

# Geophysical Fluid Dynamics

## Lecture I: Introduction & Properties of fluids I

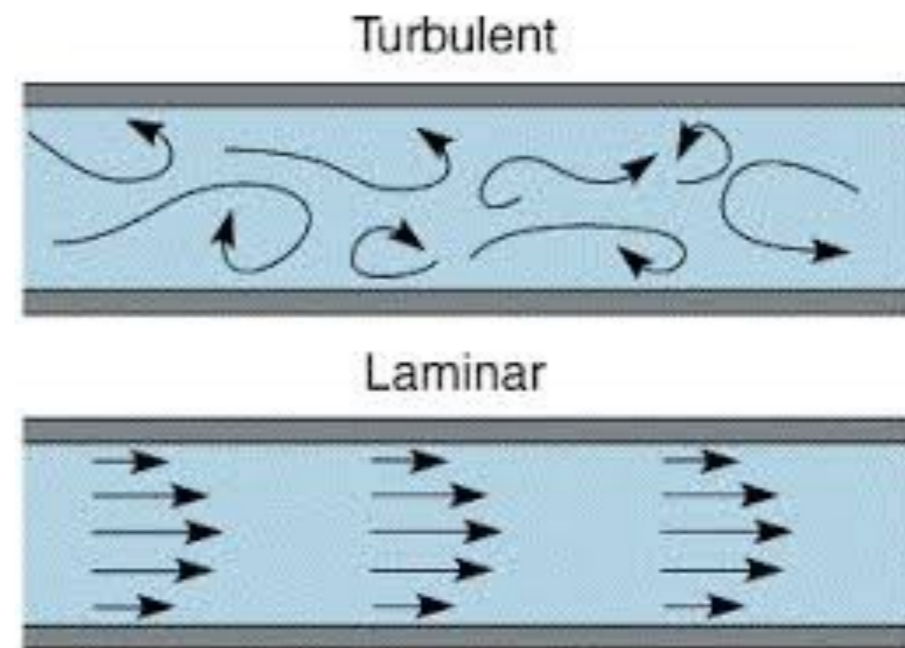
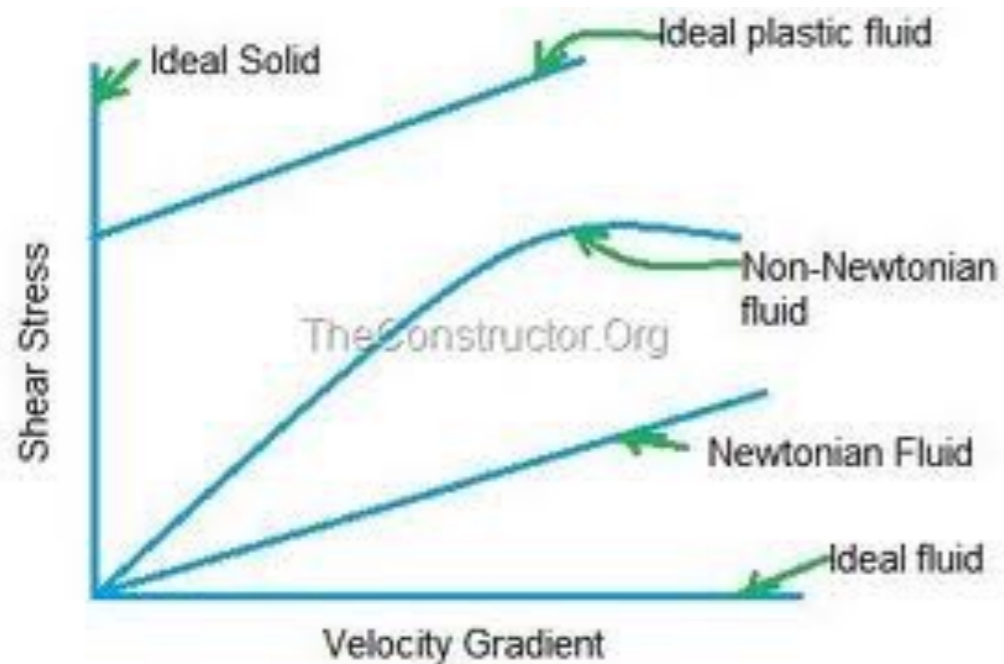


# Fluids are Everywhere



a single storm eddy (the Great Red Spot) on Jupiter is larger in size than planet Earth

they have many useful properties ...



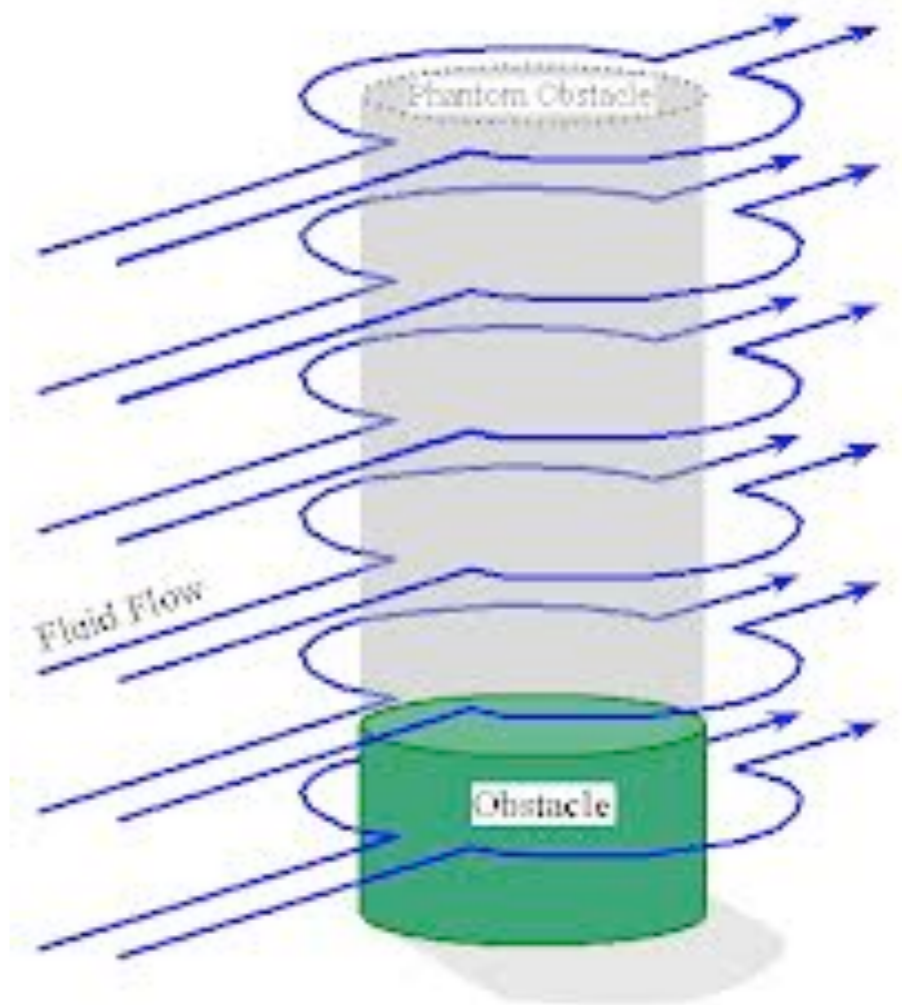
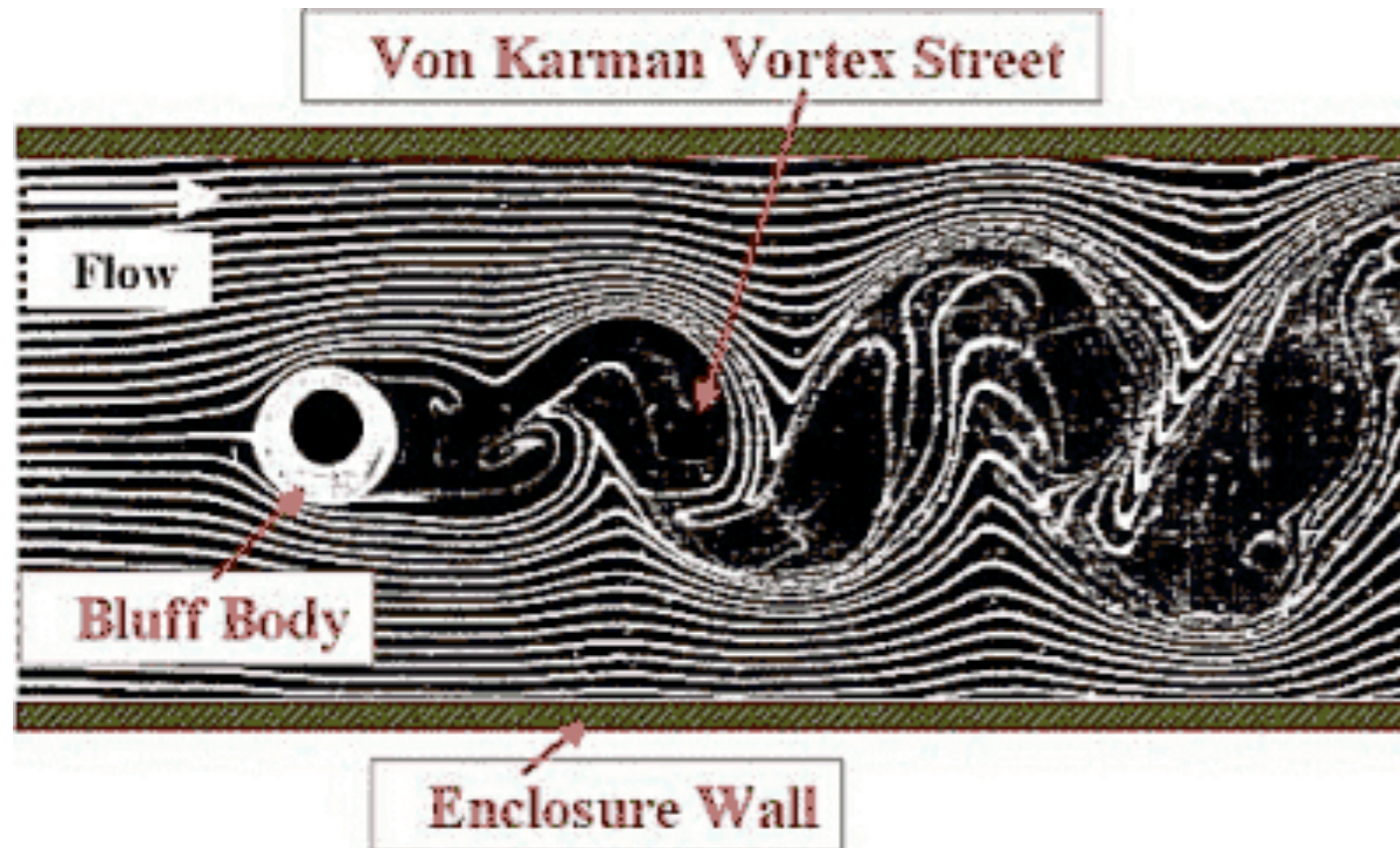


