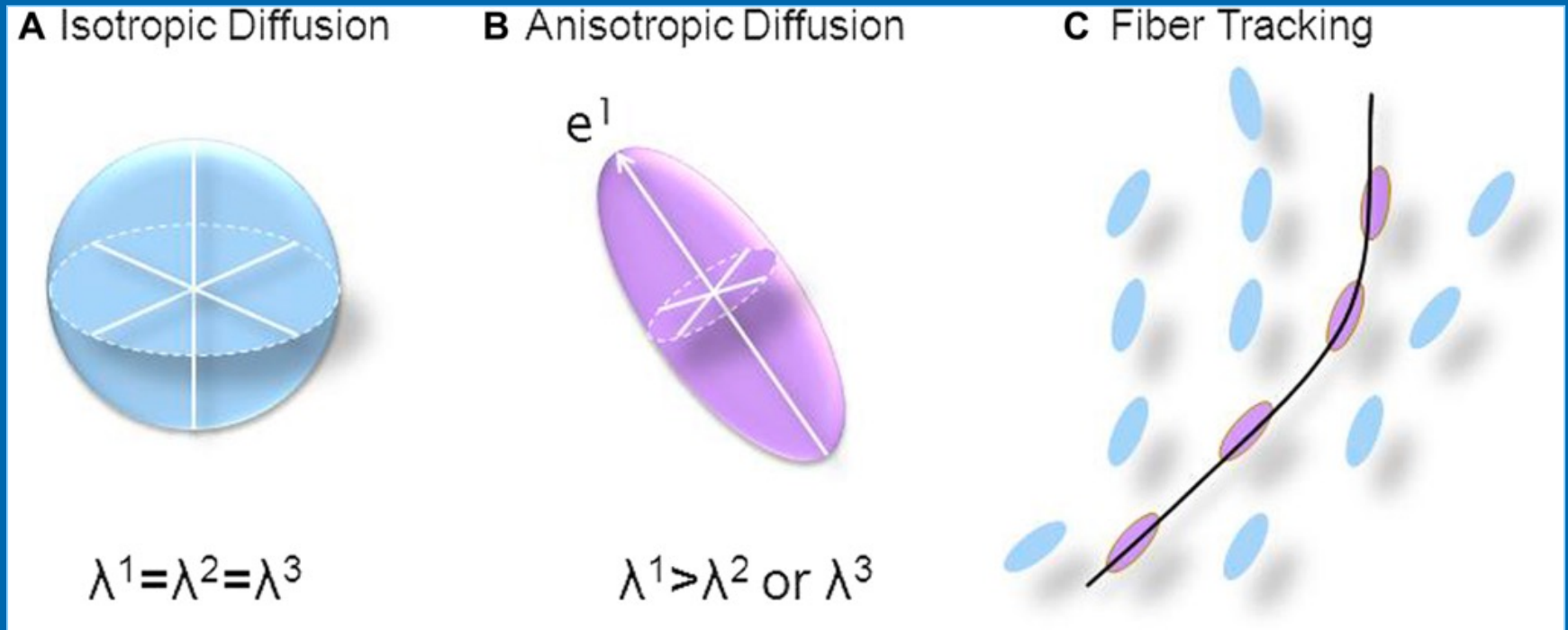
- FA reflects the shape of the tensor

d) Streamlining tractography proceeds by tracing a line through the tensor field, following the principal diffusion direction

- The schematic shows a grid of voxels: the grayscale reflects FA ranging from 0 (black) to 1 (white)
- The corresponding tensors are illustrated by the ellipses shown at each voxel



