

Artificial Intelligence for Cyber-Physical Systems

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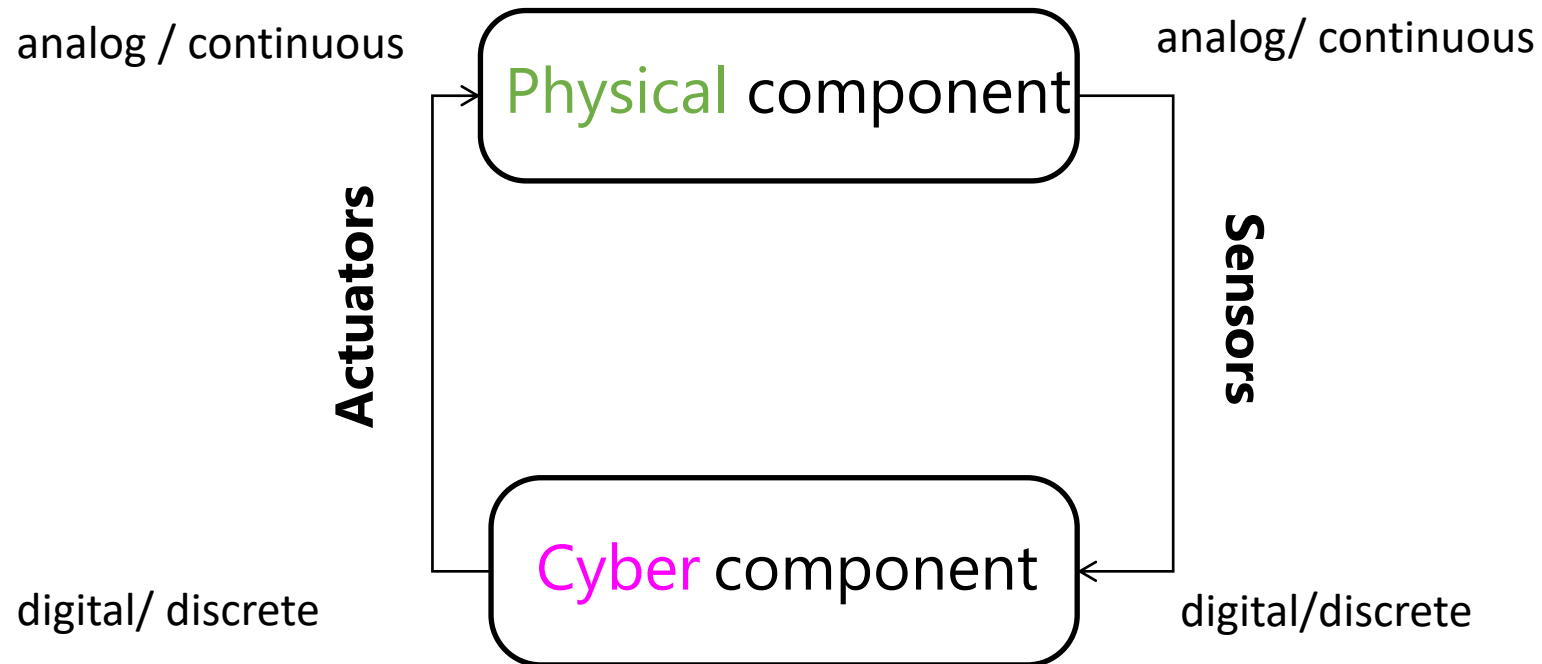
I Semestre 2024

Lecture 2: Modeling (Introduction) Concurrent Modeling

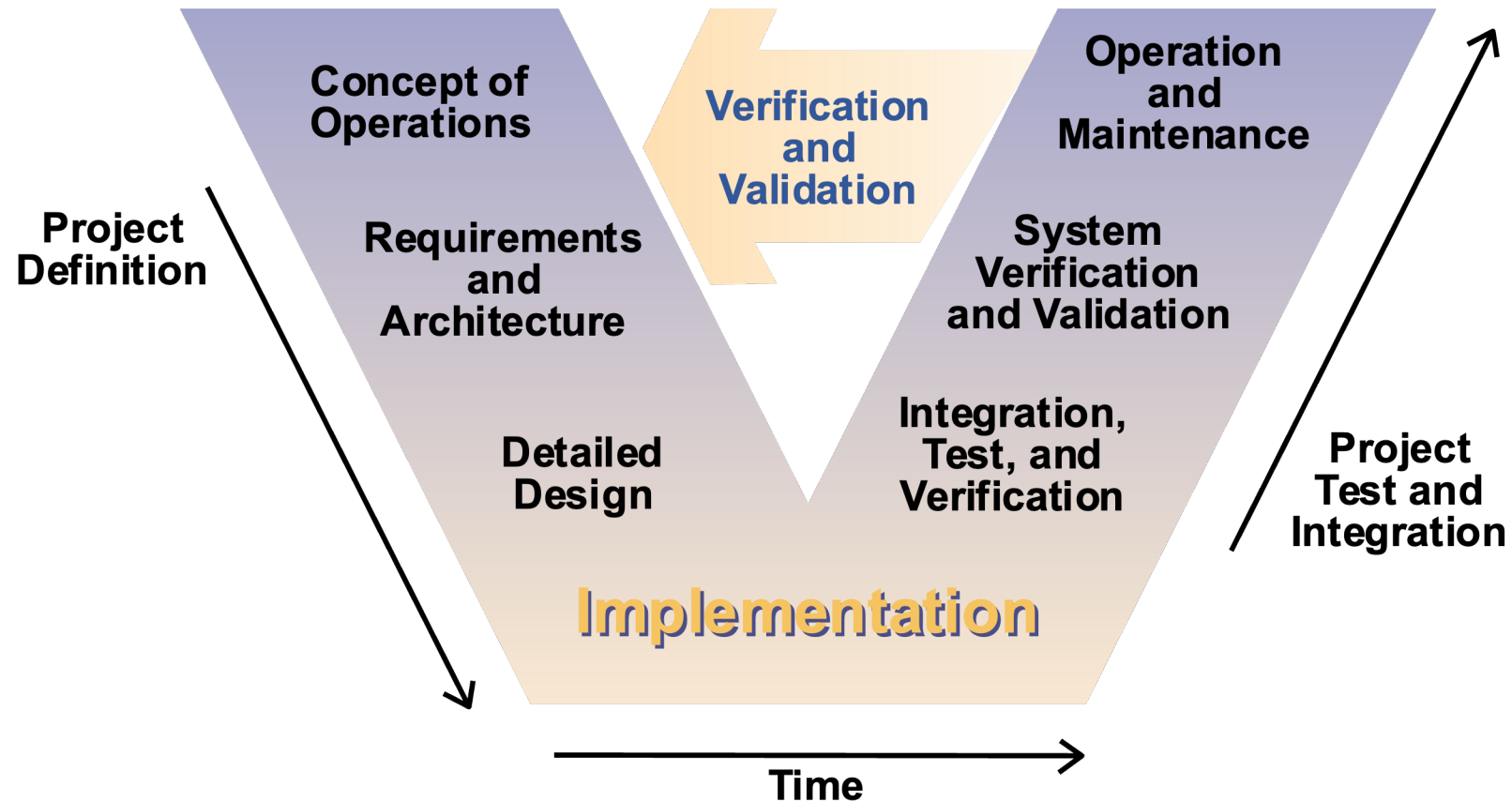
[Many Slides due to J. Deshmukh, Toyota]

Cyber-Physical System (CPS)

Combination of **physical** (environment / plant / process / system) with a **cyber** (computation / software / code) components **potentially networked** and **tightly interconnected**



Model-based Design Approach

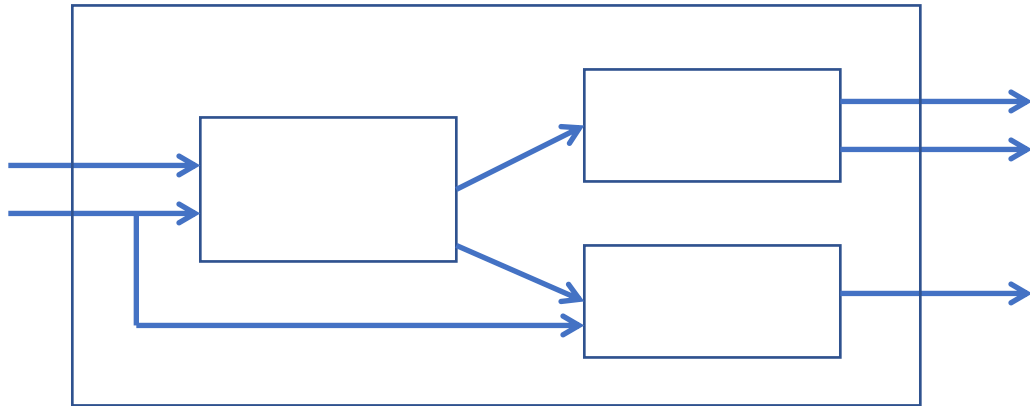


Validation : "Are you building the right thing?"

Verification : "Are you building it right?"

Model-based Design Approach

MBD languages are often visual and block-diagram based, e.g. Simulink



Functional Components

1. *Classical* model of computation: Functional or Transformational Programs
 - ▶ Start from a given input,
 - ▶ Produce a certain output and then **terminate**
 - ▶ Desired functionality can be described by a mathematical function
 - ▶ Emphasis is on data computation

Reactive Components

2. Reactive Programs:

- ▶ It maintains and internal state
- ▶ Continuously interact with the environment at a rate decided by the environment
- ▶ Emphasis is on system-environment interaction; e.g. airline autopilot, mail-servers, etc.

Models of Computation: Timing

- ▶ What's the notion of time in the model?
 - ▶ Real-time or Logical time-steps of execution?
- ▶ What time do different components in the model use?
 - ▶ Single global clock for full synchronization?
 - ▶ Different clocks in each component?
- ▶ What level of granularity do we need in time?
 - ▶ Discrete time-steps or Continuous dense time?

Reactive Component

*Most convenient model of computation for an (Autonomous) CPS is a **reactive and concurrent model of computation.***



*An autonomous CPS can be viewed as a **network of components** that communicate either **synchronously** or **asynchronously**.*

Models: abstractions of CPS

Examples of type of modeling for CPS components:

- Modeling physical phenomena (dynamical systems) – differential equation
- Feedback control systems – time-domain modeling
- Modeling modal behavior – FSMs, hybrid automata, ...
- Modeling sensors and actuators – models that help with calibration, noise elimination,
- Modeling hardware and software – capture concurrency, timing, ...
- Modeling networks – latencies, error rates, packet loss,

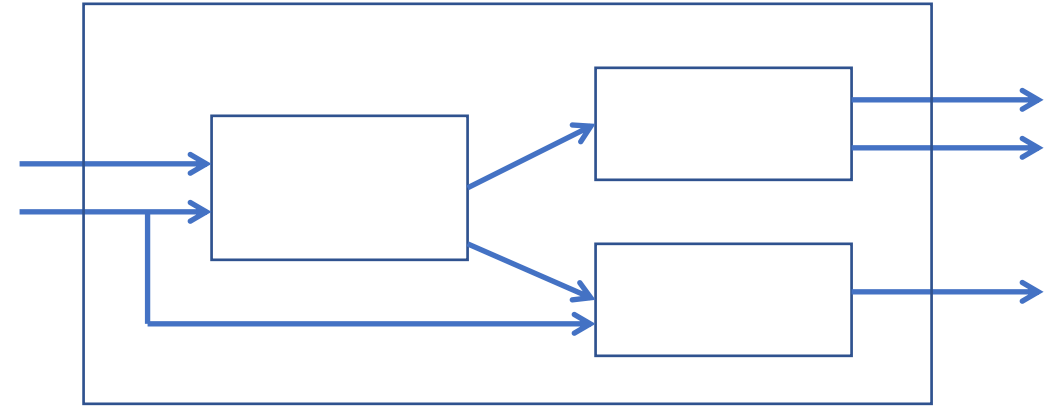
Models of Computation

- Synchronous Model of Computation
- Asynchronous Model of Computation
- Timed Models
 - Like Asynchronous models, but with explicit time information
 - Can make use of global time for coordination
- Continuous-time models/Dynamical system models
 - Like Synchronous, but time evolves continuously
- Hybrid Dynamical Models

Synchronous Models

Synchronous Models

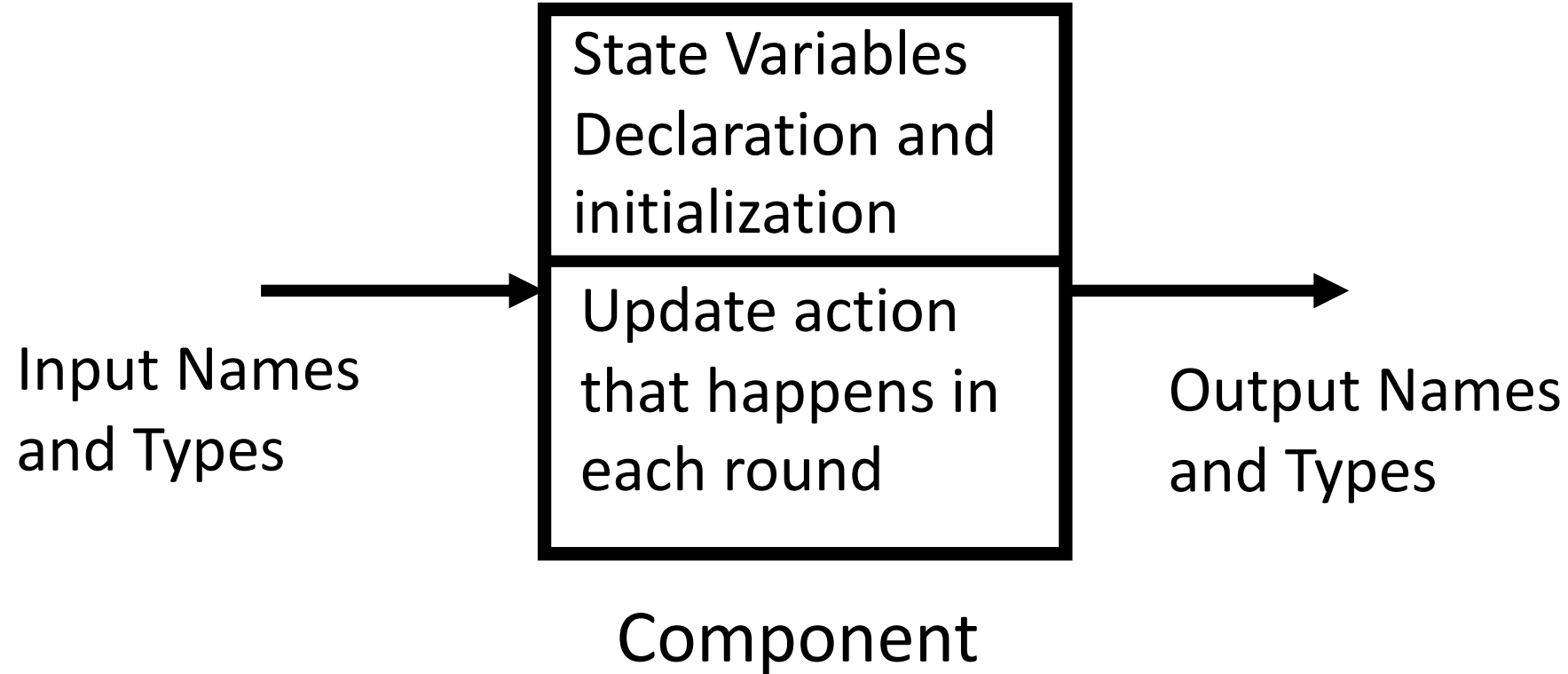
- ▶ All components execute in a sequence of rounds in lock-step
- ▶ Example:
 - ▶ Components in a digital hardware circuit with a central global clock
 - ▶ Fixed-step Simulation Models of Discrete Components in Simulink



Synchronous languages

- ▶ Benefit: system design is simpler if we use a simple round-based computation
- ▶ Challenge: How do we ensure synchronous execution when components may execute on different hardware?