# properties change with the environment



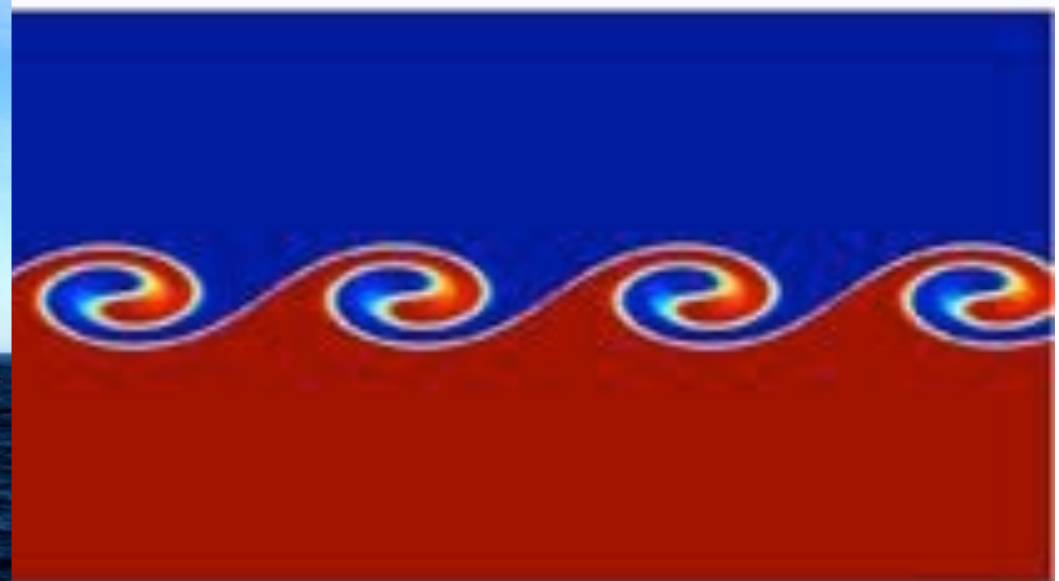


# laminar & turbulent flow boundary layers instabilities



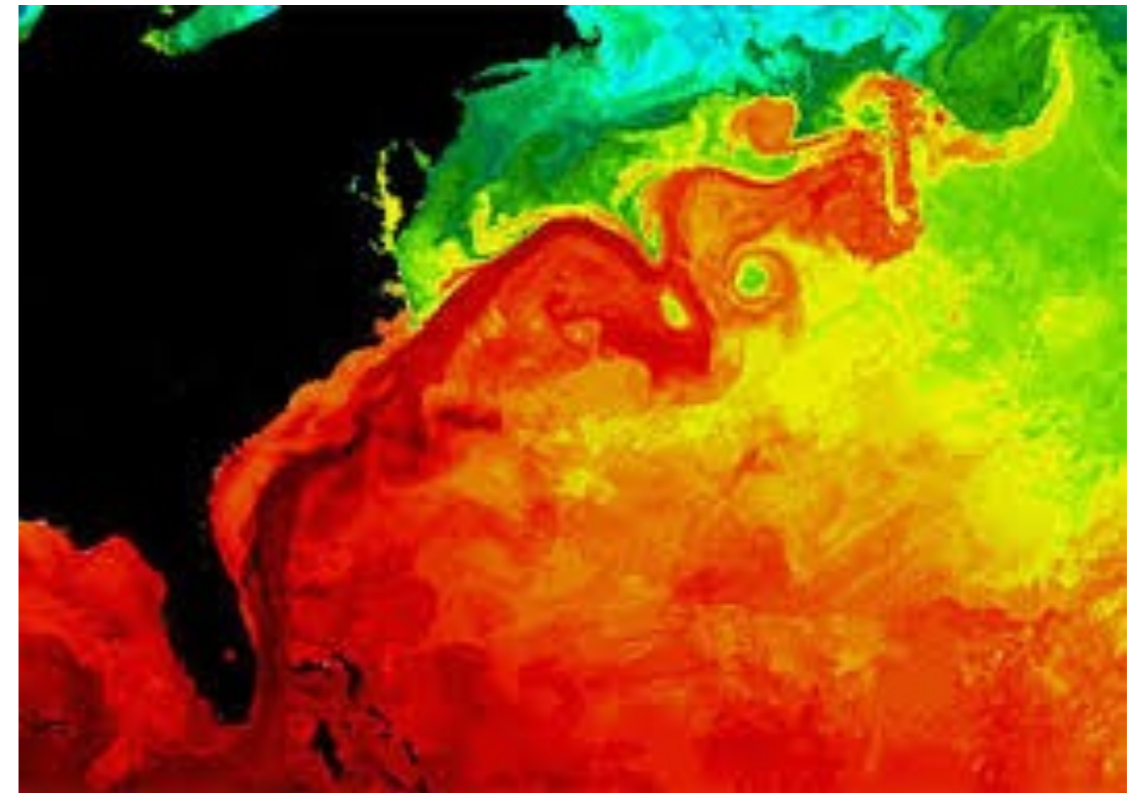
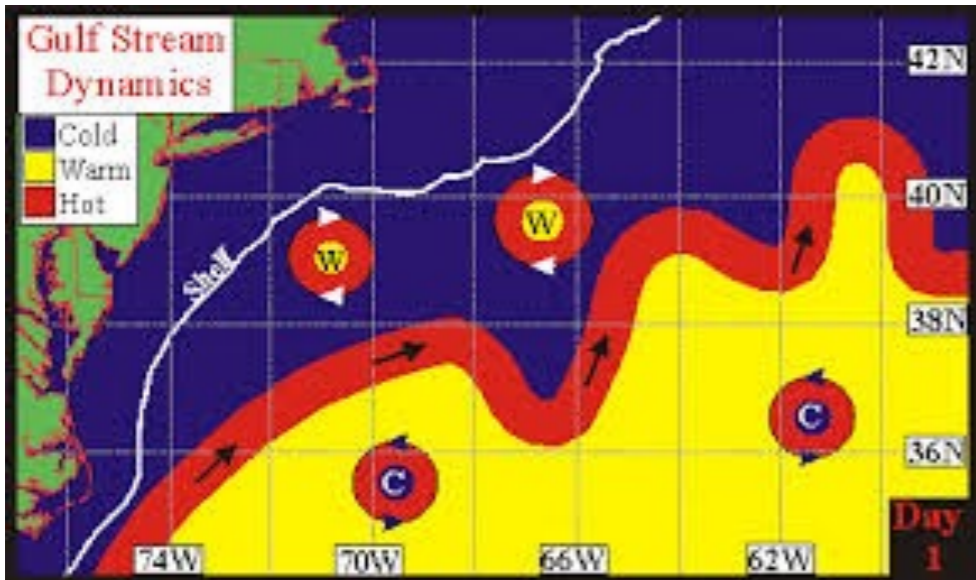
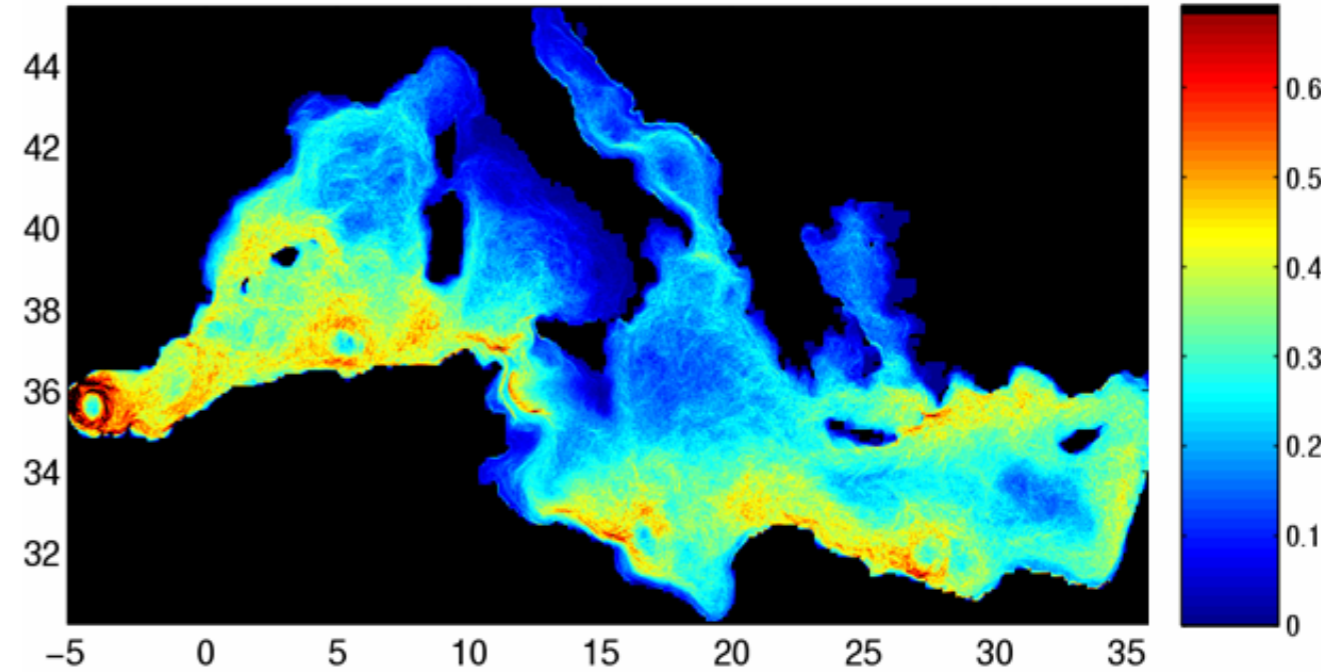
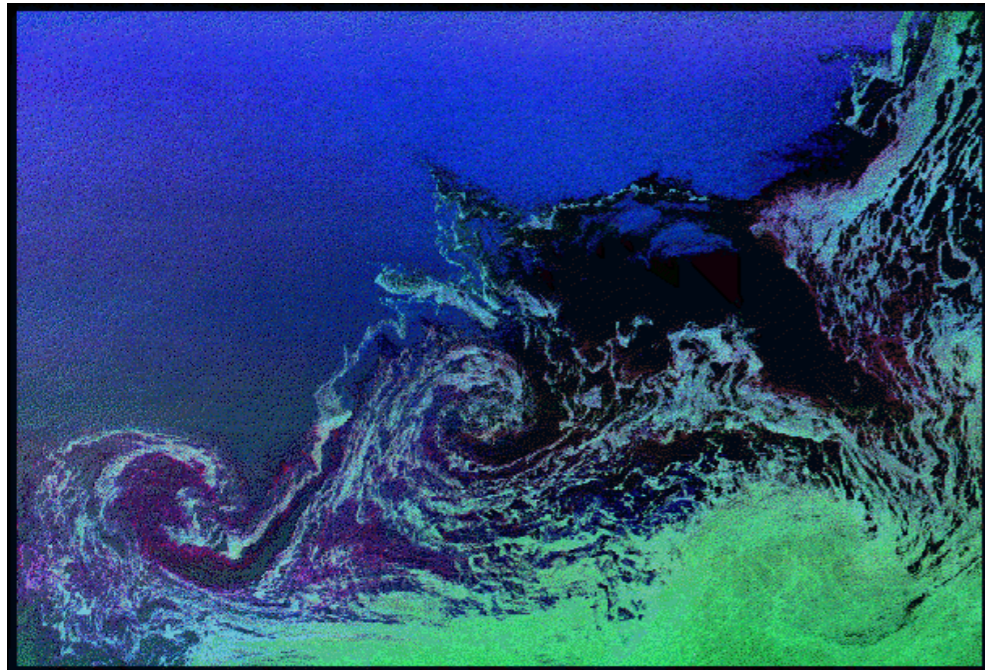


