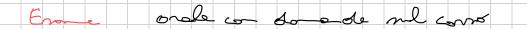
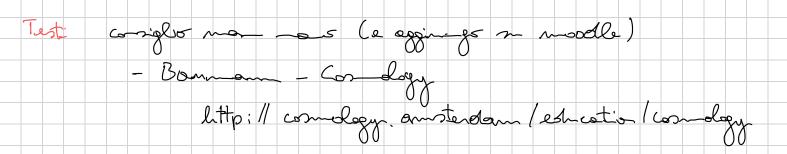
(Osmology and

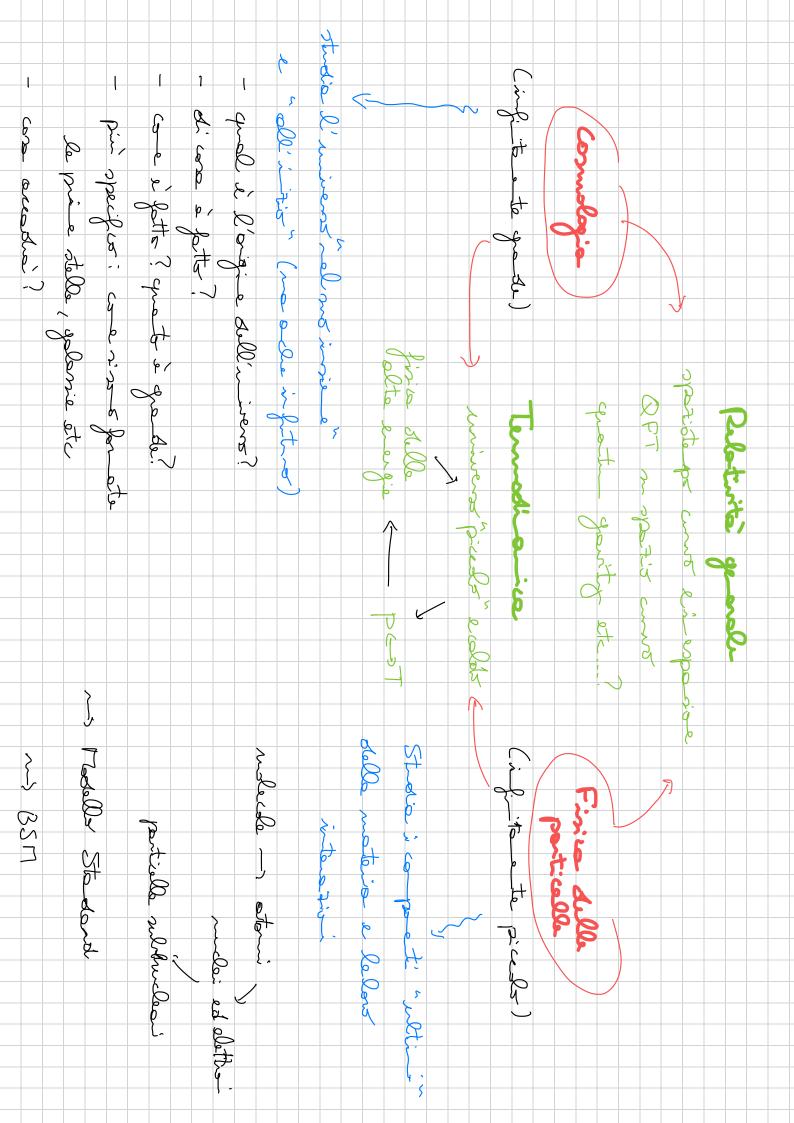
Porticle Physics

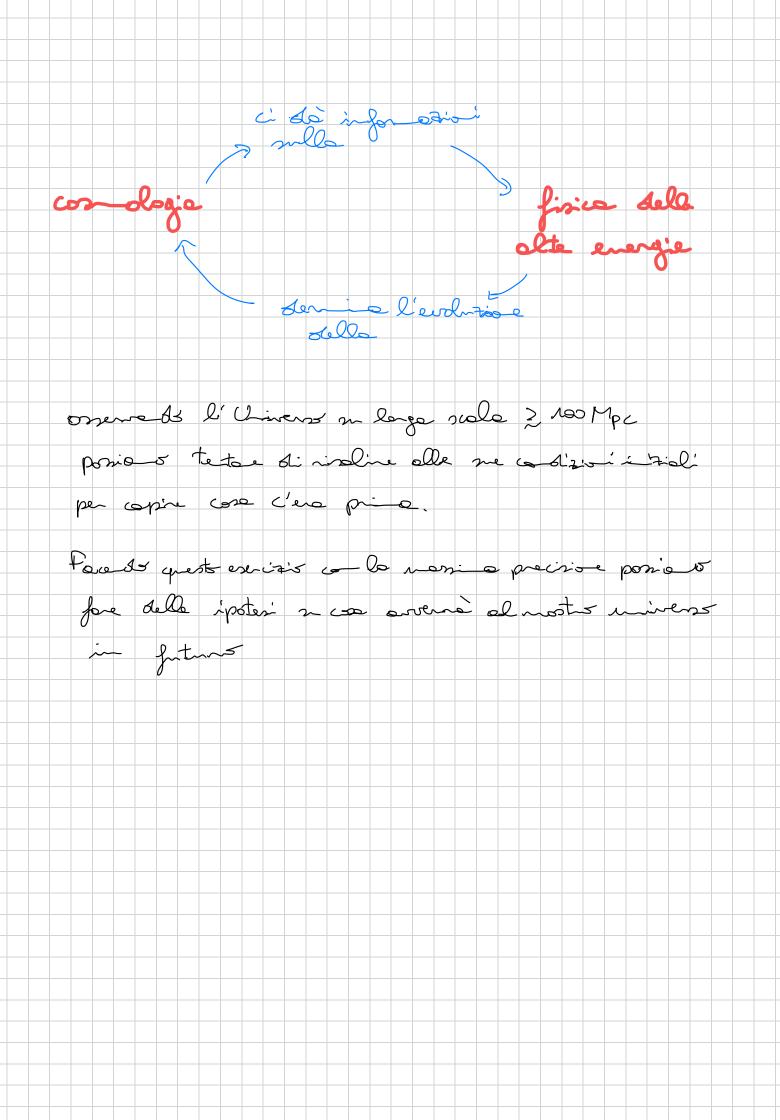




ossioni e moterio oscro

Ter





Event	time t	redshift z	temperature T
Singularity	0	To	∞
Quantum gravity	$\sim 10^{-43}{\rm s}$	4-	$\sim 10^{18}{\rm GeV}$
Inflation	$\gtrsim 10^{-34}{\rm s}$	9-	_
Baryogenesis	$\lesssim 20\mathrm{ps}$	E 1013	$> 100 {\rm GeV}$
EW phase transition	$20\mathrm{ps}$	1015	$100{ m GeV}$
QCD phase transition	$20\mu s$	4012	$150{ m MeV}$
Dark matter freeze-out	?	A	?
Neutrino decoupling	$1\mathrm{s}$	6×10 ³	$1{ m MeV}$
Electron-positron annihilation	$6 \mathrm{s}$	2×10^{9}	$500\mathrm{keV}$
Big Bang nucleosynthesis	$3\mathrm{min}$	4×10^{8}	$100\mathrm{keV}$
Matter-radiation equality	$60\mathrm{kyr}$	3400	$0.75\mathrm{eV}$
Recombination	$260380\mathrm{kyr}$	1100-1400	$0.26 - 0.33 \mathrm{eV}$
Photon decoupling	$380{ m kyr}$	1100	$0.26\mathrm{eV}$
Reionization	$100400\mathrm{Myr}$	10-30	$2.67.0\mathrm{meV}$
Dark energy-matter equality	$9\mathrm{Gyr}$	6A	$0.33{ m meV}$
Present	13.8 Gyr		0.24 meV

ster

. }

Here

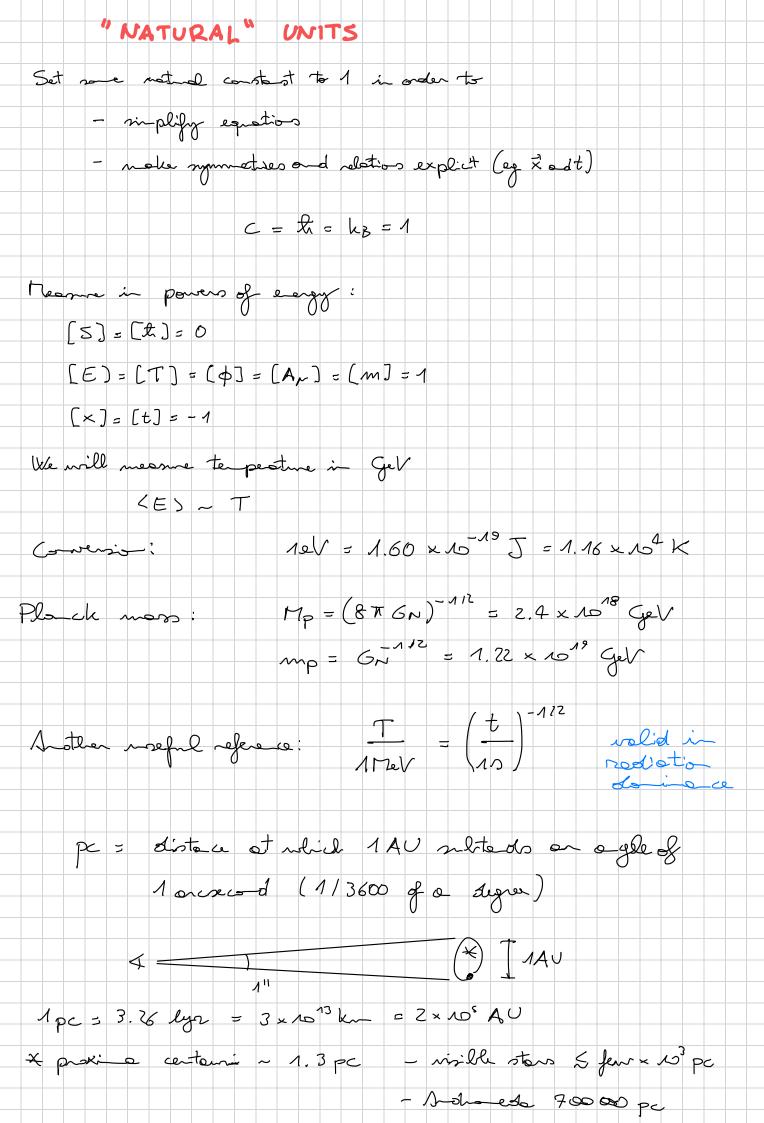
Pint

F I

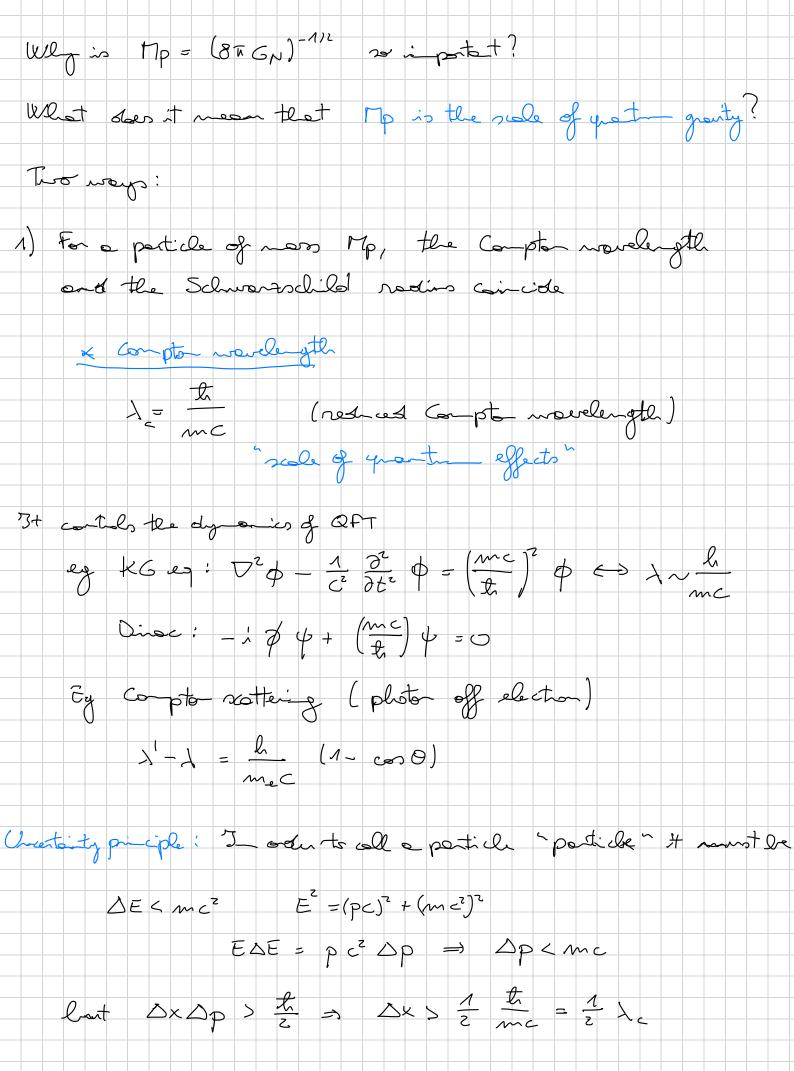
 Table 3.1: Key events in the thermal history of the universe.
 Z.73K