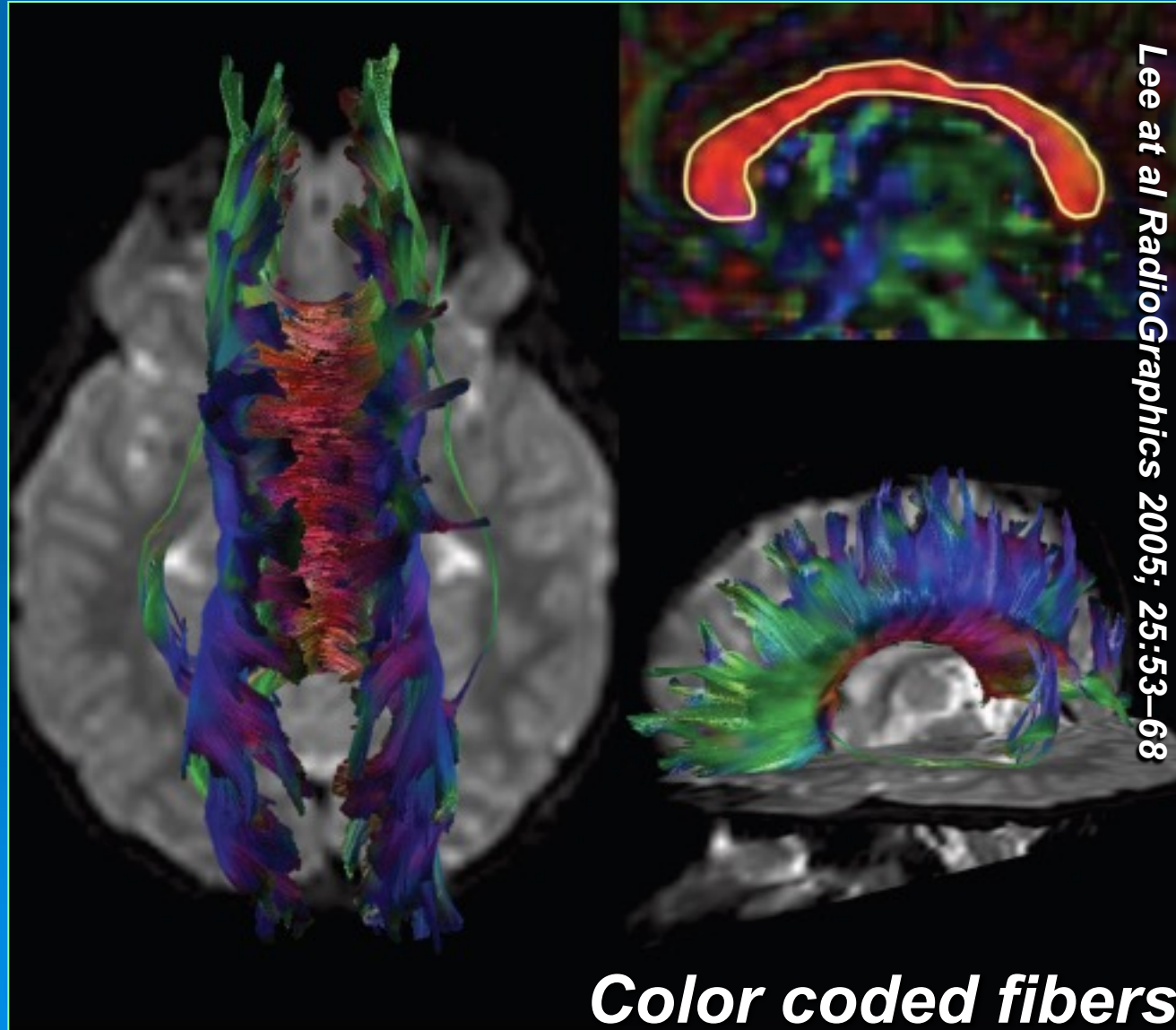
# Modeling diffusion



Fiber tracking is initiated at a pixel or region of interest (ROI) and tracking is propagated along adjacent ellipsoids that meet certain thresholds for FA and trajectory curvature.