# atmospheric phenomena



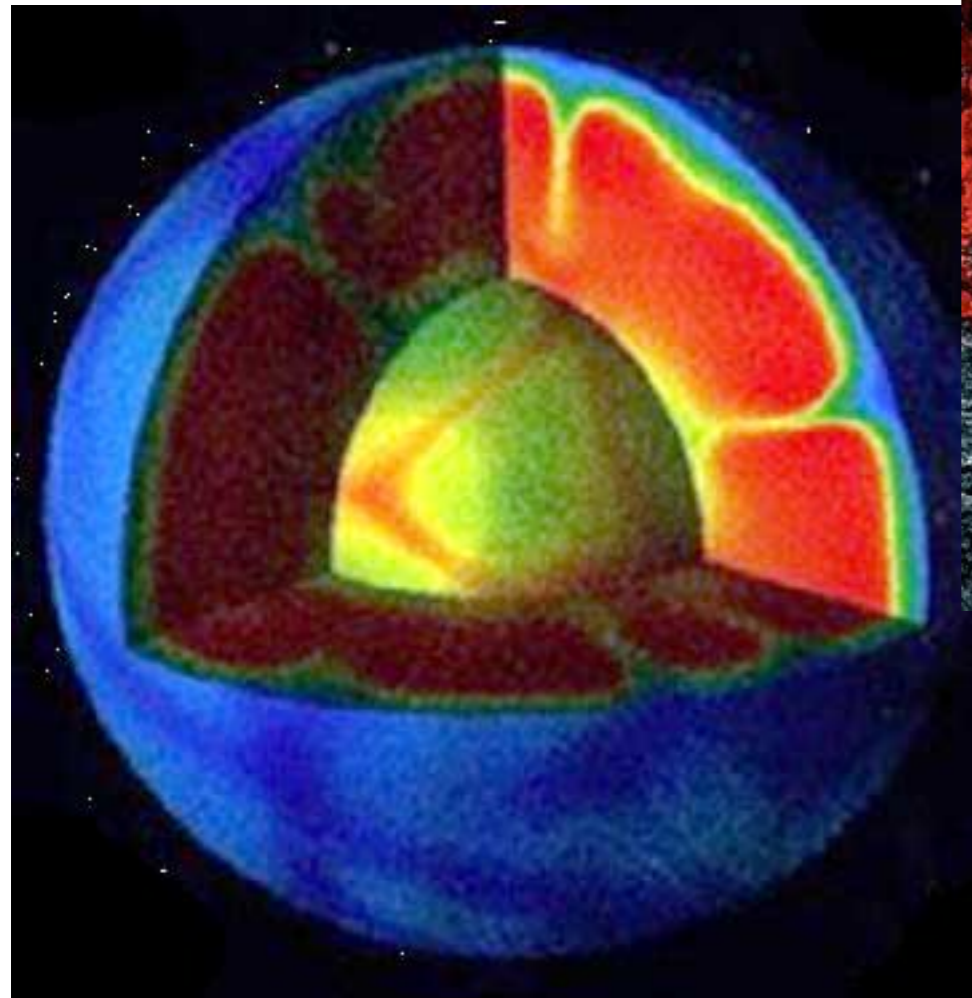


# Oceanic phenomena





# Earth Interior





# What is a fluid

- water



- air



- oil



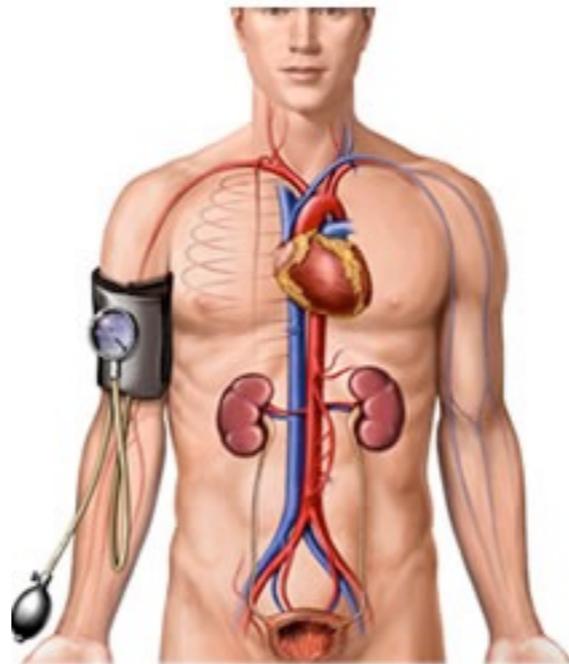


# Fluid vs non-fluid

- it flows ...



- it deforms



- takes the form of its container (glass, balloon)





# Scope of Fluid Mechanics:

it tries to explain fluids and their motions

- Fluids are: liquids and gases
- Engineering: flow in pipes, jets, aerodynamics, projectile motion, lubrication, irrigation, combustion
- Environmental: meteorology, oceanography, geophysics, sedimentation, irrigation
- Medicine: blood vessels