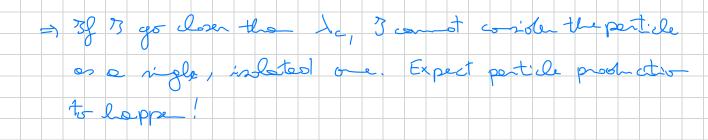
く

-st observable stars ~65 ~ 30 Myr f; MK/-rized goloxies ~ 400 Myr finst $\sim M$

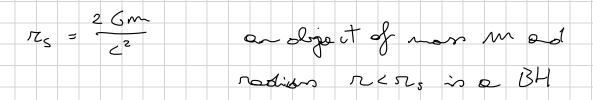


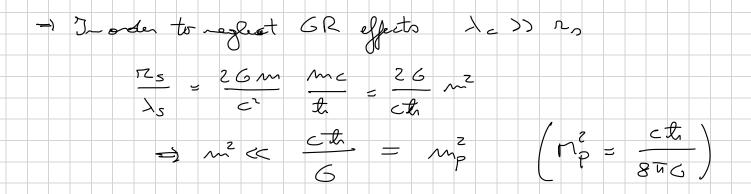
Planck mars

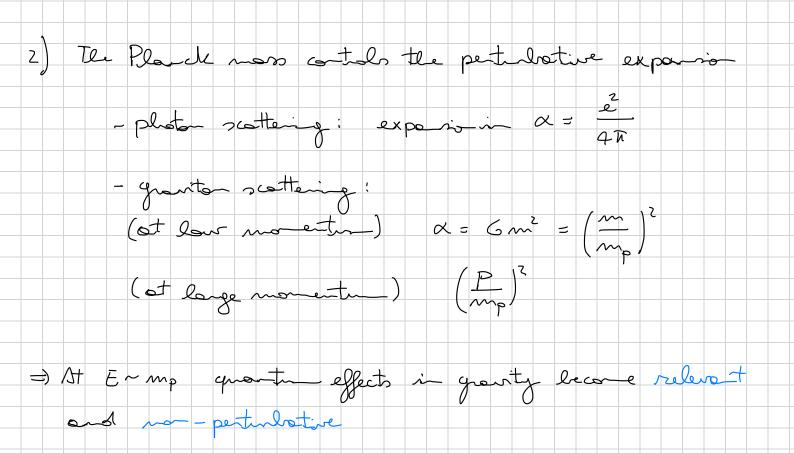




* Schwartskhild radius







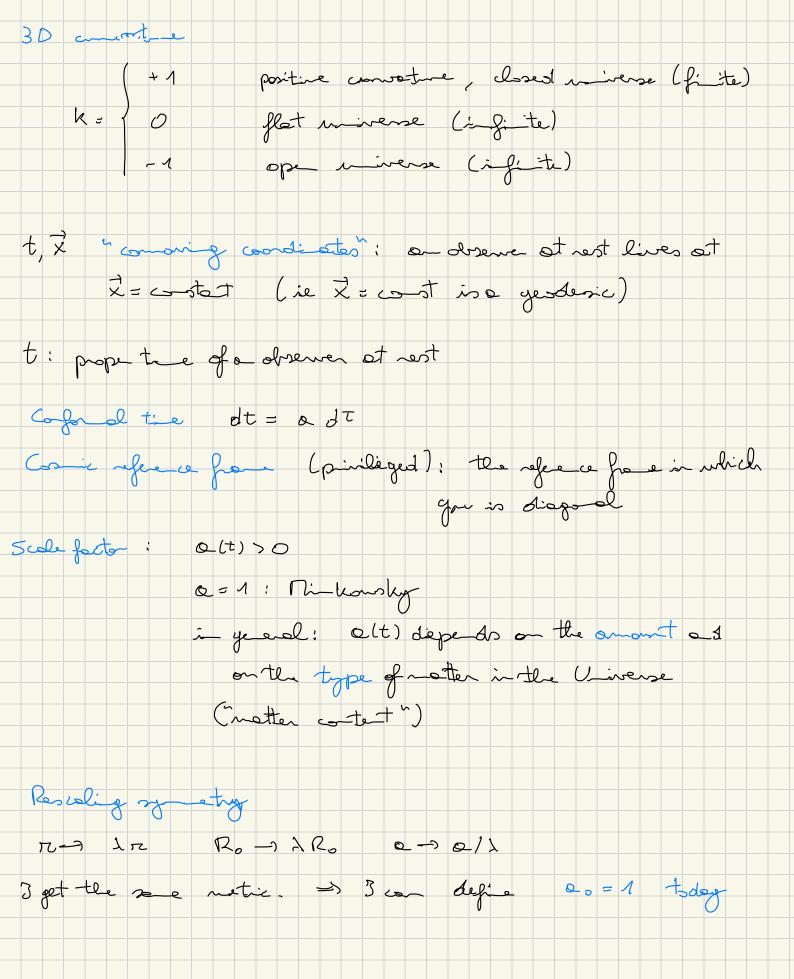
OBSERVED UNIVERSE

not equivalet : - E + O miljon is horogreens let not instropic - D=D(T) is instropic when see for the centre, but not horogreens

FLRW metric the stic of a horogeness and instropic minerse can be marte as

$$ds^{2} = -dt^{2} + o^{2}(t) \left(\frac{dn^{2}}{1 - kn^{2}/R_{o}^{2}} + n^{2}d\theta^{2} + n^{2}m^{2}\theta^{2} \right)$$
mother of 3-space i ${}^{3}K(t) = \frac{k}{\sigma^{2}(t)}$

2

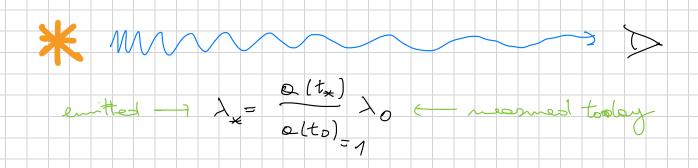


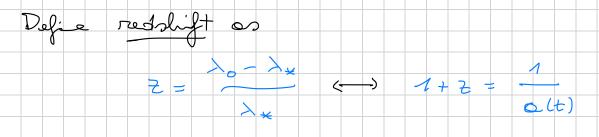
Peculian relacity and herefore floor porition a yalaxy : ripeyo = a ri => plysial relacity: rplys = driplys = 0 rt 0 rt $= \left(\frac{\dot{a}}{a}\right) a \vec{n} + a \vec{n}$ = H ripege + Specilion peculiar relacity: N pec = a Ti velocity reasoned by a convig (ie fre folling) observer at position is Hulble flour: Hriphys Hulle constant : (1203) · Copleid sters in distat yelexies \longrightarrow measure distance (intrisic lui osty I known, measure $\overline{\Phi} = \frac{\overline{I}}{4\overline{n} d^2}$) \Rightarrow $x \propto d$ $x = H_0 d$ $H_0 = 100 h H_p^{-1} km s^{-1}$ ~~/ h ~ 0.7

interpretation : This do not more every for my, we being at the center The minense expands, il distances your Golaries line at fixed coordinates X * Q(to) Q(t)to) Ze ter distace is Dr= 0 Dx $\vec{v} = \vec{n} = \vec{o} \vec{\Delta x} = \vec{o} \vec{\Delta n}$ than Hullde toolog: (Ho = Hitto) = 100 le km 5-1 Mpc-1 L ≈ 0.7 $(1pc = 3.26 lyr = 2 \times 10^{5} AU)$ = 3.09 × 10¹³ km = 2.2 h × 10 - 42 Gel @ Disto as one tricky in condogy. (comoing distance DX physical distance Dr = O(t) DX ore not measurable because defined from two separate events at fired time

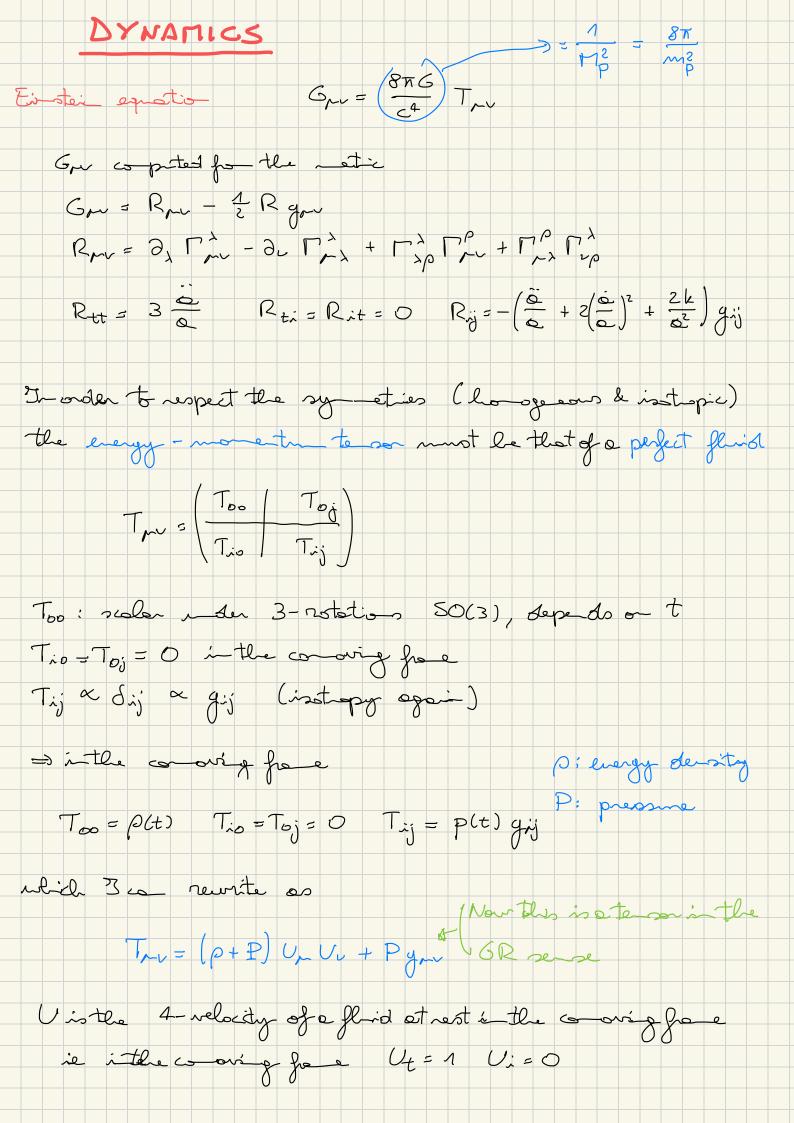
Redshift Evengtling me know about the Universe is igened for light received from distant objects. Hour stores the expansion officit -le light ?

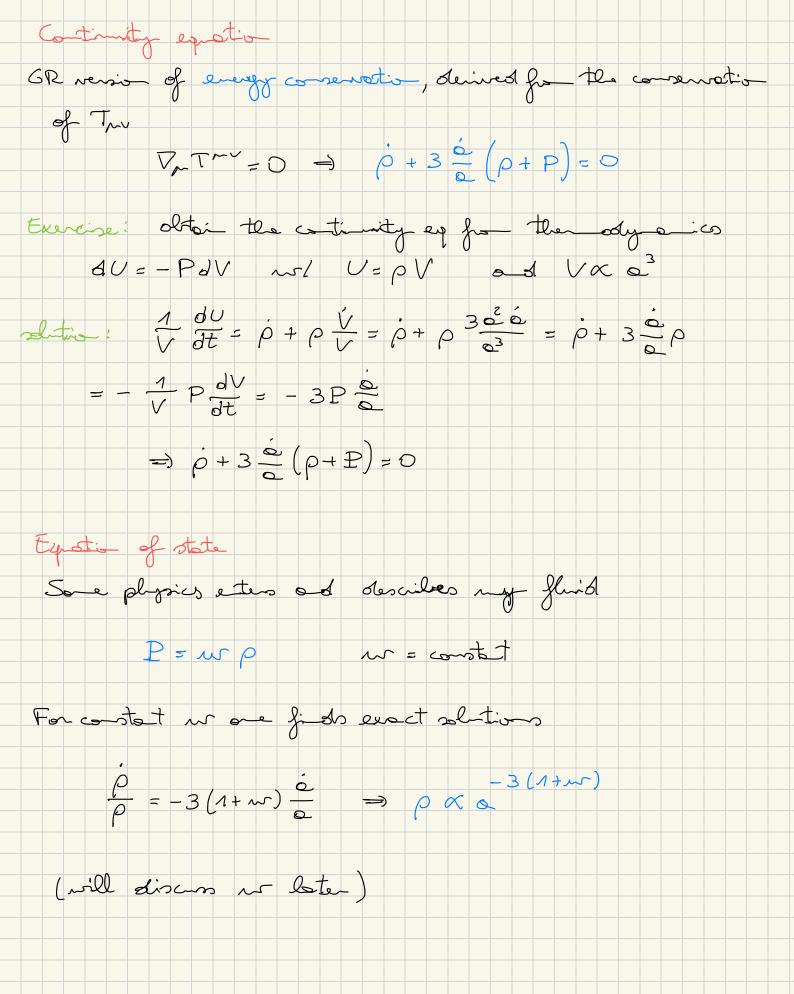
Look at geodesics mil 23=0 in FLRW:





Redshift is a measure of time (closen to actual deservations: redshift is measured, while time is derived for 2 w/anodel)





First Friedmann equation

$$G_{0}^{\circ} = 8\pi G T_{0}^{\circ} : H = \left(\begin{array}{c} 0 \\ 0 \end{array} \right)^{c} = \frac{8\pi G}{3} p - \frac{k}{3^{2}}$$

$$\left(\begin{array}{c} G_{0}^{\circ} = 8\pi G T_{0}^{\circ} : \frac{0}{3} = -\frac{4\pi G}{3} \left(p + 3P \right) \right)$$

$$\left(\begin{array}{c} \sigma & \circ + cotimity \end{array} \right)$$

$$i \cdot structure Neutono deinottion is obso possible$$

$$F = -G \frac{1}{n^2} \qquad m/ \ln = \frac{4}{3} \pi n^3 \rho$$

and
$$3 = define a energy (1 = -G \frac{1}{72})$$

The energy of the test patile is $E = \frac{1}{2}mn + \frac{1}{72} = \frac{1}{72}$

Use comoning condinates
$$\overrightarrow{r}(t) = o(t) \overrightarrow{x}$$

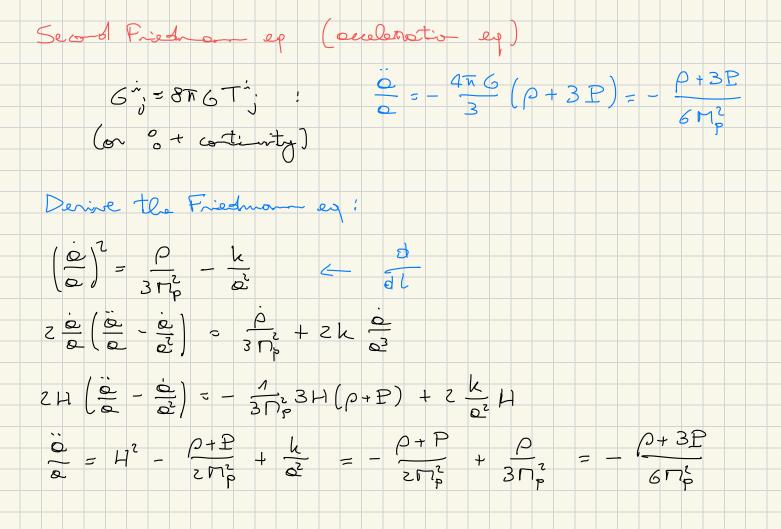
$$-7 \quad E = \frac{1}{2} m \dot{o}^{2} x^{2} - Gm \frac{1}{0 \times 3} \frac{4}{3} \pi \rho \dot{o}^{3} x^{2}$$

$$\frac{2E}{m \times 2} = \dot{o}^{2} - \frac{\rho}{3 \Pi_{p}^{2}} \dot{o}^{2} \qquad = \frac{2E}{m \times 2} \quad in \times i dependent$$

$$ZE = \dot{o}^{2} - \frac{\rho}{3 \Pi_{p}^{2}} \dot{o}^{2} \qquad = M \times 2 \quad in \times i dependent$$

$$\Rightarrow \left(\frac{\dot{\omega}}{\omega}\right)^2 = \frac{\rho}{3\Gamma_p^2} = \frac{k}{\omega^2}$$

.

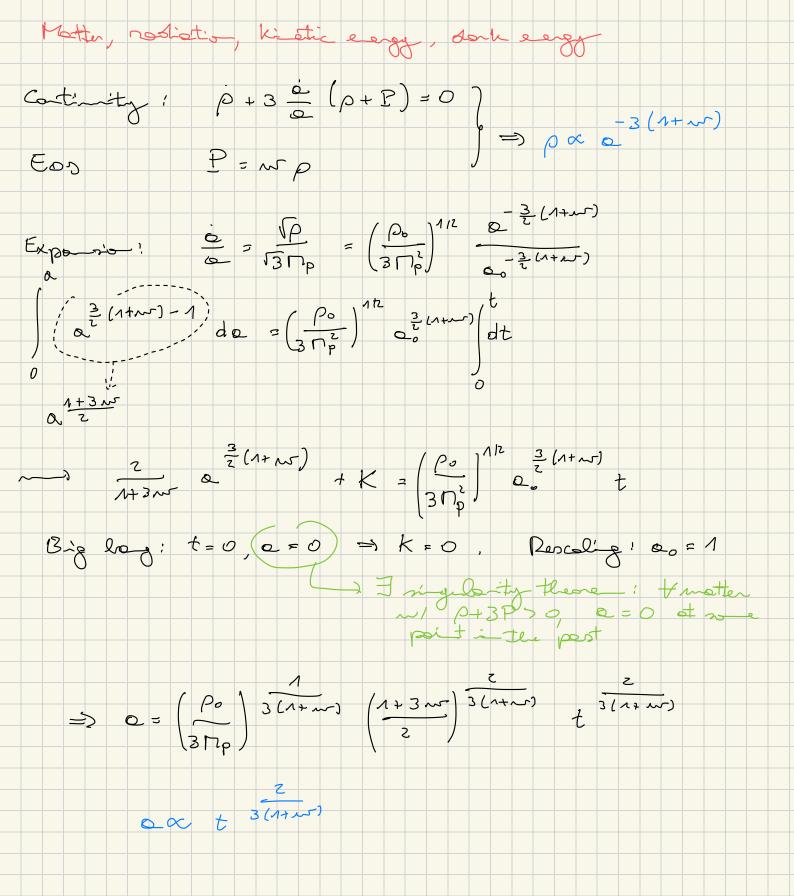


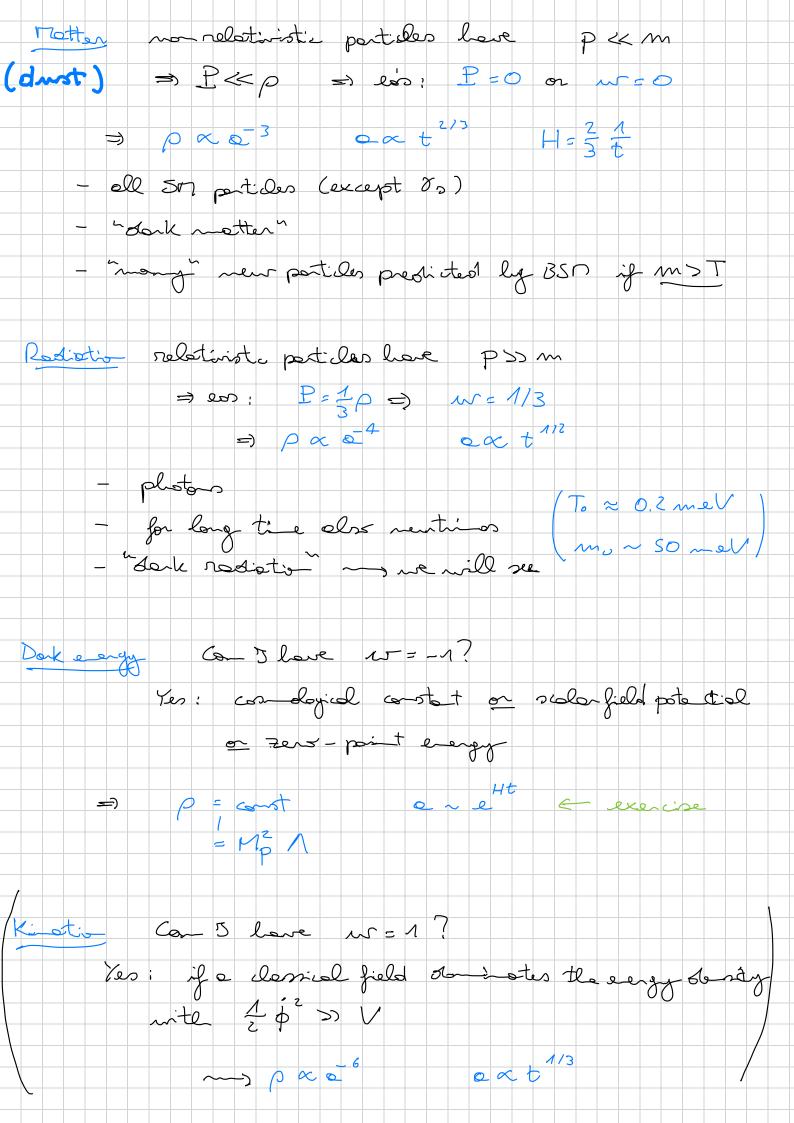
For all for ilion fluids: p+32>0 => a < D

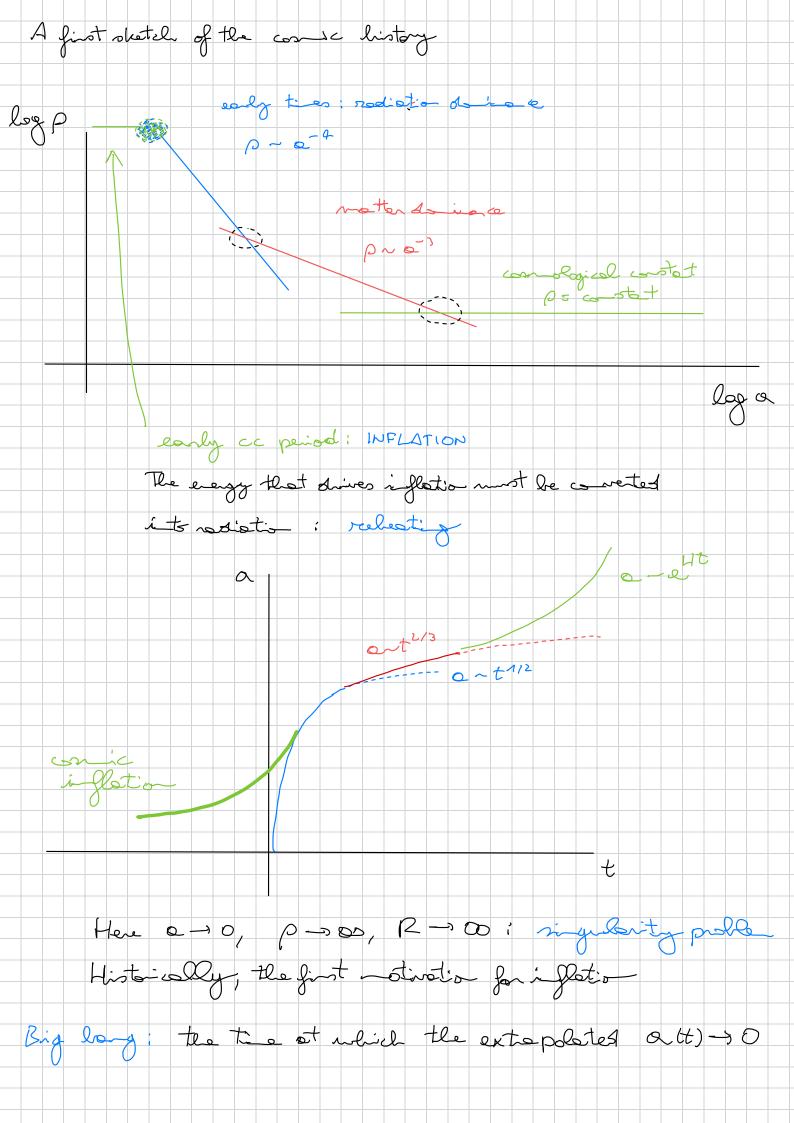
ie: gravity pulls the Chivense together

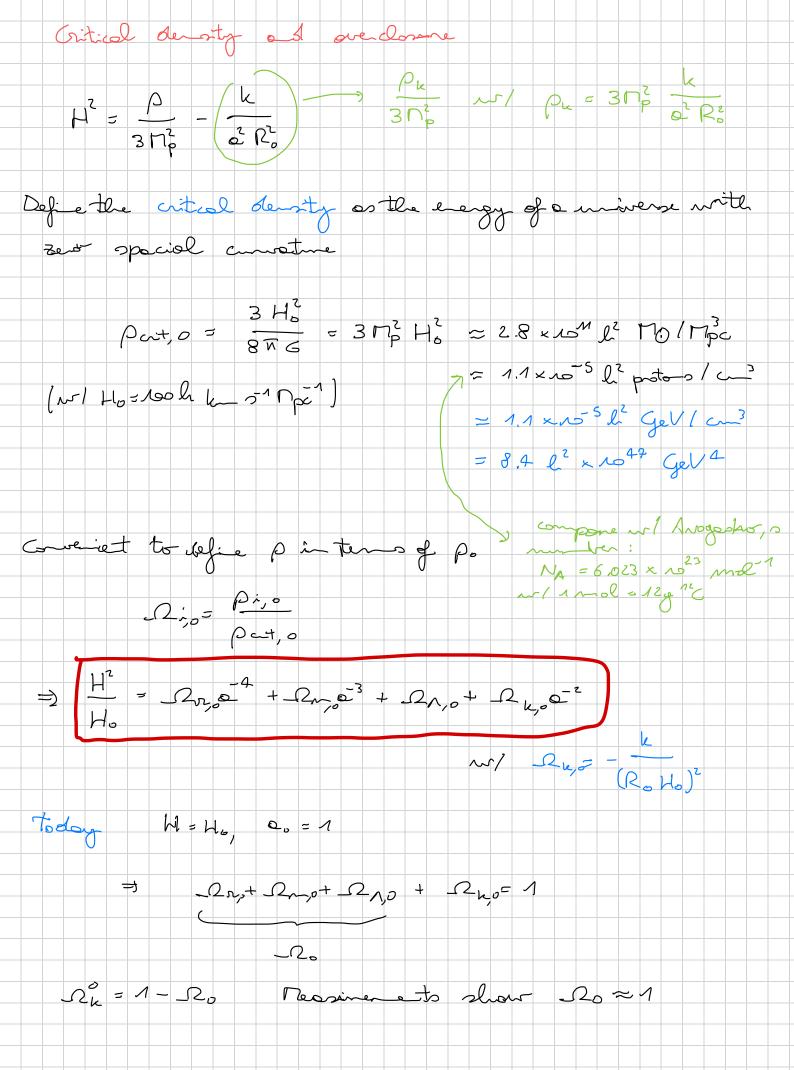
lat desenations tell us a > > our minerse

