

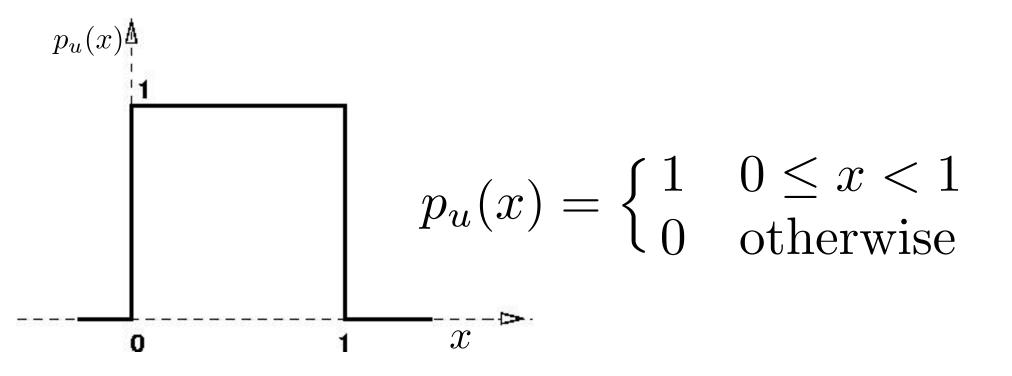
993SM - Laboratory of Computational Physics week V October 23, 2023

Maria Peressi

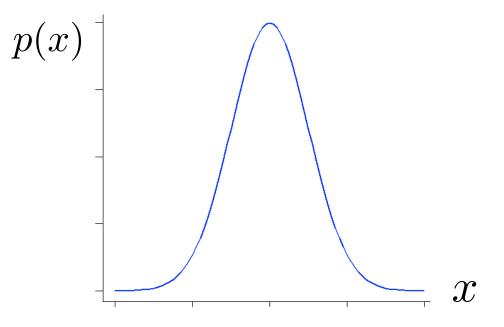
Università degli Studi di Trieste – Dipartimento di Fisica Sede di Miramare (Strada Costiera 11, Trieste) e-mail: <u>peressi@units.it</u> tel.: +39 040 2240242 Part I -Random numbers with non uniform distributions

M. Peressi - UniTS - Laurea Magistrale in Physics Laboratory of Computational Physics - week V last lecture:

generation of real (pseudo)random numbers with uniform distribution in [0;1[

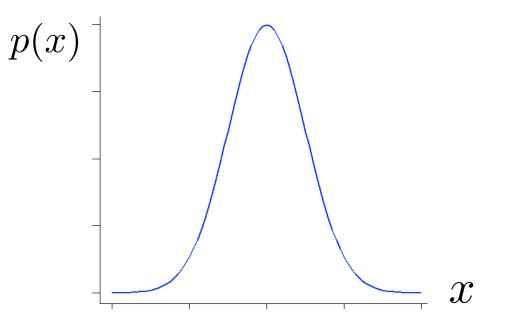


Random numbers with non uniform distributions:



How can we generate random numbers with a given distribution p(x)?

Random numbers with non uniform distributions:

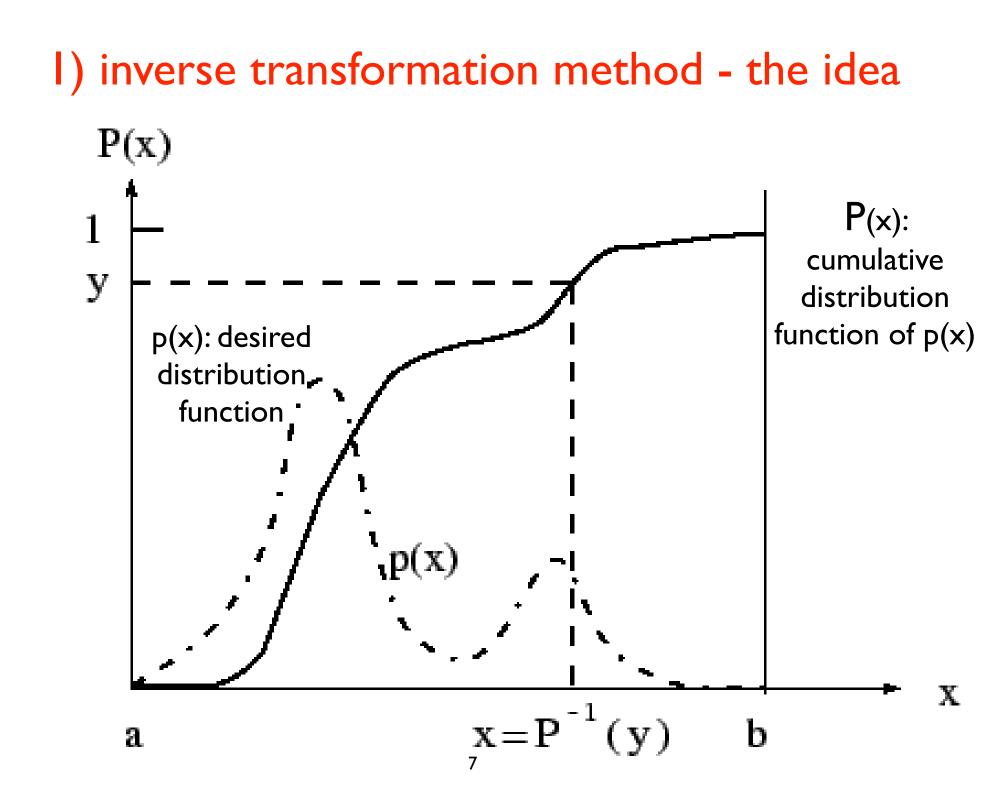


 inverse transformation method (general)
 rejection method (even more general)
 some "ad hoc" methods: the Box-Muller algorithm for the gaussian distribution; the central limit theorem I) inverse transformation method (general)

Problem: Generate sample of a random variable (or *variate*) X with a given distribution p.

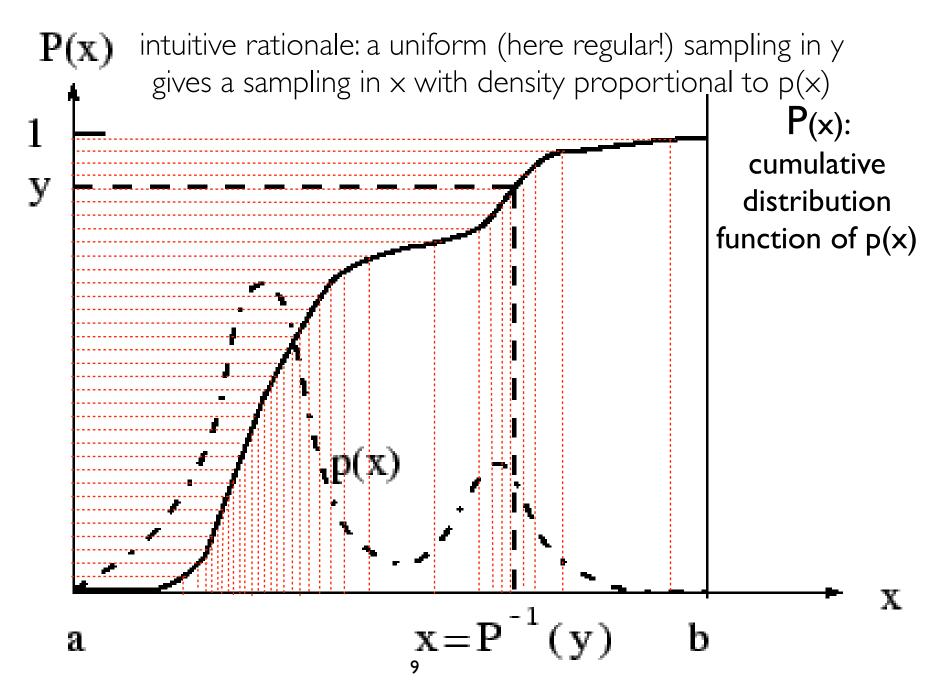
Solution: 2-step process

- \bullet Generate a random variate uniformly distributed in [0,1] .. also called a $\mathit{random\ number}$
- Use an appropriate transformation to convert the random number to a random variate of the correct distribution