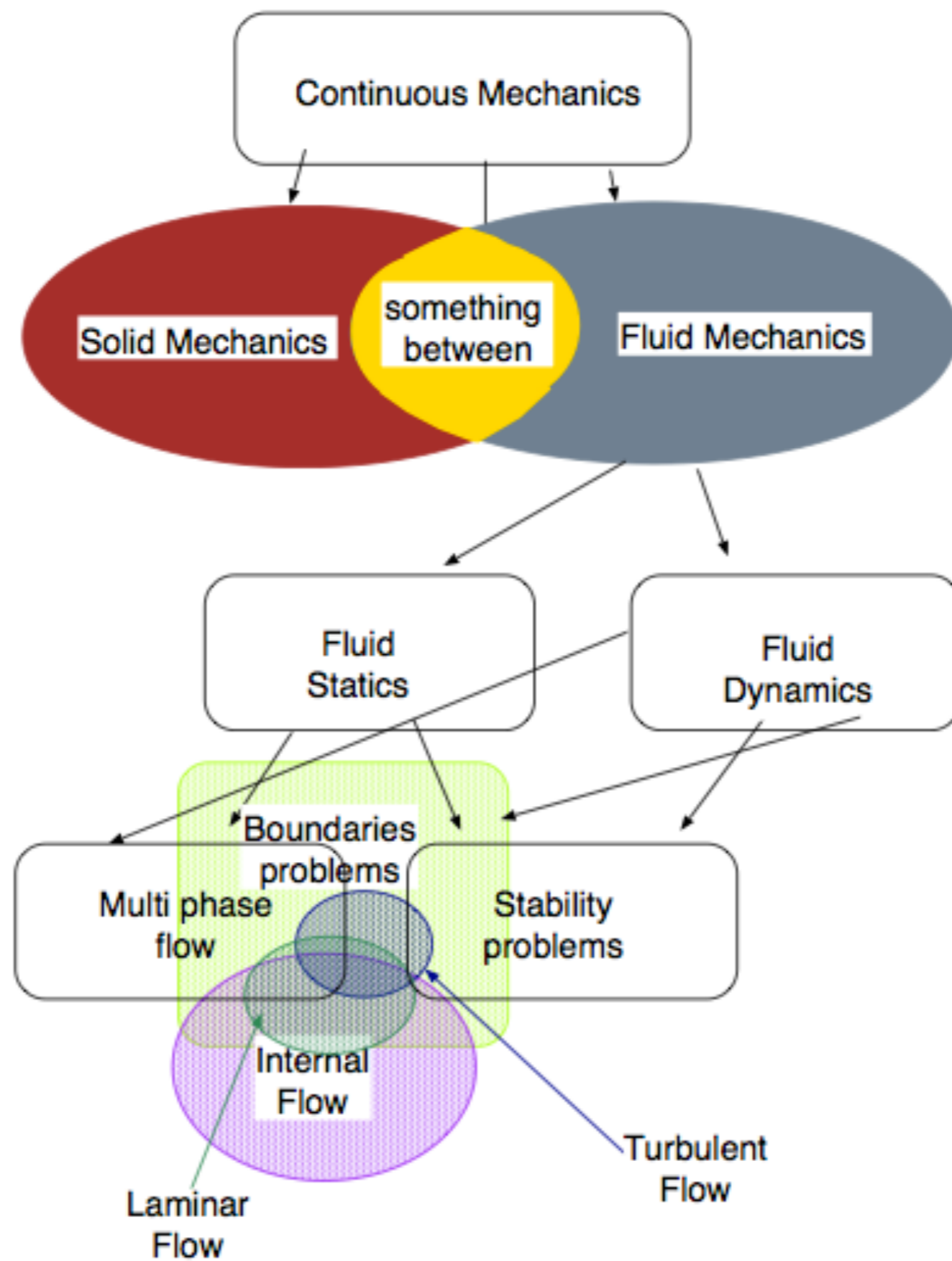


Fig. -1.1. Diagram to explain part of relationships of fluid mechanics branches.



# Branches

- **Statics:** fluids at rest
- **Kinematics:** velocities and streamlines
- **Dynamics:** velocity & accelerations, forces
- ... we'll get into Geophysical Fluid Dynamics



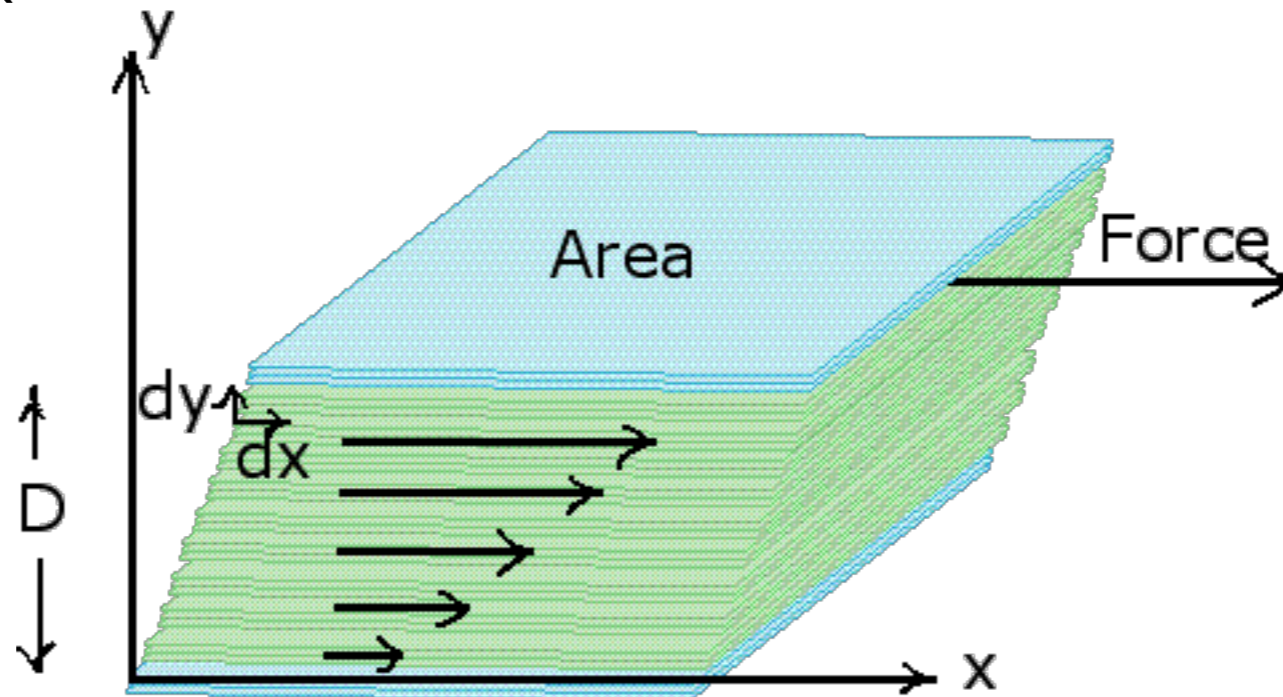
# Properties of Fluids

- definition of a Fluid
- dimensions and units
- mass and weight
- density and specific weight

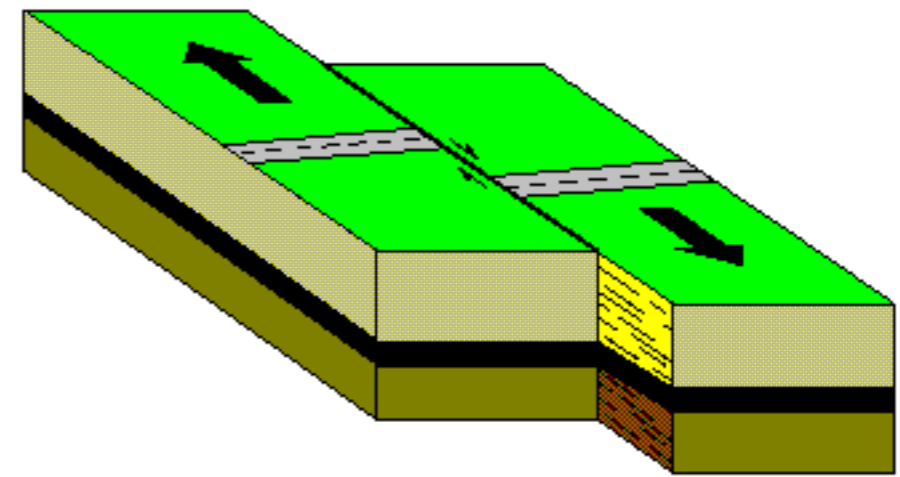
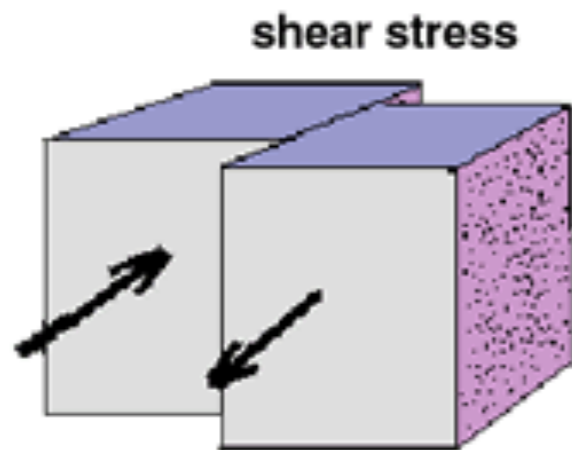
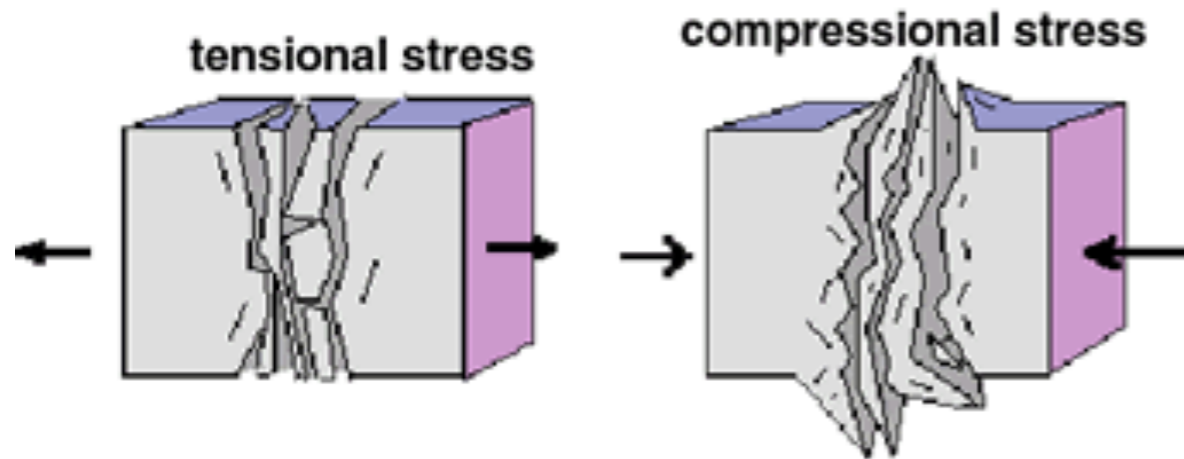


