

FINANCIAL MARKETS AND INSTITUTIONS
A.Y. 2023/24

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# A2. INTEREST RATES

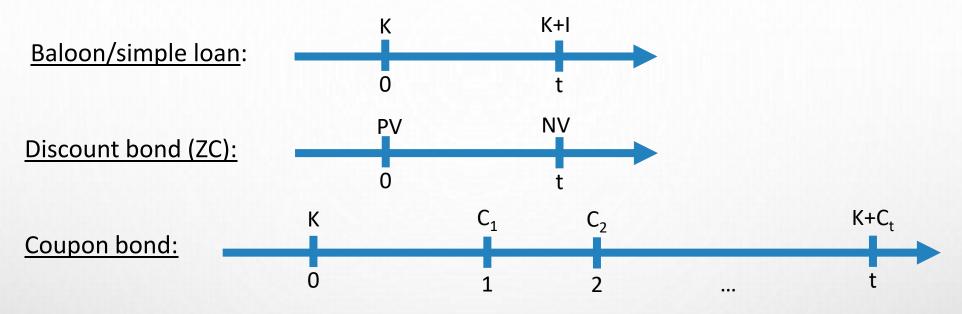


- WHY IR AND HOW DO WE MEASURE THEM?
- REAL IR: WHY ARE THEY IMPORTANT?
- HOW DO WE USE IR TO MEASURE RETURNS AND RISKS?
- CAN WE PREDICT INTEREST RATES?

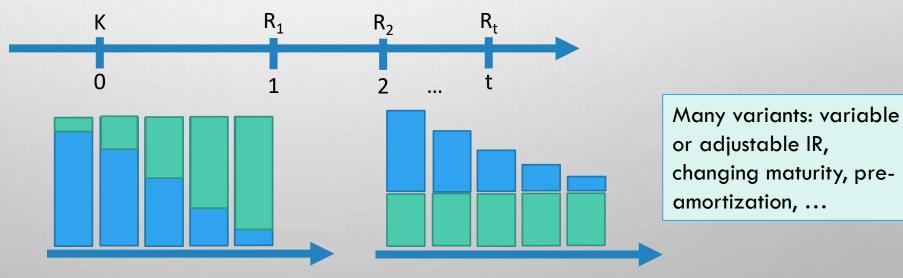
# MEASURES OF IR



# IR AND FINANCIAL CONTRACTS



### Fully amortised loan:



## MEASURES OF IR



How to compare different debt instruments?

### Yield to maturity (YTM)

- Strikes a balance across cashflows
- For simple loans only it equals the nominal rate

• ZC: 
$$YTM = \sqrt[n]{\frac{FV}{CV}} - 1$$

• Coupon bonds (and others):  $CV = \sum_{t=1}^{n} \frac{CF_t}{(1+YTM)^t}$   $VA = \sum_{t=1}^{n} \frac{C_t}{(1+YTM)^t} + \frac{FV}{(1+YTM)^n}$ 

• + YTM, - CV: an increase in IR lowers the current value (and v.v.)

## ISSUES WITH THE YTM



#### YTM:

- Assumes holding period equals maturity
- Assumes reinvesting at the same rate
- Nominal!

Risks and opportunity costs?

Yields vary over time!