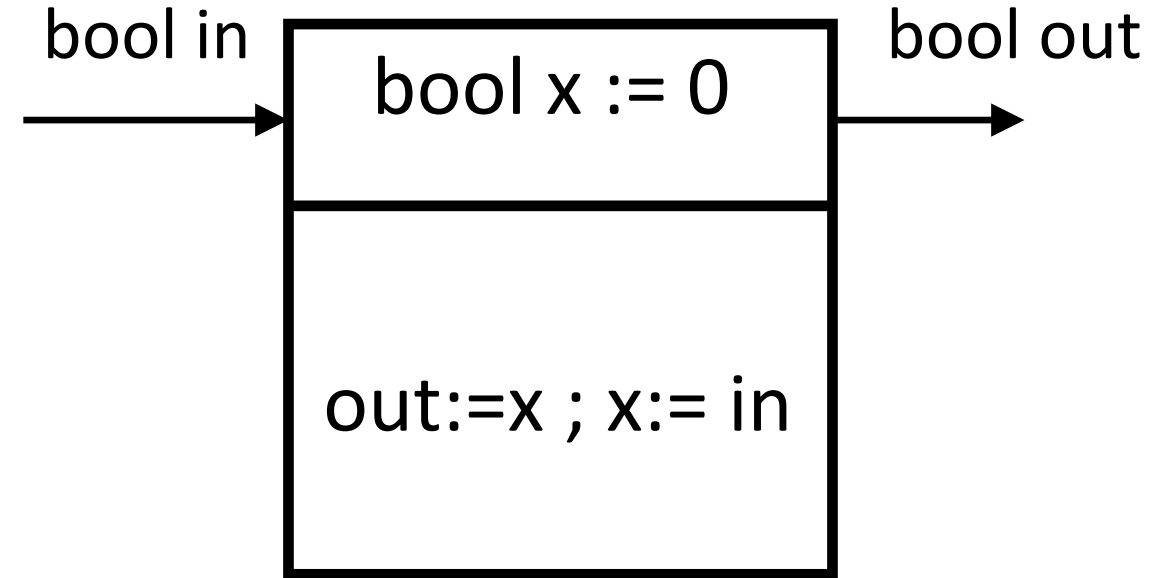
Simple Representation of a Synchronous Component



Simplest synchronous component: delay

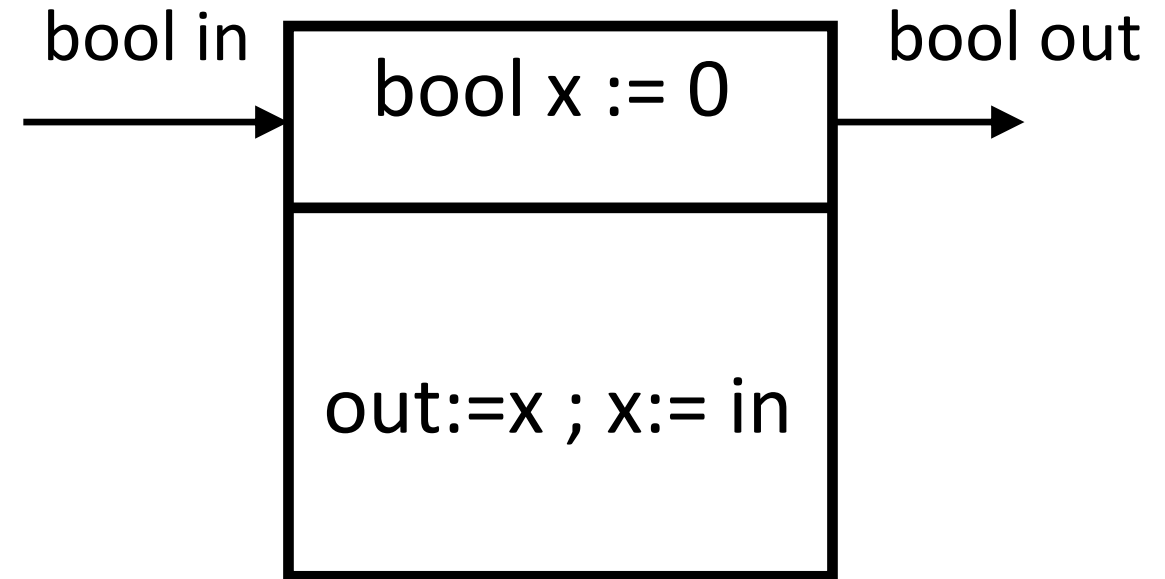
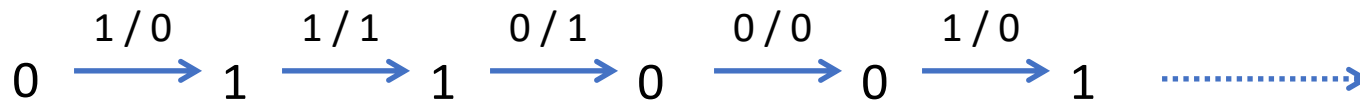
(Boolean = { 0, 1})

- ▶ Input variable: in of type Boolean
- ▶ Output variable: out of type Boolean
- ▶ State variable: x of type Boolean, initialized to 0
- ▶ In each round, component updates output from the state and state from input



Execution of “Delay”

- ▶ Initialize state to 0
- ▶ Repeatedly execute rounds
- ▶ In each round:
 - ▶ Choose value for input (provided from environment, e.g. by user)
 - ▶ Execute update code



Synchrony hypothesis

- ▶ Time needed to execute update is negligible compared to arrival times between consecutive inputs
- ▶ Synchronous execution is a *logical abstraction*
 - ▶ *Execution time of update code is 0*
 - ▶ *Production of outputs, updates to state and arrival of inputs happen instantaneously*
- ▶ With multiple components, assume all execute synchronously and simultaneously

Let's Formalize an SRC (Synchronous Reactive Component)

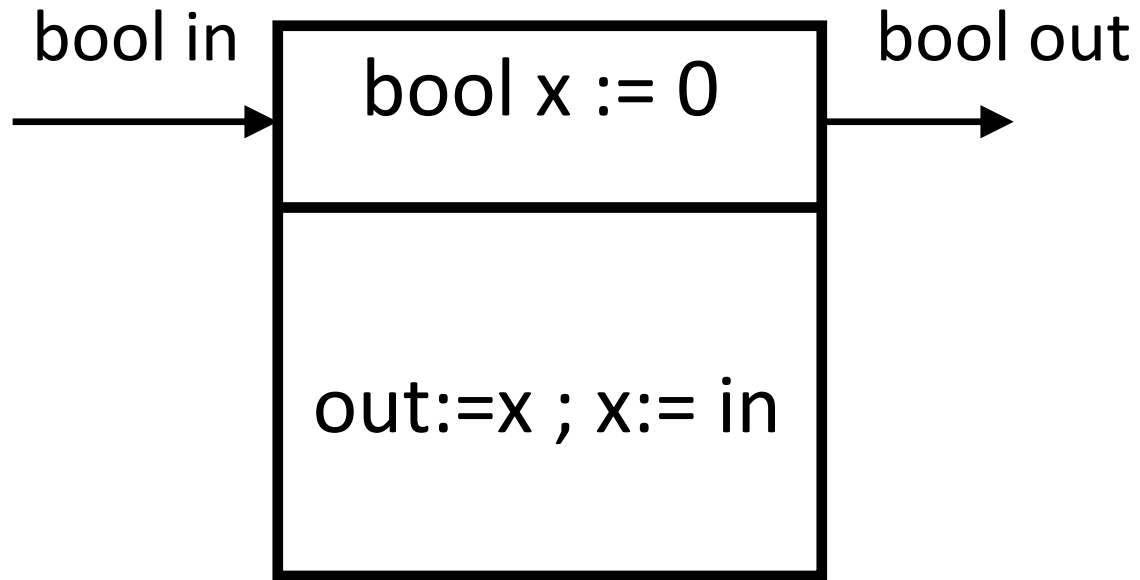
- ▶ SRC is defined as a tuple: $(Q_I, Q_x, Q_o, \llbracket init \rrbracket, \llbracket react \rrbracket)$, where:

Symbol	Designation	Examples
Q_I	Set of Inputs	$\{\text{bool } in\}$
Q_x	Set of State Variables	$\{\text{bool } x\}$
Q_o	Set of Outputs	$\{\text{bool } out\}$
$\llbracket init \rrbracket$	Set of initial States	$x := 0$
$\llbracket react \rrbracket$	Set of Updates	$out := x$ $x := in$

Semantics of updates & initialization

- ▶ Let the set of input, output, and state values be Q_I, Q_O, Q_X
- ▶ Semantics of the initialization function $\llbracket init \rrbracket$:
 - ▶ At time/round 0, maps the state variables to some specified value (or values) in Q_X
- ▶ Semantics of the update function $\llbracket react \rrbracket$ (some sequence of conditionals and assignments):
 - ▶ A set R of transitions where each transition is of the form: $q \xrightarrow{i/o} q'$, where q is the old value of the state variables, q' is the new value of the state variables, i is the value of the input in that round, and o is the value of the output
 - ▶ R is a subset of $Q_X \times Q_I \times Q_O \times Q_X$

Transitions for Delay



$$0 \xrightarrow{0/0} 0$$

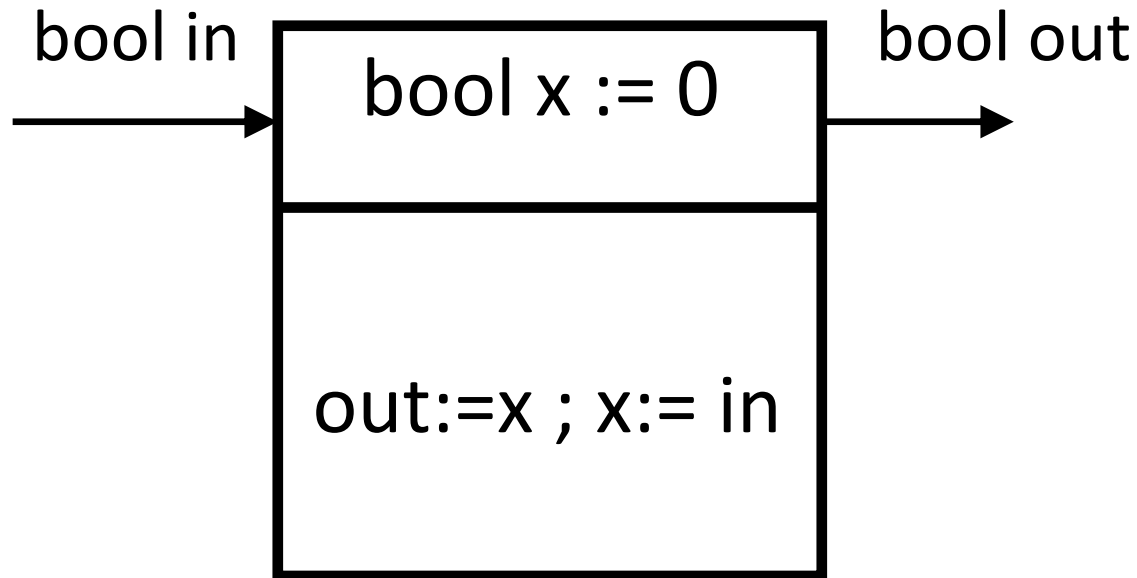
$$0 \xrightarrow{1/0} 1$$

$$1 \xrightarrow{0/1} 0$$

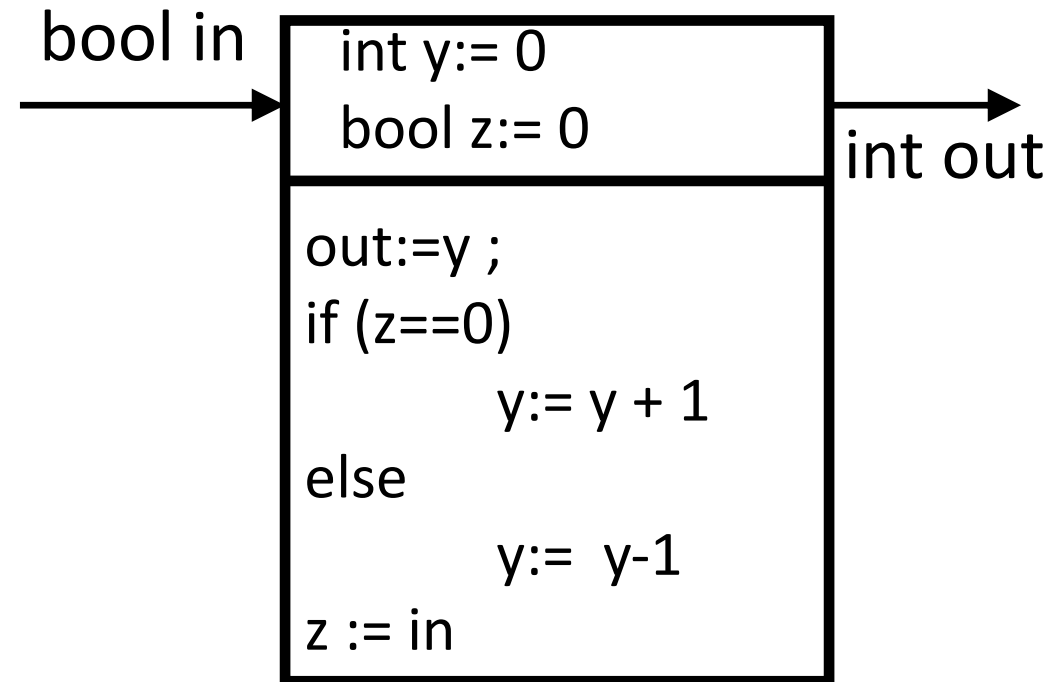
$$1 \xrightarrow{1/1} 1$$

$$q \xrightarrow{i/o} q'$$

What are the Q_I, Q_O, Q_X for these SRCs?