# Definition of Fluid

- A substance that deforms continuously when acted on by a shearing stress (water, air, syrup)
- **SHEAR STRESS** tangential force per unit area (different from a normal stress)

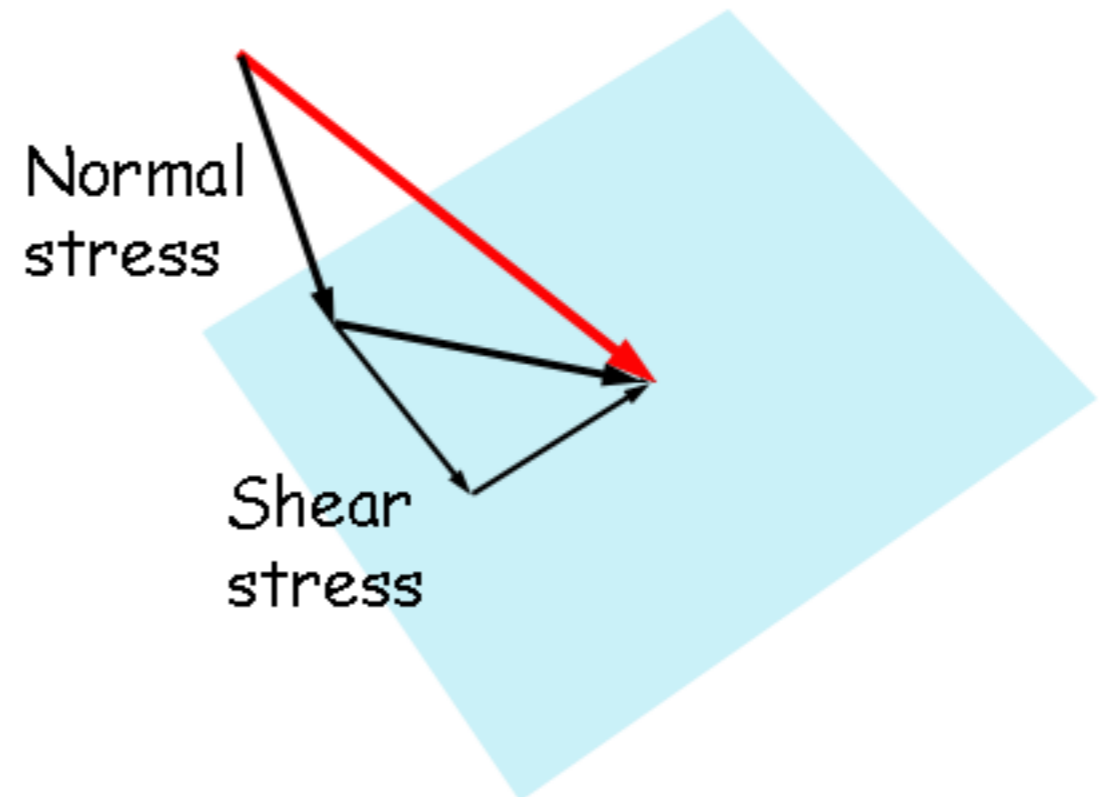






This fault is an example of shearing stress within the Earth

Stress or traction on a plane





# Non-fluids

- rubber
- ice
- steel
- These are SOLID: they can deform to a new equilibrium state when shearing stress is applied. They don't flow like a liquid because of **structural rigidity**

# Another definitions is

- a substance that takes the shape of the container in which it is placed





# Fluids vs Non-Fluids

- **FLUID:** Liquid water deforms assuming shape of glass. Gravity provides the force. Balance is achieved when force by walls is balanced by force of gravity = **STATICS**



# Fluids vs Non-Fluids

- **NON-FLUID:**  
solid ice cubes  
maintain shape  
with air gaps  
between the  
cubes. A solid  
will not deform.





# Distinction between a Solid and a Fluid

- Molecules of solid closer together than those of fluid
- Solid: intermolecular forces larger than in fluid
- Elastic solid: 1. deforms under load 2. recovers state when unloaded
- Plastic solid: 1. deforms under load 2. does not return to original state

# Distinction between a Gas and a Liquid

- Fluids: gases or liquids
- GAS: molecules farther apart; very compressible; tends to expand indefinitely
- LIQUID: relatively incompressible; does not expand if no pressure.



# Distinction between a Gas and a Liquid

- VAPOR: 1. gas whose T and P very near the liquid phase 2. steam is vapour, state near that of water
- GAS: super-heated vapour, far away from liquid phase.

# Dimensions and Units

- qualitative and quantitative description of fluid characteristics
- Qualitative: DIMENSIONS (length, time, velocity)
- Quantitative: a number plus a UNIT (9.8 m/s)



# DIMENSIONS

- PRIMARY (basic): mass  $M$ , length  $L$ , time  $T$   
or force  $F$ , length  $L$ , time  $T$
- SECONDARY (derived): velocity  $[V] = L/T$ ,  
acceleration  $[a] = L/T^2$ , Newton's Second  
Law  $F = [m][a] = M L/T^2$

# Units (S.I. Units)

- Length (m) meter
- Mass (kg) kilogram
- Force (N) Newton ( $\text{kg m/s}^2$ )
- Time (s) second
- Temperature (K) Kelvin for absolute (-273.15 C)
- Temperature (C) Celsius for ordinary



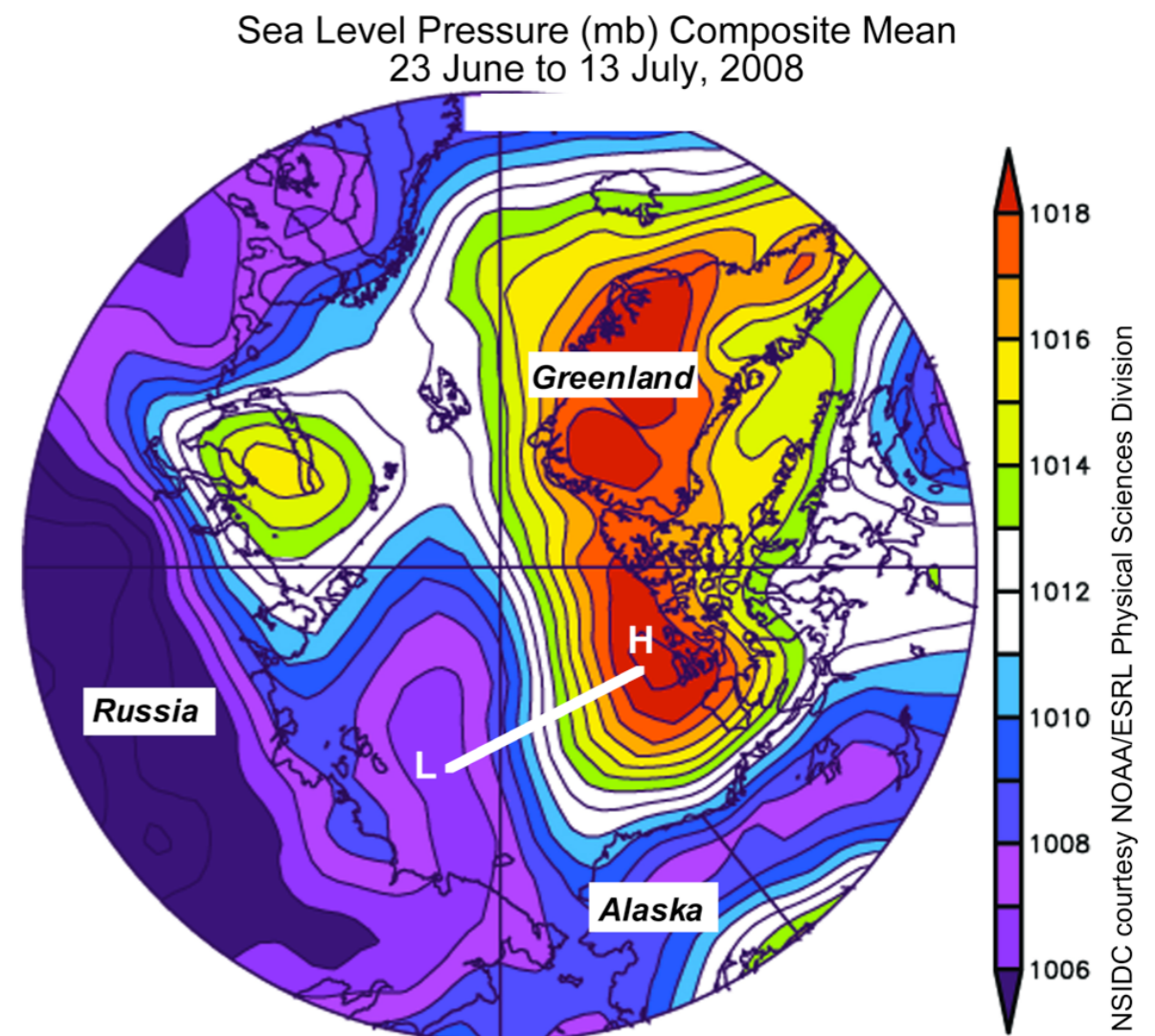
# Mass and Weight

- Weight,  $W = m g$  ( $g$  gravitational acceleration =  $9.81 \text{ m/s}^2$ )
- $W = mg = (1 \text{ kg}) (9.81 \text{ m/s}^2) = 9.81 \text{ N}$
- same mass different weight for 2.5 kg of water
- On Earth:  $W = (2.5\text{kg})(9.81 \text{ m/s}^2) = 24.53 \text{ N}$
- On Moon:  $W = (2.5\text{kg})(9.81 \text{ m/s}^2)/6 = 4.087 \text{ N}$