accelhrates









Engy Indget of the Universe Plotons plotons for the CT23, with a temperature of $T_{\gamma} \approx 2.73 \text{ K} \implies p_{\gamma} \sim T_{\delta}^{4} \sim 10^{-52} \text{ GeV}^{4}$ -Qryo ~ 9.4× 10⁻⁵ Nertion ne expect the existence of a cosmic W lockyron of $rac{T_{u}}{T_{v}} = T_{y} \Rightarrow \rho_{u} = \Lambda \rho_{z}^{-\Lambda s} \rho_{z}^{-\Lambda s}$ Bongons (ie no nel potiles) qu'ile esti ate (grat me brens are ~ rondon) $P_{\mathcal{B}} = \frac{M_{\text{cyplexy}}}{D_{\text{cyplexy}}^3} \sim \frac{10^{12} M_{\odot}}{(10 M_{\text{pc}})^3} \sim \frac{C_{\text{pel}}}{m^3} \sim 10^{-2} \rho_c$ more qua titatiely if mber are chose in mel a way to get the conect brendt Rz, 0 2 0.05 Ully "loyon? electrons are mostly trapped in atom and they weight way law the the scent =) most of the man ear on for p, m Dark mater $-2c\partial n_{1}o \simeq 0.27$

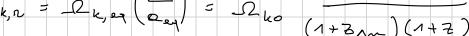
Dork energy 22 ~ 20.68

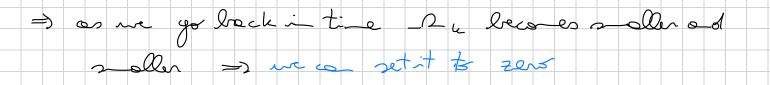
Event	time t	redshift \boldsymbol{z}	temperature T
Singularity	0	∞	∞
Quantum gravity	$\sim 10^{-43}{\rm s}$	_	$\sim 10^{18}{\rm GeV}$
Inflation	$\gtrsim 10^{-34}{\rm s}$	-	_
Baryogenesis	$\lesssim 20\mathrm{ps}$	$> 10^{15}$	$> 100 {\rm GeV}$
EW phase transition	$20\mathrm{ps}$	10^{15}	$100{ m GeV}$
QCD phase transition	$20\mu s$	10^{12}	$150{ m MeV}$
Dark matter freeze-out	?	?	?
Neutrino decoupling	$1\mathrm{s}$	6×10^9	$1{ m MeV}$
Electron-positron annihilation	$6\mathrm{s}$	2×10^9	$500\mathrm{keV}$
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Present	13.8 Gyr	0	$0.24 \mathrm{~meV}$

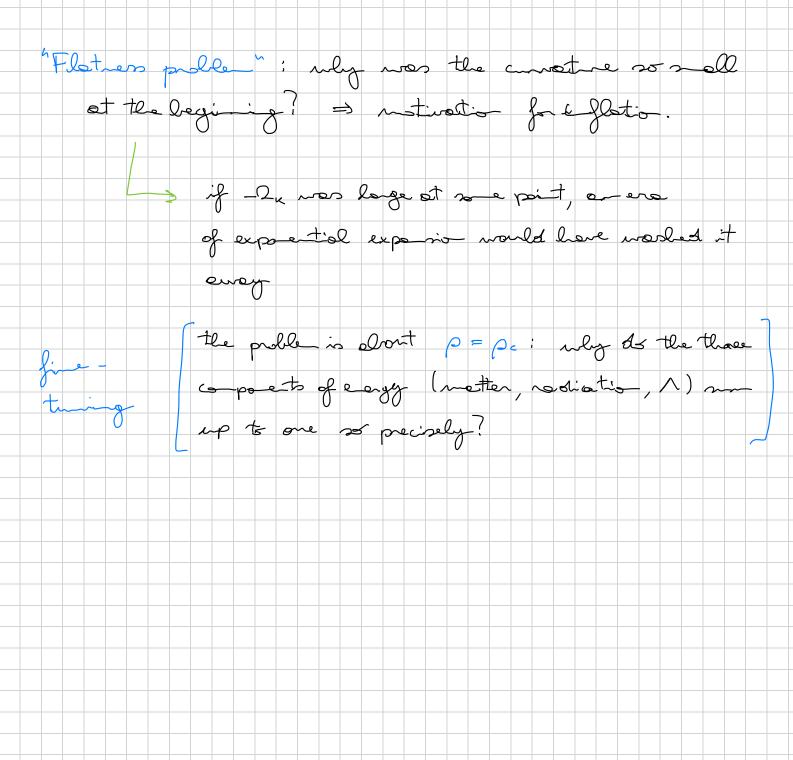
 Table 3.1: Key events in the thermal history of the universe.











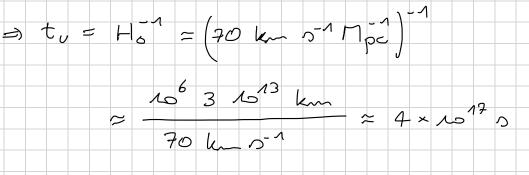
Age of the Universe

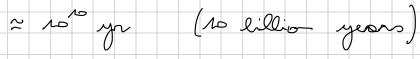
Noire estite We have seen that yelexies receed at a

oversige speed

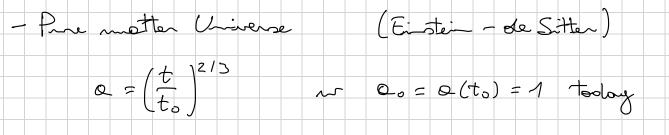
 $N = H_{od}$

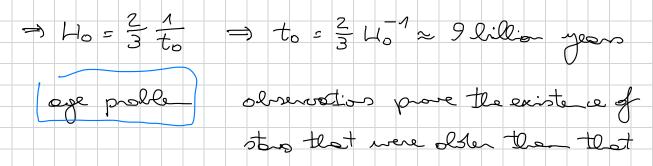
Assuming constat is => d= i tu = Hod tu



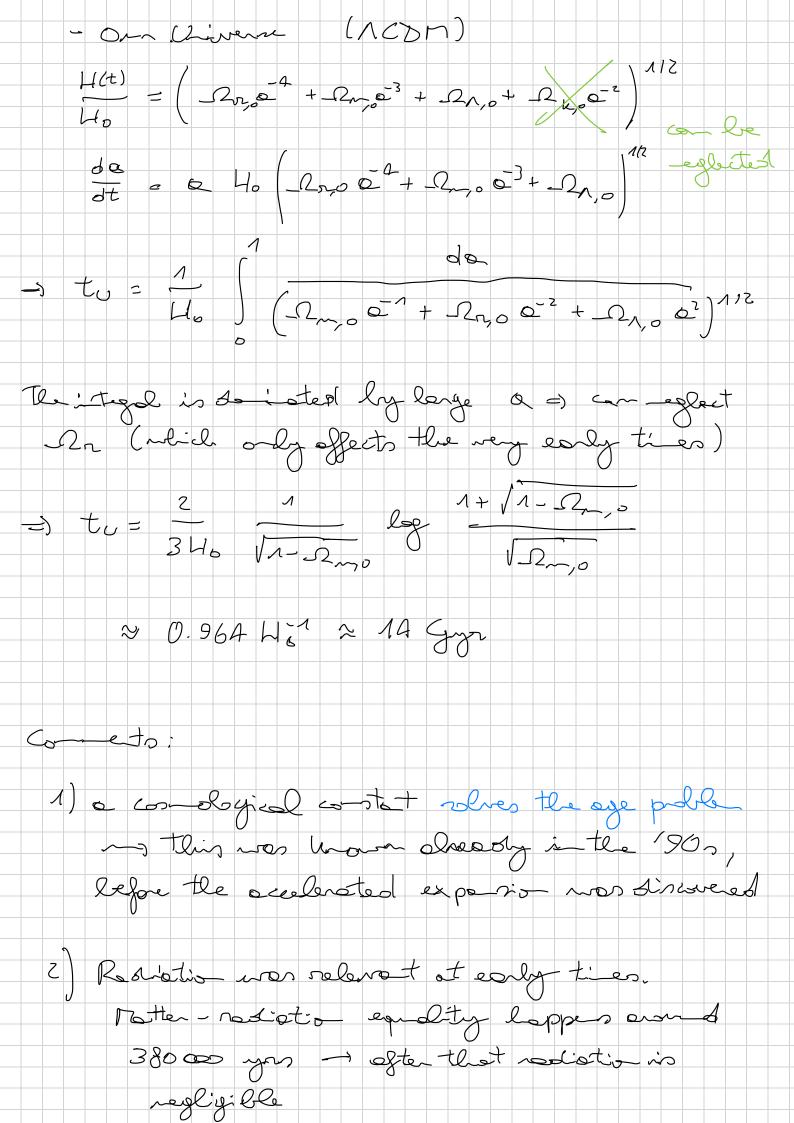








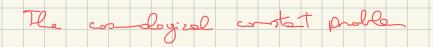
odel refere ca here!!

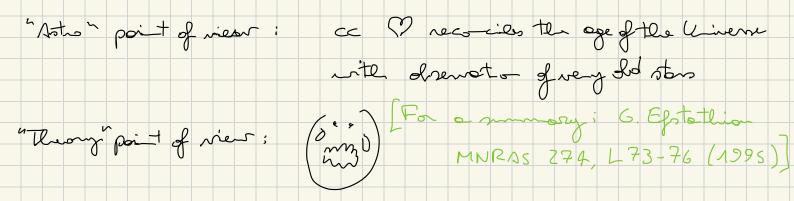


COSNOLOGICAL

CONSTANT







Field theory (clamical): potential energy contributes to A

QFT: every part de ainses as a glictation of a quantum field Fields can be represented by a man ber of Formier mades with feynercy wk. These modes satisfy the ear of a honoic oscillator ~ respontifications with energy 2 there. Let's m mp there engies $P_{\alpha FT} = \sum_{k} \frac{2}{V} \frac{\omega_{k}}{V} = h^{3} \omega_{k} - h^{4} \rightarrow +\infty$ Mayle put a cut off at le ~ Mx ie the lighest engry at which we know QFT works POPT ~ Emi mi ~ Sti masses? $P_{QGT} = (1 T_{UV})^4 \sim 10^{60} P_{\Lambda}$ Verth

10/10 yourty this doesn't effect the world (even though Cosieffect is a real thing.) But granty couples to The in paintantes.