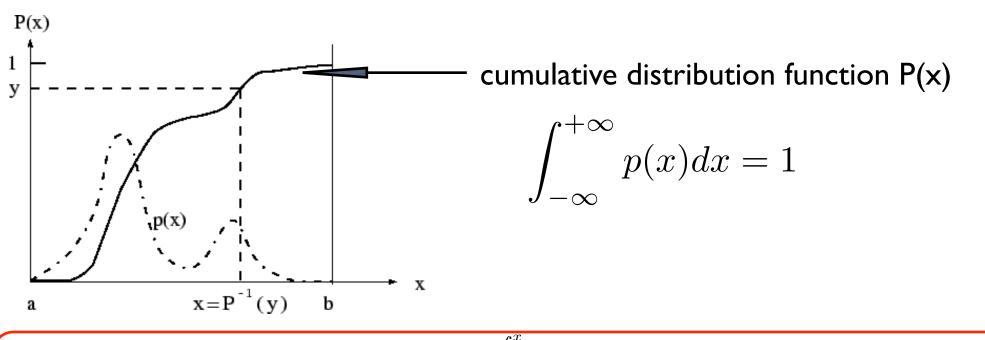


I) inverse transformation method - the idea intuitive rationale: a uniform (here regular!) sampling in y P(x)**P**(x): cumulative y distribution function of p(x)p(x) \mathbf{v}) a

I) inverse transformation method - the idea



I) inverse transformation method - algorithm



Let p(x) be a desired distribution, and $y = P(x) = \int_{-\infty}^{\infty} p(x')dx'$ the corresponding *cumulative distribution*. Assume that $P^{-1}(y)$ is known.

- Sample y from an equidistribution in the interval (0,1). (i.e., use $p_u(y)$)
- Compute $x = P^{-1}(y)$.

The variable x then has the desired probability density p(x).

$$y = P(x) \Longrightarrow dy = dP(x) \Longrightarrow p_u(y)dy = dP(x) \text{ (since } p_u(y) = 1 \text{ for } 0 \le y \le 1)$$

But : $dP(x) = p(x)dx$, therefore $p(x)dx = p_u(y)dy$

I) inverse transformation method - examples

$$\begin{array}{ll} \mathbf{p}(x) = \begin{cases} \frac{1}{b-a} & a \leq x \leq b \\ 0 & \text{otherwise} \end{cases} \\ y = P(x) = \begin{cases} \int_{a}^{x} \frac{1}{b-a} dx' = \frac{x-a}{b-a} & a \leq x \leq b \\ 1 & b-a dx' = \frac{x-a}{b-a} & a \leq x \leq b \\ x > b \end{cases} \\ x = y(b-a) + a \end{aligned}$$

$$\begin{array}{ll} \mathbf{p}(x) = \begin{cases} 0 & x \leq 0 \\ ae^{-ax} & x \geq 0 \\ 1 - e^{-ax} & x \geq 0 \end{cases} \\ y = P(x) = \begin{cases} 0 & x \leq 0 \\ 1 - e^{-ax} & x \geq 0 \\ 1 - e^{-ax} & x \geq 0 \end{cases} \\ x = -\frac{1}{a} \ln(1-y) \text{ or (same distribution!)} \end{cases} \\ x = -\frac{1}{a} \ln y \end{aligned}$$

I) inverse transformation method - examples

$$\begin{array}{ll} \mathbf{p}(x) = \begin{cases} \frac{1}{b-a} & a \leq x \leq b \\ 0 & \text{otherwise} \end{cases} \\ y = & P(x) = \begin{cases} \int_{a}^{0} \frac{1}{b-a} dx' = \frac{x-a}{b-a} & a \leq x \leq b \\ 1 & b-a & a \leq x \leq b \\ 1 & b-a & a \leq x \leq b \\ x > b & a \\ \end{array} \\ x = & y(b-a) + a \end{aligned}$$

$$\begin{array}{ll} \mathbf{p}(x) = \begin{cases} 0 & x \leq 0 \\ ae^{-ax} & x \geq 0 \\ 1 - e^{-ax} & x \geq 0 \\ \end{array} \\ y = & P(x) = \begin{cases} 0 & x \leq 0 \\ 1 - e^{-ax} & x \geq 0 \\ \end{array} \\ x = & -\frac{1}{a} \ln(1-y) & \text{or (same distribution!)} \\ x = & -\frac{1}{a} \ln y \\ \end{array}$$

Codes available on moodle

expdev.f90

subroutine expdev(x)

```
REAL, intent (out) :: x
REAL :: r
```

do

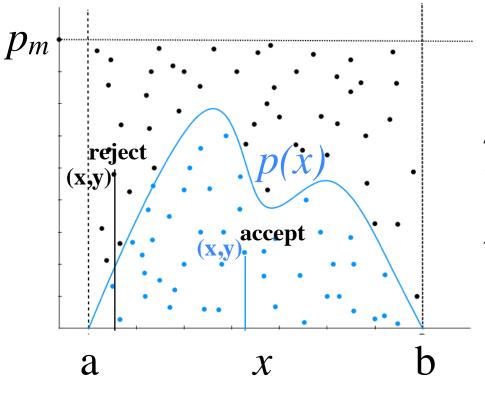
```
r is generated in [0,1[;
  call random number(r) but r=0 has to be discarded;
                             if r=0, generate another random number;
  if(r > 0) exit
                             if not, exit from the unbounded loop
end do
                             and calculate its log
x = -\log(r)
```

END subroutine expdev

2) rejection method (general)

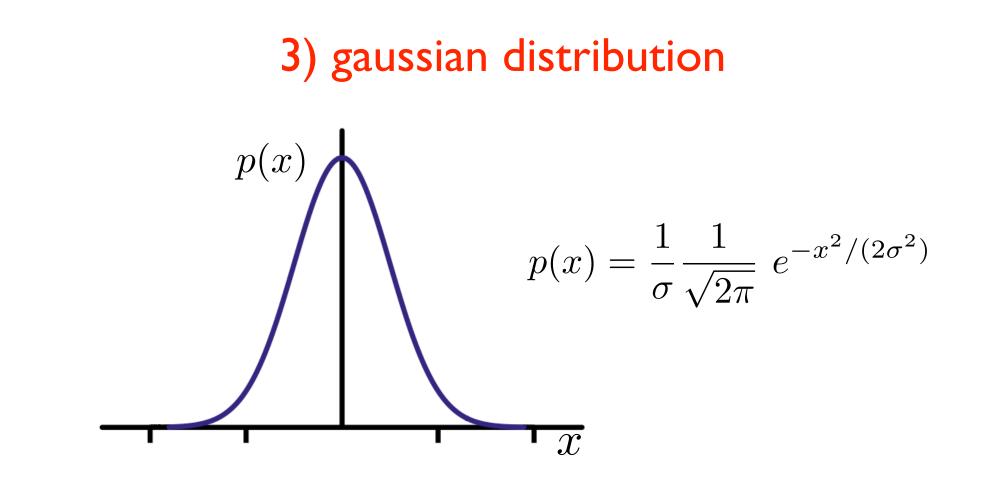
Let [a, b] be the allowed range of values of the variate x, and p_m the maximum of the distribution p(x).