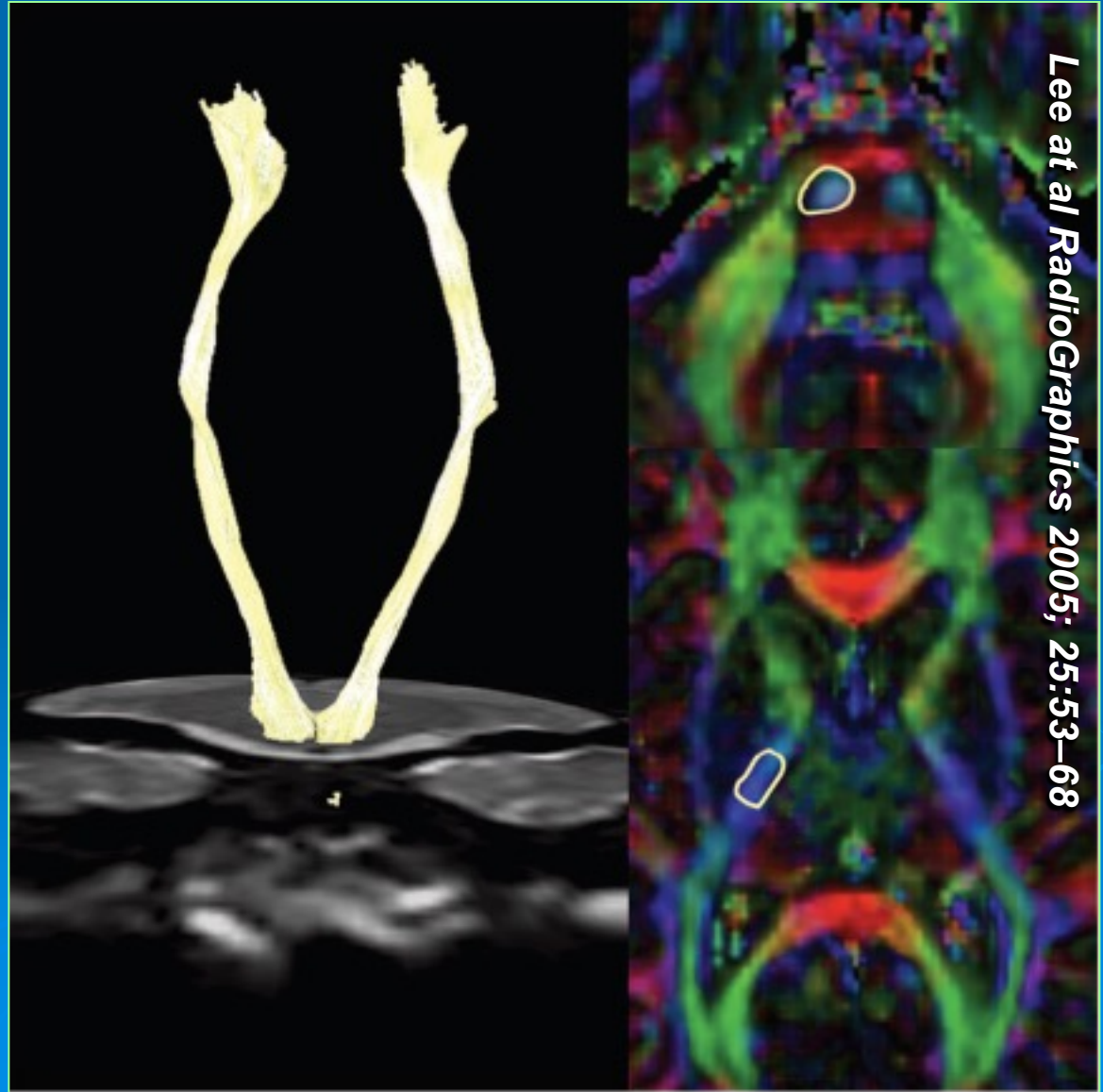
# FT of the corpus callosum

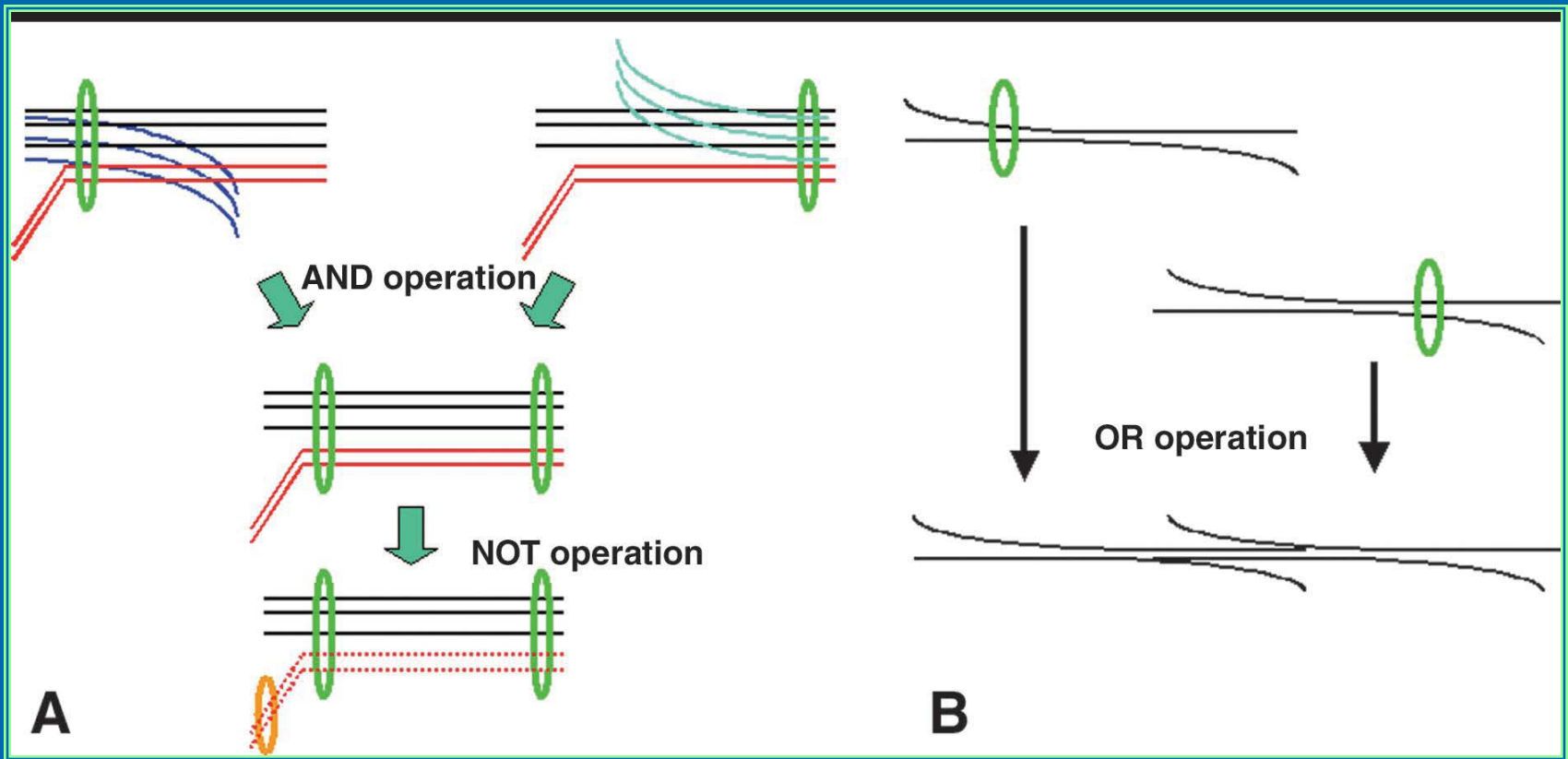
FT images of the corpus callosum (*left and bottom right*) are generated from a single ROI at the precise anatomic locations on the sagittal color map (*top right*).



# FT of the CST

FT image of the corticospinal tract generated from the fibers connecting two ROIs in the longitudinal pontine fibers and the posterior limb of the internal capsule (*right*)



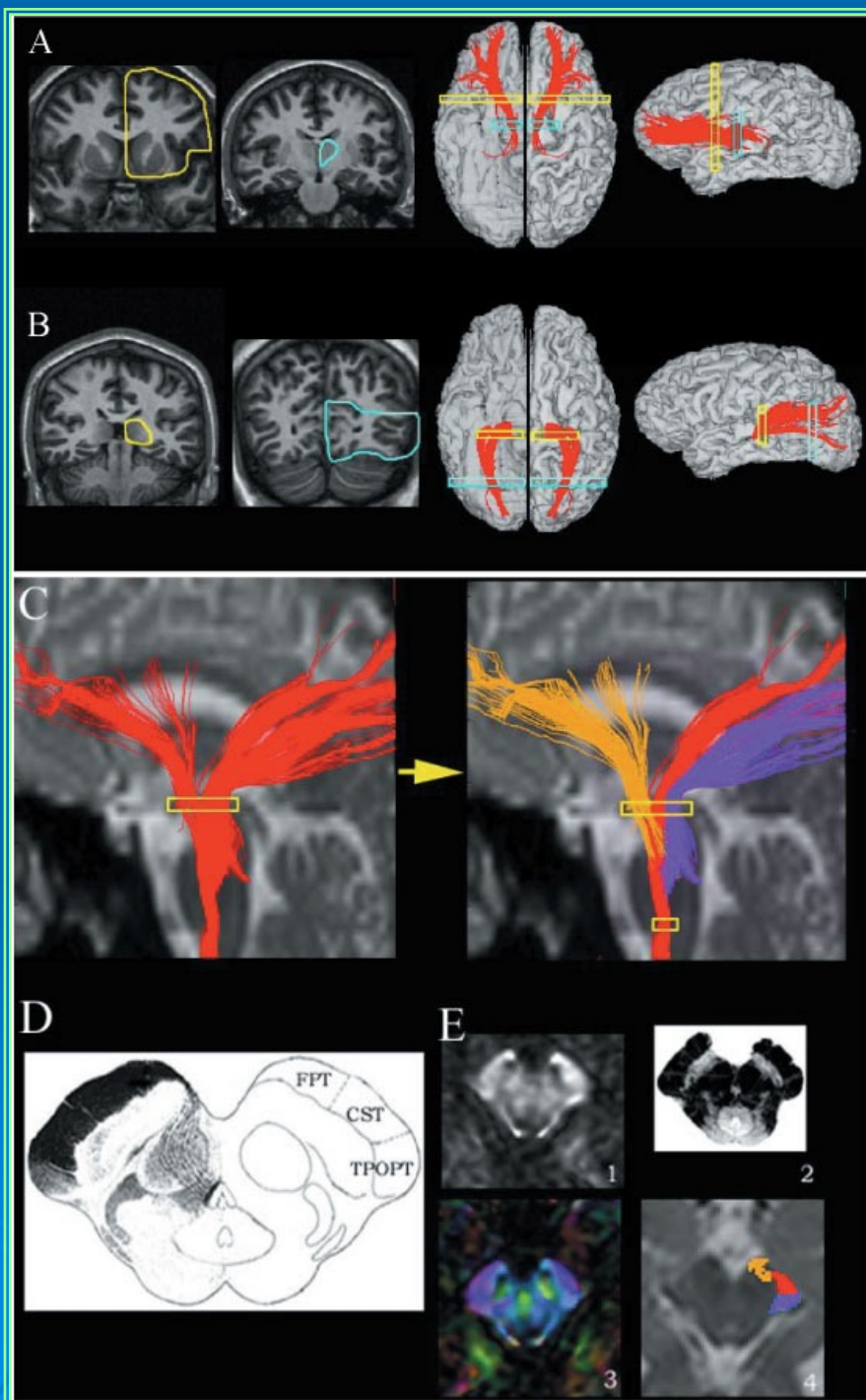


## Three operations used FT: AND, NOT, OR

- A. Two ROIs (green) are placed on anatomic landmarks. When the AND operation is used, tracts that penetrate both ROIs are selected. NOT operation is used to remove specific tracts that penetrate one or multiple ROIs (orange). In this example, red tracts are removed.
- B. OR operation.