Scalar field vite logingo

$$\mathcal{L} = \frac{1}{z} \partial_{\mu} \phi \partial^{\mu} \phi - V(\phi)$$

Cornical fields: a field displaced for the minum of the
potential velocies clarically

$$\begin{bmatrix} \phi, \phi \end{bmatrix} \approx 0$$
Energy momentum tenson:

$$Trr = \frac{2}{1-g} \frac{\delta(1-g L)}{\delta grv}$$

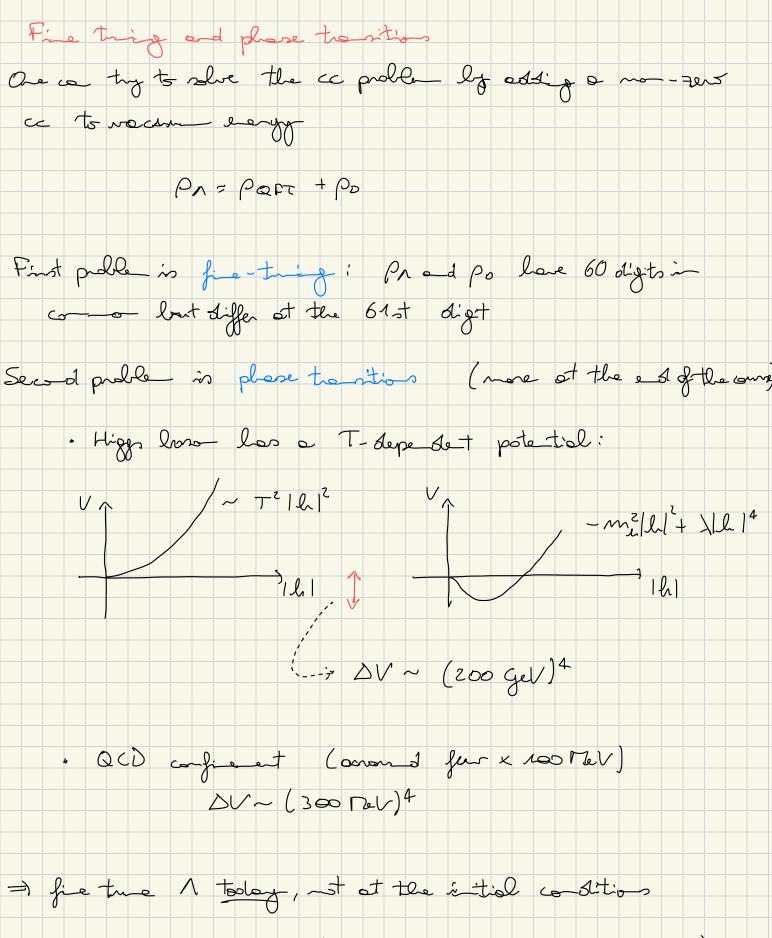
$$T_{or} = \rho \phi = \frac{1}{2} \partial_{rr} \phi \Rightarrow \phi + V(\phi) + \dot{\phi}^{2}$$

$$T_{ij} = E \phi g_{ij} = g_{ij} \left(-\frac{1}{2} \partial_{r} \phi \Rightarrow \phi - V(\phi)\right) + \partial_{z} \phi \partial_{j} \phi$$
Neglecting spatial derivatives (minfor field)

$$P \phi = \frac{1}{2} \dot{\phi}^{2} + V(\phi)$$

$$= m = \frac{1}{p} \frac{\dot{\phi}^{2}}{\delta \phi} + V(\phi)$$
Now armonic $\dot{\phi} \approx 0$ (for evolution field with in a

 \Rightarrow $w = \frac{-V}{V} = -1 \Rightarrow$ scalar potential behaves as a cc.



· lands for NS (QCD is decoupied at the core)

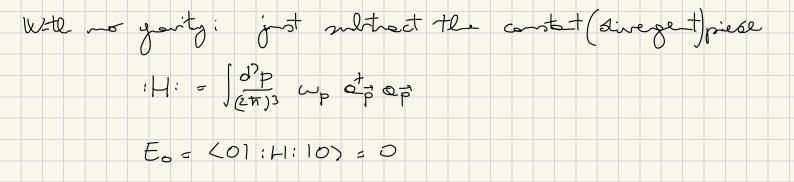
Vocume energy in QFT & Comin effect Are vocument flectuations a real thing? Scolor field $\mathcal{L} = \frac{1}{2} \partial_{\mu} \phi \partial^{\mu} \phi - \frac{1}{2} m^{2} \phi^{2}$ cojgete moret Tr = 50 Handtania $\mathcal{H} = \pi \dot{\phi} - \mathcal{L}$ (denty) $\mathcal{H} = \int d^3 \times \mathcal{H} = \int d^3 \times \frac{1}{2} \pi^2 + \frac{1}{2} (\nabla \dot{\phi})^2 + \mathcal{V}(\phi)$ $e = \left(\dot{\phi} = \frac{\partial \mathcal{H}}{\partial \pi} \qquad \dot{\pi} = -\frac{\partial \mathcal{H}}{\partial \phi} \right)$ $\Phi = \int \frac{d^3 k}{(2\pi)^3} \frac{1}{\sqrt{2\omega_k}} \left[\begin{array}{c} i \vec{k} \cdot \vec{x} \\ \phi \vec{k} & \phi \vec{k} \\ \phi \vec$ Questination: $\overline{n} = \int \frac{d^3 k}{(k\pi)^3} (-i) \sqrt{\frac{\omega_k}{2}} \left(\begin{array}{c} i \overline{k} \cdot \overline{z} \\ \overline{\omega_k} & 2 \end{array} \right) - \overline{\omega_k} \left(\begin{array}{c} -i \overline{k} \cdot \overline{z} \\ \overline{\omega_k} & 2 \end{array} \right)$ $\left(\phi,\overline{n}\right) = i\delta^{3}(\overline{x}-\overline{q})$ $\left[\phi_{\overline{p}},\phi_{\overline{q}}\right] = (2\pi)^{3}\delta^{(3)}(\overline{p}-\overline{q})$ Compte the Hailtonia; $= \int \frac{d^{3}p}{(2\pi)^{3}} \exp\left(\frac{1}{2\pi} + \frac{1}{2}(2\pi)^{3}\right) \left(\frac{1}{2\pi}\right) + \frac{1}{2}(2\pi)^{3} = \frac{1}{2}\left(\frac{1}{2\pi}\right) + \frac{1}{2}\left(\frac{1}{2\pi}\right)$ nor of ordered $ihi = \int (2\pi)^3 (2\pi)^3 (2\pi)^2 \Phi_{\vec{p}}^2 \Phi_{\vec{p}}^2$

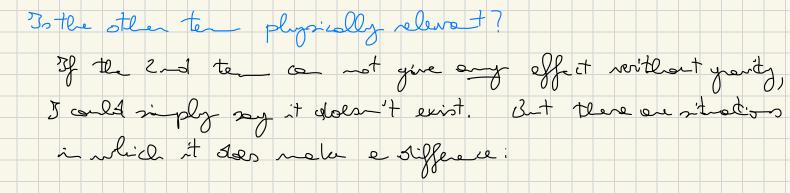
(doubly diverget) (doubly diverget)

53707: IR diverge a -> it rendy represents a volume

$$(2\pi)^{3} \delta^{(3)}(0) = \left(\begin{array}{c} L^{(2)} & \overrightarrow{p} \cdot \overrightarrow{z} \\ d^{3}x & e \end{array} \right) = \left(\begin{array}{c} L^{(2)} & \overrightarrow{p} \cdot \overrightarrow{z} \\ d^{3}x & e \end{array} \right) = \left(\begin{array}{c} d^{3}x & e \end{array} \right)$$

 $\Rightarrow E_{regy} den'ty: E_{p} = \frac{E_{0}}{V} = \int d^{3}p \frac{1}{2} \omega_{p} \qquad (UV diverget)$

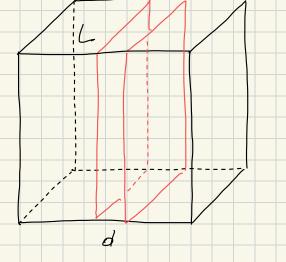




QFT à fite volne

Box of fite size DX = L (if: Ze for siplicity in y,7) Periodic be $\phi(\vec{x}) = \phi(\vec{x} + L\hat{x})$

Frent turs parallel, reflecting plates reporte by a distance dech



(eg the plates are imors and \$ at the plates $\phi = 0$ is the electric field)

 $\vec{p} = \left(m\frac{\pi}{d}, P_{\sigma}, P_{z}\right)$ $(\mathbb{Z} \setminus \{0\})$ $m \in \mathbb{Z}^{+}$

Energy per muit morface (leturen the plates)

 $\frac{E(d)}{A} = \sum_{n=1}^{\infty} \int \frac{dp_{n} dp_{n}}{(2\pi)^{2}} \frac{1}{2} \sqrt{\left(\frac{m\pi}{d}\right)^{2} + p_{n}^{2} + p_{n}^{2}}$

 $E = E(d) = E(L-d) \qquad \text{not exact last only soll}$ $A = A + A \qquad \text{constants for the brandomy}$ Total eagy:

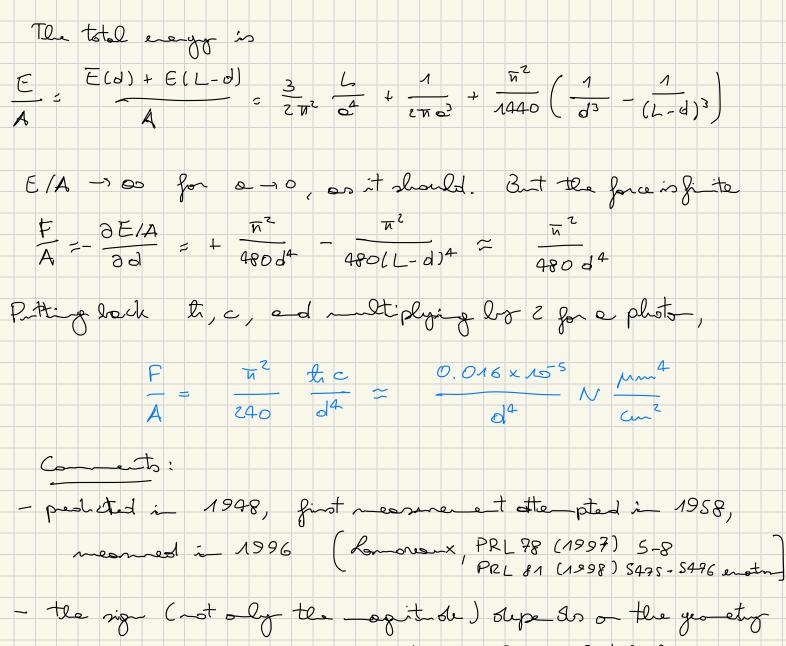
$$E(d)/A \quad in \quad \text{firsts} \quad (UV) \quad die to althorney light momenta
Not playnowl: a minimum const le presit above me fragmency!
This is a first even ple of remained ratio (PK playne)
Tothe study : me und to cut - for the integral at some high
fragmency, regarding modes $P \gg a^{-1}, m/a \ll d$.
The production is somewhat address, this the random most not
depend on a

$$\frac{E(d)}{A} = \sum_{n=1}^{\infty} \int \frac{dPo}{(DT)^n} \frac{dP}{2} \int \frac{dP}{(DT)^n} \frac{dP}{2} + P_{2}^{i} + P_{2}^{i} = \frac{a}{\sqrt{(T_{1}^{int})^{i}} + P_{2}^{i} + P_{2}^{i}}$$
(gives locatile periors could for $a \rightarrow 0$)
Define $P_{2} = P \cos q$ $P_{2} = P \sin q$

$$\frac{E(d)}{A} = \sum_{n=1}^{\infty} \int \frac{dPo}{(2T)^n} \frac{dP}{2} \int \left(\frac{mT}{d}\right)^{i} + P_{2}^{i} + P_{2}^{i} = a^{-1}$$

$$\frac{P}{4} + \left(\frac{mT}{d}\right)^{i} = m^{2}$$
 $p dP = \frac{1}{2} dP^{2} = \frac{A}{2} dM^{2} - ndm$

$$\frac{E(d)}{A} = \frac{2T}{2} \int \frac{D}{dM} \frac{dM}{dM} - \frac{2}{a^{-n}} = \frac{A}{2T} \int \frac{dT}{dM} \int \frac{dM}{dM} = \frac{2}{a^{-n}} \int \frac{dT}{dM} = \frac{M}{a^{-n}} \int \frac{dT}{dM} = \frac{1}{a^{-n}} \int \frac{$$$$



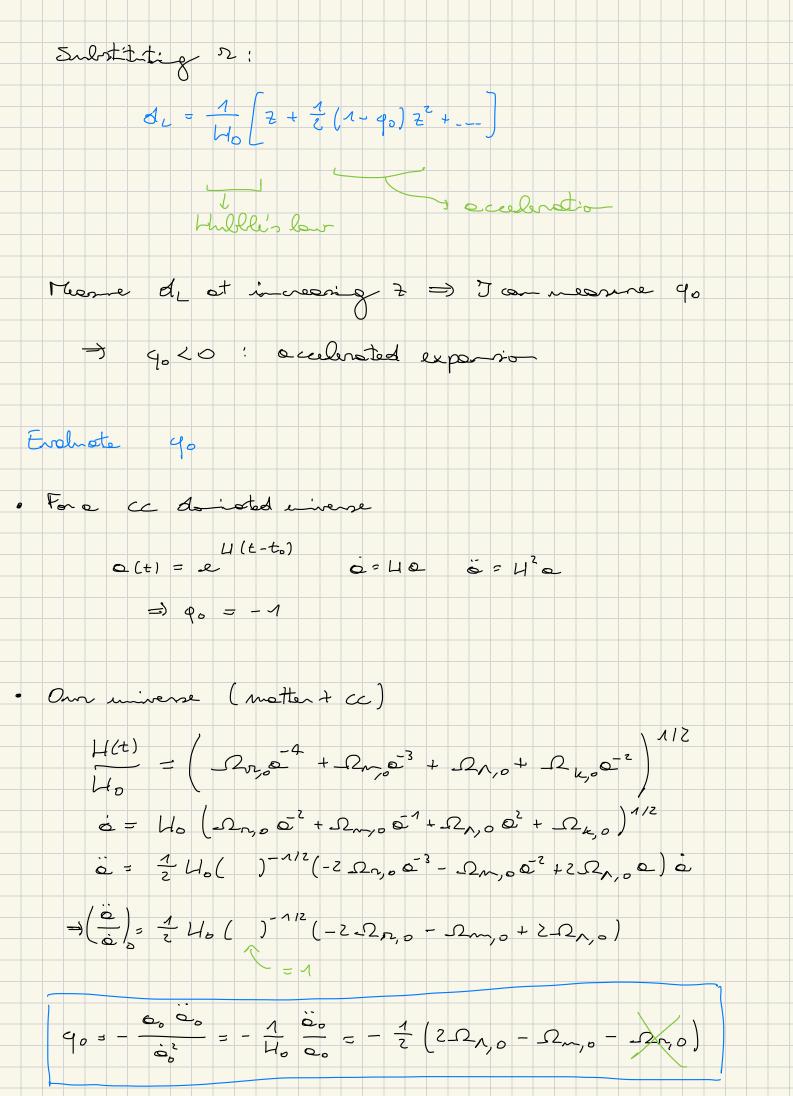
- somehans related to Van Sen Vools force, but I have a isles har it works.