- 1. Sample a pair of equidistributed random numbers, $x \in [a, b]$ and $y \in [0, p_m]$.
- 2. If $y \le p(x)$, accept x as the next random number, otherwise return to step 1.



Due to Von Newmann (1947). Applicable to almost all distributions. Can be inefficient if the area of the rectangle $[a,b] \otimes [0,p_m]$ is large compared to the area below the curve p(x)

[no exercises on that]



How to produce numbers with gaussian distribution?

- Inverse transformation method: impossible The cumulative distribution function P(x) cannot be analytically calculated!
- Rejection method: inefficient

$$p(x) = \frac{1}{\sigma} \frac{1}{\sqrt{2\pi}} e^{-x^2/(2\sigma^2)}$$

Hint: consider the distribution in 2D instead of ID (here $\sigma = I$):

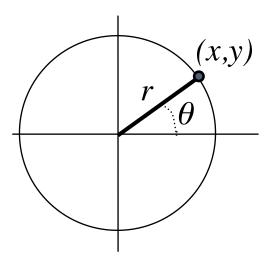
$$p(x)p(y)dxdy = (2\pi)^{-1} e^{-(x^2+y^2)/2} dxdy$$

$$p(x) = \frac{1}{\sigma} \frac{1}{\sqrt{2\pi}} e^{-x^2/(2\sigma^2)}$$

Hint: consider the distribution in 2D instead of ID (here $\sigma = I$):

$$p(x)p(y)dxdy = (2\pi)^{-1} e^{-(x^2+y^2)/2} dxdy$$

Use polar coordinates: $r=\sqrt{x^2+y^2}$, $heta=rctan\,(y/x)$; def.: $ho\equiv r^2/2$



$$p(x) = \frac{1}{\sigma} \frac{1}{\sqrt{2\pi}} e^{-x^2/(2\sigma^2)}$$

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Use polar coordinates: $r=\sqrt{x^2+y^2}$, $heta=rctan\,(y/x)$; def.: $ho\equiv r^2/2$

$$\rightarrow dxdy = r \ dr \ d\theta = d\rho \ d\theta$$

and therefore:

$$p(x)p(y) \ dx \ dy = p(\rho,\theta) \ d\rho \ d\theta = (2\pi)^{-1} \ e^{-\rho} \ d\rho \ d\theta$$

$$p(x) = \frac{1}{\sigma} \frac{1}{\sqrt{2\pi}} e^{-x^2/(2\sigma^2)}$$

Hint: consider the distribution in 2D instead of ID (here $\sigma = I$):

$$p(x)p(y)dxdy = (2\pi)^{-1} e^{-(x^2+y^2)/2} dxdy$$

Use polar coordinates: $r=\sqrt{x^2+y^2}$, $heta=rctan\,(y/x)$; def.: $ho\equiv r^2/2$

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and therefore:

$$p(x)p(y) \ dx \ dy = p(\rho,\theta) \ d\rho \ d\theta = (2\pi)^{-1} e^{-\rho} \ d\rho \ d\theta$$

If
$$\begin{cases} \rho \text{ exponentially distributed} \\ \theta \text{ uniformly distributed in}[0, 2\pi] \end{cases} \rightarrow \begin{cases} x = r \cos \theta = \sqrt{2\rho} \cos \theta \\ y = r \sin \theta = \sqrt{2\rho} \sin \theta \\ x, y \text{ have gaussian distribution} \\ \text{with } \langle x \rangle = \langle y \rangle = 0 \text{ and } \sigma = 1 \end{cases}$$

If $\begin{cases} \rho \text{ exponentially distributed} \\ \theta \text{ uniformly distributed in}[0, 2\pi] \end{cases} \rightarrow \begin{cases} x = r \cos \theta = \sqrt{2\rho} \cos \theta \\ y = r \sin \theta = \sqrt{2\rho} \sin \theta \\ x, y \text{ have gaussian distribution} \\ \text{with } \langle x \rangle = \langle y \rangle = 0 \text{ and } \sigma = 1 \end{cases}$

Recipe #1 (BASIC FORM):

$$\begin{cases} X, Y \text{ unif. distrib. in } [0,1[\\ \rho = -\ln(X) \text{ distributed with } p(\rho) = e^{-\rho} \\ \theta = 2\pi Y \text{ distributed with } (2\pi)^{-1} p_u \end{cases} \begin{cases} x = r \cos \theta = \sqrt{-2\ln X} \cos(2\pi Y) \\ y = r \sin \theta = \sqrt{-2\ln X} \sin(2\pi Y) \end{cases}$$

NOTE:

x, y are normally distributed and statistically independent. Gaussian variates with given variances σ_x ,

 σ_v are obtained by multiplying x and y by σ_x and σ_y respectively

If
$$\begin{cases} \rho \text{ exponentially distributed} \\ \theta \text{ uniformly distributed in}[0, 2\pi] \end{cases} \Rightarrow \begin{cases} x = r \cos \theta = \sqrt{2\rho} \cos \theta \\ y = r \sin \theta = \sqrt{2\rho} \sin \theta \\ x, y \text{ have gaussian distribution} \\ \text{with } \langle x \rangle = \langle y \rangle = 0 \text{ and } \sigma = 1 \end{cases}$$

 \mathbf{S}

Recipe #2 (POLAR FORM) (implemented in **boxmuller.f90**) :

 $X, Y \text{ uniformly distributed in } [-1,1]; \\ \text{take } (X,Y) \text{ only within the unitary circle;} \rightarrow \begin{cases} x = \sqrt{-2 \ln R^2} \frac{X}{R} \\ y = \sqrt{-2 \ln R^2} \frac{Y}{R} \\ y = \sqrt{-2 \ln R^2} \frac{Y}{R} \\ \text{since:} \\ \cos \theta = \frac{X}{R}, \sin \theta = \frac{Y}{R} \\ \text{Advantages: avoids the calculations of sin and cos functions} \end{cases}$

Codes available on moodle

boxmuller.f90

A look at the boxmuller.f90 code

```
SUBROUTINE gasdev(rnd)
  IMPLICIT NONE
  REAL, INTENT(OUT) :: rnd
  REAL :: r2, x, y
  REAL, SAVE :: g
  LOGICAL, SAVE :: gaus_stored=.false.
  if (gaus stored) then
                            Every two calls
    rnd=g
                            uses the random number
    gaus_stored=.false.
  else
                            already generated in the previous call
    do
      call random_number(x)
      call random_number(y)
                                           2 examples of optimization!
      x = 2.*x - 1.
      y=2.*y-1.
      r2=x**2+y**2
      if (r_2 > 0..and. r_2 < 1.) exit
    end do
                                             x = \sqrt{-2\ln R^2} \ \frac{X}{R} = X\sqrt{-2\ln R^2/R^2}
    r2=sqrt(-2.*log(r2)/r2) \longrightarrow since:
    rnd=x*r2
                                           (thus avoiding the calculation of
    g=y*r2
                                           another \sqrt{1} to calculate R separately)
    gaus_stored=.true.
  end if
END SUBROUTINE gasdev
```