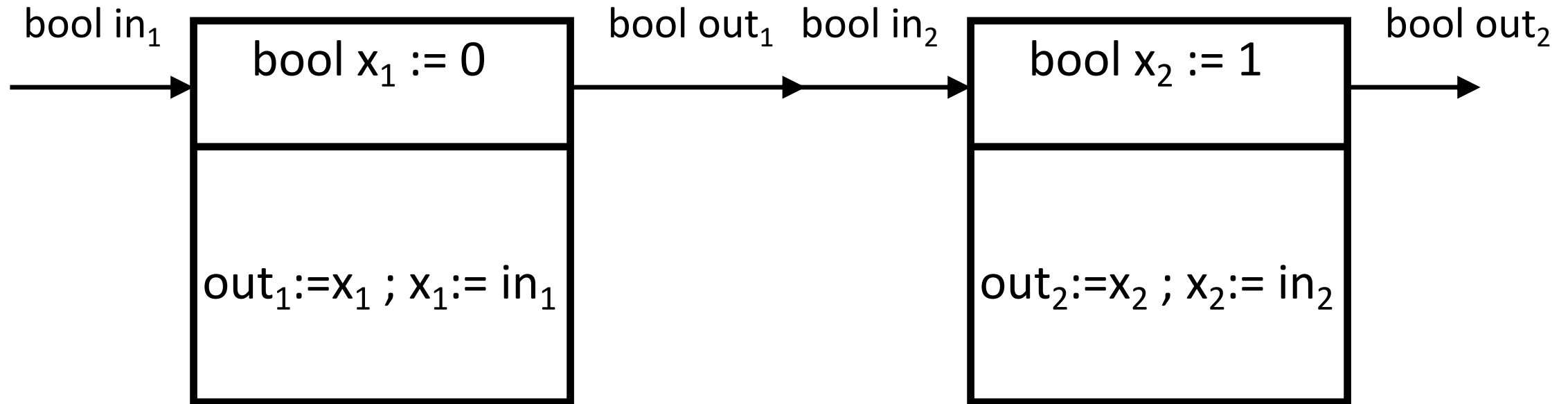


$Q_I = \{0,1\}, Q_X = \{0,1\}, Q_O = \{0,1\}$



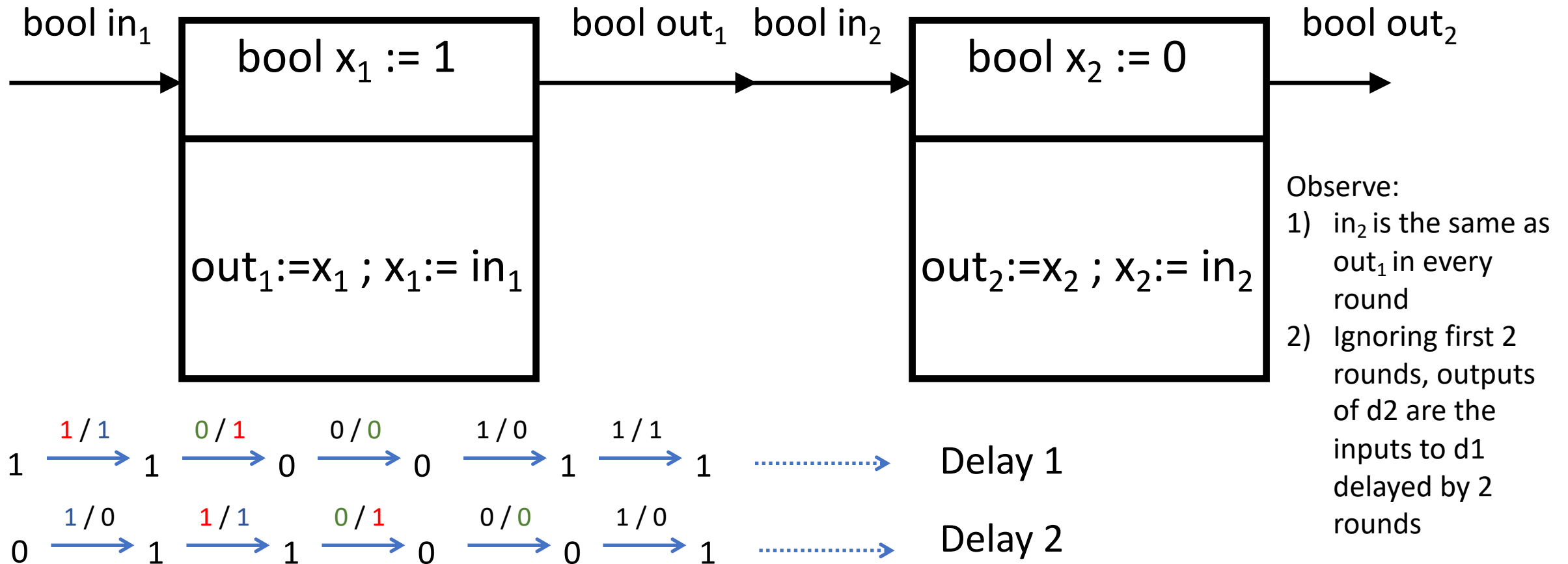
$Q_I = \{0,1\}, Q_X = \text{int} \times \{0,1\}, Q_O = \text{int}$

Composition of Synchronous Components

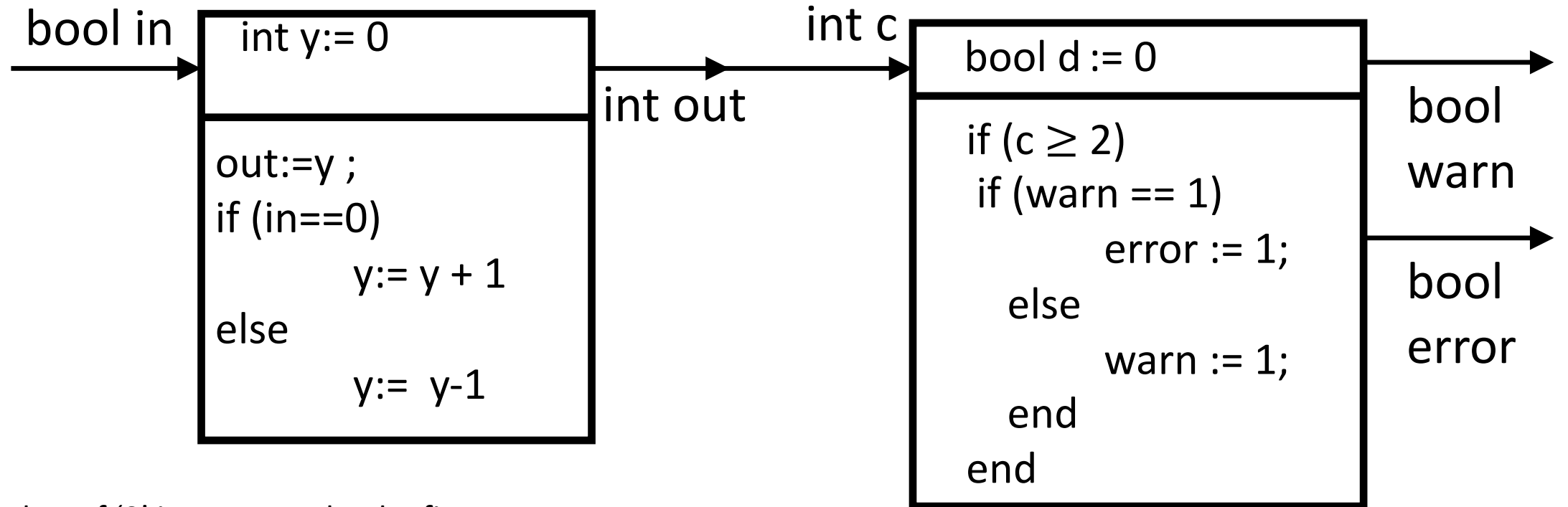


Delay sequentially composed with Delay

Composition of Synchronous Components



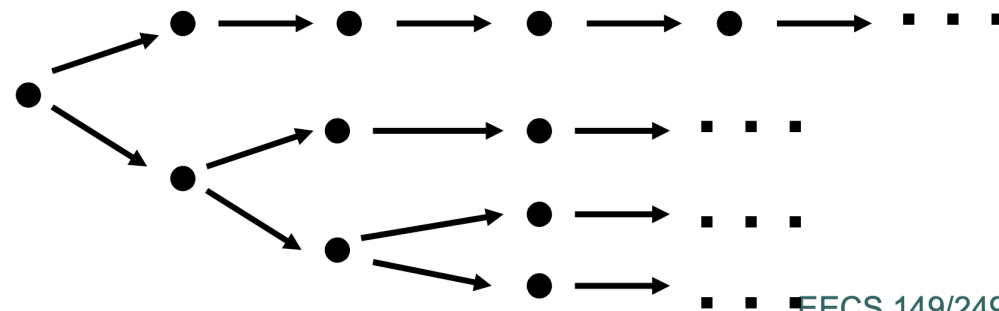
What does this model achieve?



If number of '0' inputs seen by the first component exceeds the number of '1' inputs it has seen by 2, at any point in its execution, then the 'warn' light becomes high
If this happens again, the 'error' light becomes high

Deterministic Component

- ▶ An SRC is deterministic if:
 - ▶ It has a single initial state
 - ▶ Updates ensure that for every state q and input i , there is a unique state q' and output o such that (q, i, o, q') is a transition
- ▶ Determinism means for same input sequence, you get same state/output sequence every single time
- ▶ Note:
 - ▶ Nondeterminism is useful for modeling uncertainty/unknown and compactness



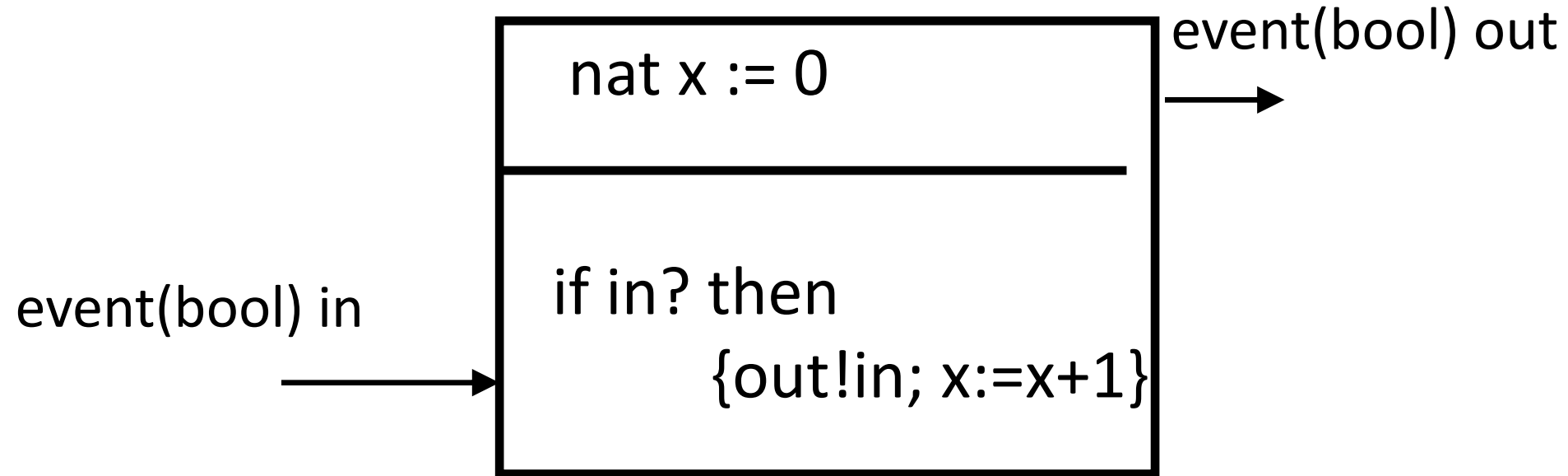
- ▶ It is not the same as probabilistic/random choice!