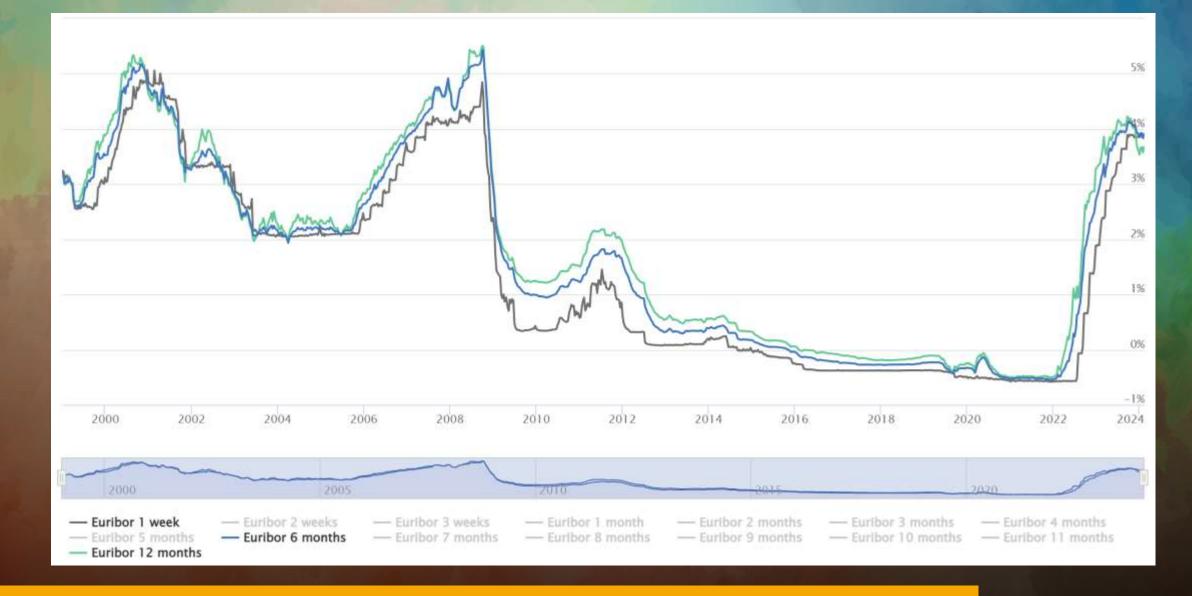
Real values matter more...

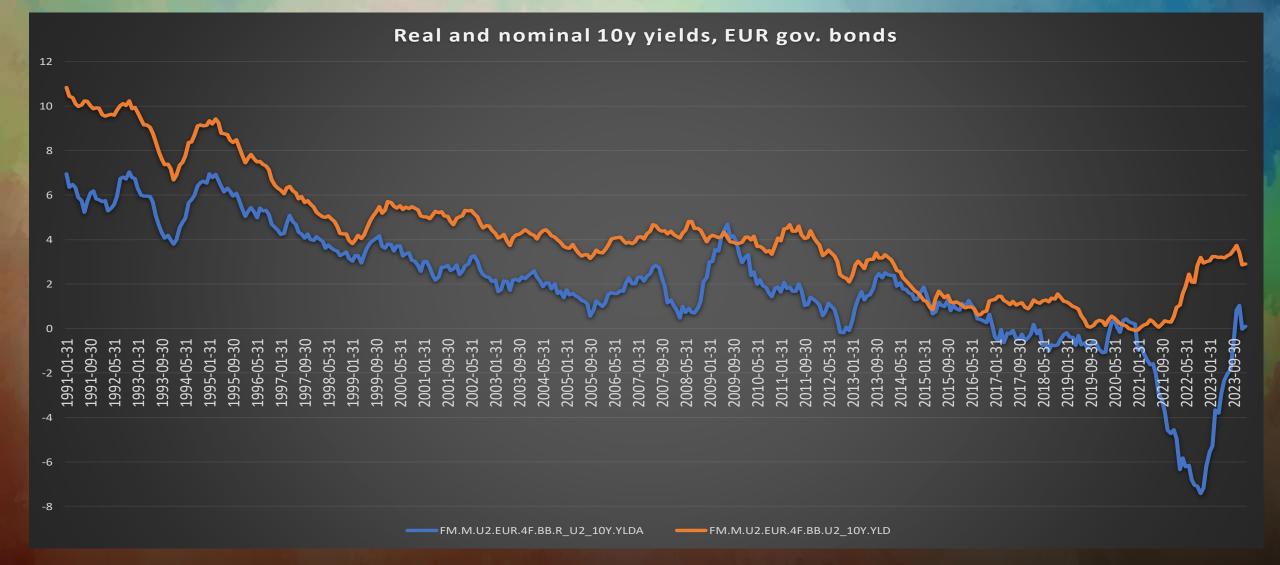
Ex-ante real IR consider the expected change in price levels (effective IR):