# Multi-ROI tracking approach



**Figure 4.** Example of using the multi-ROI approach to reconstruct white matter tracts of interest. Coronal images show the locations of two reference ROIs for each tract. The reconstruction results for the anterior (A) and posterior (B) thalamic radiation are presented in the axial and sagittal view. Images in (C)–(E) show examples of the parcellation of homogeneous-looking white matter based on 3D tract trajectories. Results of tract reconstruction that penetrate the cerebral peduncle are shown in (C). Tracts excluded by the second ROI at the lower pons level are shown by green and blue. Yellow boxes indicate the locations of ROIs. The postulated parcellation of the cerebral peduncle based on anatomical studies is shown in (D). Images in (E) shows anisotropy map (E-1), histological preparation (E-2), color-coded map (E-3), and  $T_2$ -weighted image with the location of reconstructed results superimposed (E-4). The figures were reproduced from Mori *et al.*<sup>52</sup> (A,B), Stieltjes *et al.*<sup>42</sup> (C,E) and Carpenter<sup>49</sup> (D) with permission

# Additional material

- [https://www.youtube.com/watch?v=J\\_aamnpRJE8](https://www.youtube.com/watch?v=J_aamnpRJE8)
- <https://www.youtube.com/watch?v=twsv81UFFcE>

# A diffusion tensor imaging tractography atlas for virtual in vivo dissections

CORTEX 44 (2008) 1105–1132

Marco Catani<sup>a,b,\*</sup> and Michel Thiebaut de Schotten<sup>a,b,c</sup>

## A b s t r a c t

- Diffusion tensor imaging (DTI) tractography allows perform virtual dissections of white matter pathways in the living human brain. [..]
- Here [...] we provide a template to guide the delineation of ROIs for the reconstruction of the association, projection and commissural pathways of the living human brain. The template can be used for single case studies and case–control comparisons.
- An atlas of the 3D reconstructions of the single tracts is also provided as anatomical reference in the Montreal Neurological Institute (MNI) space.

# Corpus callosum

- **Anatomy.** The corpus callosum is the largest bundle of the human brain [...]
- **Identification on the color maps:**
  - The red fibers of the body of the corpus callosum are ventral to the cingulum and medial to the lateral ventricles (MNI 35 to 29).
  - The body of the corpus callosum separates into the genu, anteriorly (MNI 27 to 1), and the splenium, posteriorly (MNI 27 to 11).
    - The tapetum is not visible on the color map.
- **Delineation of the ROIs on the FA maps:**
  - A single ROI (CC) is defined around the body, the genu and the splenium of the corpus callosum (MNI 35 to 5). The shape of the regions follows the anatomy of the different parts of the corpus callosum, butterfly-shaped for the body, horseshoe-shaped for genu and splenium.

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**A diffusion tensor imaging tractography atlas for virtual in vivo dissections**

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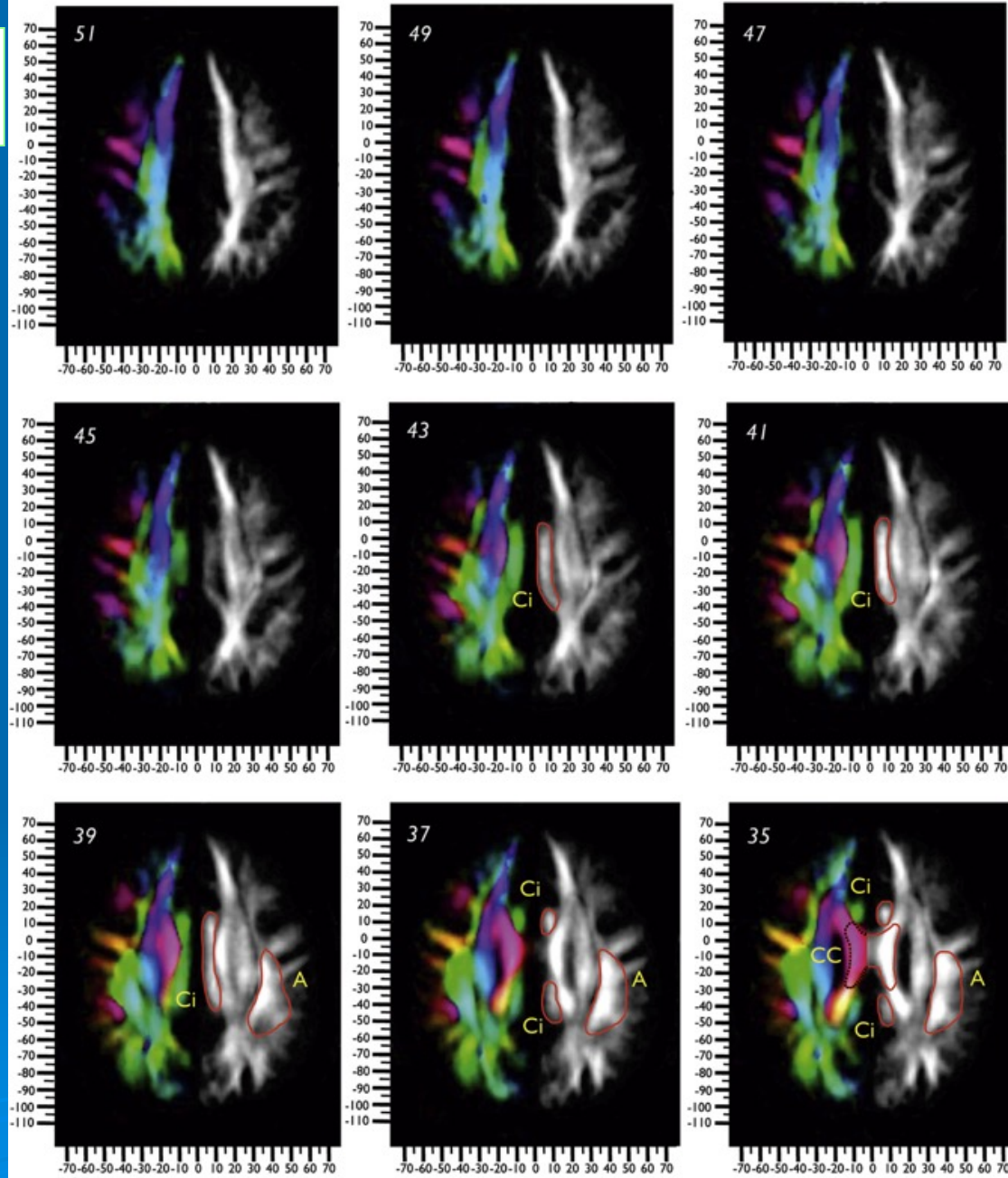
➤ Diffusion tensor image template of an average data set and delineation of ROIs