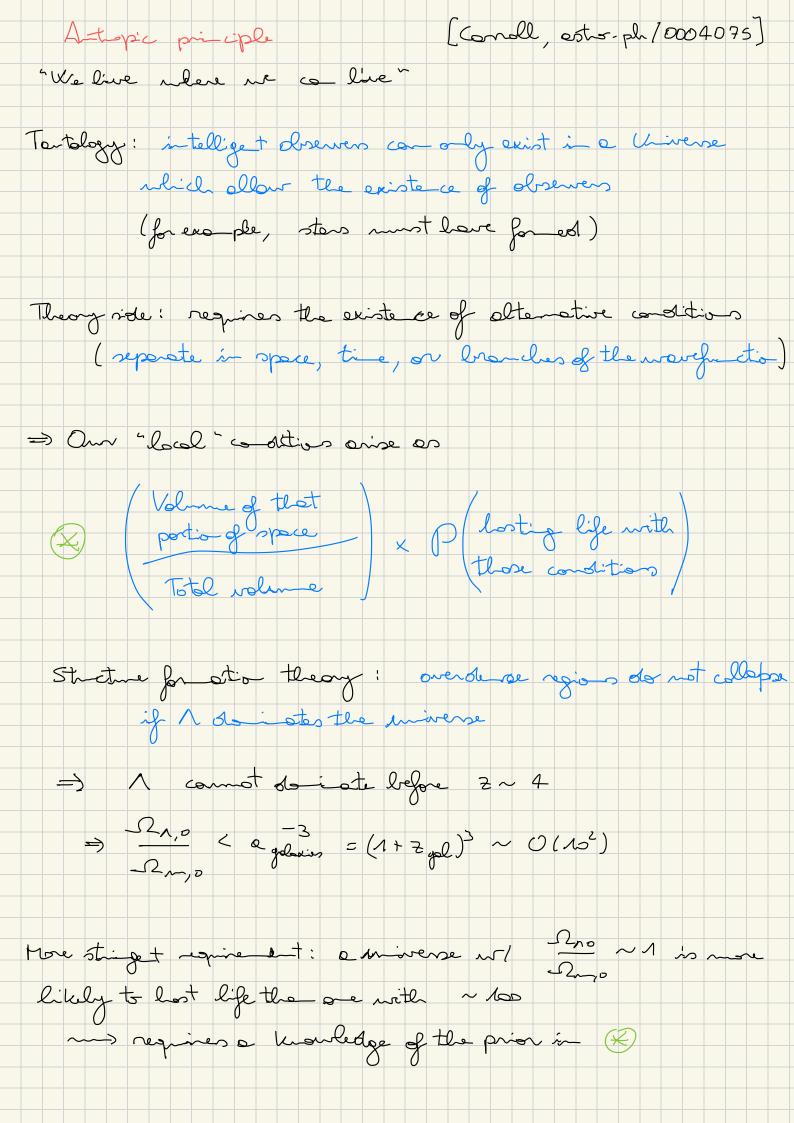
- only photo field matters :

ent-off frequery of ~ O(wp) - week << me mentions one not reflected

Condinions: 1) Voum engy exists. 2) 12/10 yourty, only engy differences on inportet 3) cc in a real question! Messing the accelerated expansio

de liniosty distance: attendent of light comp for a distat surce Depedro a (t) olog the path - area correred by may sutector : 5 4Tr 02 r2 - for ension until almentio instinichal photos have a stearence in energy of (1+2)-7 - photons entted once every St one detected once every St (1+7) =) detected pourer is real shifted os (1+2)-2 $\Rightarrow d_{L}^{2} = e_{0}^{2} r_{1}^{2} (1+2)^{2}$





THE UNIVERSE

IN THERMAL EQUILIBRIUM

Themal equilibrium

Example: weak interactions (at
$$p < m_w$$
)
 $T \simeq G_p^2 p^2$ at terperature $T \longrightarrow T = G_p^2 T^2$

interaction note [= molN]

$$me \operatorname{congreen} : m = N/2 = 1$$

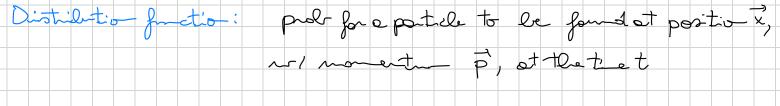
$$p \sim e^{-1} \operatorname{lnt} p \sim T$$

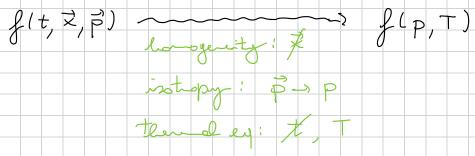
$$= 1 \sim T^{3}$$

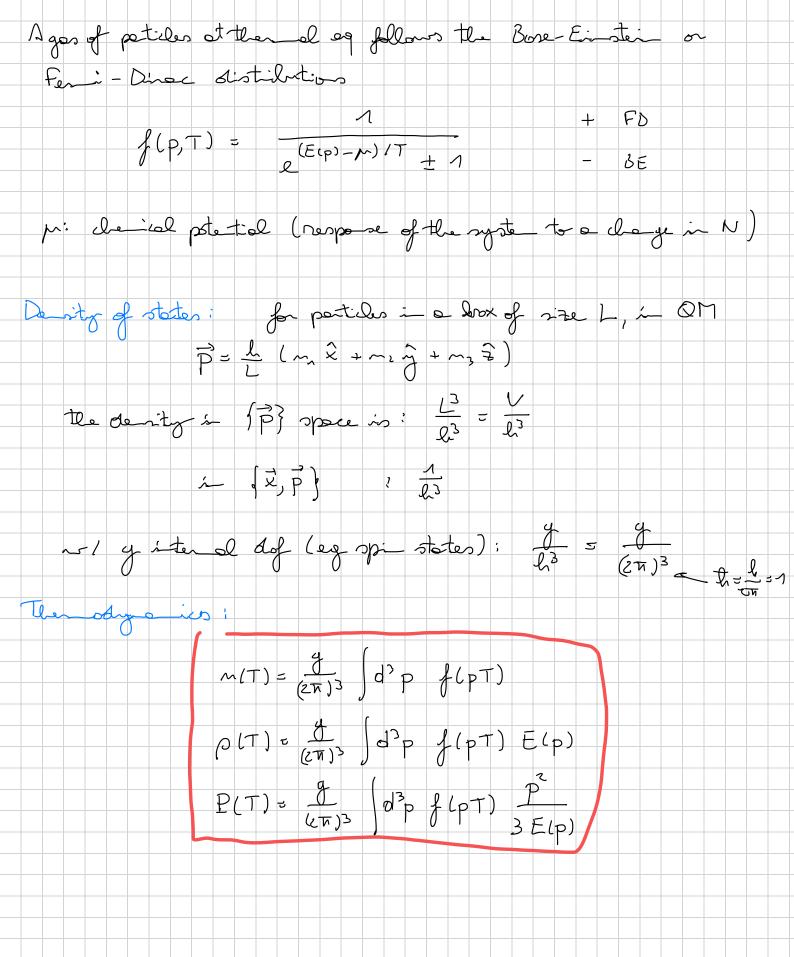
$$= 1 \quad T \sim G_{p}^{2} T^{5}$$

co-blitio for equilibrium !

Some statistical mechanics

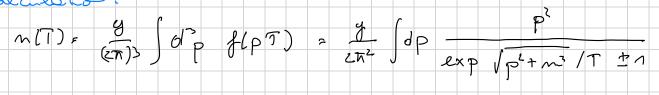






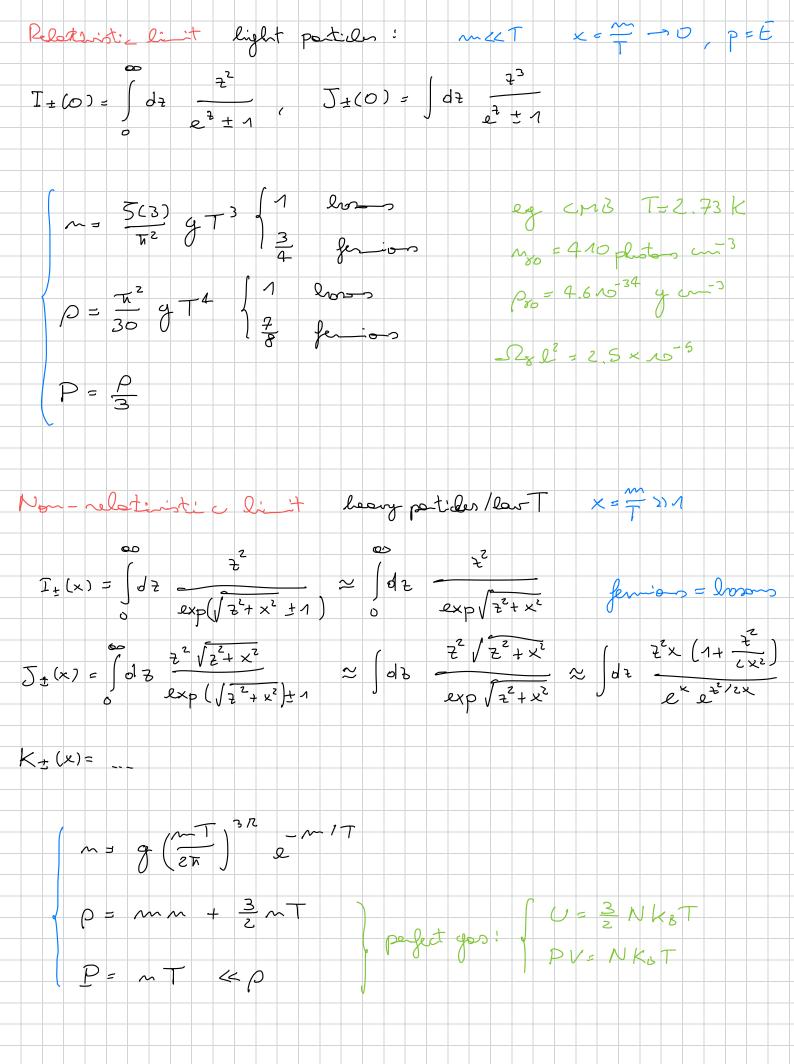
Charical pota tol con le set to zero (see Barmanno Delar) For most of the evolution pri << T, for photons pro = 0 by definition

Colculation



- $\begin{array}{c} \mathcal{Aefie} \times = \underbrace{\begin{array}{c} & \\ \hline \\ \hline \\ \end{array}} \\ \Rightarrow \\ \mathcal{Aefie} \\ \mathcal{Aefie$

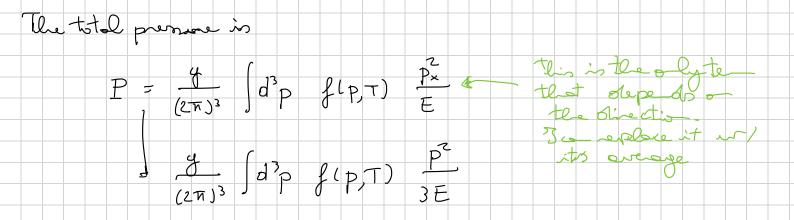
$$P = \frac{y}{2\pi^2} \int_{\pm} (x) T^4 \qquad \int_{\pm} (x) = \int_{0}^{\infty} \frac{z^2 \sqrt{z^2 + x^2}}{2x^2 + x \sqrt{z^2 + x}}$$



Demotion of the prome equation

$$dN = dn dV = \begin{pmatrix} 1 \\ 2 \\ (2\pi)^{3} \end{pmatrix} f(p) A n_{x} dt \qquad n/n_{x} > 0$$

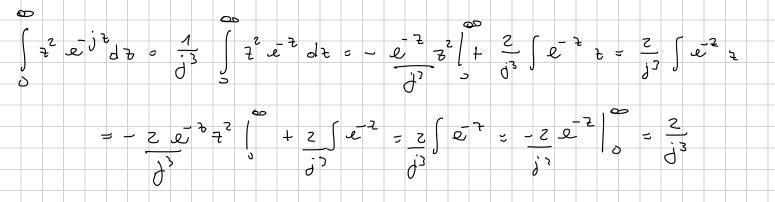
$$=) dP = \begin{pmatrix} 1 \\ dp \\ dt = \frac{1}{2} \times 2 \begin{pmatrix} q \\ (2\pi)^{3} \end{pmatrix} f(p,T) \\ E \end{pmatrix} \qquad N_{x} = \frac{P_{x}}{E}$$