$$i_n = i_r + \pi^e [+i_r \cdot \pi^e]$$

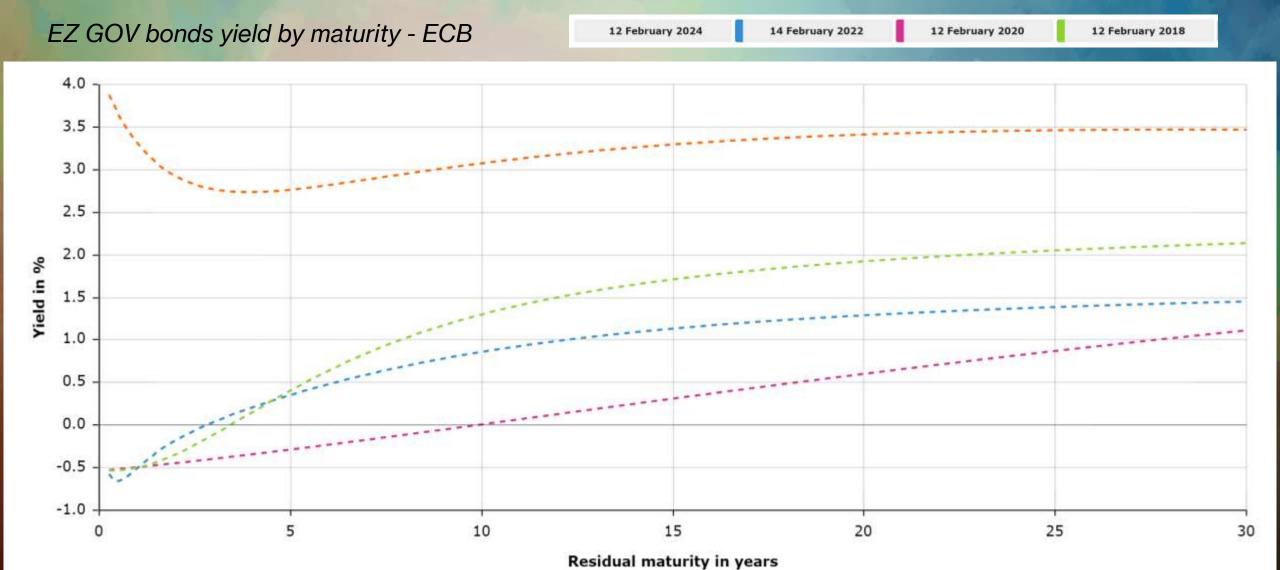
Ex-post real IR consider effective inflazione (but when the transaction is over!)

Then, tax issues may have impacts (charges on interest income, discounts on interest expense)