Event-triggered Components

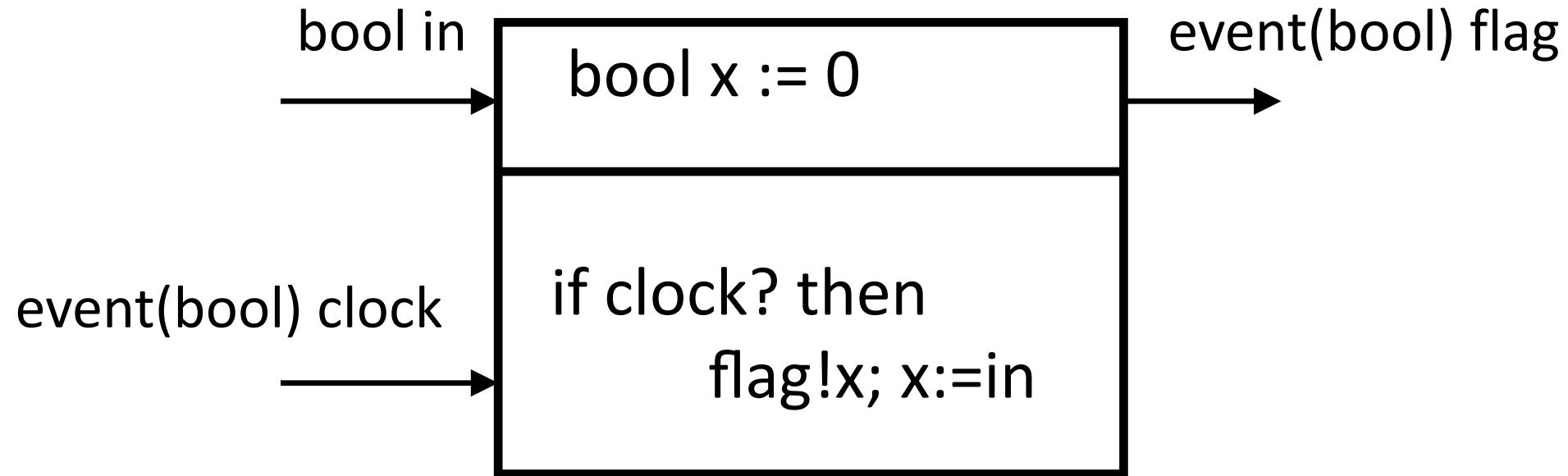
- ▶ What to do if we want some components to *not* participate in some rounds?
- ▶ Event is a special input/output variable, which can be *absent* or *present*
- ▶ Event variable has value only if it is *present*
- ▶ Syntax:

e?	True if e is present
e!a	e gets the value of the assignment a

Event-triggered Copy

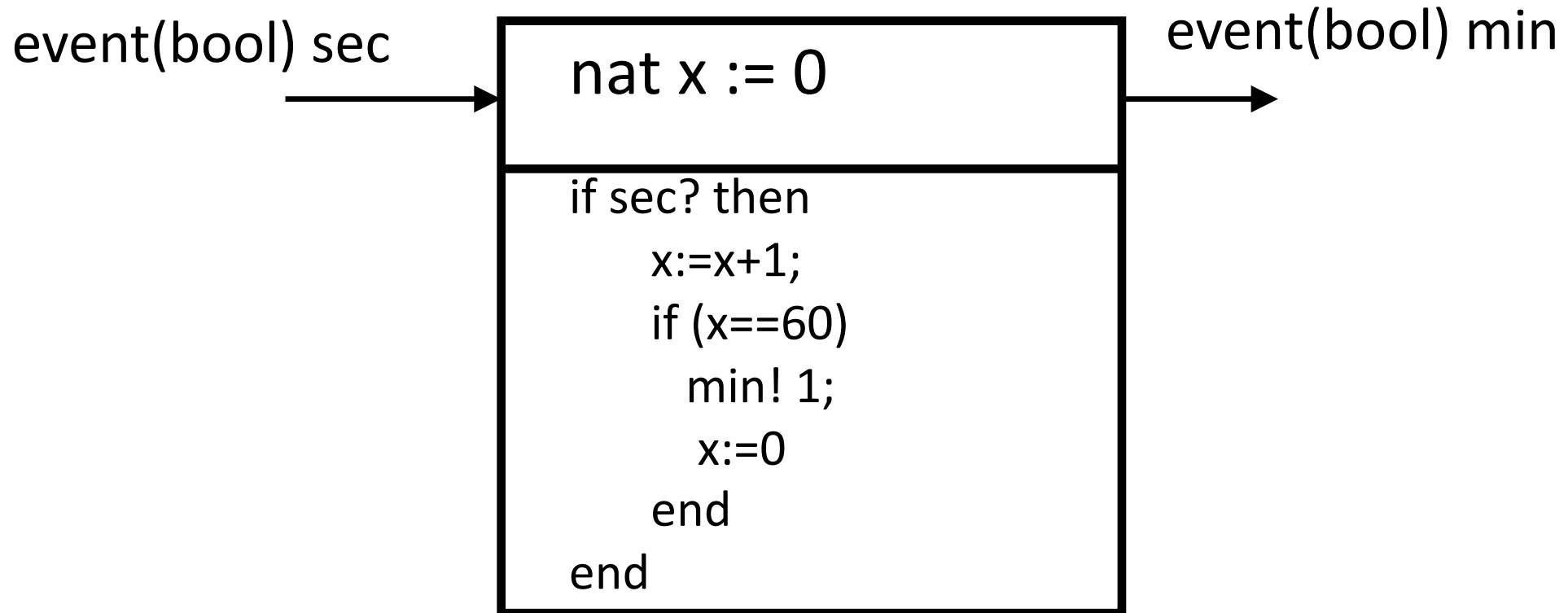


Event-triggered ClockedCopy



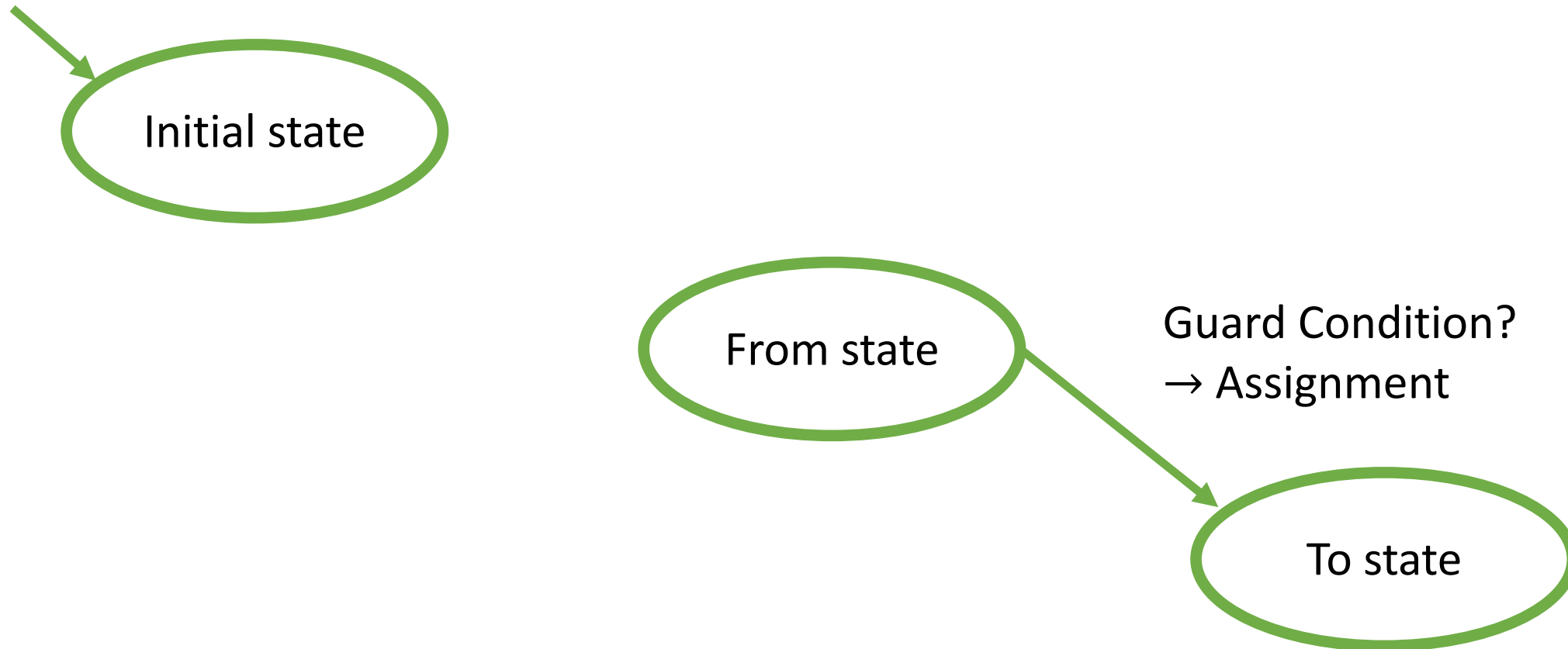
Event-triggered Components

- ▶ No need to execute in a round where triggering events are absent



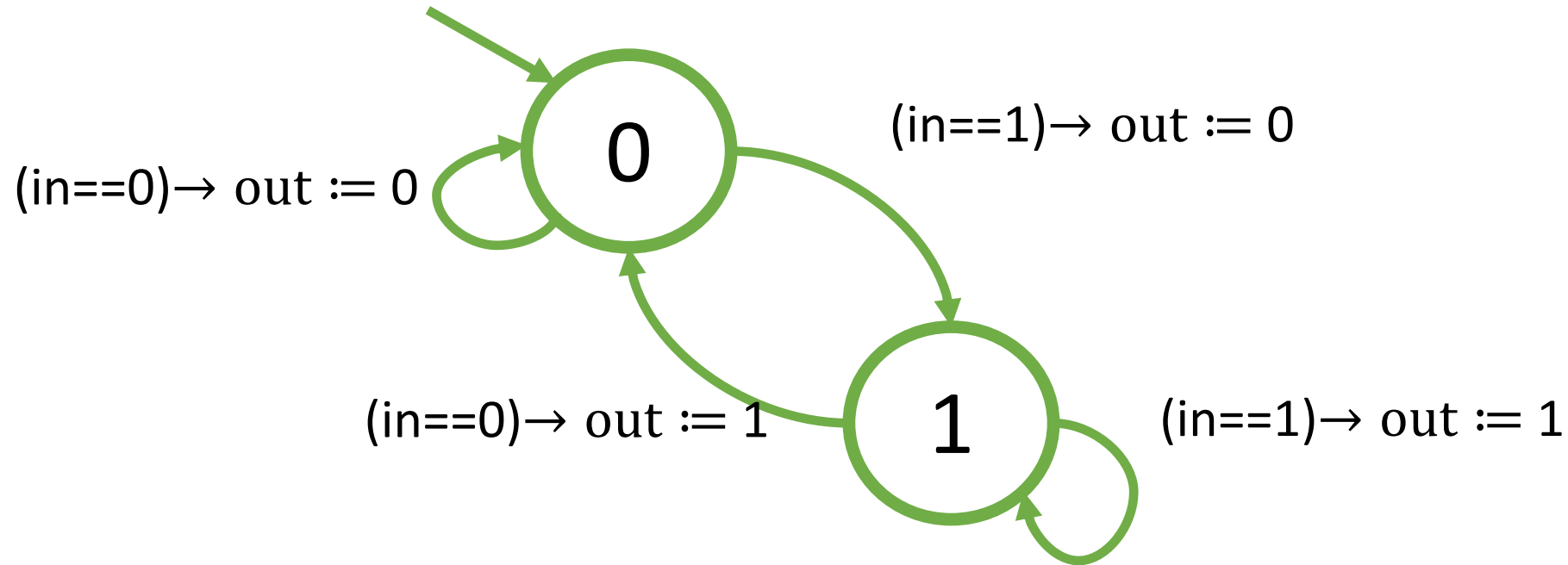
Extended State Machines

- ▶ Commonly used to describe behavior of MBD models

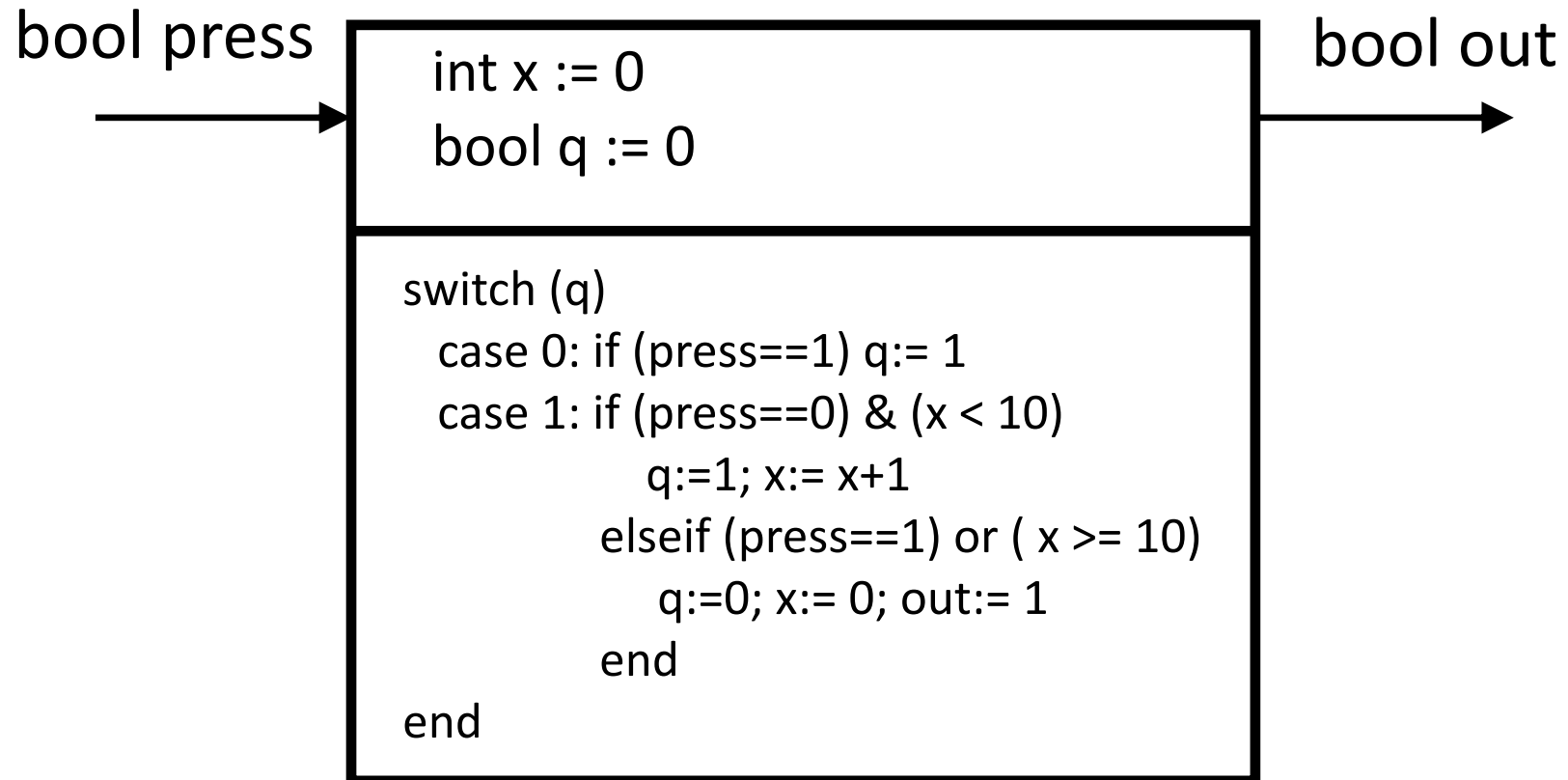


Extended State Machines

- ▶ Does this ESM remind you of something?