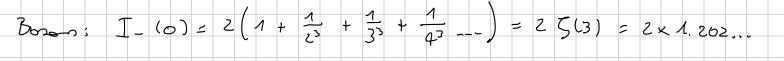


Comptation of the the solynamic qualities

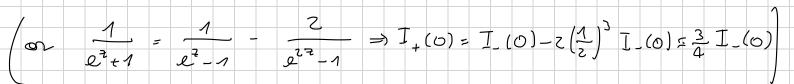
Relativistic lint x= 7 - 30

- $\boxed{I_{\pm}(0)} = \int dz \frac{z^2}{z}$ $0 \qquad z^2 \pm 1$
- $\frac{1}{e^{2}\pm 1} = \frac{1}{1\pm e^{2}} = \frac{1}{e^{2}} = \frac{1}{e^{$

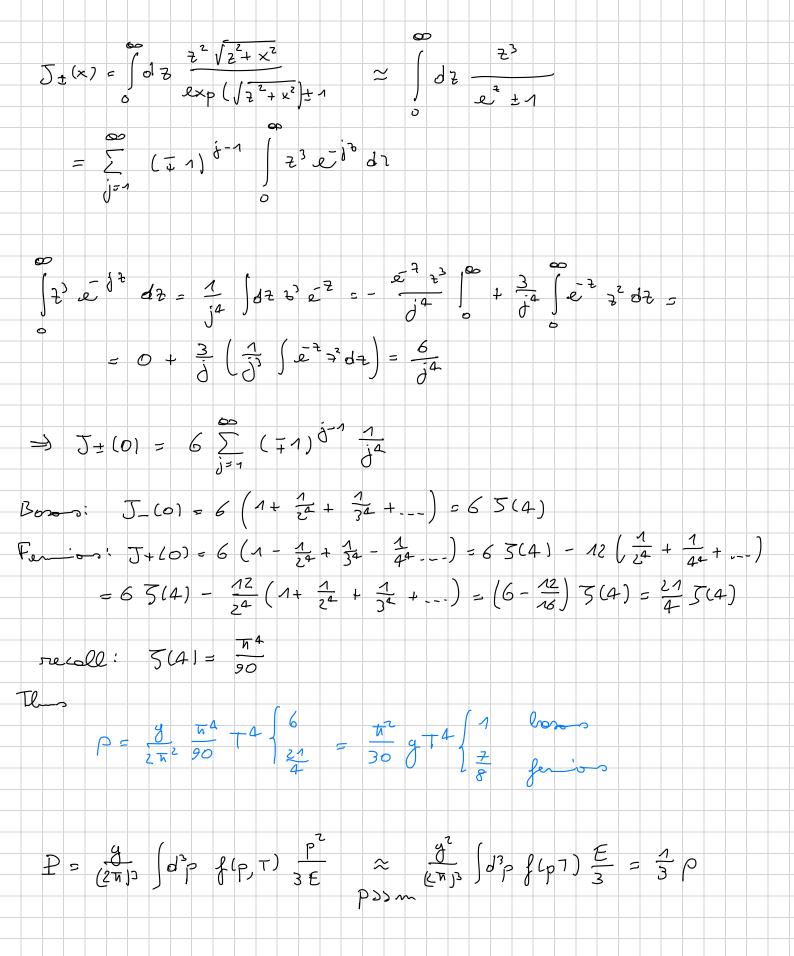




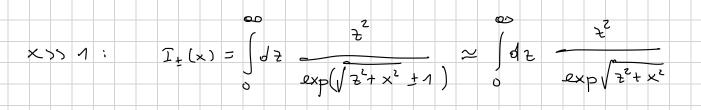
Ferriors $I_{+}(0) = 2\left(1 - \frac{1}{2^{2}} + \frac{1}{3^{3}} - \frac{1}{4^{3}} - \frac{1}{4^{3}} - \frac{1}{4^{3}} - \frac{1}{4^{3}} + \frac{1}{4^{3}} + \frac{1}{6^{3}} - \frac{1}{4^{3}} + \frac{1}{6^{3}} - \frac{1}{2^{3}} + \frac{1}{3^{3}} - \frac{1}{2^{3}} + \frac{1}{2^{3}} + \frac{1}{4^{3}} + \frac{1}{6^{3}} - \frac{1}{2^{3}} + \frac{1}{3^{3}} + \frac{1}{3^{3}} + \frac{1}{3^{3}} - \frac{1}{2^{3}} + \frac{1}{3^{3}} + \frac{1}{3^{3}} + \frac{1}{3^{3}} - \frac{1}{2^{3}} + \frac{1}{3^{3}} + \frac{1}{3^{3}} - \frac{1}{3^{3}} + \frac$

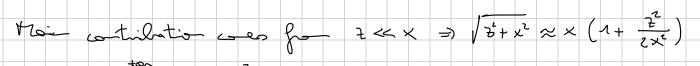


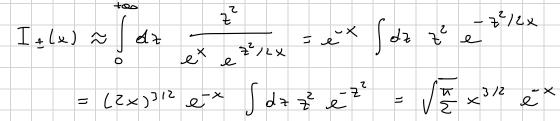
 $= \frac{5(3)}{\pi^2} + \frac{1}{\sqrt{3}} +$

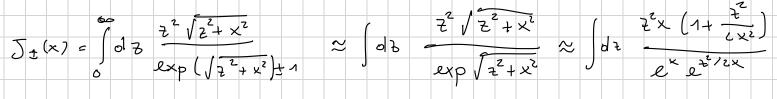


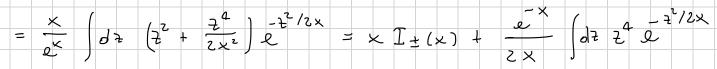
Non - relativistic light

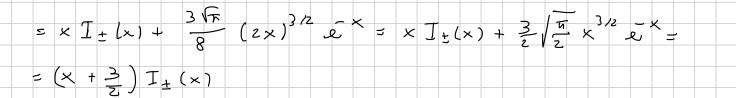


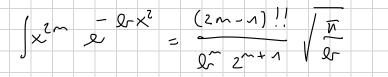










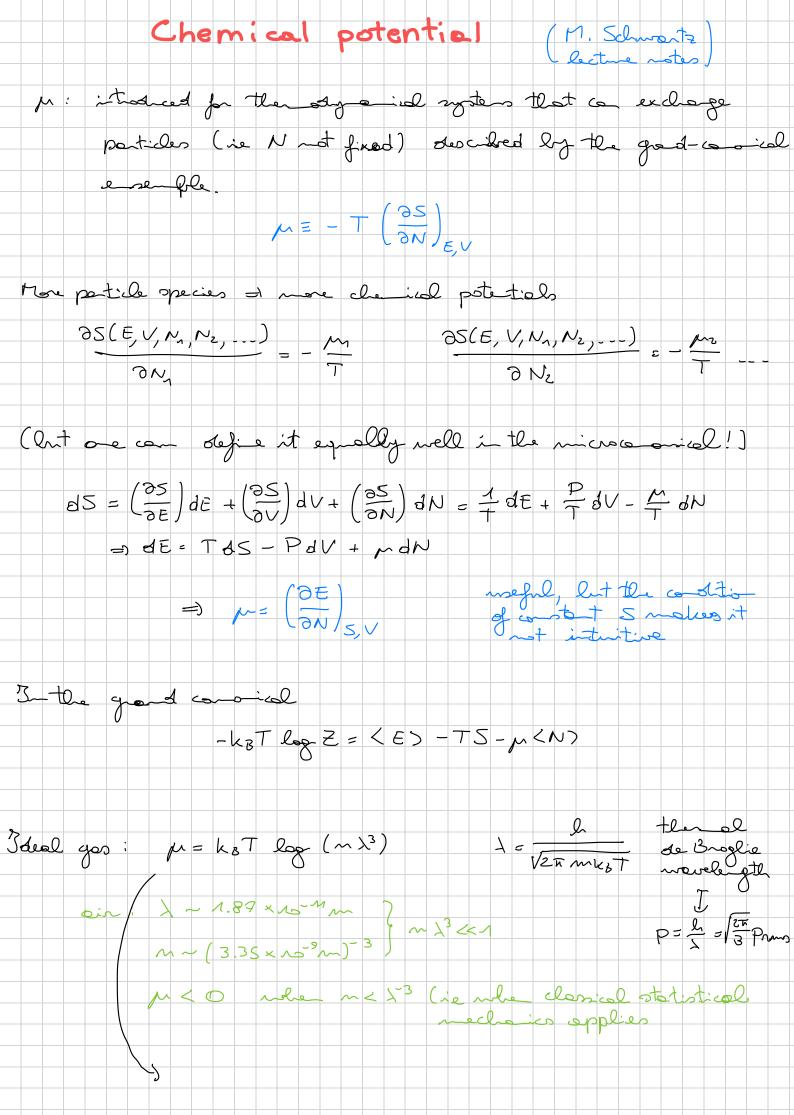


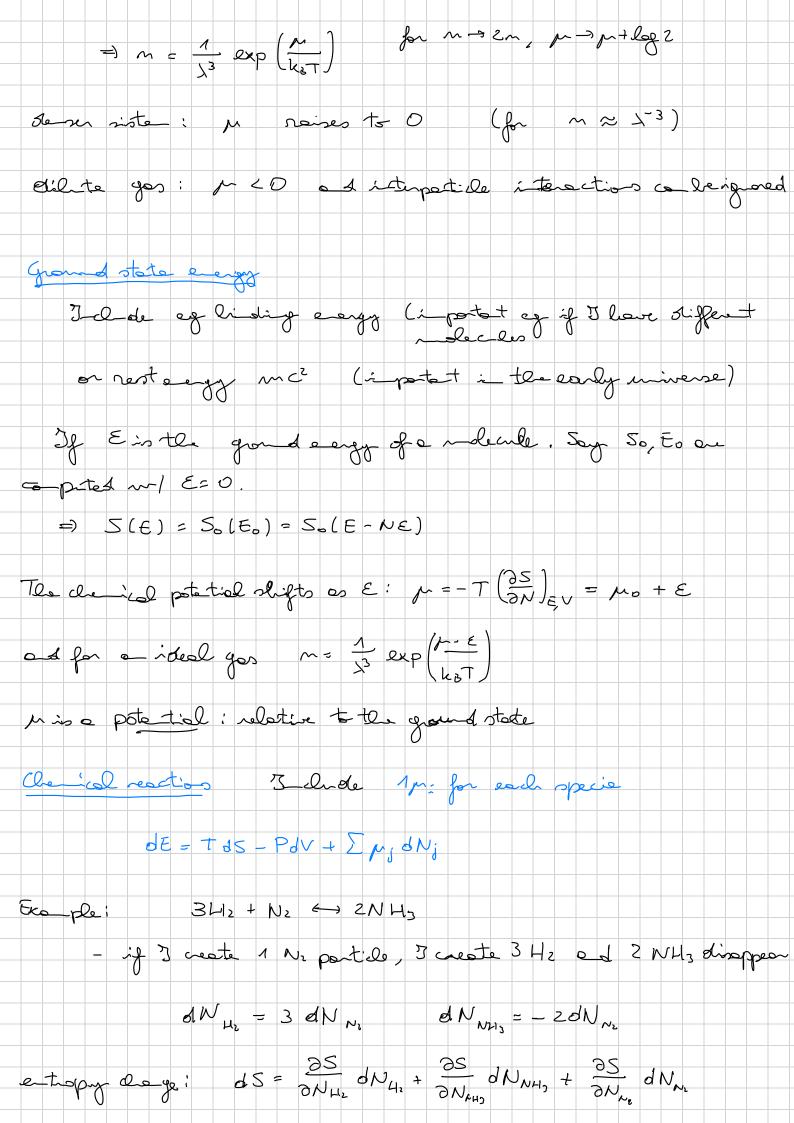
$$\int \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{3!!}{2^{3} (\frac{1}{2^{3}})^{2}} \sqrt{\frac{\pi}{1}} \frac{3\sqrt{\pi}}{1(2x)} = \frac{3\sqrt{\pi}}{8} (2x)^{5/2}$$