# Properties of Fluids:

# Density

- Density  $\rho = M / V$   
(mass per unit volume)
- Density can vary :
- from one fluid to another
- with temperature and pressure  $\rho = f(T, P)$
- in space



# Densities of common Fluids

- water  $1000 \text{ kg/m}^3$
- seawater  $1030 \text{ kg/m}^3$
- crude oil  $800 \text{ kg/m}^3$
- air  $1.2 \text{ kg/m}^3$
- helium  $0.166 \text{ kg/m}^3$





# Perfect gases

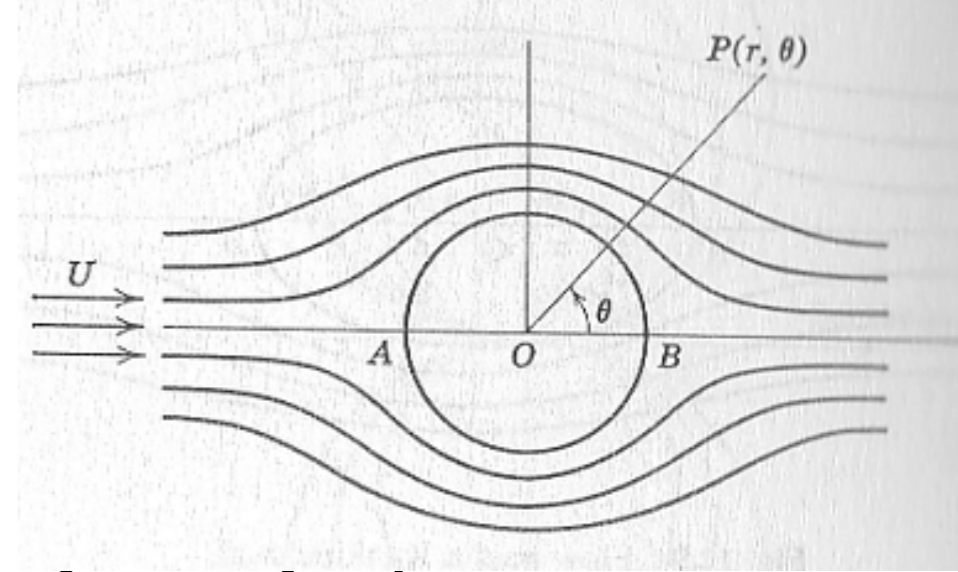
Gases with constant Specific Heats that obey the perfect-gas law

$$p/\rho = R T$$

Remember that: The Specific Heat is the amount of HEAT per unit mass required to raise the temperature by one degree Celsius:  $Q = c m \Delta T$   
heat = (specific heat)(mass)(change in T)

# Ideal Fluids

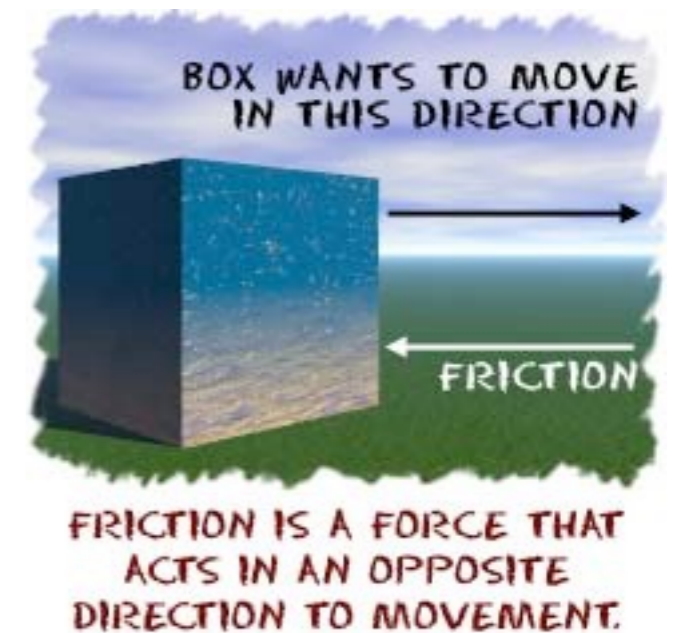
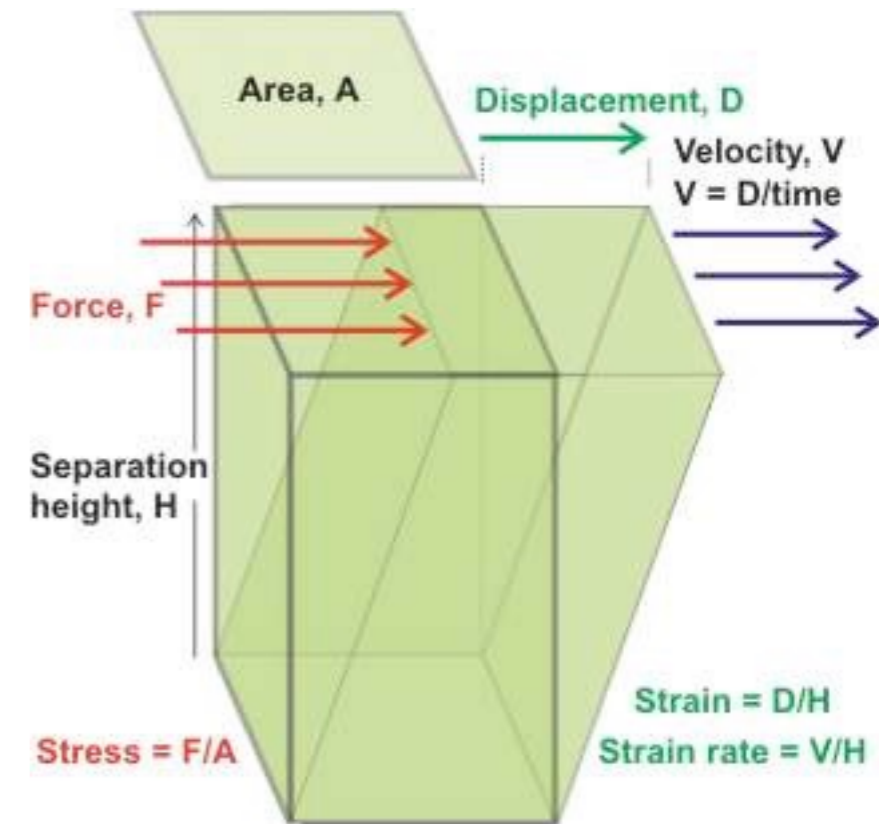
- a fluid with no friction
- said to be an 'inviscid fluid' (zero viscosity)
- internal forces at any section are normal (pressure forces)
- Many flows are almost frictionless flow away from solid boundaries (some GFD approx.)
- Do not confuse ideal fluid with a perfect gas
- Steady - incompressible - nonviscous - irrotational



Ideal fluid is only an imaginary fluid as all the fluids which exist have some viscosity

# Real Fluids

- Tangential or shearing forces always develop where there is motion relative to solid body
- fluid friction is created
- Shear forces oppose motion of one particle past another
- Friction forces give rise to a fluid property called **VISCOSITY**



Remember: Shear is a sideways force. Friction is drag - from any direction.



# Viscosity

- Definition of viscosity
- how shear stress and velocity are related
- Newton's law of viscosity
- how to determine shear stress in viscous fluid flow
- values of viscosity for different fluids

# Viscosity

Viscosity is a measure of the resistance of a fluid to being deformed by a shear stress.

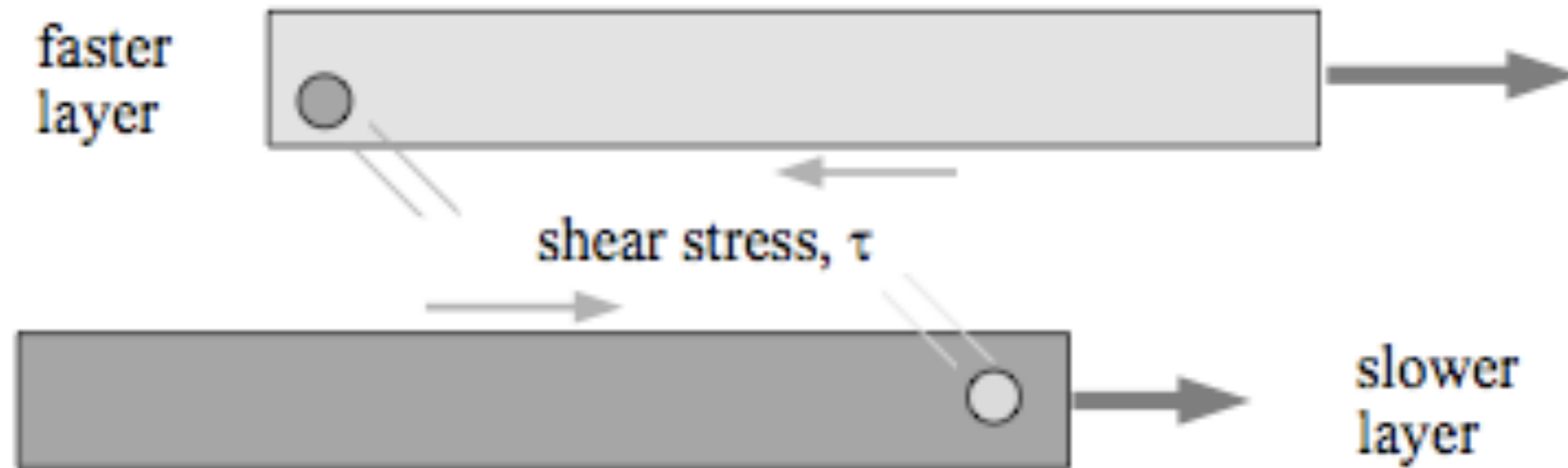
Fluids with low viscosity are 'thin' and are easily deformed by a small shear stress.