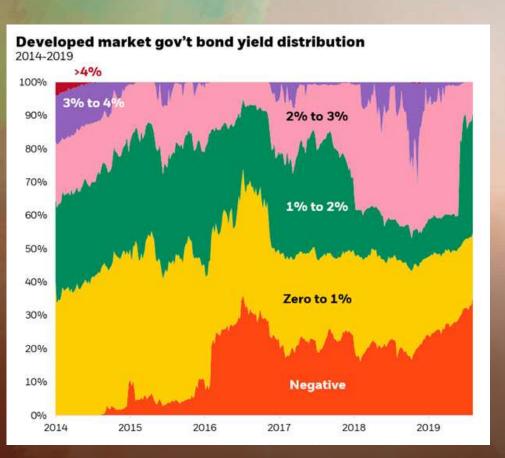
### **EXAMPLES**

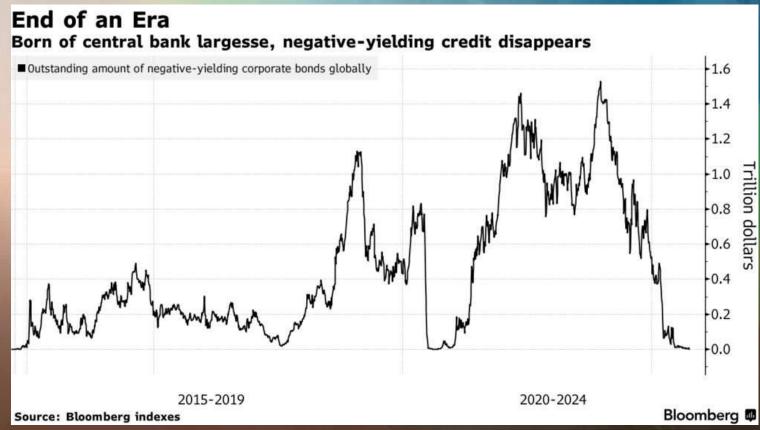


## **NEGATIVE RATES?**

- "Paying for lending? Nobody can be that stupid..."
  - CB: BCE -0.2% on deposits from 9/2014 (also DEN, SWE, CH)
  - GOV: DE, NED, SWE, DEN, CH, AUT, ... some (FIN, DE) from issue (2/2015)
  - Firms: Nestlé experienced it on 4y € bonds (2/2015)
  - Retail: Jyske Bank sold 10y mortgages at -0,5% (8/2019)
- "But for borrowers this is great!"
  - Lenders less likely to lend, credit institutions at a loss
  - Search for higher yields → riskier! (Zombie firms)
  - Trading/currency wars?
- Any sense?
  - Real IR negative are the real problem (rare and short, but today?)
  - Cash reserves and access to payment systems costs (or is worth something)
  - Access to central bank operations requires bonds
  - Taxes are levied on nominal returns
  - Nominal and real IR are rooted on expectations...







## IR AND PERFORMANCE

- Rate of return: payments to the owner of a security plus the relative change in value
- IR and RoR differ because of capital gains:

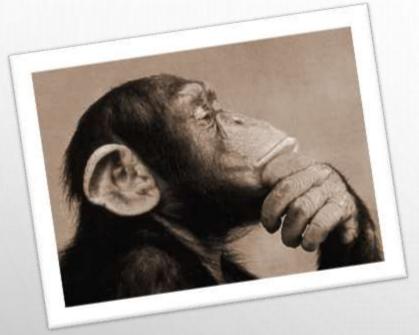
$$RoR = \frac{C + P_{t+1} - P_t}{P_t} = \frac{C}{P_t} + \frac{P_{t+1} - P_t}{P_t} = i_c + g$$





- If holding period equals time to maturity, return equals YTM only for ZCs: reinvestment risk (if holding period is longer, even more reinvestment risk)
- The bigger the time to maturity, the bigger the effect on capital gains due to changes in IR: <u>interest-rate risk</u>
- Inverse relationship between IR and capital gains
- Even if <u>unrealised</u>, capital gains represent an <u>opportunity cost</u>

## IR AND RISKS: DURATION



How to compare IR risks in debt instruments with different features?