A look at the gasdev.c code

```
#include <math.h>
float gasdev(long *idum)
{
    float ran1(long *idum);
                                Every two calls
    static int iset=0;
    static double gset;
                                uses the random number
    double fac,rsq,v1,v2;
                                already generated in the previous call
    if (iset == 0) {
        do {
                                         2 examples of optimization!
             v1=2.0*ran1(idum)-1.0;
             v2=2.0*ran1(idum)-1.0;
             rsq=v1*v1+v2*v2;
        } while (rsq >= 1.0 || rsq == 0.0);
        fac=sqrt(-2.0*log(rsq)/rsq); \longrightarrow since: x = \sqrt{-2 \ln R^2} \frac{X}{R} = X \sqrt{-2 \ln R^2/R^2}
        gset=v1*fac;
                                           (thus avoiding the calculation of
        iset=1;
        return (float)(v2*fac);
                                           another \sqrt{1} to calculate R separately)
    } else {
        iset=0;
        return (float)gset;
    }
}
```

Consider a continuous random variable x with probability density f(x). characterized by $\langle x^m \rangle = \int x^m f(x) \, dx$ and $\sigma_x^2 = \langle x^2 \rangle - \langle x \rangle^2$. Consider y s.t. y_n corresponding to the average of n values of x: $y = y_n = \frac{1}{n}(x_1 + x_2 + \ldots + x_n)$

Suppose that we make many measurements of y. The variable y is distributed according to a probability density $P(y) \neq f(x)$

quantities of interest are the mean $\langle y \rangle$, the variance $\sigma_y^2 = \langle y^2 \rangle - \langle y \rangle^2$, and P(y) itself.

The random variable:

$$y = y_n = \frac{1}{n}(x_1 + x_2 + \dots + x_n)$$

is distributed according to:

with: P(y): gaussian distribution $< y > = < x > \qquad \sigma_y \approx \sigma_x / \sqrt{n}$

(Therefore, the sample mean of a random sample is better than a single observation)

provided $\langle x \rangle$ and $\langle x^2 \rangle$ exist (finite) and n is large!

Analogously, is instead of considering the new random variable as the **average** we consider just the **sum:**

$$y = x_1 + x_2 + \ldots + x_n$$

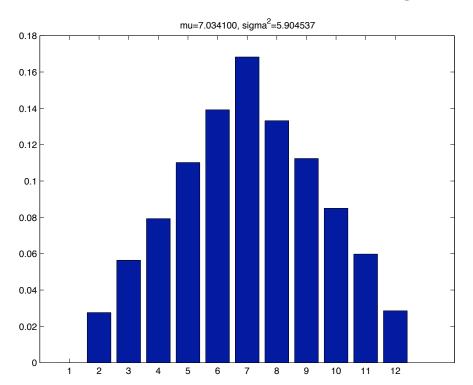
it also has a gaussian distribution but with:

$$\langle y \rangle = n \langle x \rangle$$
 and $\sigma_y \approx \sqrt{n} \sigma_x$

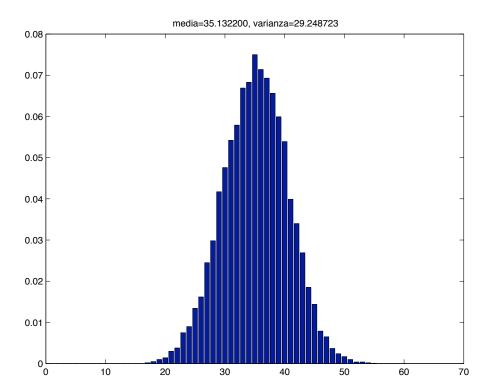
provided $\langle x \rangle$ and $\langle x^2 \rangle$ exist (finite) and n is large!

Note: large enough n needed to obtain the gaussian distribution. Suppose that f(x) is uniform: e.g., playing dice:

n=2 not enough



n=100 OK



The previous example was for UNIFORM distribution (dice) but the central limit theorem work also with random deviates x with NON UNIFORM distribution; e.g. with exponential distribution:

$$f(x) = \begin{cases} e^{-x}, & \text{if } x \ge 0\\ 0, if & x < 0 \end{cases}.$$

???

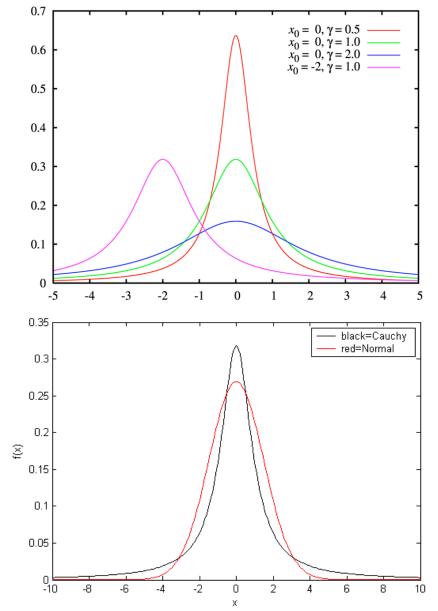
the central limit theorem

...but sometimes it doesn't work: **Cauchy-Lorentz** probability density function $f(x; x_0, \gamma) = \frac{1}{\pi \gamma \left[1 + \left(\frac{x - x_0}{\gamma}\right)^2\right]}$ $= \frac{1}{\pi} \left[\frac{\gamma}{(x - x_0)^2 + \gamma^2}\right]$

The Cauchy-Lorentz distribution is an example of "fat-tailed" distribution. Fat-tailed distributions decay to infinity slower than exponentially. For instance, they can decay with a power law:

 $f(x) \sim x^{-(l+a)}$ as $x \to +\infty$

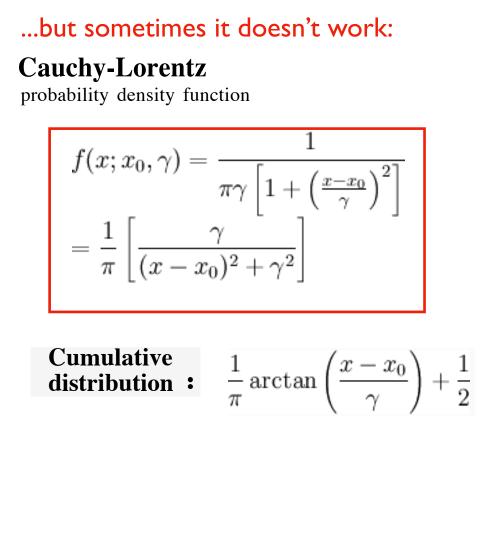
In some cases the expression "fat-tailed" indicates distributions where 0 < a < 2.