Fluids with high viscosity are 'thick' and need higher shear stress to deform.

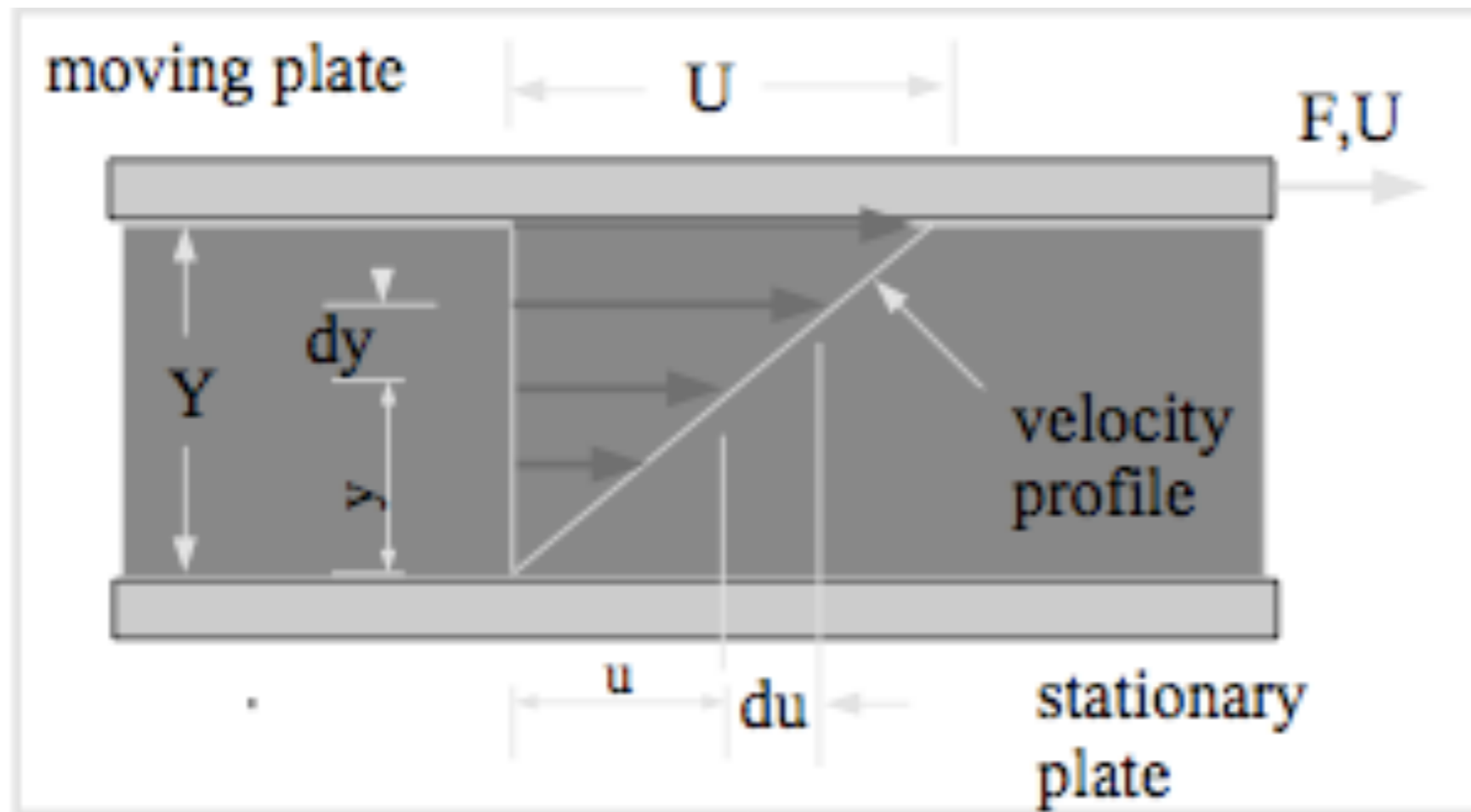


# Velocity and shear stress (to define viscosity)



- fast-moving molecule into slow-moving layer: speeds up the layer
- slow-moving molecule into fast-moving layer: slows down the layer





Shear stress is:

$$\tau = F/A$$

Experiments show that:

$$F \sim AU/Y$$

- Fluid particles adhere to walls: *no-slip condition*
- $U(\text{bottom}) = 0$ ;  $U(\text{top}) = U$
- For small  $U$  and  $Y$ , velocity profile is linear (and no net flow)

$$\tau \propto U/Y$$

$$\tau = \mu du/dy$$

# Newton's law of viscosity

shear stress is proportional to the velocity gradient

For an incompressible and isotropic Newtonian Fluid:  
shear stress = shear viscosity x velocity gradient

$$\tau = F/A = \mu du/dy$$

proportionality constant = viscosity coefficient

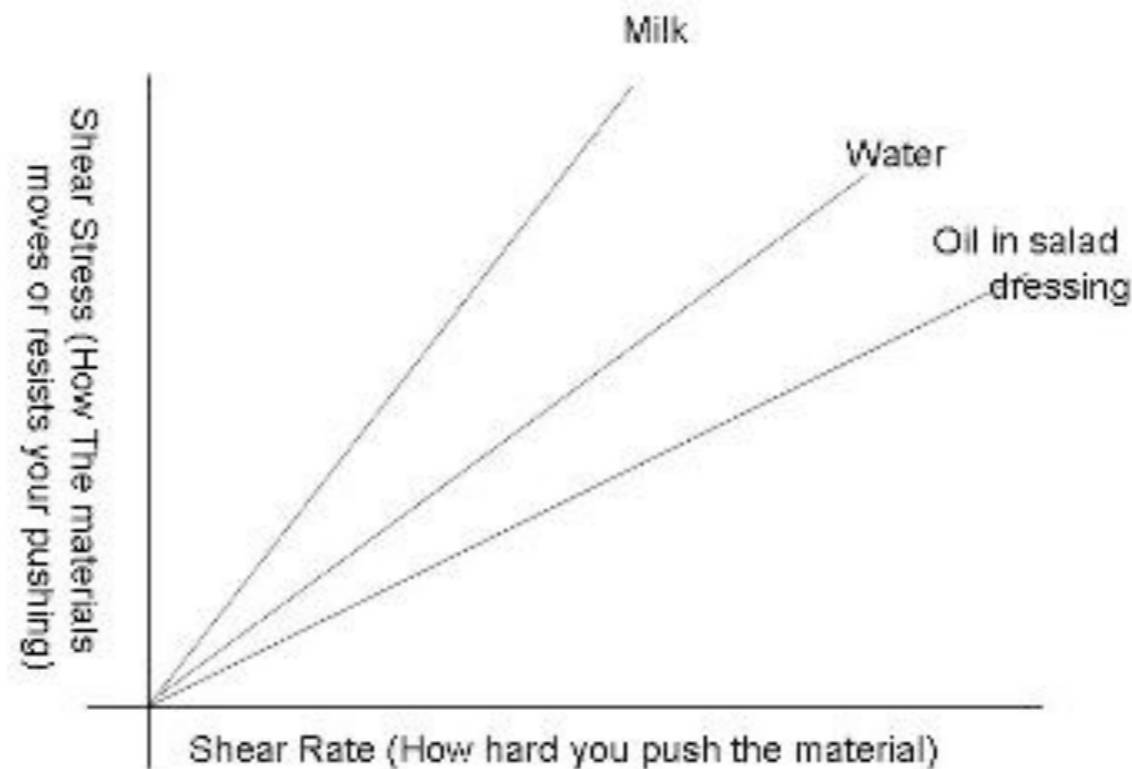


# Newtonian Fluid

- Obeys Newton's Law of Viscosity
- velocity gradient = shear rate  $\tau = \mu du/dy$
- slope = viscosity (constant)