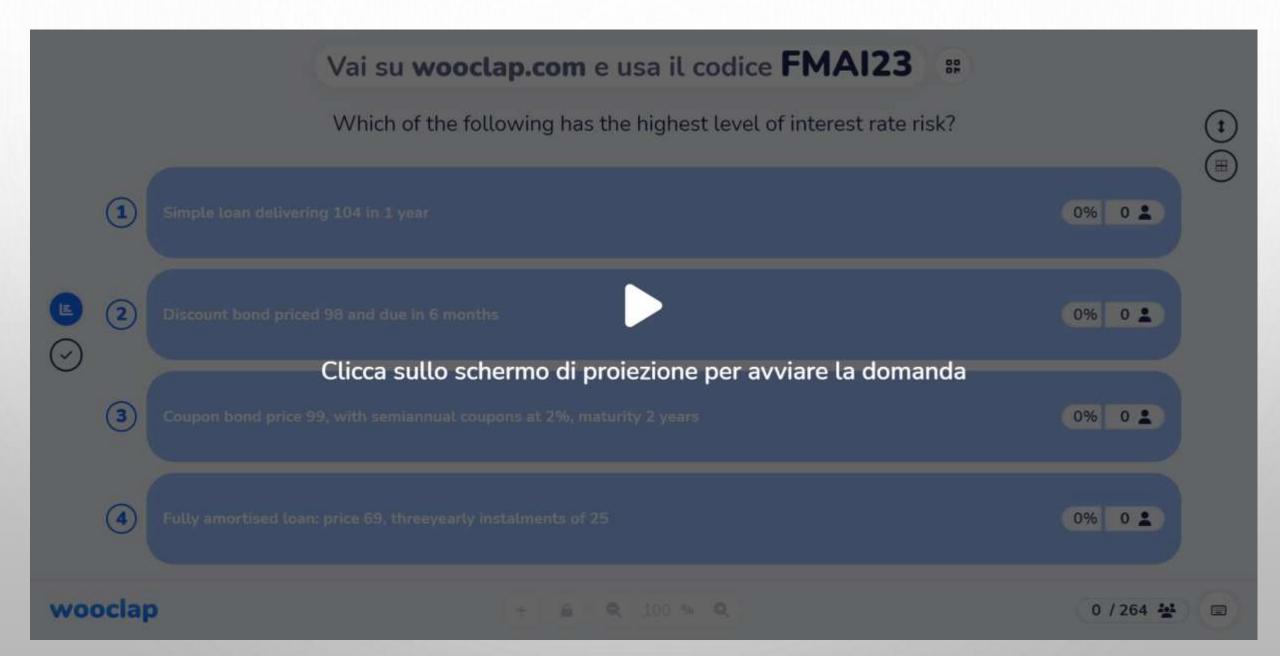
- Closer maturities and larger coupons lead to smaller losses if IR change
- BUT, bonds with similar maturities have also other risks (f.i. IT/DE spread), or even if maturities are different they may incur similar risks
- **How to compare them?** Weighting the time to maturity of each CF (effective maturity, or duration)
- **ZC** are simple: one flow, then DUR equals the TTM
- Other instruments can be considered as portfolios of ZC (since *duration* is additive):

$$DUR = \frac{\sum_{t=1}^{n} \frac{FC_{t}}{(1+i)^{t}} \cdot t}{\sum_{t=1}^{n} \frac{FC_{t}}{(1+i)^{t}}} + \text{maturity, - cashflows, + interest} = + \text{duration}$$

• And finally, duration proxies interest rate risks:

$$\% \Delta P = \frac{(P_{t+1} - P_t)}{P_t} = -DUR \cdot \frac{\Delta i}{(1+i)}$$

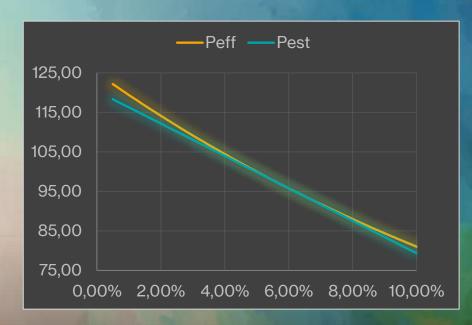
## IR AND RISKS



#### **ISSUES WITH DURATION**

Linear proxy of a convex relationship between P and i





Example: bond 5y annual coupon 6% (= mkt) P=95,79 and MD=-4,28 If  $\Delta i=1\%$ ,  $P_{\rm eff}=91,80$  and  $P_{\rm est}=91,69$ 

Duration as the 1st derivative... convexity as the 2nd!