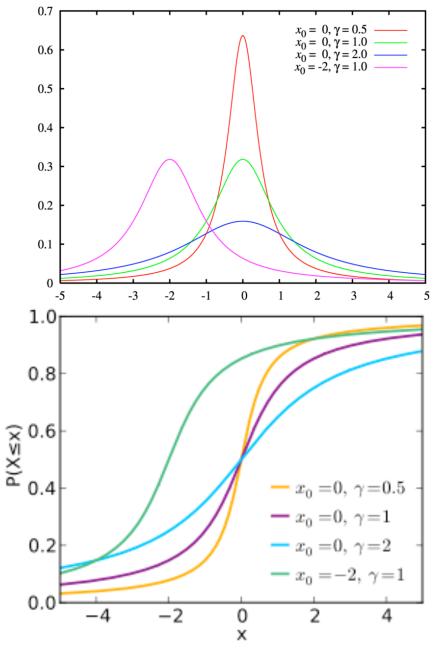


???

the central limit theorem

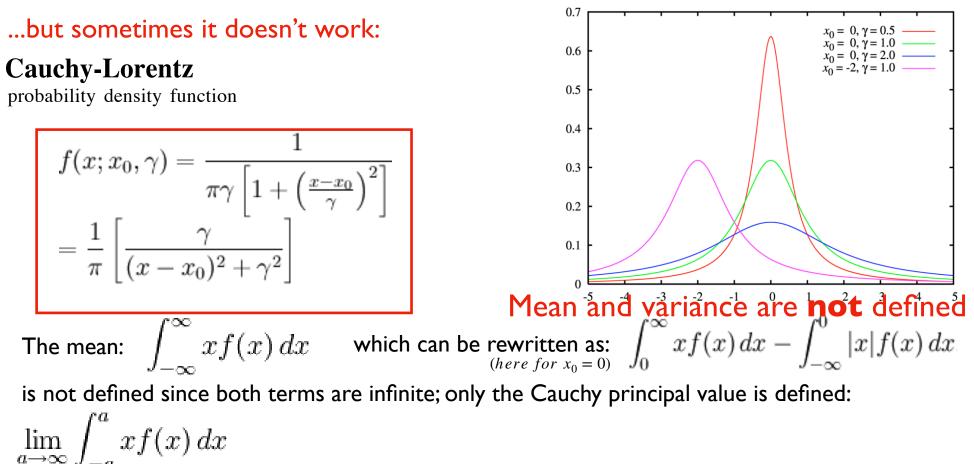
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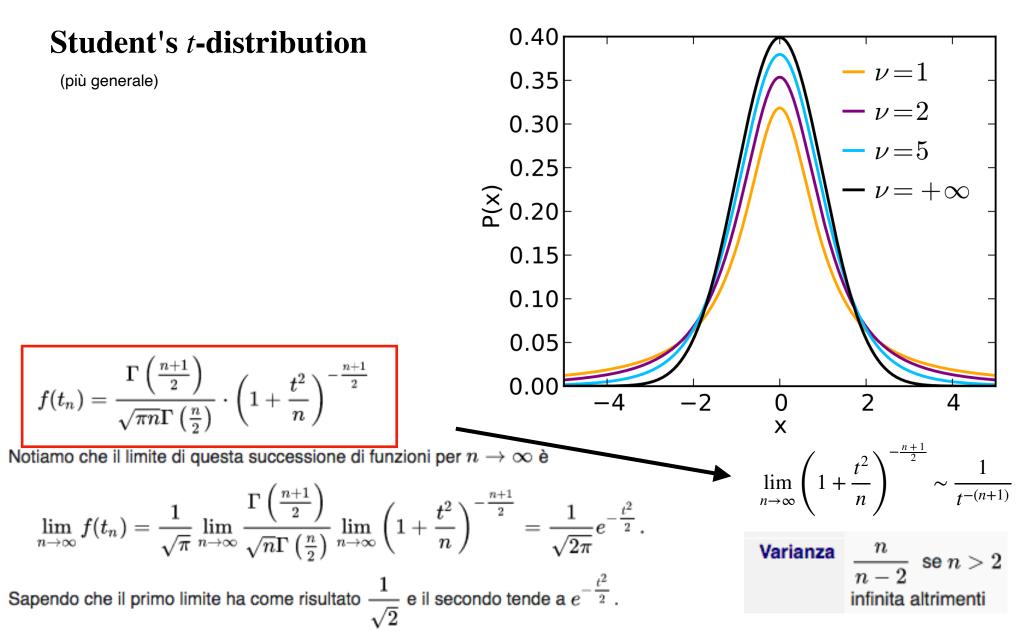
???

the central limit theorem



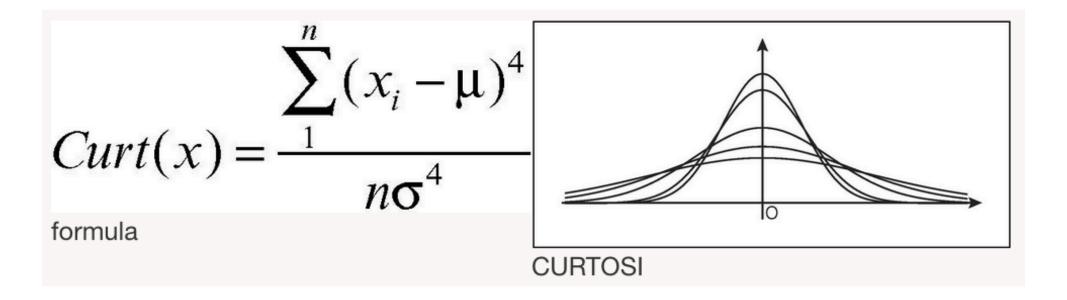
Without a defined mean, it is impossible to define the variance (but the second moment is defined and it is infinite). Some results in probability theory about expected values, such as the law of large numbers, do not work in such cases.

Also, the mean of a set of random variates drawn from a Cauchy distribution is no better than a single observation, because the chance of including extreme values is high.



In pratica, prendendo una popolazione di numerosità N molto grande, la variabile aleatoria t tende ad essere una normale standard.

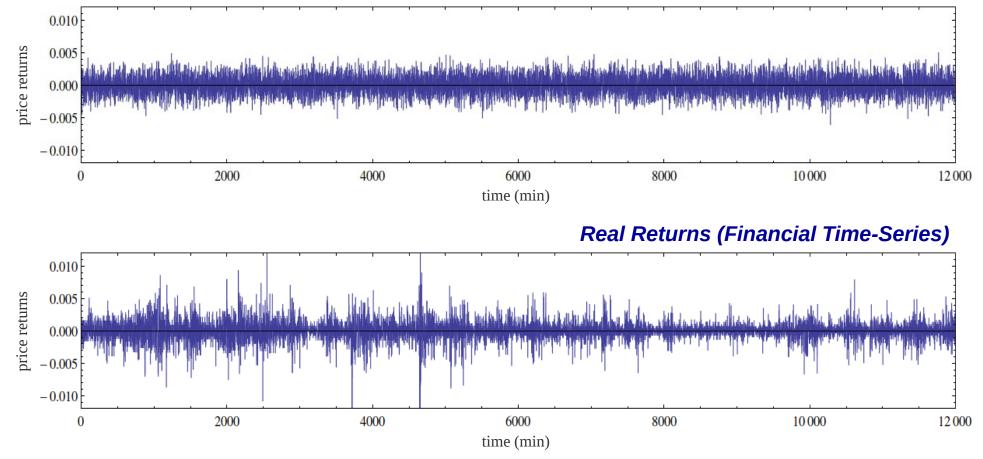
Curtosi (dal greco *kurtós*, gobba) in statistica, termine che indica quanto una distribuzione di dati si allontani da una curva normale standardizzata (cioè se è, rispetto a questa, per la quale l'indice è 0, più "schiacciata" o meno "schiacciata"). L'*indice di curtosi* per una distribuzione discreta X di *n* elementi è dato da:



... a short digression ...