Units:  $(\text{N/m}^2) / (\text{m/s} / \text{m}) = \text{N s} / \text{m}^2$

## Examples of Newtonian Fluids





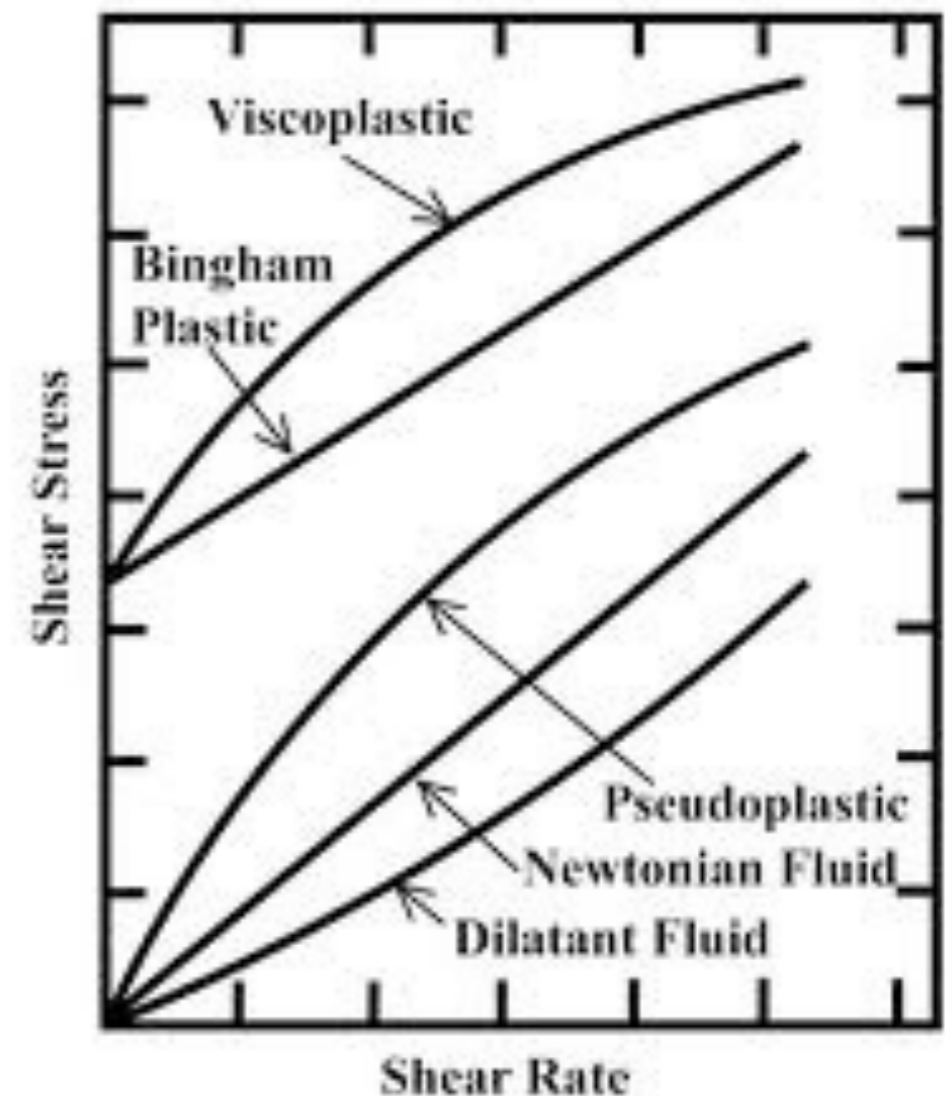
# Non-Newtonian Fluids

Examples: paint, blood, lava, water-corn starch.

- viscosity depends on shear rate
- shear thinning (pseudoplastic: paints, ketchup)
- shear thickening (dilatant: corn starch)
- Bingham Plastic: not a solid, not a fluid (toothpaste, mayonnaise)



$$\mu = f(du/dy)$$



When stress is applied to the liquid it exhibits properties of a solid.

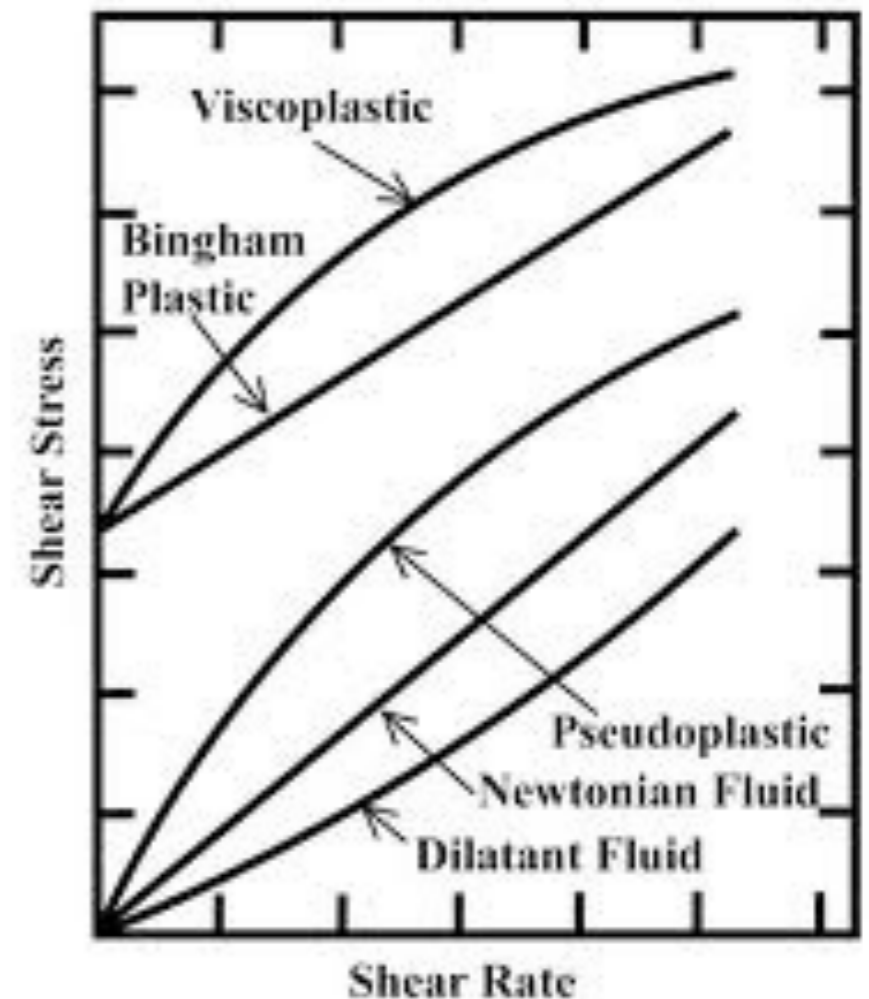
[VIDEO](#)



- **Shear thinning** is an effect where a fluid's viscosity—the measure of a fluid's resistance to flow—decreases with an increasing rate of shear stress. Another name for a shear thinning fluid is a **pseudoplastic**. This property is found in certain complex solutions, such as **lava**, ketchup, whipped cream, blood, paint, and nail polish



**LAVA**

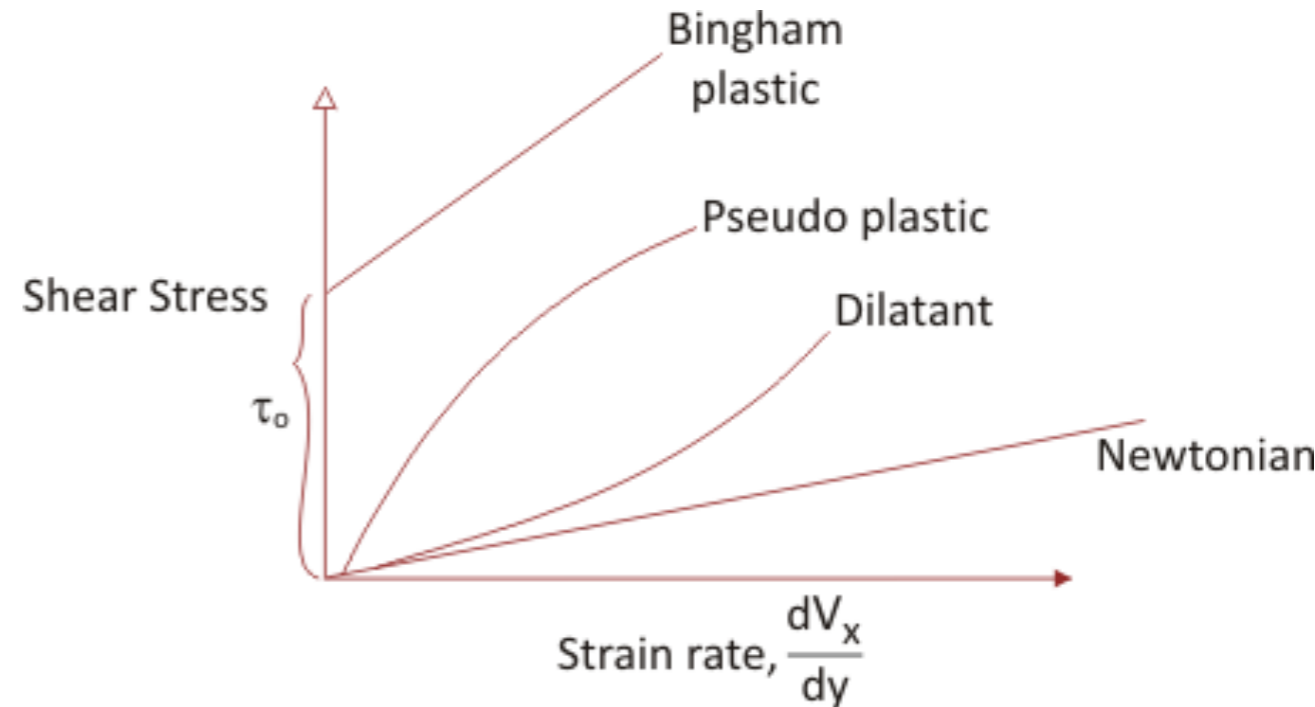


# Dynamic / Kinematic Viscosity

- Dynamic viscosity [N s/(m<sup>2</sup>)]
- Kinematic viscosity [m<sup>2</sup>/s]
- dynamic useful for most fluids because independent of pressure
- kinematic for gases since it changes with pressure (changes in density)

$$\tau = \mu du/dy$$

$$\nu = \mu/\rho$$



- what is  $\mu$  for an ideal fluid?

# Summary

- Viscosity is an important fluid property
- It causes fluid to stick to a surface, creates boundary layers
- Newton's law of viscosity:  $\tau$  is proportional to fluid  $\mu$  and the velocity gradient
- Newtonian vs No-Newtonian
- liquid have high viscosity
- gases have low viscosity