$$CON = \frac{1}{P \cdot (1+i)^2} \cdot \sum_{t=1}^{N} \left[ \frac{CF_t}{(1+i)^t} \cdot (t^2 + t) \right]$$

### **EXAMPLES**

## FORECASTING IR

#### Why do interest rates change?

#### • Bonds' demand:

- (+) Wealth owned by an individual
- (+) Expected return relative to other assets
- (–) Expected future interest rates
- (–) Expected future inflation
- (–) Risk (uncertain return) relative to other assets
- (+) Liquidity relative to other assets

#### • Bonds' supply:

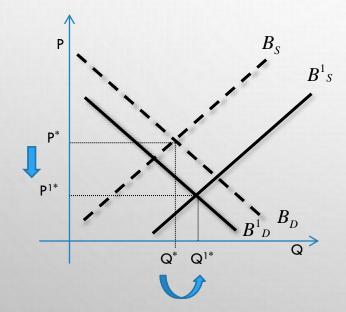
- (+) Profitability of investments (more earnings)
- (+) Expected inflation (cheaper borrowing)
- (+) Government deficits (more public debt)

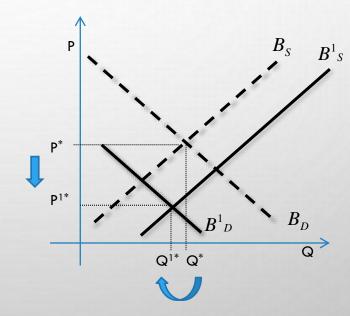


# FORECASTING IR

### Changes in IR due to inflation:

- An increase in expected inflation affects simultaneously demand (decrease of expected return) and supply (cheaper borrowing)
- IR will increase (prices fall)
- Effect on quantity is not readily predictable