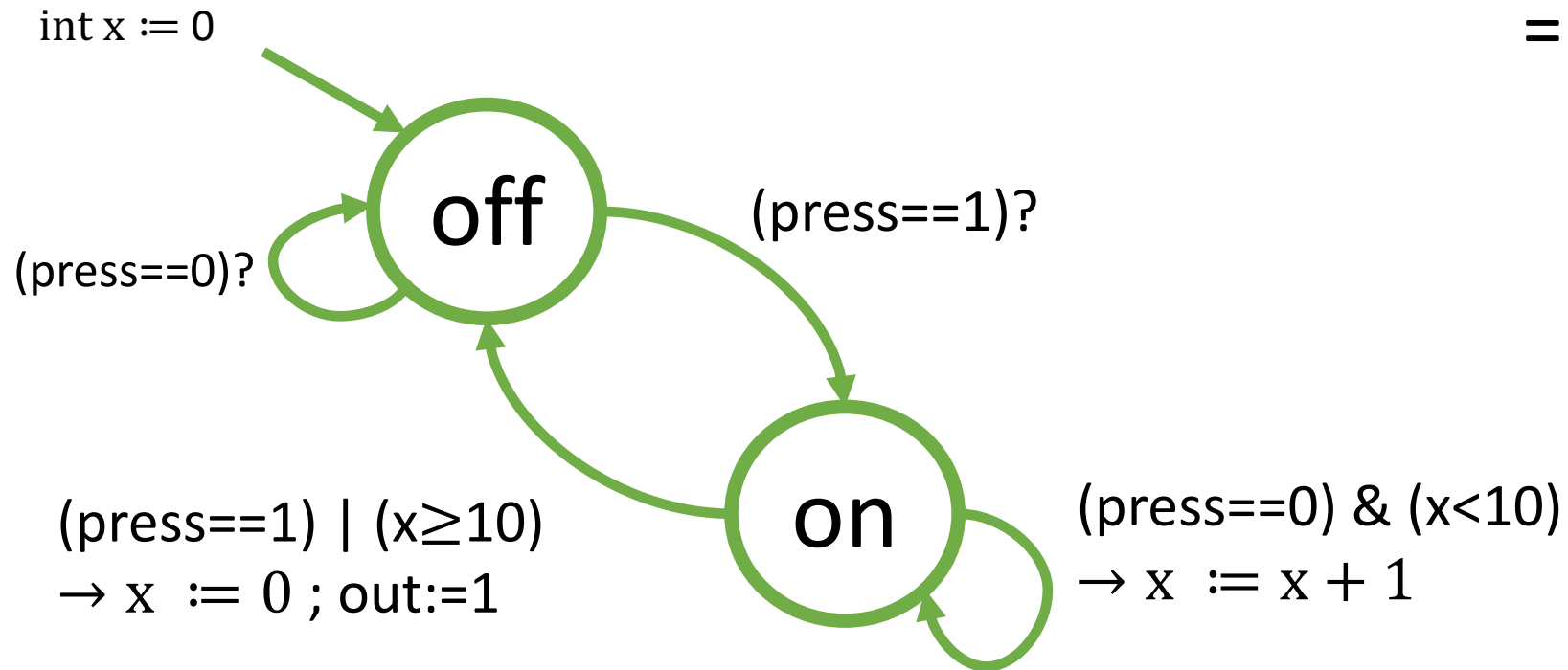


Component Switch: What does this do?

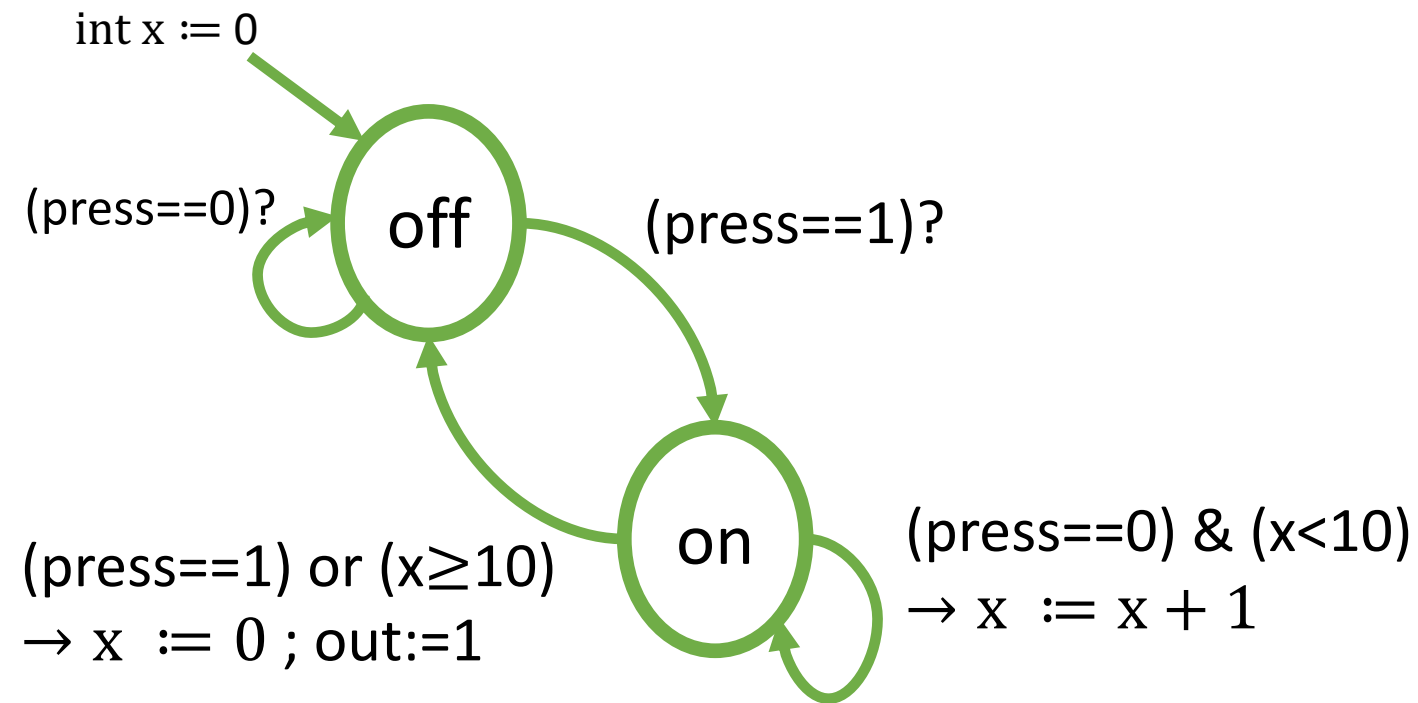


ESM corresponding to Switch SRC

q = 0 : off
= 1 : on

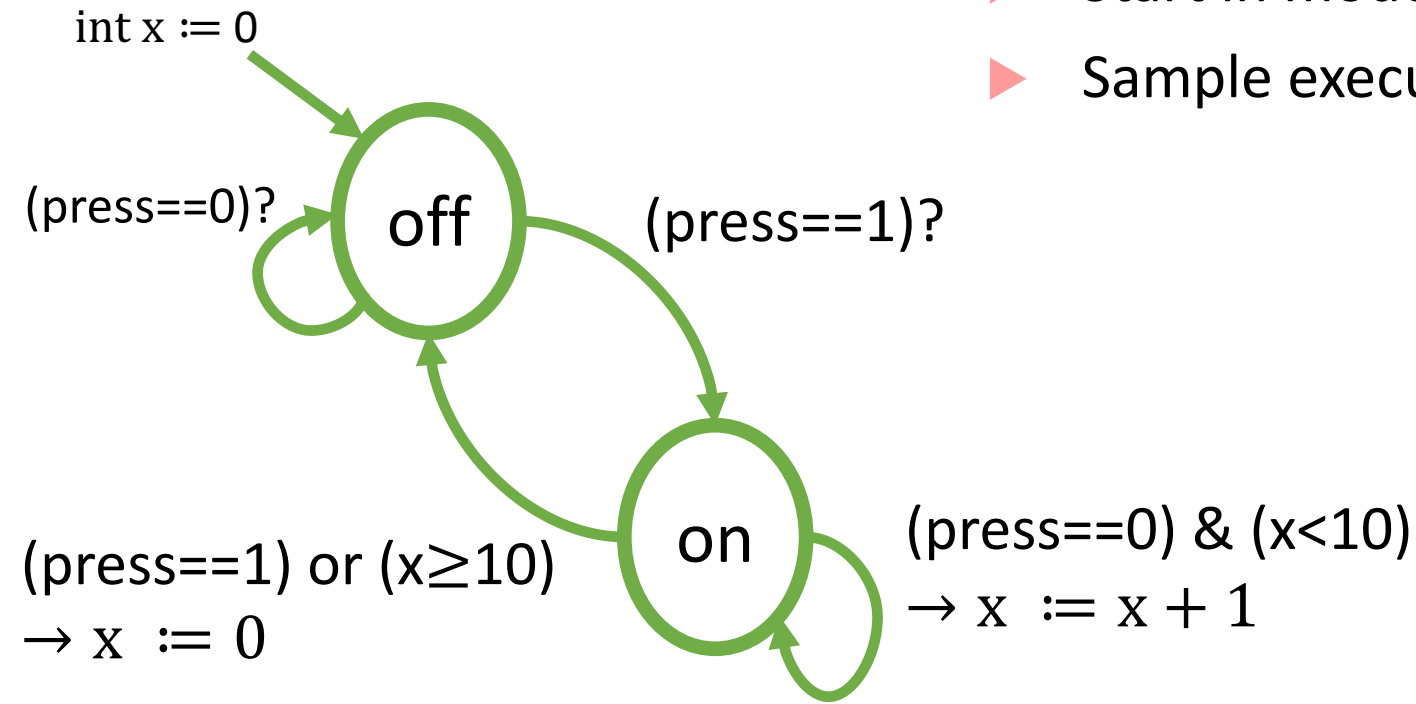


ESM notation



- ▶ Implicit variable called “mode” that is a *discrete* state variable over some finite enumeration. Here: {on, off}
- ▶ SRC transition may correspond to mode-switch
- ▶ Each mode-switch has guard/update. Example:
 - ▶ Guard: $(\text{press}==0) \ \& \ (x < 10)$ and
 - ▶ Update: $x := x + 1$

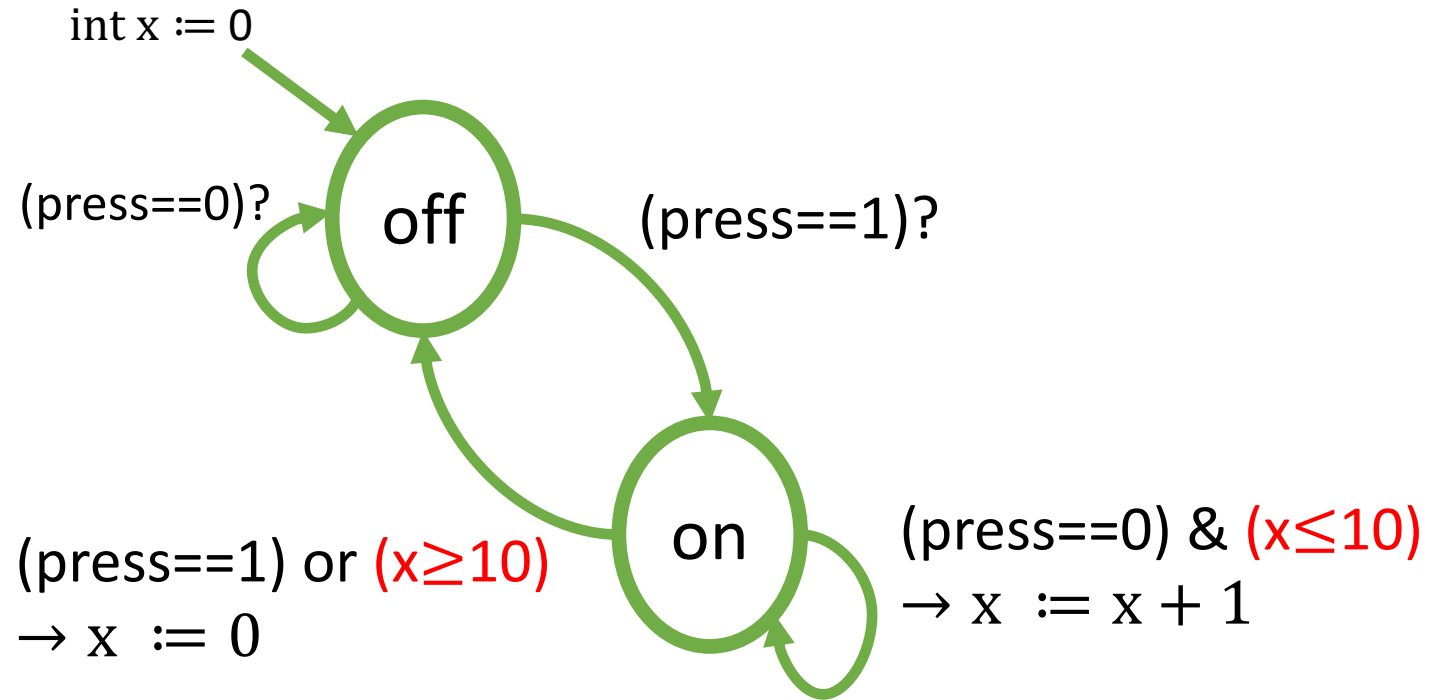
ESM execution



- ▶ Start in mode off; initial state = (off,0)
- ▶ Sample executions:

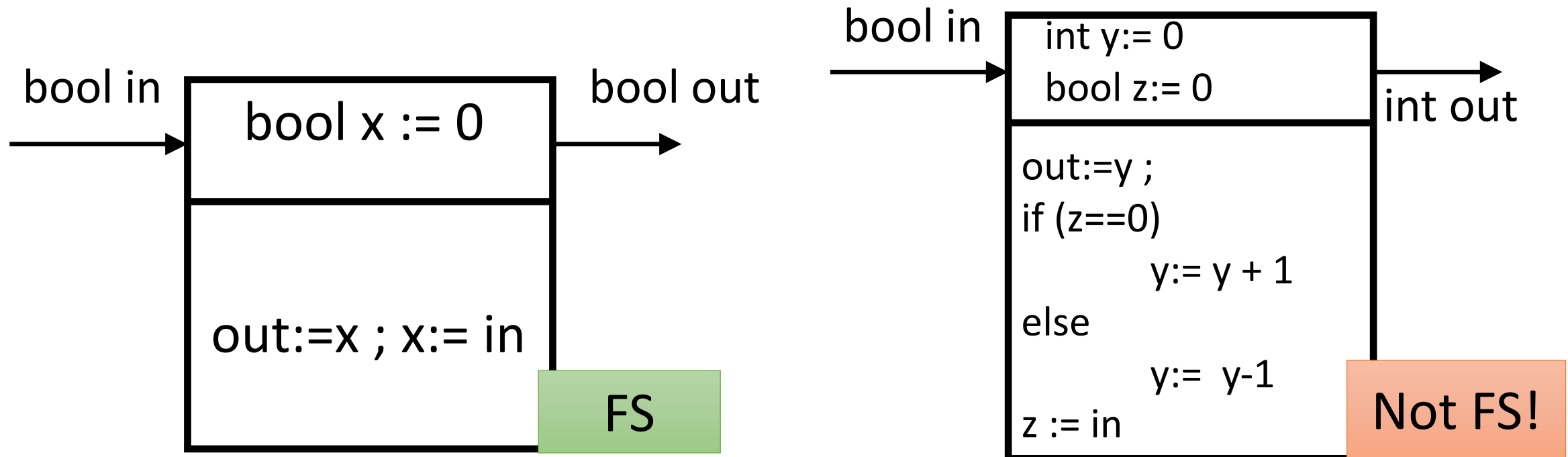
<i>(off, 0)</i>	<i>(off, 0)</i>
↓ 0	↓ 0
<i>(off, 0)</i>	<i>(off, 0)</i>
↓ 1	↓ 1
<i>(on, 0)</i>	<i>(on, 0)</i>
↓ 0	↓ 0
<i>(on, 1)</i>	<i>(on, 1)</i>
⋮	⋮
↓ 0	↓ 0
<i>(on, 10)</i>	<i>(on, 5)</i>
↓ 0	↓ 1
<i>(off, 0)</i>	<i>(off, 0)</i>

ESM transitions could be nondeterministic!