➤ The FA maps on the right provide information about the general anatomy

- the major association, commissural and projection white matter tracts

➤ The color maps on the left provide additional information on the local orientation of the tracts

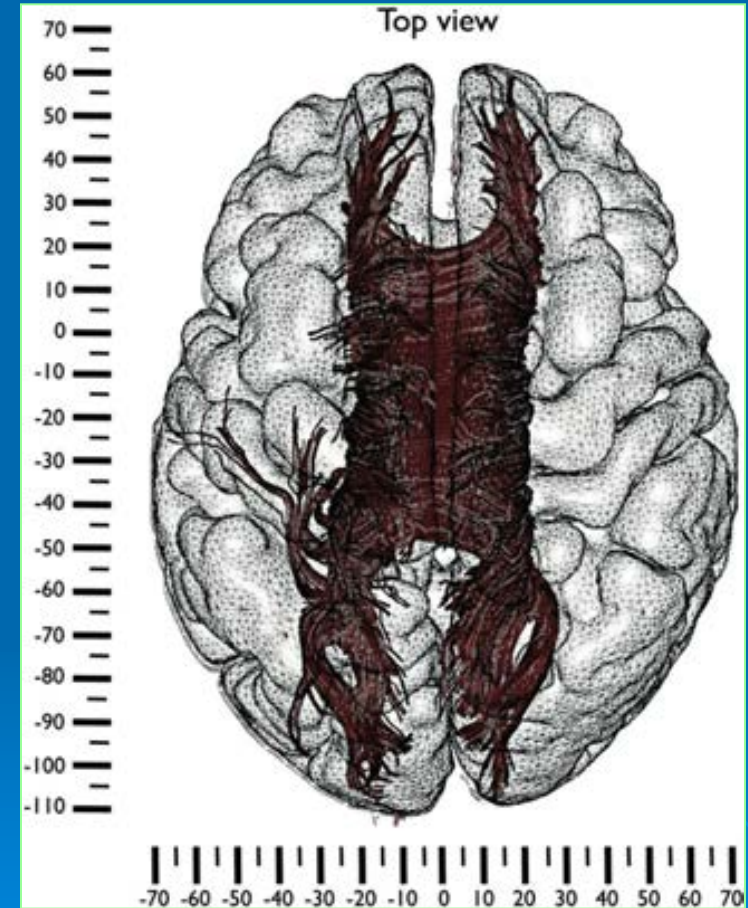
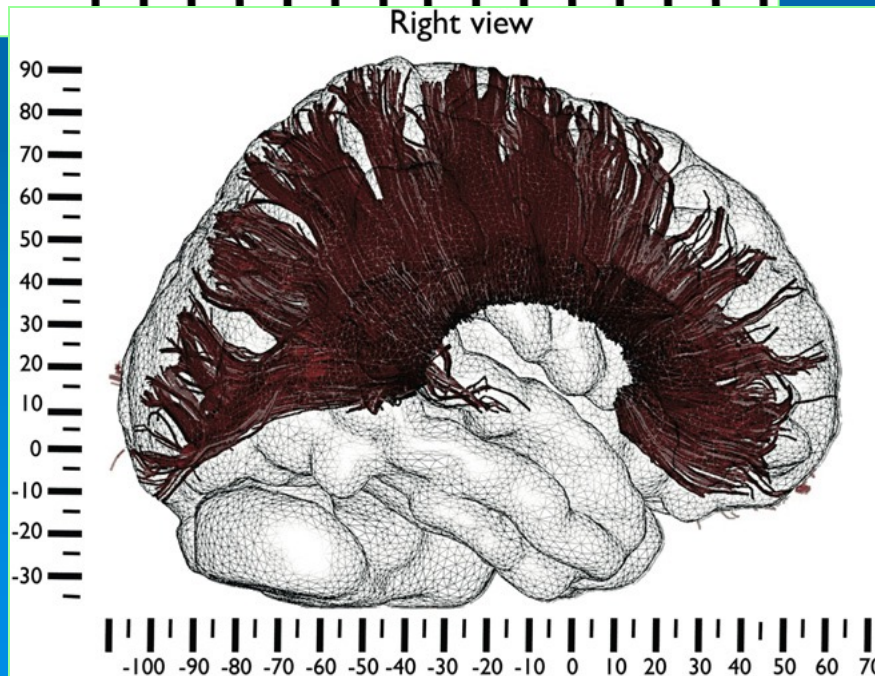
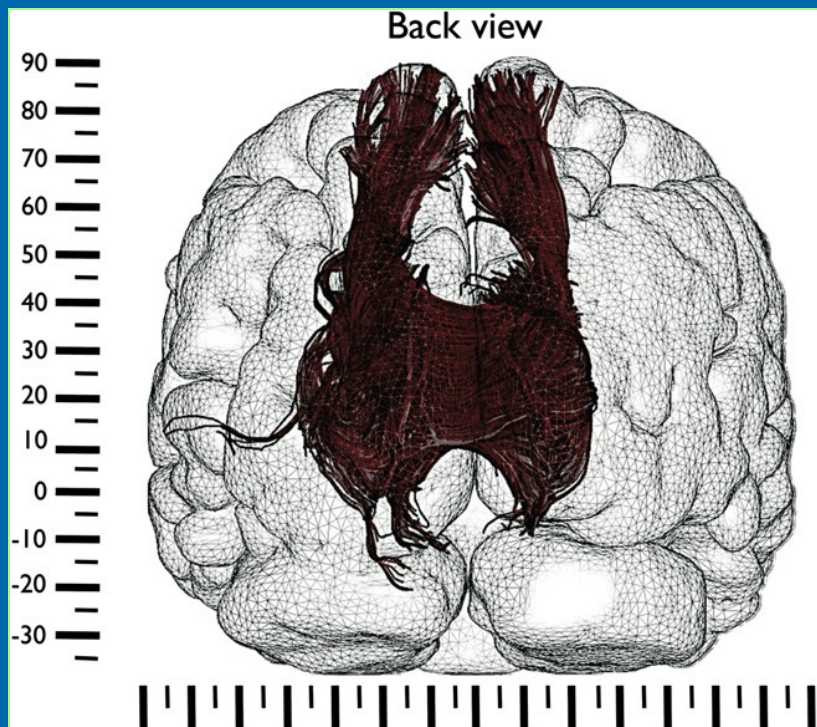
- red color indicates a laterolateral direction green color an anterior–posterior direction, and blue color a dorsal–ventral direction.
- Other colors indicate intermediate directions.