Statistical Properties of Price Returns

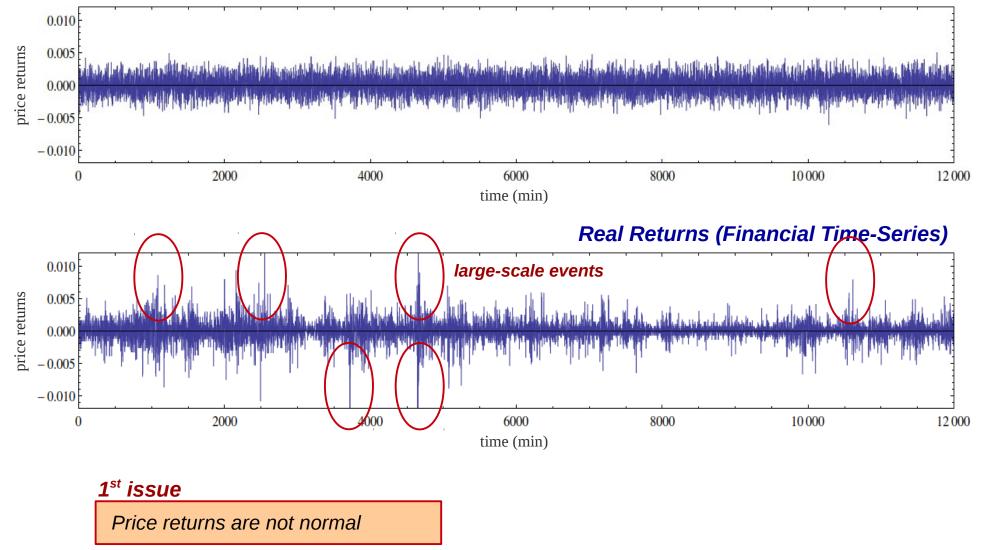
Simulated Returns (Geometric Brownian Motion)



Cont, Empirical properties of asset returns, stylized facts and statistical issues, 2001

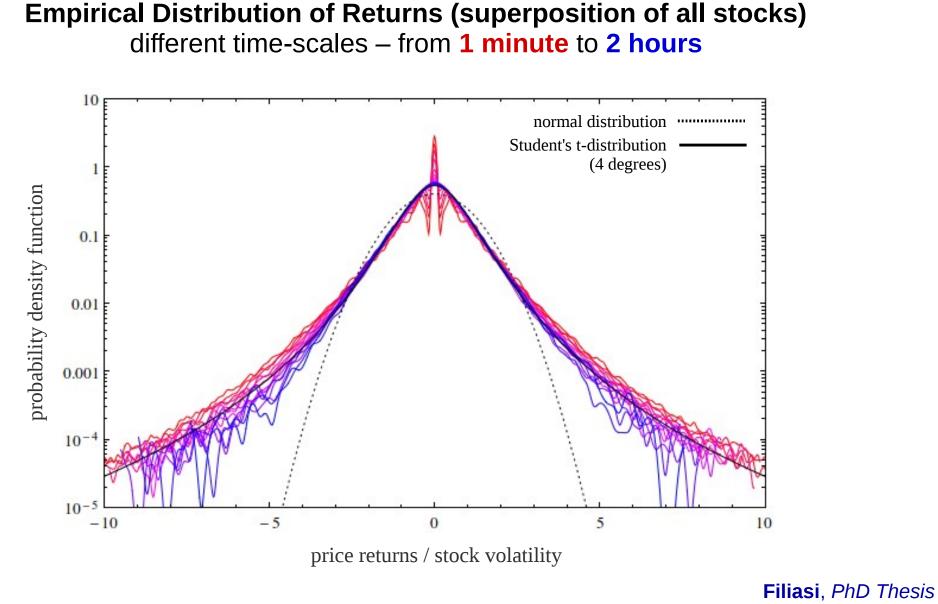
Statistical Properties of Price Returns

Simulated Returns (Geometric Brownian Motion)



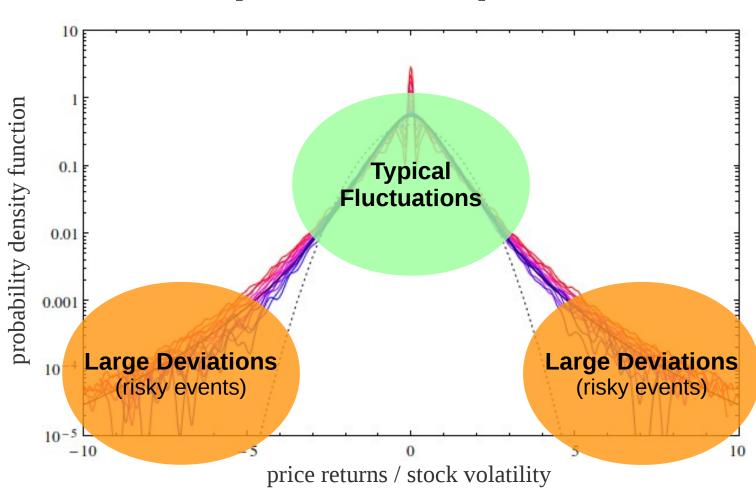
Cont, Empirical properties of asset returns, stylized facts and statistical issues, 2001

Empirical Distribution of Price Returns



Cont, Empirical properties of asset returns, stylized facts and statistical issues, 2001

Empirical Distribution of Price Returns



empirical distribution of price returns

Filiasi, PhD Thesis Cont, Empirical properties of asset returns, stylized facts and statistical issues, 2001 Part II -Using random numbers to simulate random processes

Random processes: radioactive decay

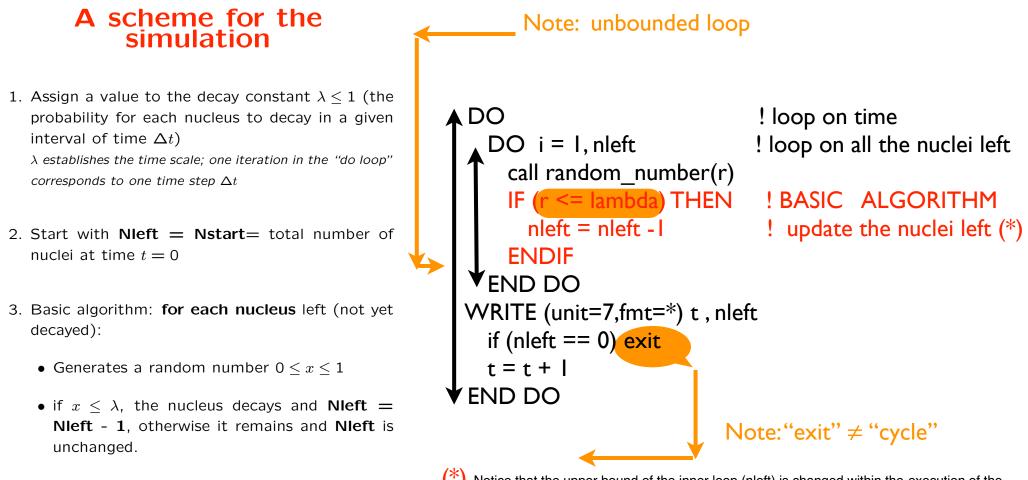
N(t) Atoms present at time t λ Probability for each atom to decay in Δt $\Delta N(t)$ Atoms which decay between t and $t+\Delta t$

$$\Delta N(t) = -\lambda N(t)\Delta t$$

we use the probability λ of decay of each atom to simulate the behavior of the number of atoms left; we should be able to obtain (on average):

$$N(t) = N(t=0)e^{-\lambda t}$$

Radioactive decay: numerical simulation



- 4. Repeat for each nucleus
- 5. Repeat the cycle for the next time step

(*) Notice that the upper bound of the inner loop (nleft) is changed within the execution of the loop; but with most compilers, in the execution the **loop** goes on up to the **initial value of the upper bound** (nleft); this ensures that the implementation of the algorithm is correct. The program checkloop.f90 is a test for the behavior of the loop. Look also at decay_checkloop.f90. If nleft would be changed (decreased) during the execution, the effect would be an overestimate of the decay rate. CHECK with your compiler!