Finite-state Components

- ▶ Component is finite state if all variables are over finite types



Finite State Machine

A FSM is a tuple $\{S, Q_I, Q_O, update, s_0\}$ where:

- S is a finite set of states;
- Q_I is a set of input valuations;
- Q_O is a set of output valuations;
- $update: S \times Q_I \rightarrow S \times Q_O$ is an update function, mapping a state and an input valuation to a next state and an output valuation;
- s_0 is the initial state.

Extended Finite State Machine

A EFSM is a tuple $\{S, Q_I, Q_O, V, update, s_0\}$ where:

- S is a finite set of states;
- Q_I is a set of input valuations;
- Q_O is a set of output valuations;
- V is a set of variables;
- $update: S \times Q_I \times V \rightarrow S \times V \times Q_O$ is an update function, mapping a state and an input valuation to a next state and an output valuation;
- s_0 is the initial state.

Non-deterministic Finite State Machine

A non-deterministic FSM is a tuple $\{S, Q_I, Q_O, possibleUpdate, s_0\}$ where:

- S is a finite set of states;
- Q_I is a set of input valuations;
- Q_O is a set of output valuations;
- $possibleUpdate: S \times Q_I \rightarrow 2^{\{S \times Q_O\}}$ is an update relation, mapping a state and an input valuation to a set of possible (next state, output valuation) pairs;
- s_0 is the initial state.

Mealy machines and Moore machine

The state machines we describe here are known as **Mealy machines**, named after George H. Mealy, a Bell Labs engineer who published a description of these machines in 1955 (Mealy, 1955). Mealy machines are characterized by producing outputs when a transition is taken.

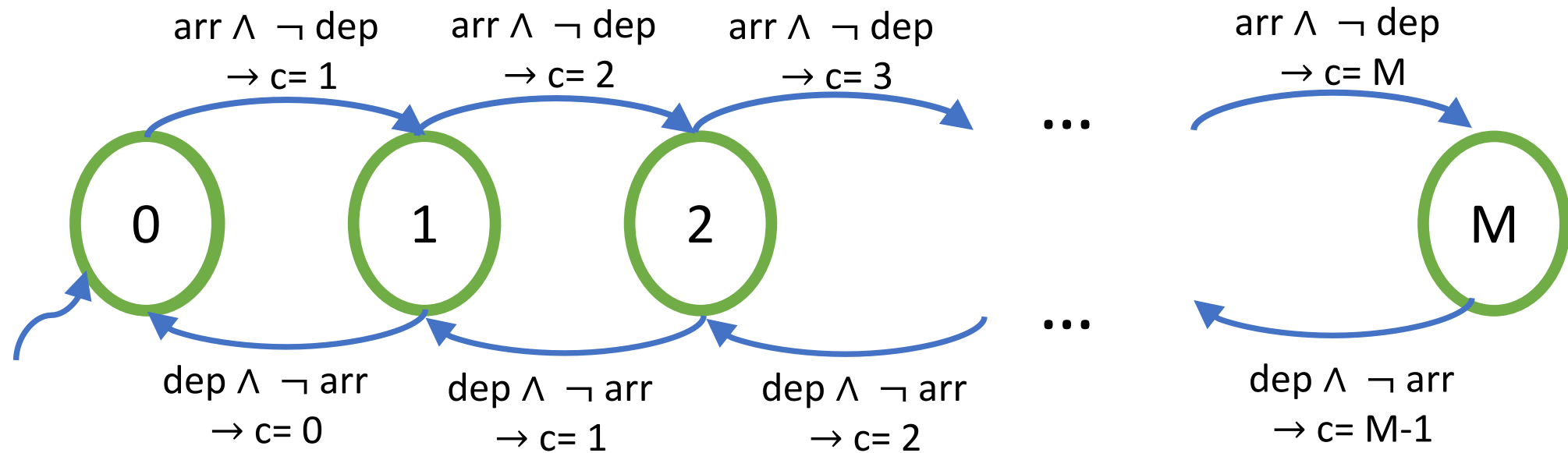
An alternative, known as a **Moore machine**, produces outputs when the machine is in a state, rather than when a transition is taken. That is, the output is defined by the current state rather than by the current transition. Moore machines are named after Edward F. Moore, another Bell Labs engineer who described them in a 1956 paper (Moore, 1956).

Ex: Parking Finite State Machine

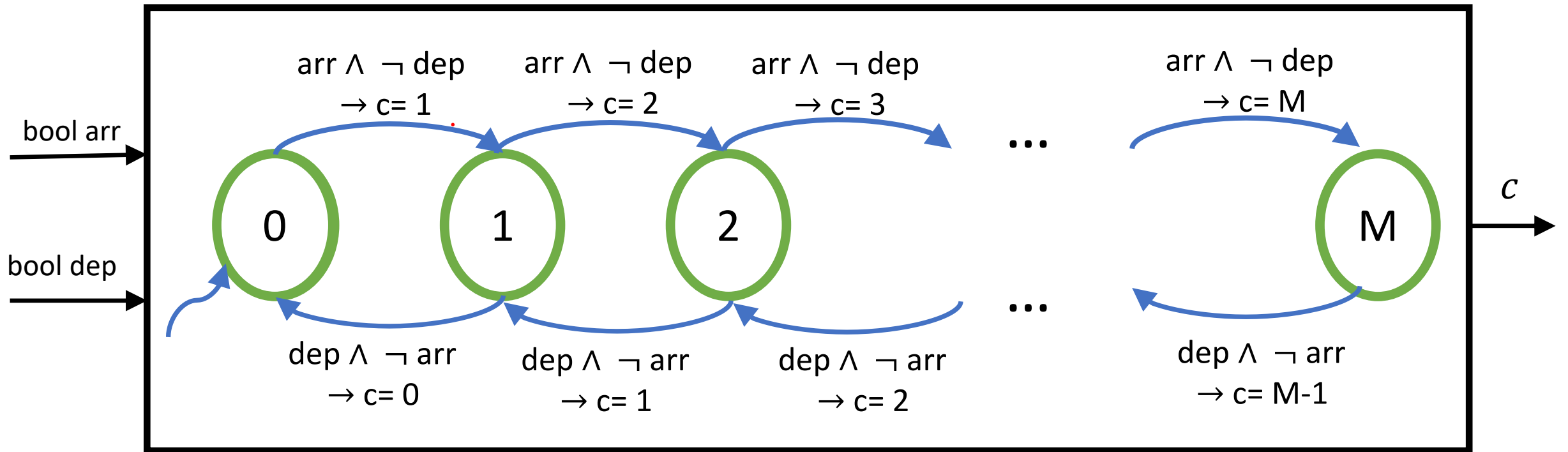
Try to define the FSM of a car park, where a car can arrive or depart, and you have a maximum number of slots equal to M .

Hint: the modes are the number of occupied slots

Parking Finite State Machine

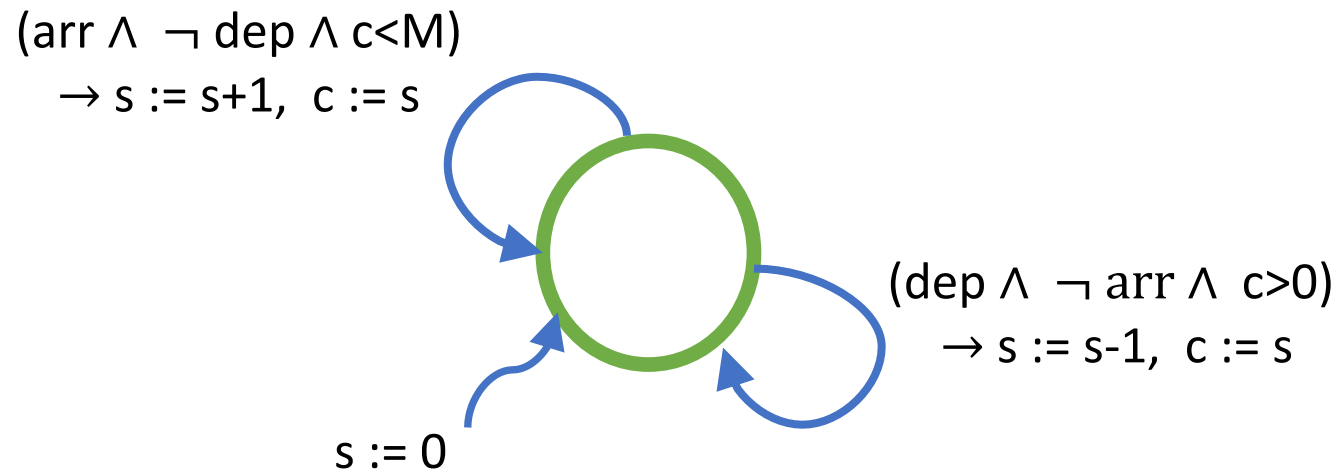


Parking Finite State Machine

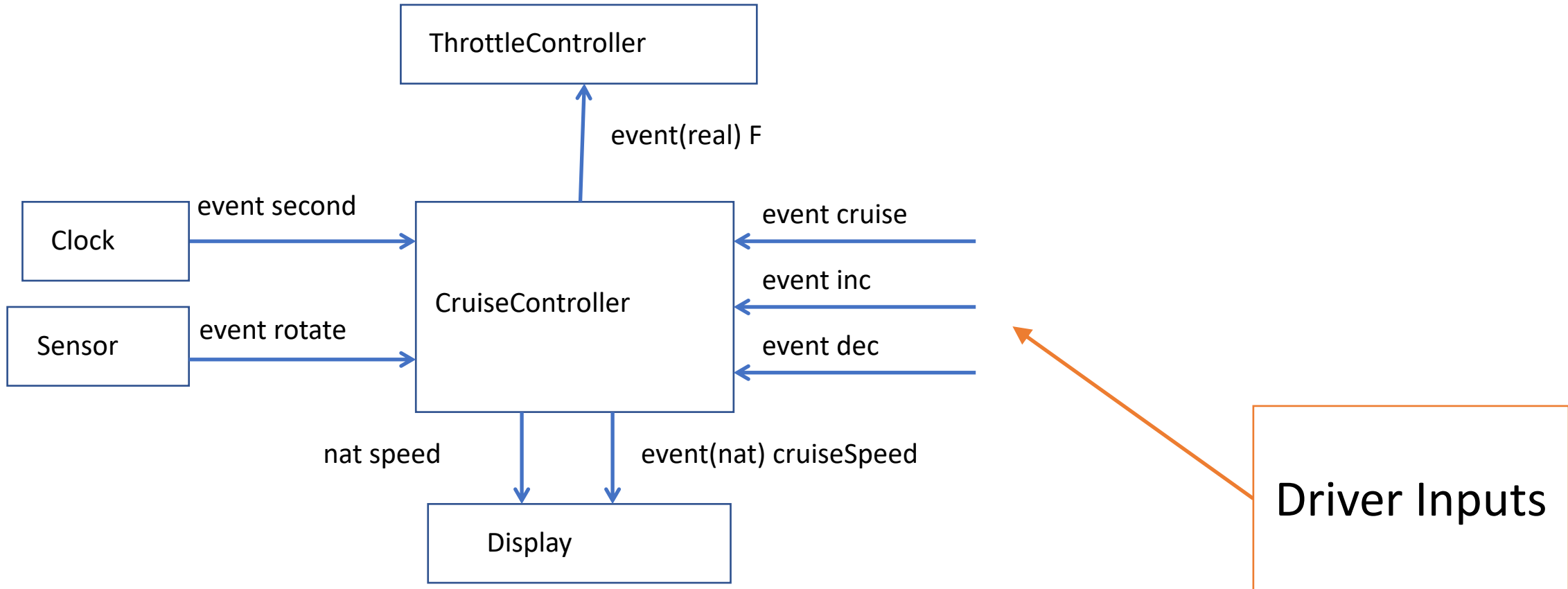


Parking Extended State Machine

Consider a system that counts the number of cars that enter and leave a parking garage in order to keep track of how many cars are in the garage at any time.