**ROIs legend**

A	Arcuate	Fx	Fornix body	SCP	Superior cerebellar peduncle
AC	Anterior Commissure	Fl	Fimbriae of fornix left	MCP	Middle cerebellar peduncle
CC	Corpus Callosum	T	Temporal	ICP	Inferior cerebellar peduncle
Ci	Cingulum	O	Occipital	DCN	Deep cerebellar nuclei
CP	Cerebral peduncle	IC	Internal capsule		
E	External/Estreme capsule				

# Corpus callosum



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# Material and methods (1)

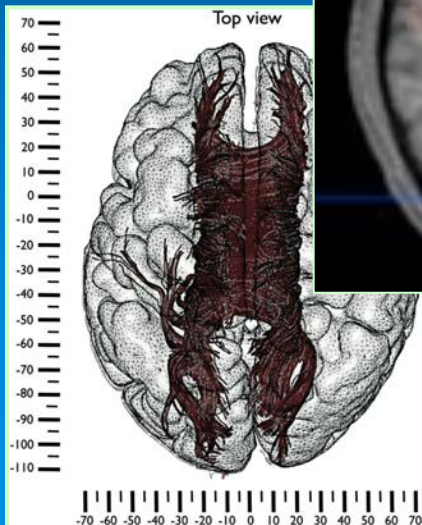
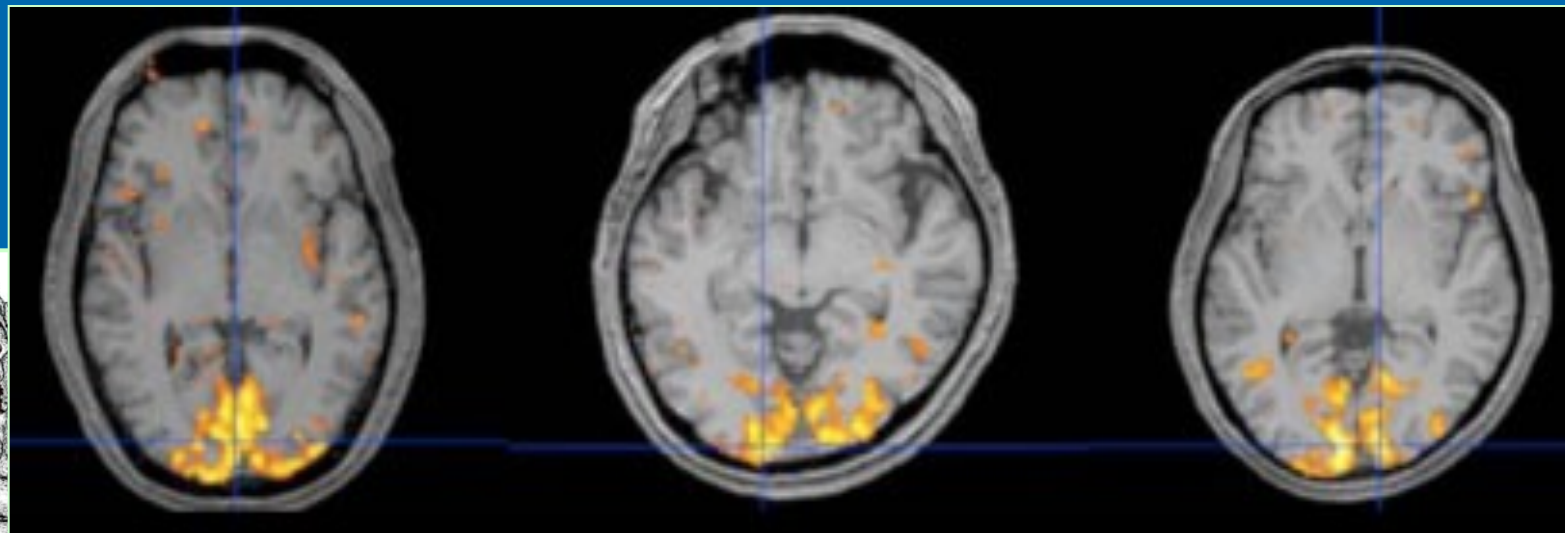
- **12 right-handed male subjects**
  - **34.3 ± 5.7 years old**
- **MRI data were acquired using echo-planar imaging at 1.5 T [..] with a standard head coil for signal reception.**
- **T1-weighted anatomical images were acquired [..]**
- **DTI axial slices acquisition parameters: repetition time 19 s; [..] voxel size 1.88x1.88x2 mm<sup>3</sup>, 200 independent directions, b-value 3000 s/mm<sup>2</sup>**

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# Material and methods (2)

- [...] The 12 data sets were spatially normalized and averaged [...]. Briefly, the method includes the following steps:
- i. registration of individual T1 images with the diffusion tensor data sets;
  - ii. normalization of the registered T1 using both linear and non-linear parameters;
  - iii. normalization of the diffusion tensor data sets using the deformation parameters derived from (ii);