decay.f90 decay_checkloop.f90

checkloop.f90

Details on Fortran: unbounded loops

[name:] DO exit [name]

or [name:] DO END DO [name]

(name is useful in case of nested loops for explicitly indicating which loop we exit from)

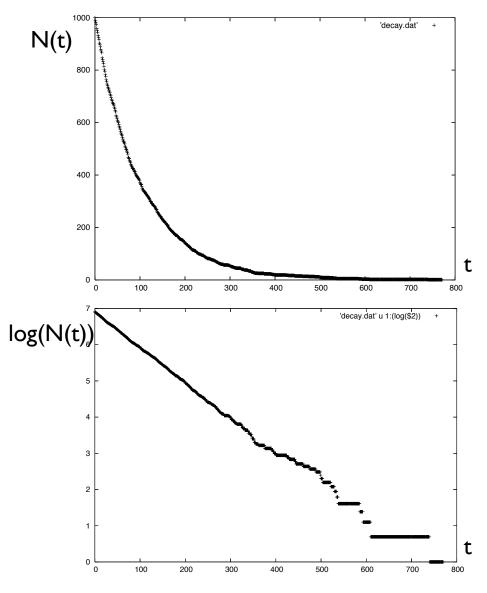
Alternative form: "do while" loop

Always set a condition to exit from a loop! E.g.: DO if (condition)exit END DO or: DO WHILE (.not. condition) ... END DO

NOTE: first is better ("if () ..exit" can be placed everywhere in the loop, whereas DO WHILE must execute the loop up to the end)

```
- Additional note:
Difference between EXIT and CYCLE
```

Radioactive decay: results of numerical simulation

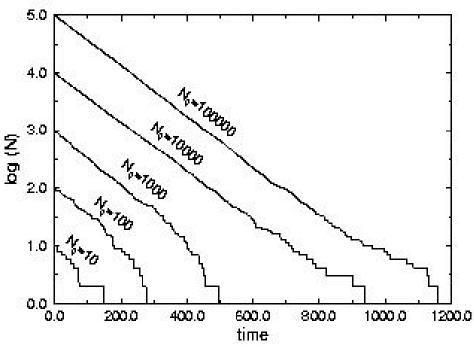


results of decay simulation (N vs t) with N=1000

 $N(t) \sim N_0 \exp(-a t)$

semilog plot (log(N) vs t)=> $log(N(t)) = log N_0 - a t$ => slope is -a

Radioactive decay: results of numerical simulation

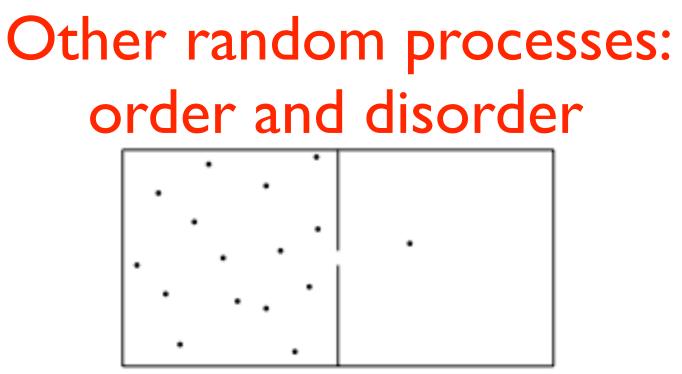


Semilog plots of the results of simulations for the same decay rate and different initial number of atoms: almost a straight line, but with important deviations (stochastic) for small N

Stochastic simulations give reliable results when obtained:

- on average and for large numbers
- fine discretisation of time evolution

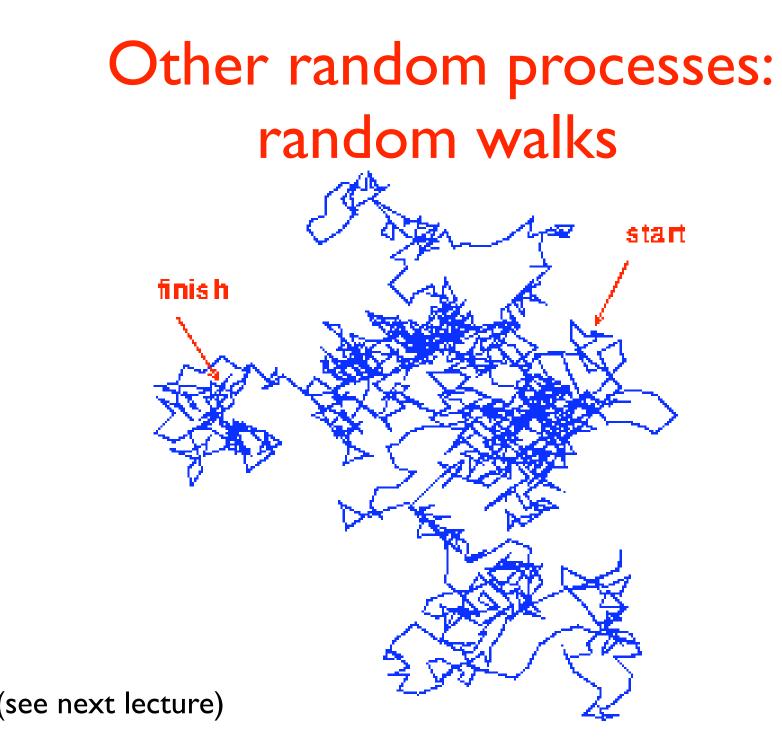
(in the exercise: change λ ; compare the value obtained from the simulation with the one inserted; does the "quality" of the results change with λ ?)



A box is divided into two parts communicating through a small hole. One particle randomly can pass through the hole per unit time, from the left to the right or viceversa.

 $N_{left}(t)$: number of particles present at time t in the left side Given $N_{left}(0)$, what is $N_{left}(t)$?

(more on that in a future Lecture)



miscellanea

list of EXERCISES; more on fortran90, fit, gnuplot...

LIST OF EXERCISES V week

Random numbers with non uniform distributions

I) exponential distribution generated with Inverse Transformation Method

2) another distribution generated with ad-hoc algorithms (compare!), including Inverse Transformation Method

3) gaussian distribution generated with Box-Muller algorithm

4) gaussian distribution generated with the central limit theorem

5) other random distributions (different algorithms, subroutines from the web...). [optional]

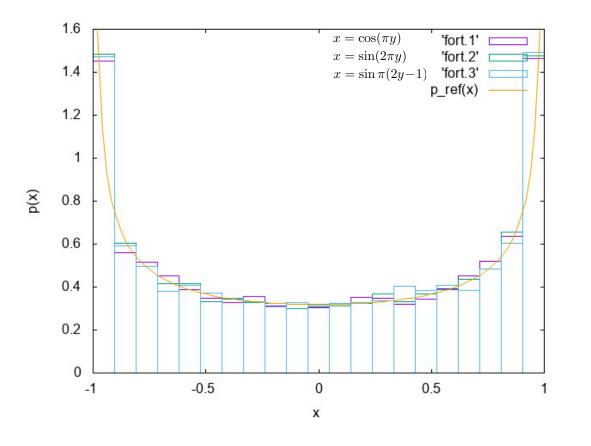
To do: implementation of the algorithms (or understanding...), histogram, fit...