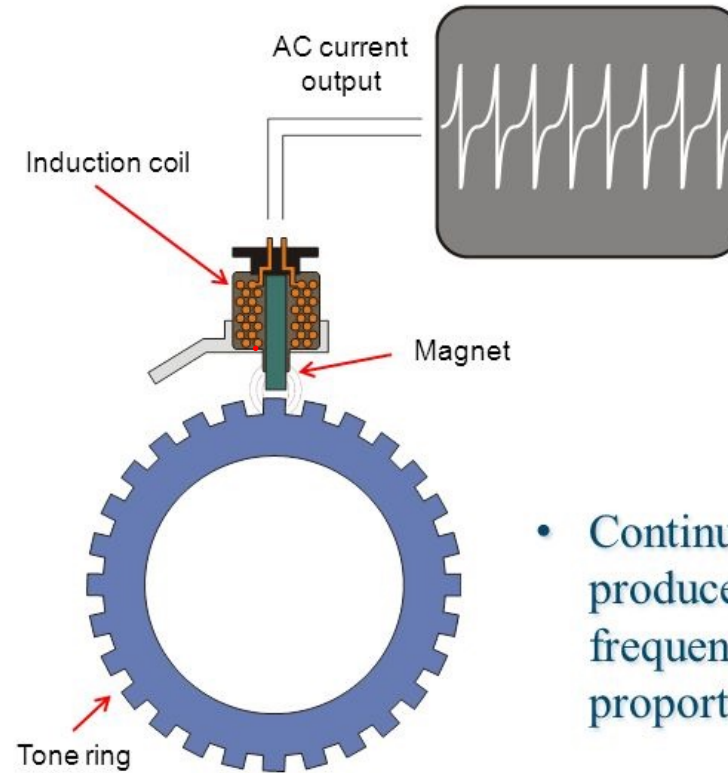


Cruise Controller Example



Sensors

- ▶ Rotation Sensor: Wheel speed sensor or vehicle speed sensor
- ▶ Type of a tachometer
- ▶ Counts number of rotations per second and as the wheel radius is known, can compute the linear speed of the car

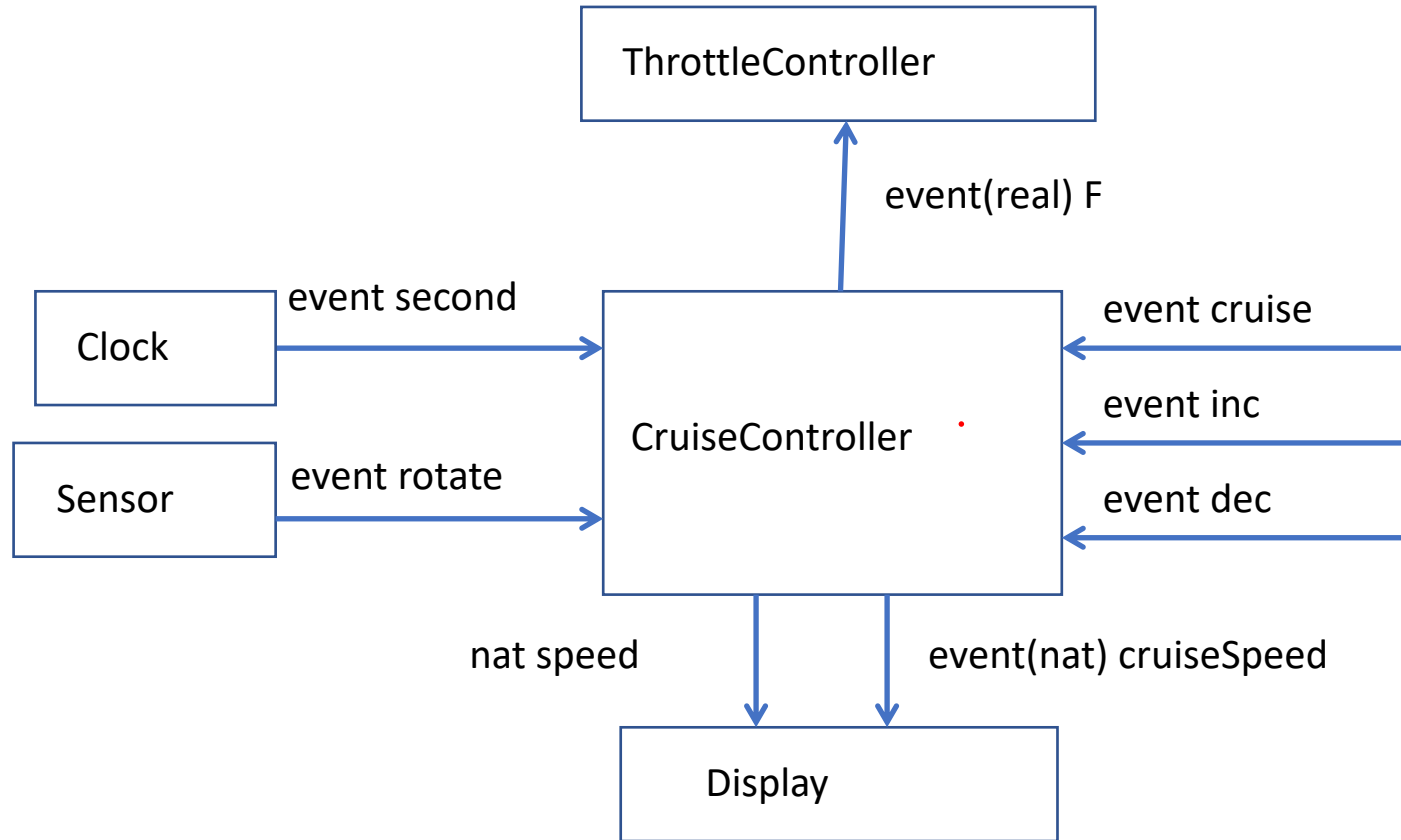


- The ABS wheel speed sensor generates a small electrical pulse whenever a tooth on the tone ring moves through the magnetic field of the pick up coil

- Continuous rotation of the tone ring produces an AC current whose frequency – measured in Hertz – is proportional to wheel speed

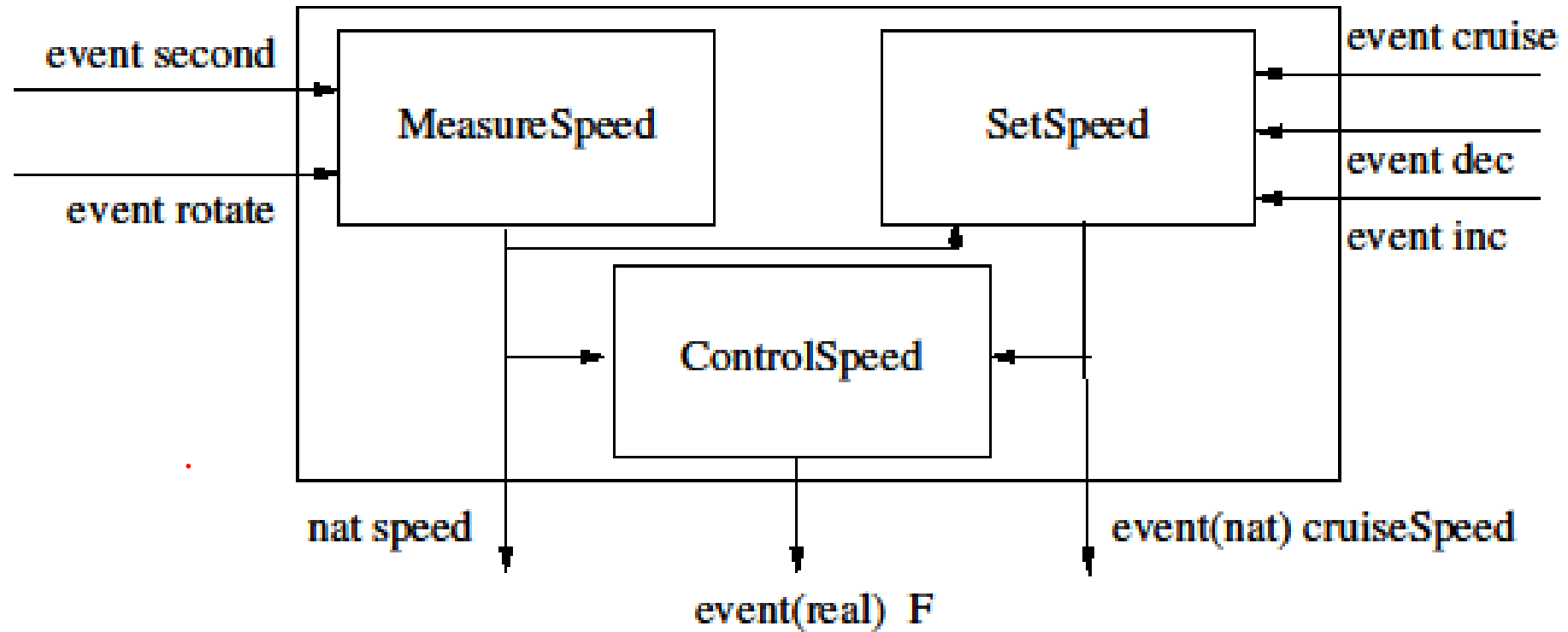
(From Porter and Chester Institute slides on Google Image Search)

Actuator

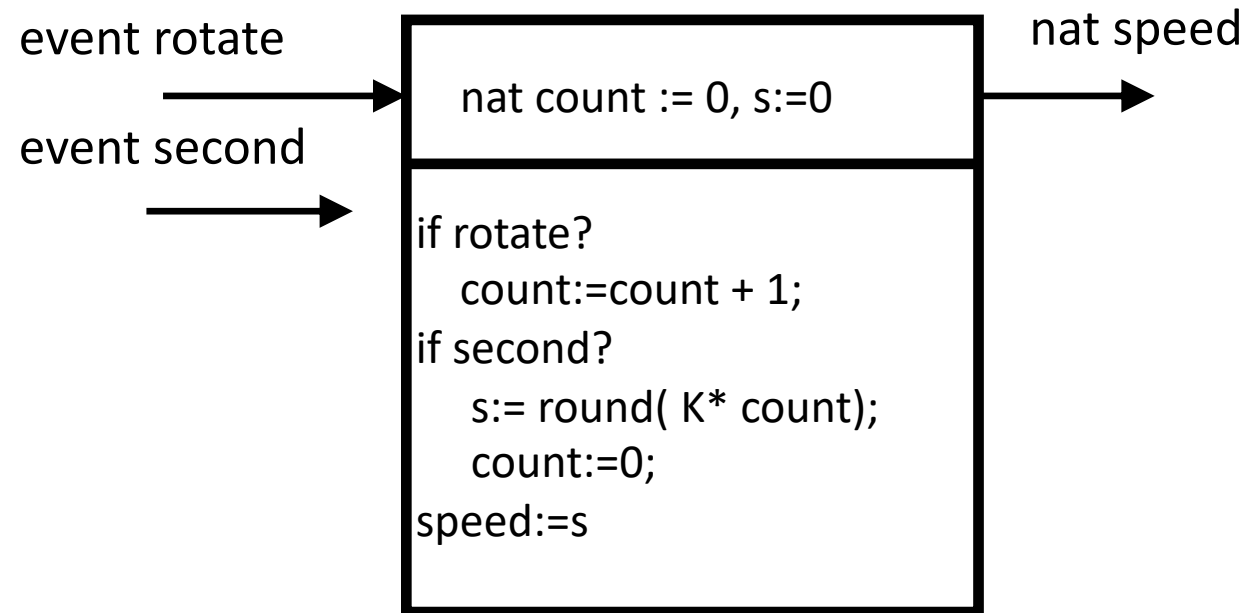


- ▶ ThrottleController is an actuator that gets a force/torque required to adjust the throttle plate which leads to tracking the desired speed