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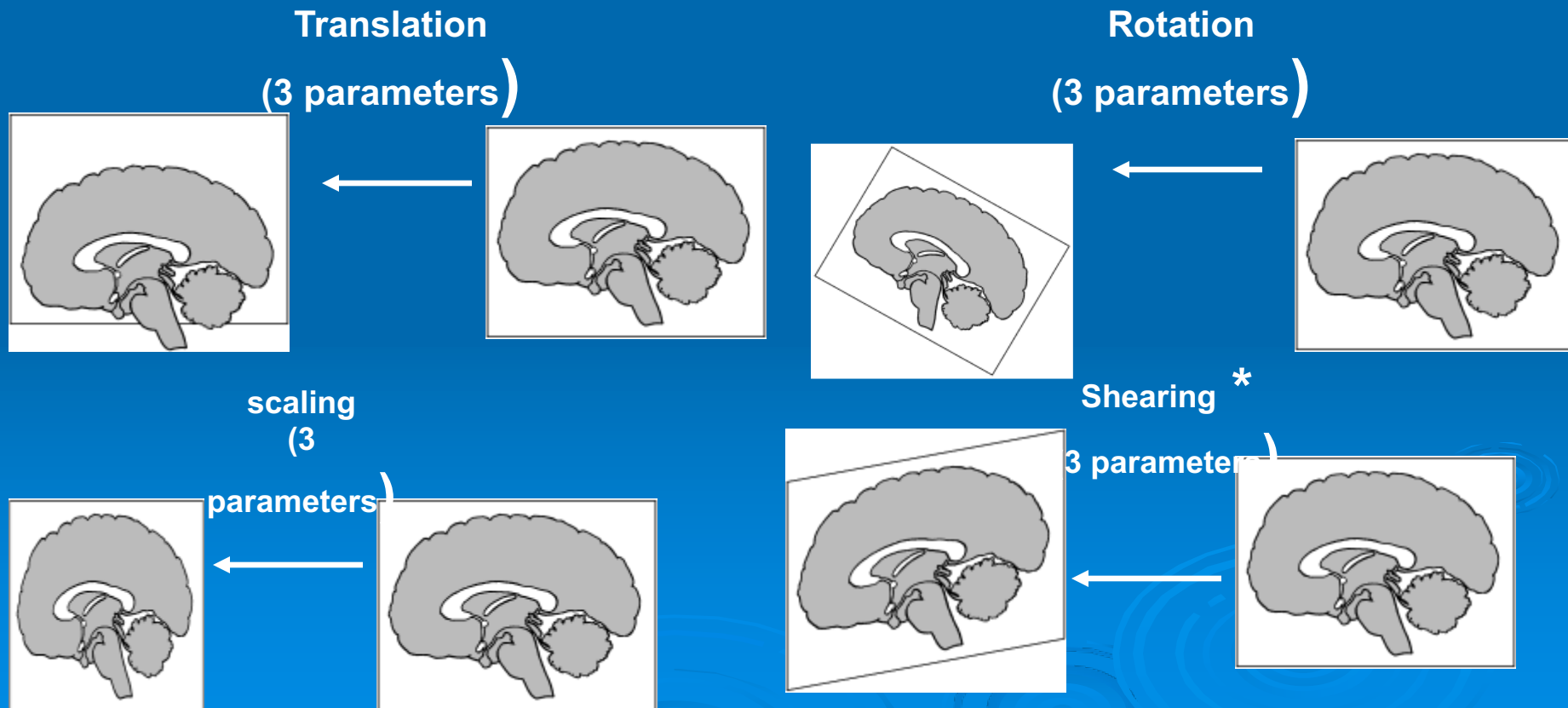
Marco Catani<sup>a,b,\*</sup> and Michel Thiebaut de Schotten<sup>a,b,c</sup>



# AFFINE REGISTRATION

An affine transform can include rotation, scaling, shearing and translation

Rigid registration includes only rotation and translation



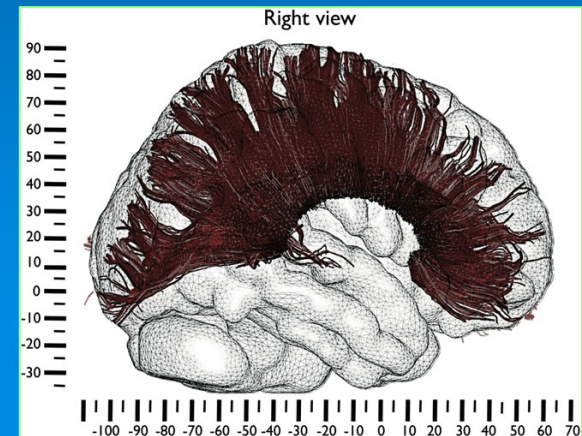
\* Shearing slides one edge of an image along the X or Y axis, creating a parallelogram

# Material and methods (3)

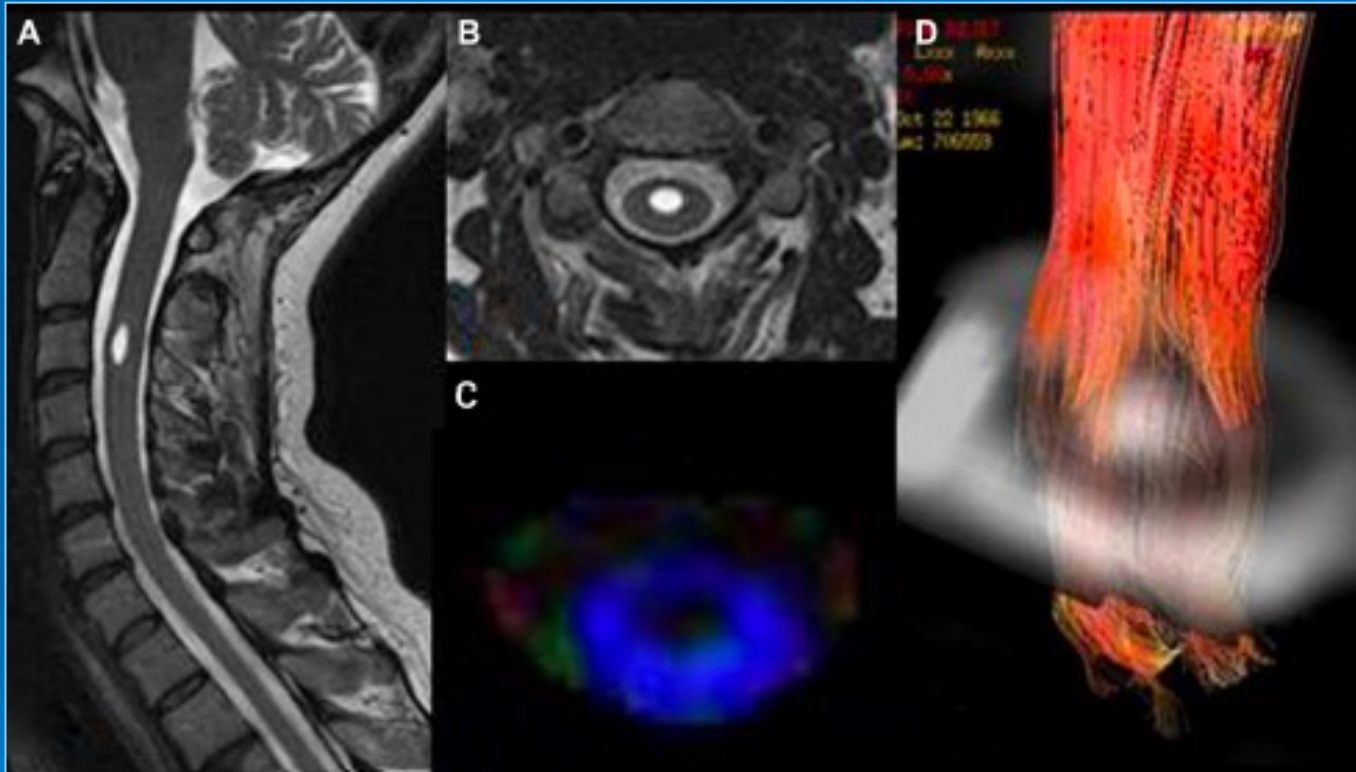
- [...] The 12 data sets were spatially normalized and averaged [...].
- For the normalization we used statistical parametric mapping software (SPM5, [www.fil.ion.ucl.ac.uk/](http://www.fil.ion.ucl.ac.uk/)) [..]
  - Images were spatially normalized to the standard T1 template provided in SPM5.
- The 3D tractography reconstructions of each tract were registered in the MNI space and visualized within a glass brain using BRAINVISA 3.0.2.