Making histograms: use int() or similar intrinsic functions?

e.g. Ex. 2:

Suppose you want to generate a random variate x in (-1,1) with distribution

$$p(x) = \frac{1}{\pi}(1 - x^2)^{-1/2}.$$



$$y = P(x) = \int_{-1}^{x} \frac{1}{\pi} (1 - x^2)^{-1/2} dx$$
$$= \frac{1}{\pi} \arcsin(x) \Big|_{-1}^{x} = \frac{1}{\pi} \arcsin(x) + \frac{1}{2}$$

and invert...

Here:

different histograms, from distributions generated with different algorithms

=> how to do these histograms?

Making histograms: use int() or similar intrinsic functions?

AINT(A[,KIND])

 \cdot Real elemental function

 \cdot Returns A truncated to a whole number. AINT(A) is the largest integer which is smaller than |A|, with the sign of A. For example, AINT(3.7) is 3.0, and AINT(-3.7) is -3.0.

 \cdot Argument A is Real; optional argument KIND is Integer

ANINT(A[,KIND])

 \cdot Real elemental function

 \cdot Returns the nearest whole number to A. For example, ANINT(3.7) is 4.0, and AINT(-3.7) is -4.0.

 \cdot Argument A is Real; optional argument KIND is Integer

FLOOR(A,KIND)

- Integer elemental function
- Returns the largest integer \leq A. For example, FLOOR(3.7) is 3, and FLOOR(-3.7) is -4.
- Argument A is Real of any kind; optional argument KIND is Integer
- Argument KIND is only available in Fortran 95

INT(A[,KIND])

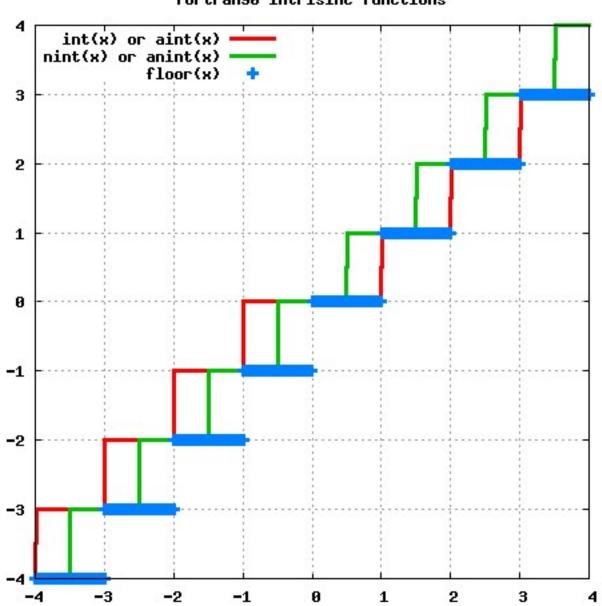
Integer elemental function

• This function truncates A and converts it into an integer. If A is complex, only the real part is converted. If A is integer, this function changes the kind only.

• A is numeric; optional argument KIND is Integer.

NINT(A[,KIND])

- Integer elemental function
- Returns the nearest integer to the real value A.
- \cdot A is Real



fortran90 intrisinc functions

Example: fit using gnuplot - I

Suppose you want to fit your data (say, 'data.dat') with an exponential function. You have to give: 1) the functional form ; 2) the name of the parameters

gnuplot> f(x) = a * exp(-x*b)

Then we have to recall these informations together with the data we want to fit: it can be convenient to inizialize the parameters:

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gnuplot> a=0.; b=1. (for example)

gnuplot> fit f(x) 'data.dat' via a,b

On the screen you will have something like:

```
Final set of parameters Asymptotic Standard Error
```

a = 1 +/- 8.276e-08 (8.276e-06%) b = 10 +/- 1.23e-06 (1.23e-05%)

correlation matrix of the fit parameters:

a b a 1.000 b 0.671 1.000

It's convenient to plot together the original data and the fit:

gnuplot> plot f(x), 'data.dat'

Example: fit using gnuplot - II

If you prefer to use linear regression, **use logarithmic data in the data file**, **or** directly fit the log of the original data using **gnuplot**:

gnuplot> f(x) = a + b*x

. . .

Then we have to recall these informations together with the data we want to fit (in the following example: x=log of the first column; y=log of the second column):

gnuplot> fit f(x) 'data.dat' u (log(\$1)):(log(\$2)) via a,b

Also in this case it will be convenient to plot together the original data and the fit:

gnuplot> plot f(x), 'data.dat' u (log(\$1)):(log(\$2))

In case of needs, we can limit the set of data to fit in a certain range [x_min:x_max]:

gnuplot> fit [x_min:x_max] f(x) 'data.dat' u ... via ...

A few notes on Fortran

related to the exercises

Intrinsic functions:

LOGARITHM

log returns the natural logarithm
log 10 returns the common (base 10) logarithm
(NOTE: also in gnuplot, log and log 10 are defined with the same meaning)

INTEGER PART

nint(x) and the others, similar but different (see Lect. II) =>
ex. II requires histogram for negative and positive data values

Arrays:

possible to label the elements from a negative number or 0: **dimension array(-n:m)** (e.g., useful for making histograms) [default in Fortran: n=1; in c and c++: n=0]

Array dimension:

default : dimension array([1:]n)
but also using other dimensions e.g.:

dimension array(-n:m)

Important to **check dimensions** of the array when compiling or during execution ! If not done, it is difficult to interpret error messages (typically:

"segmentation fault"), or even possible to obtain unpredictable results!

Default in gfortran: boundaries not checked; use **compiler option**:

gfortran -fcheck=bounds myprogram.f90

(obsolete but still active alternative: -fbounds-check)

Typing (Unix line command):

man gfortran

you can scroll the manual pages and see the possible compilation options

Some Fortran compiler options

. . .

-fcheck=bounds enables checking for array subscript expressions

- -fbacktrace generate extra information to provide source file traceback at run time Specify that, when a runtime error is encountered or a deadly signal is emitted (segmentation fault, illegal instruction, bus error or floating-point exception), the Fortran runtime library should output a backtrace of the error. This option only has influence for compilation of the Fortran main program.
- -Wall Enables commonly used warning options

Structure of a main program with one function or subr.

program name_program implicit none (*) <declaration of variables> <executable statements> (see: expdev.f90 or boxmuller.f90)

```
contains
subroutine ... (or function)
...
end subroutine
```

end program

(*) General suggestion for variable declaration: Use "implicit none" + explicit declaration of variables

See also the use of module

Other programs:

(optional, but useful!)

random.f90 (is a module - generation of rnd with different distributions) t_random.f90 (main test program)

to compile:

\$gfortran random.f90 t_random.f90
(the module first!)

or in more than one step: Compile the module with the option -c: this produces .mod and .o (the objects): gfortran -c random.f90

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Compile the main program:

gfortran -c t_random.f90

Finally you link all the files *.o and produce the executable:

gfortran -o a.out random.o t_random.o