 $\Rightarrow p = m n + \frac{3}{2} n T$

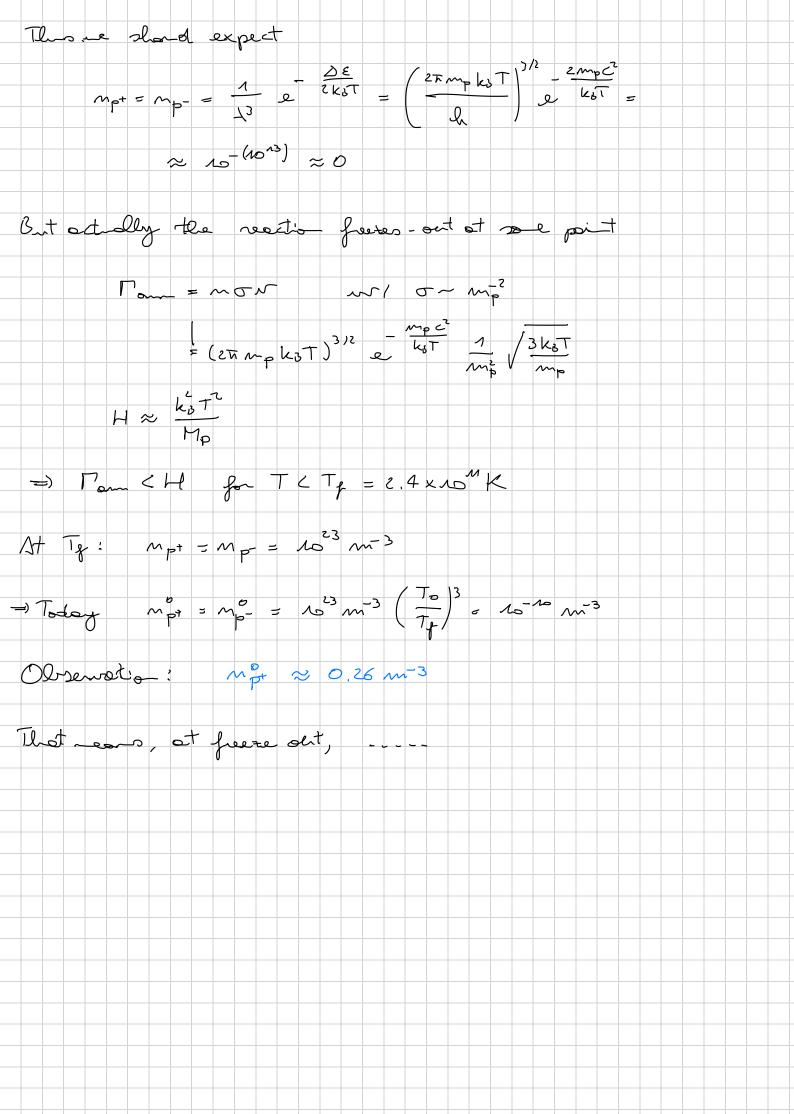
$$K_{\pm}(x) = \frac{2}{3} \int_{0}^{\infty} dz \frac{2^{4}}{(zxp(\sqrt{z^{2}+x^{2}})\pm 1]\sqrt{z^{2}+x^{2}}} \approx \frac{4}{3} \int_{0}^{\infty} dz \frac{z^{4}}{(zxp(\sqrt{z^{2}+x^{2}})\sqrt{z^{2}+x^{4}})}$$

$$\approx \frac{4}{3} \int_{0}^{\infty} dz \frac{z^{4}}{(zxp(\sqrt{z^{2}+x^{2}})) \times (x+\frac{z^{4}}{zxx^{4}})} \approx \frac{z^{4}}{3x} \int_{0}^{\infty} dz \frac{z^{4}}{z} \frac{z^{4}}{z^{4}} \frac{z^{4}}{z^{4$$





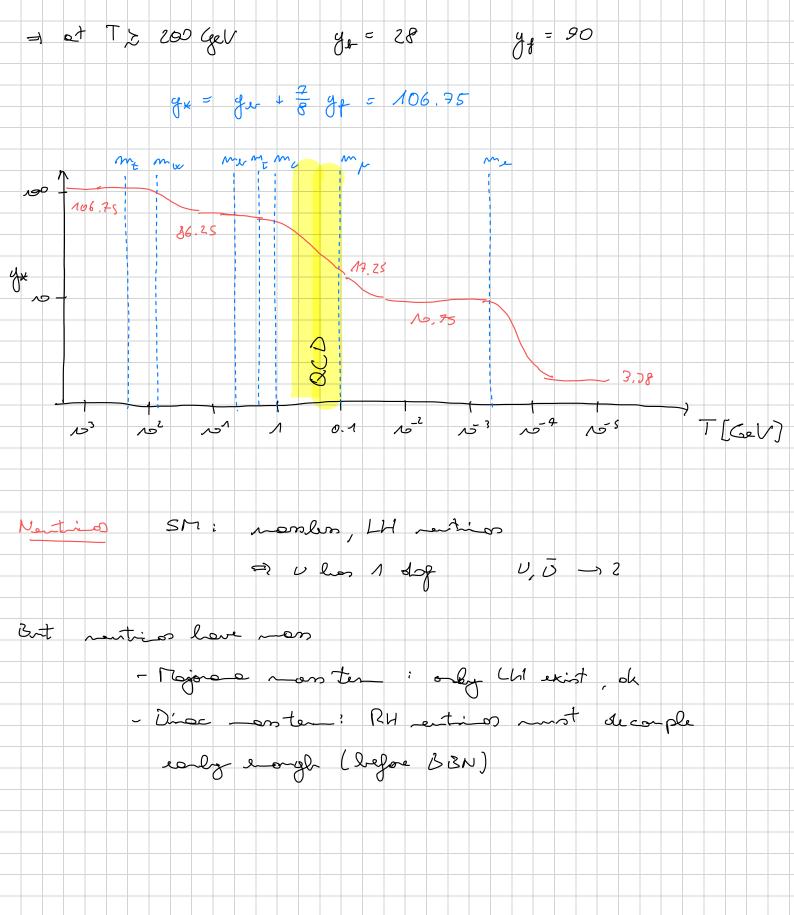
et equilibrian: $\mathbb{O} = dS = \frac{\partial S}{\partial N_{\mu_2}} \frac{\partial N_{\mu_1}}{\partial N_{\mu_2}} + \frac{\partial S}{\partial N_{\mu_3}} \frac{\partial N_{\mu_1}}{\partial N_{\mu_3}} + \frac{\partial S}{\partial N_{\mu_2}} \frac{\partial N_{\mu_3}}{\partial N_{\mu_4}} + \frac{\partial S}{\partial N_{\mu_4}} \frac{\partial N_{\mu_4}}{\partial N_{\mu_5}} + \frac{\partial S}{\partial N_{\mu_5}} \frac{\partial N_{\mu_5}}{\partial N_{\mu_5}} + \frac{\partial N}{\partial N_{\mu_5}} \frac{\partial N_{\mu_5}}{\partial N_{\mu_5}} + \frac{\partial N}{\partial N_{\mu_5}} \frac{\partial N_{\mu_5}}{\partial N_{\mu_5}} + \frac{\partial N}{\partial N_{$ $= (3 \mu_{Hz} - 2 \mu_{NH_3} + \mu_{Nz}) dN_{Nz}$ $= 3\mu_{\mu_{1}} + \mu_{\mu_{2}} = 2\mu_{\mu_{1}}$ For eq no octoric ideal gas $N_{\rm X} = \frac{1}{2^3} \exp\left(-\frac{\epsilon_{\rm X} - \mu_{\rm X}}{\epsilon_{\rm g} T}\right)$ Proton content of the Universe (Motter - on timetter any eting) $p^+ + p^- \rightarrow \delta \delta$ $\Delta E = zmpc^2 = zgeV$ (kot) E for T) 2×15¹³K) Plots not conserved: eg de es et dd $=) \quad \mu_{g} + \mu_{e} = 2\mu_{g} + \mu_{e} \quad \Rightarrow \quad \mu_{g} = 0$ Jor porticles not onocioted un/ any conservation multer 3 construction of the second Suppose nour ptp are only produced from dd -1 ptp. The pept + pro-= 0 and at equilibrium (FD distribution) mpt = mp- $\Rightarrow \mu_{p^+} = \mu_{p^-} = \Rightarrow \mu_{p^+} = \mu_{p^-} = 0$



Relativistic species

At early anylities, all particles were relationistic (STI: T 2200 GeV) $\begin{array}{c} \rho = \sum_{i} \frac{g_{i}}{2\pi^{2}} T^{4} J_{\pm} (x_{\perp}) \\ i & e^{\pi^{2}} \end{array}$ $elefie \quad y \neq i \qquad P = \sum_{n=1}^{\infty} \frac{\pi^2}{30} \quad f = \frac{1}{2} \quad \frac{1}{8} \quad \frac{1}$ $= \frac{\pi^2}{30} + 4 \left[\sum_{i=2r} q_i \left(\frac{T_i}{T} \right)^4 + \frac{2}{8} \sum_{i=2r} q_i \left(\frac{T_i}{T} \right)^4 \right]$ $= \frac{\pi^2}{30} + \frac{2}{8} \sum_{i=2r} q_i \left(\frac{T_i}{T} \right)^4 + \frac{2}{8} \sum_{i=2r} q_i \left(\frac{T_i}{T} \right)^4 = \frac{1}{1}$ boron $\gamma: q_{\gamma} = 2$ SN Wz, Z g = 3 3×3 = 9 8 K Z = 16 g gy= z H gu=1 ferios 9 gy= 2x3 (L/R, clom) 6x6x2=72 (4 port / anti-port y = 2 => 2 × 3 × 2 = 12 l 46 flowers V yu= 1 (only LH) -> 243×1=6 -> 5U(2) Joilies CQQ lrefore EWSB W+, Z: g=2 3× 2=6 Q_{L} : $Z \times 3 \times 3 \times 2 = 36$ 4 P: 3×6×2=36 H: 94 = 4 () piles L: 2 x 3 x 2 = 12 \mathcal{L}_{R} : $3 \times 2 = 6$

	م مرک	W	1,12	Q	MC	$ d^{\epsilon} $	L e	\vdash
	-مرق 							
formily	Л	1	1	3	3	3	3 3	1
	Z	2	2	1	1	-1	1 1	1
spin / helicity								
porticle (antipotide	1	Л	1	Z	Z	2	22	Z
weak isospi-	Л	3	1	Z	1	1	2 1	Ζ
color	8	1	1	3	3	3	1 1	1
	0							
statistics	1	1	Л	7/8	7/8	718 3	718 718	1
y _x	Л6	6	し こ	63/2	63/4	63/4 7	21/2 21/4	4 106.75
y×								



Entropy

Entropy is one meght the easy because it is not ally conserved

Therefyre ics; TdS = dU + PdV - mdN:

T d(sV) = d(pV) + P dV - m d(m V) (Ts - p - P + m d) dV + V (T ds - dp dT + m dm d) dT = 0

 $= D = P + \frac{P - M \cdot m \cdot}{T} \qquad \frac{d D}{d T} = \frac{\Lambda}{T} \left(\frac{d P}{d T} - M \cdot \frac{d m \cdot}{d T} \right)$

Now compute $\frac{d(2 e^{3})}{dt} = 2 \frac{d^{3}}{dt} + 3 \frac{d^{3}}{dt} = 3 \frac{e^{3}}{dt} + \frac{dT}{dt} \frac{d^{3}}{dT} = \frac{dP}{dT} = \frac{dP}{dt} + 2 \frac{dT}{dt} + \frac{dP}{dt} + \frac{dT}{dt} = \frac{dP}{dT} = \frac{dP}{dt} + 2 \frac{dT}{dt} + \frac{dP}{dt} - 2 \frac{dP}{dt} + \frac{dP}{dt} = \frac{dP}{dt} + \frac{dP}{dt} + \frac{dP}{dt} + \frac{dP}{dt} = \frac{dP}{dt} + \frac{dP}{dt$

 $mge = c_{s} t_{m} t_{g} e_{p} : \frac{dp}{dt} = -3\mu(p+P) = -3\mu(T_{s} + \mu; m;)$

= 3 2 0H - 34 2 0 - 3 H 2 4 - 2 7 dt

 $= \frac{d(so^{3})}{dt} = -\frac{m}{T} \frac{d(mo^{3})}{dt}$

Jg n=0 => d(0 est) =0 entropy is conserved

I most coses, M=O. There are other coses of entropy non-conservation, eg the decay of a heary partile which nos out of equilibrium

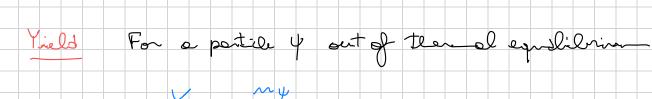
topy & relativistic specie

Collection of portule species:
$$D = \sum_{i=1}^{n} \frac{(D_{i} + P_{i})}{T_{i}}$$
 only relativistic
Time species mother

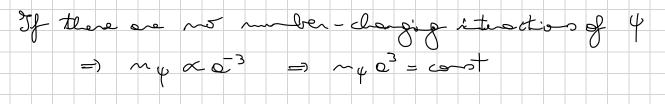
For a night relativistic specie:
$$P = p/3 = p = \frac{2\pi^2}{4S} = \frac{2}{4S} = \frac{2$$

$$Def = D = \frac{C\pi^2}{45} q_{*S} T^3$$

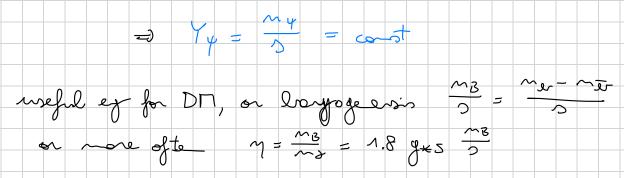
 $g_{*S} = \sum_{e} g_{\div} \left(\frac{T_{\div}}{T}\right)^{3} + \frac{7}{8} \sum_{e} g_{\div} \left(\frac{T_{\div}}{T}\right)^{3}$



$$Y_{\psi} \equiv \frac{m\psi}{s}$$







Te perature behaviora

 $S = (a \rightarrow t) = g_{*S} = (a \rightarrow t) = T \propto g_{*S} = 1$

Array for more thrusholds y* ~ contat = T ~ at

Éxpario listory

From the formulas re sour above

 $H^{2} = \frac{\rho}{3 \Pi_{p}^{2}} = \frac{\pi^{2}}{90} q^{*} \frac{\tau^{4}}{\Pi_{p}^{2}}$