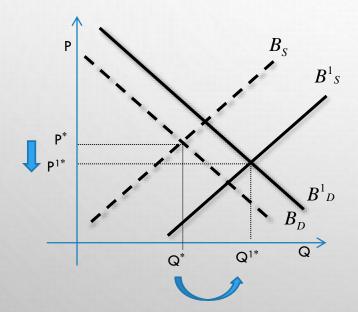


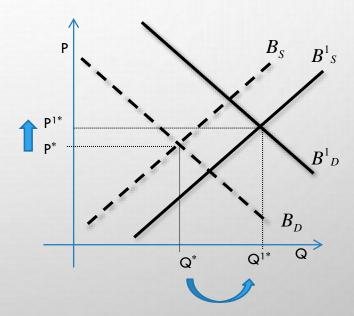


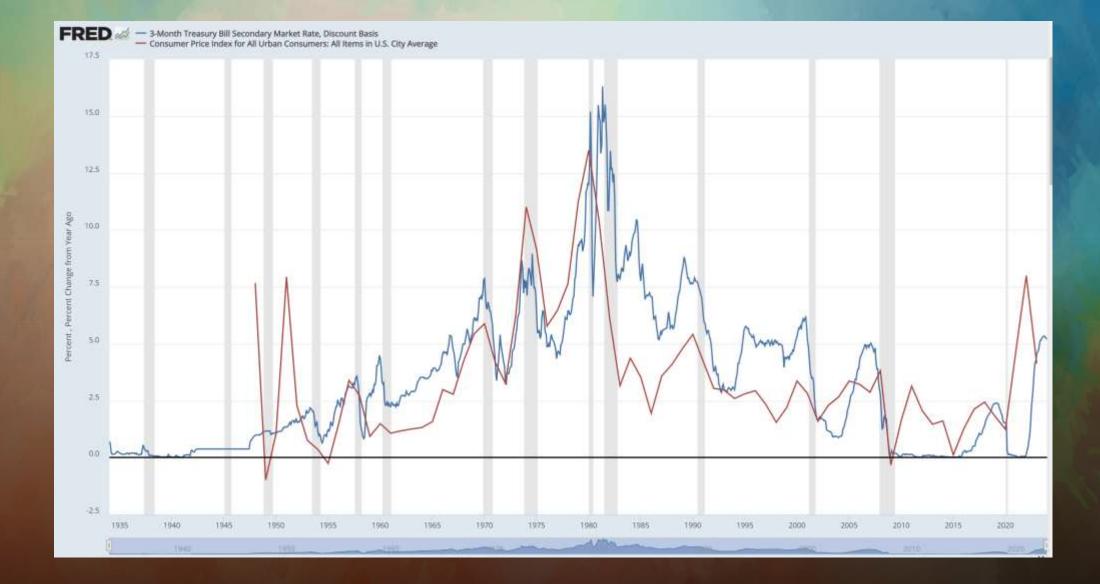
# FORECASTING IR

### Changes in IR due to business cycles:

- An economic expansion affects simultaneously demand (increase of wealth) and supply (greater expected returns on investments)
- Quantity will increase
- IR can increase or decrease (usually, increase and decrease during recessions)







### IR AND MONEY

IF WE increase the money supply, IR should decline, but:

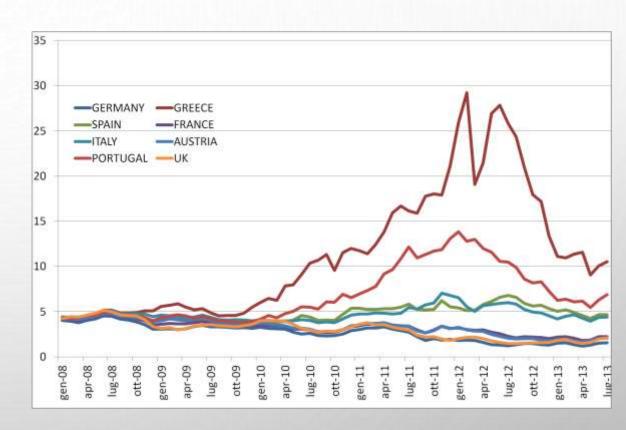
- Immediate liquidity effect reducing IR
- Economic stimulus: more income (**income effect**) and IR, but it takes time to have effects (wages, investments, ...)
- More inflation (price-level effect) and IR, but it takes time to adjust prices of goods and services
- More expected inflation (expected-inflation effect) and IR, with speed of effects depending on people's speed of adjusting expectations
- Result:
  - <u>If the liquidity effect is dominant</u>, sharp reduction in IR, then recovery up to a smaller final value
  - <u>If the liquidity effect is insufficient</u>, sharp reduction in IR, then recovery up to a higher final value
  - If the liquidity effect is marginal, people adapt their expectations on inflation and the reduction in IR does not take place, and final IR are higher immediately



### CREDIT AND OTHER RISKS

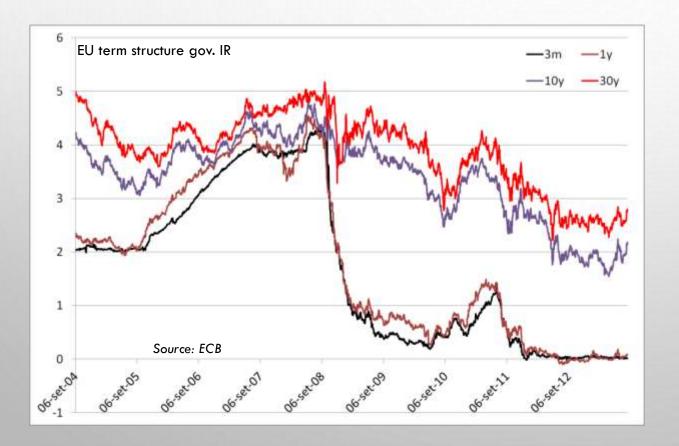
IR differ also for bonds with equal duration because of <u>default risk</u>:

- government bonds considered risk-free...
- the higher the risk the bigger the spread
- rating agencies judge borrowers' default-risk (investment grade VS junk/high yield bonds)
- IR differ also for <u>liquidity risk</u> (adding to the risk premium)
- Some bonds have tax incentives (f.i. Italy's gov.)
- And currencies!