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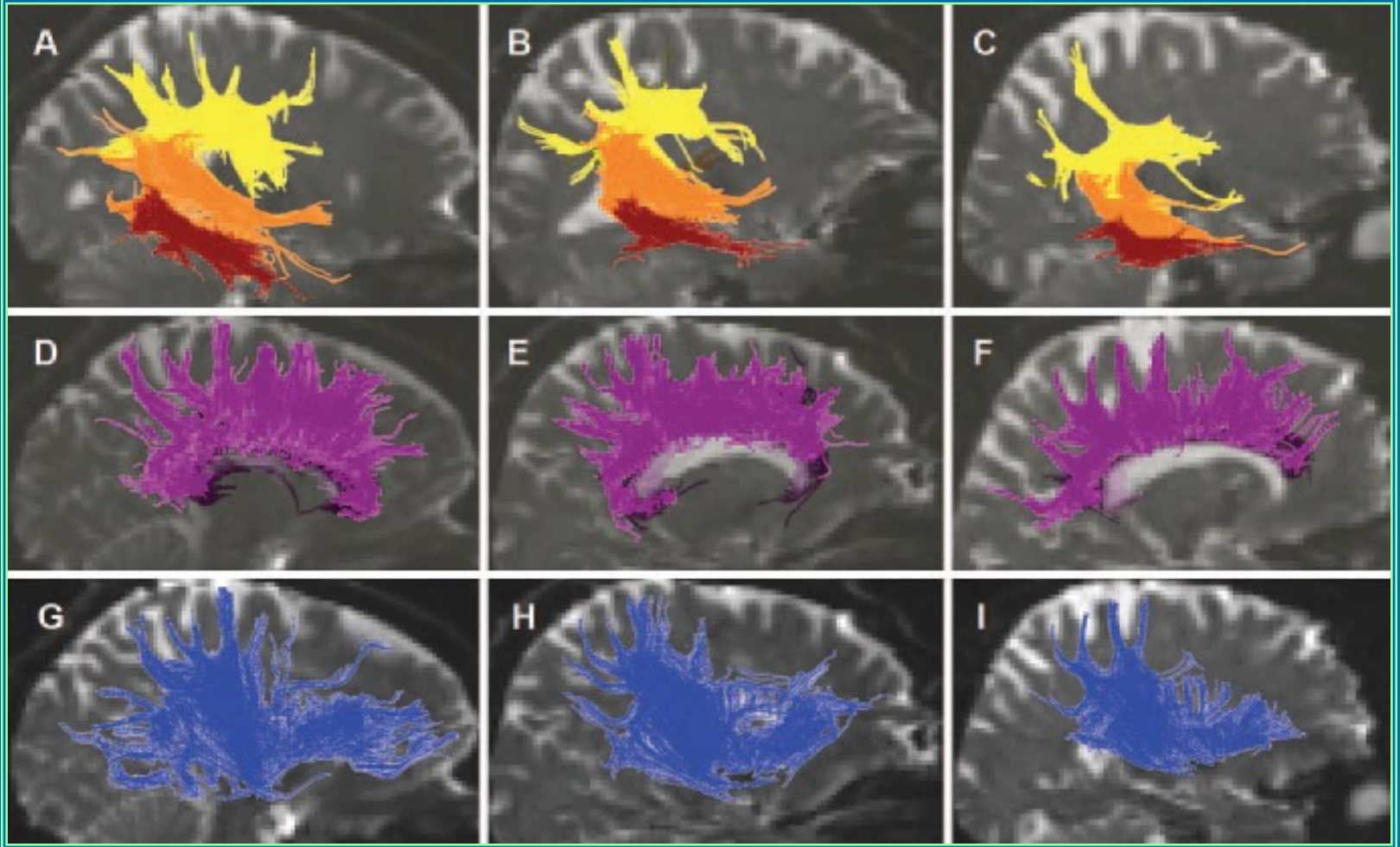


# Applications of DTI to spinal cord



- (A) and (B) T2-weighted images demonstrate a focal syrinx in the central spinal cord
- (C) FA map demonstrates no fiber tracts running through the lesion
- (D) Tractography shows displacement of the fiber tracts around the syrinx.

# Ageing



Representative sets of fiber-tracking results obtained in:

- ✓ A, D, G, a 25-year-old man
- ✓ B, E, H, a 55-year-old man
- ✓ C, F, I, an 81-year-old woman
- ✓ A–C, Association fibers are divided into superior longitudinal (**yellow**), inferior fronto-occipital (**orange**), and inferior longitudinal (**red**) fasciculi.
- ✓ D–F, Callosal fibers (**purple**)
- ✓ G–I, projection fibers (**blue**)