IR differ also based on bonds' maturity:

- Differences in IR can be plotted at different maturities to derive the term structure of IR (yield curve)
- <u>Usually yield curves are upward-sloping</u>, meaning that longer maturities are charged with higher IR
- Flat or even downward-sloping or inverted yield curves are rare



- Different maturities move similarly
- When short-term IR are high, inversion is more likely
- Inverted yield curves seem to anticipate recessions ('81, '91, 2000, '07), steep upward curves are associated with economic booms

Three theories for explaining the term structure of IR:

#### **Expectations theory**

- If bonds at different maturities are perfect substitutes, their expected return must be equal
- $(1+i_{n,0})^n = (1+i_{1,0})(1+i^e_{1,1}) \cdot \dots \cdot (1+i^e_{1,n-1}) \to i_{n,0} \approx \frac{i_{1,0}+i^e_{1,1}+\dots+i^e_{1,n-1}}{n}$
- Predicts flat curves, whereas instead are usually upward-sloping (worked... until 1915)

#### Market segmentation theory

- Bonds at different maturities are not substitutes and each has a specific market, as well as each investor has a preferred maturity
- Together with interest-rate risk aversion, <u>explains why longer investments require a risk</u>
   <u>premium</u>
- Does not explain why IR move together along time
- Does not explain why with high short-term IR inversion is more likely



#### Liquidity premium theory

- Combines the other two in a comprehensive way
- Adds to expectations theory a liquidity premium for longer term bonds that is subject to market (demand, supply) conditions for that segment
- Bonds are substitutes as long as investors' preferences are compensated with a term (liquidity) premium that is always positive and grows as maturity gets longer

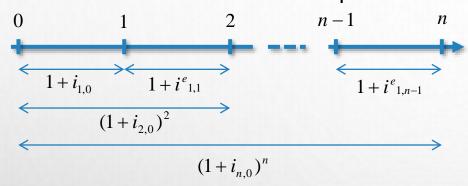
$$i_{n,0} \approx \frac{i_{1,0} + i^e_{1,1} + \dots + i^e_{1,n-1}}{n} + l_{n,0}$$

- <u>Explains inverted term structures</u>: when future expectations on short-term IR are of a
  wide fall, so that their average is not balanced even by a positive liquidity premium
  (more likely when short-term rates are high)
- Support empirical evidence that:
  - Term structure is a predictor of business cycles and inflation
  - Term structure is less reliable for intermediate movements



#### Forward and spot rates:

Term structures allow to measure expected IR



- Expected future IR are forward rates, in contrast to spot rates
- Knowing spot IR we can derive market expectations

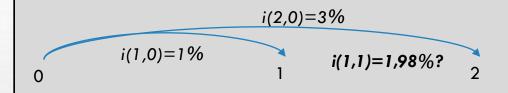
F.i.: 
$$i_{1,1}^e = \frac{(1+i_{2,0})^2}{1+i_{1,0}} - 1$$
 or, generalising:  $i_{1,k}^e = \frac{(1+i_{k+1,0})^{k+1}}{(1+i_{k,0})^k} - 1$ 

Including liquidity premiums:

$$i_{1,k}^{e} = \frac{(1 + i_{k+1,0} - l_{k+1,0})^{k+1}}{(1 + i_{k,0} - l_{k,0})^{k}} - 1$$

### Can we gain from knowing the yield curve?

Imagine that, as a CFO, you know that you are going to receive  $1 \text{mln} \in \text{in } 1 \text{ year.}$  You also know that: i(1,0)=1% and i(2,0)=3% (biannual)



+1.000.000

	0	1	2
Inflow		+ 1,000,000	
1. Loan	+990,099	-1,000,000	
2. Investment	-990,099		+1,019,802
NET RESULT	0	0	+1,019,802