Decomposing CruiseController further



MeasureSpeed SRC

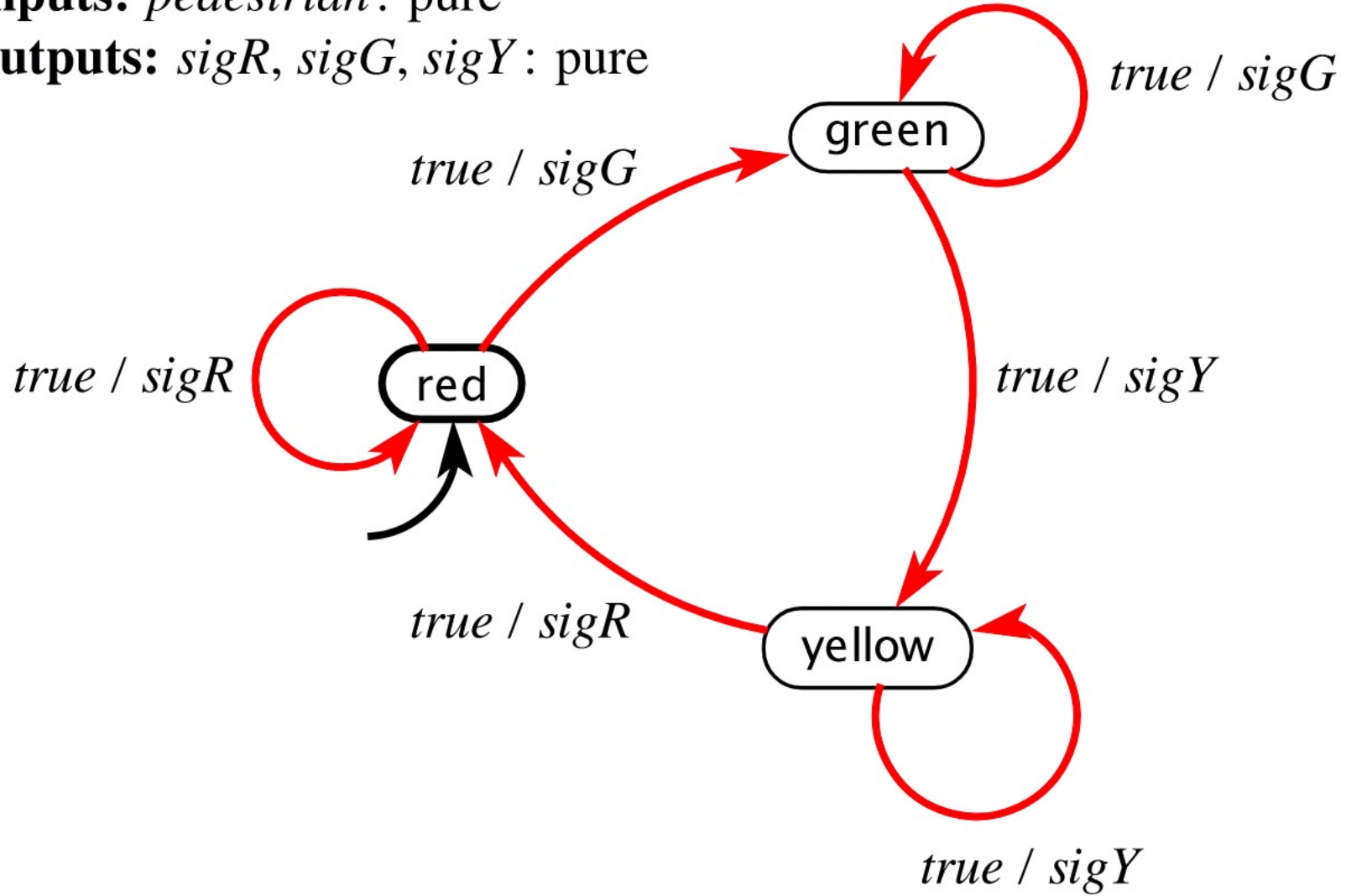


MeasureSpeed SRC

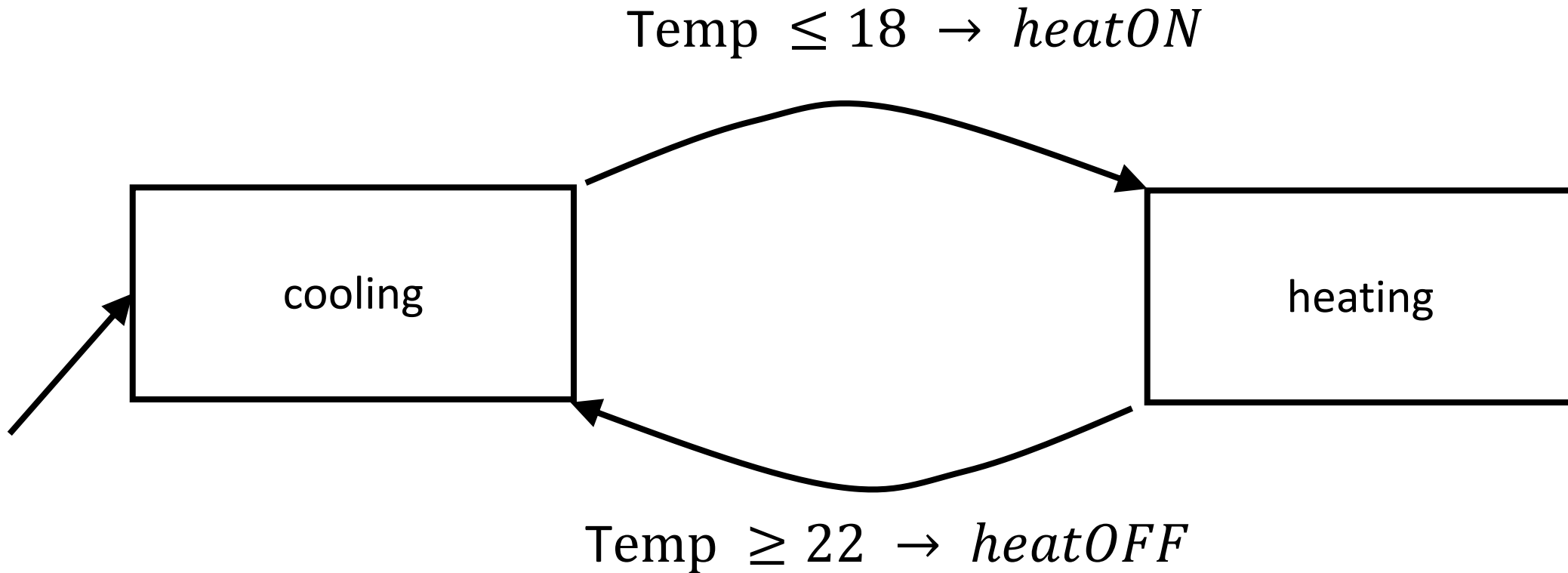
Synchronous components: summary

- ▶ Synchronous dataflow languages used to model synchronous components
 - ▶ Scade-suite from Esterel Technologies: used in many avionics' applications
- ▶ Benefit: system design is simpler
- ▶ Challenge: How do we ensure synchronous execution when components may execute on different hardware?

inputs: *pedestrian*: pure
outputs: *sigR*, *sigG*, *sigY*: pure



Thermostat FSM



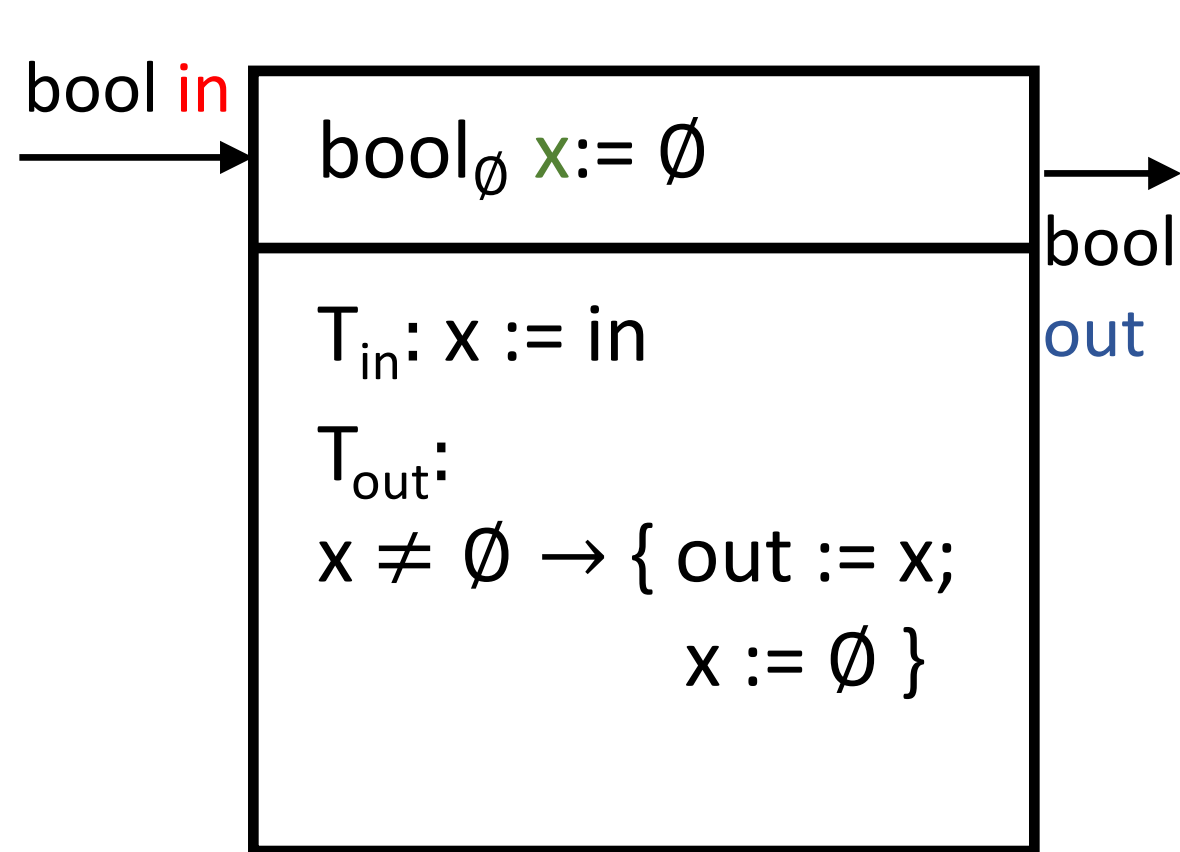
It could be **event triggered**, like the garage counter, in which case it will react whenever a *temperature* input is provided. Alternatively, it could be **time triggered**, meaning that it reacts at regular time intervals

Asynchronous Components

Asynchrony

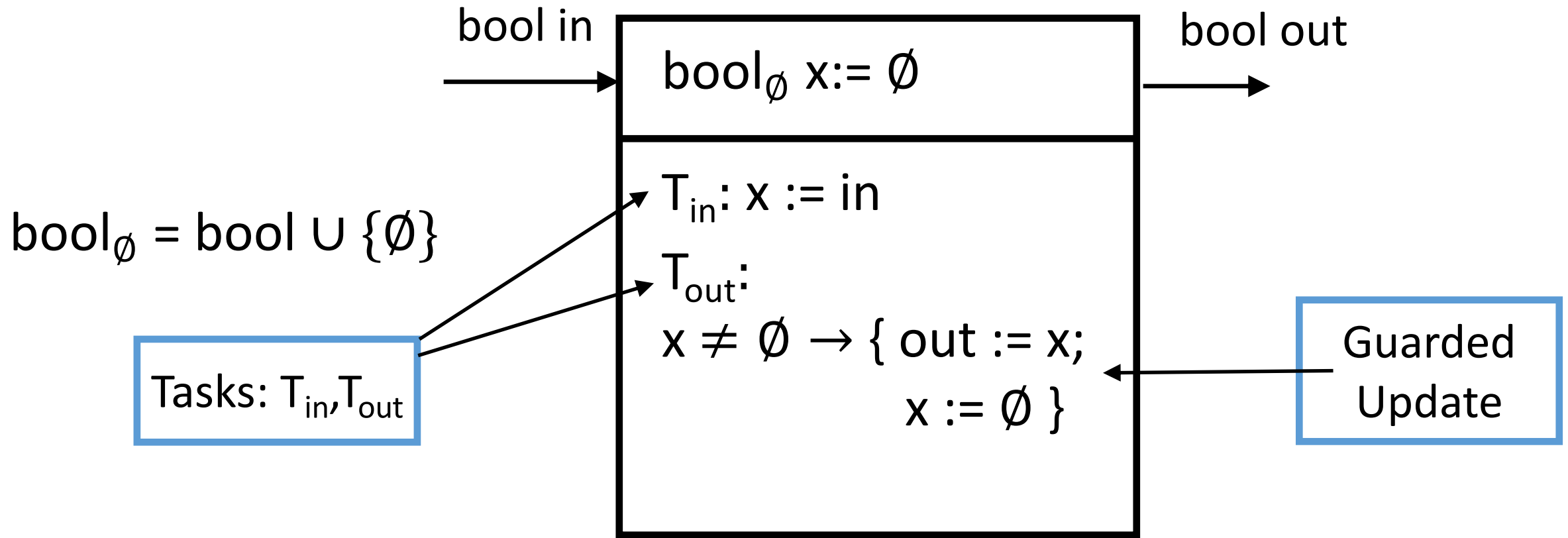
- ▶ Synchrony: All components execute in a sequence of rounds in lock-step
- ▶ Asynchrony: No lock-step computation!
- ▶ Natural model for networked, distributed communicating components executing independently and at possibly different speeds
- ▶ As there is no central, global clock, explicit coordination is required between components
- ▶ Examples:
 - ▶ Processes in distributed computation, multiple threads in any modern OS
 - ▶ Interrupt-driven processing

Asynchronous Reactive Component



- ▶ Input channel **in** of type bool
- ▶ Output channel **out** of type bool
- ▶ State variable **x** of type bool+ \emptyset . The value \emptyset indicates empty or null.
- ▶ x initialized to \emptyset
- ▶ **Input task** T_{in} reads input value into x
- ▶ **Output task** T_{out} produces output if x is not empty

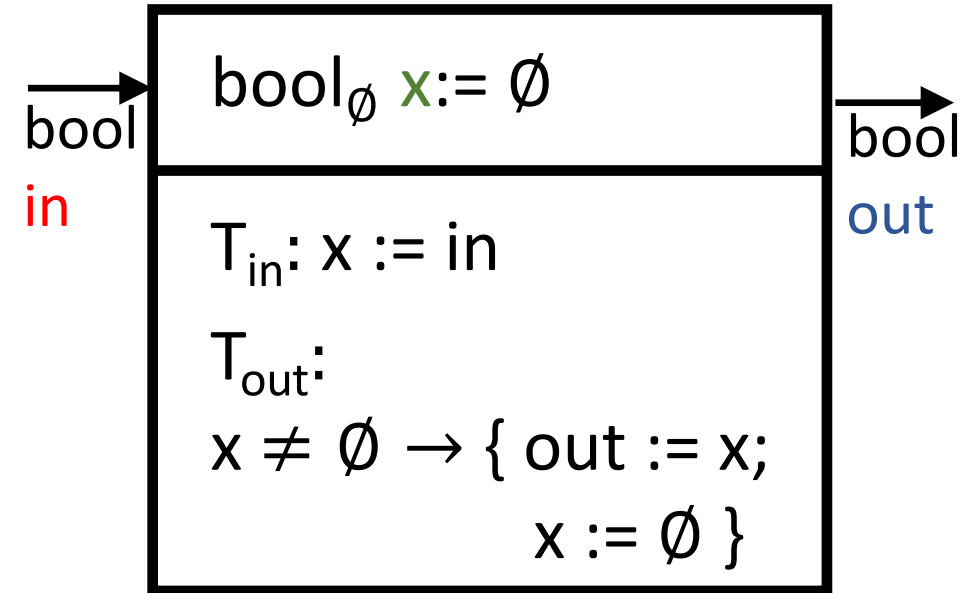
Asynchronous Reactive Component Example



Asynchronous Reactive Component Execution

- ▶ Execution Model: In each step only one task is executed
- ▶ Task can be executed only if it is enabled (i.e. if its guard condition is true)
- ▶ If multiple guard conditions are true, one task is nondeterministically executed
- ▶ Sample execution:

$$\emptyset \xrightarrow[T_{in}]{in?0} 0 \xrightarrow[T_{out}]{out!0} \emptyset \xrightarrow[T_{in}]{in?1} 1 \xrightarrow[T_{in}]{in?0} 0 \xrightarrow[T_{out}]{out!0} \emptyset$$



Buffer

Example: Asynchrony + Nondeterminism

```
int  $x := 0, y := 0$ 
```

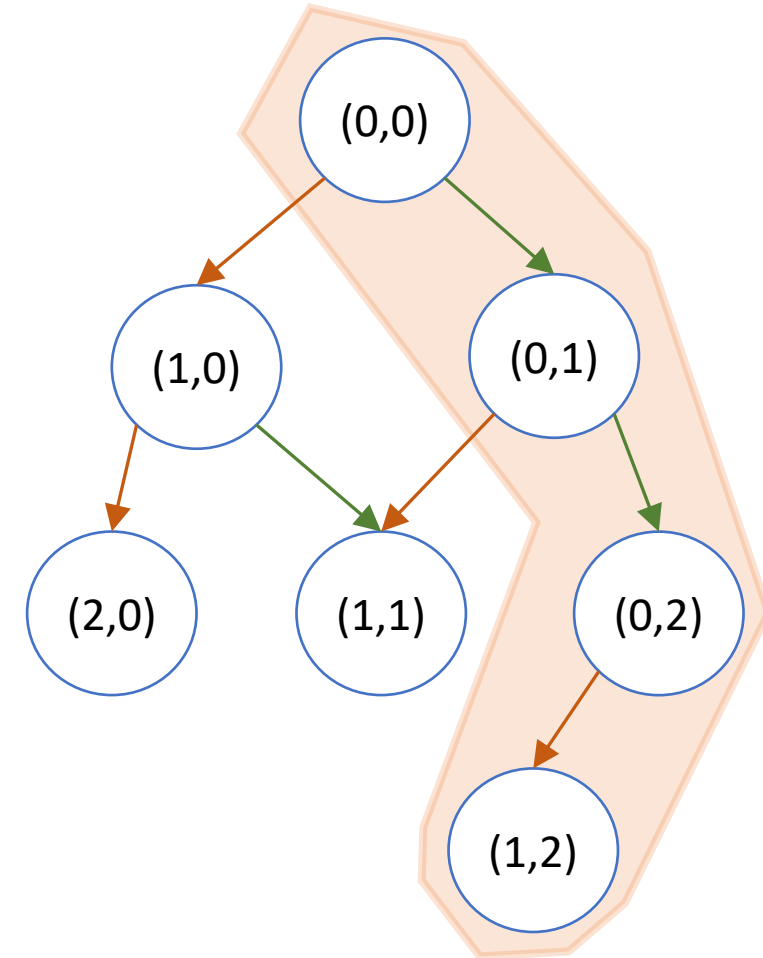
```
 $T_x: x := x + 1$ 
```

```
 $T_y: y := y + 1$ 
```

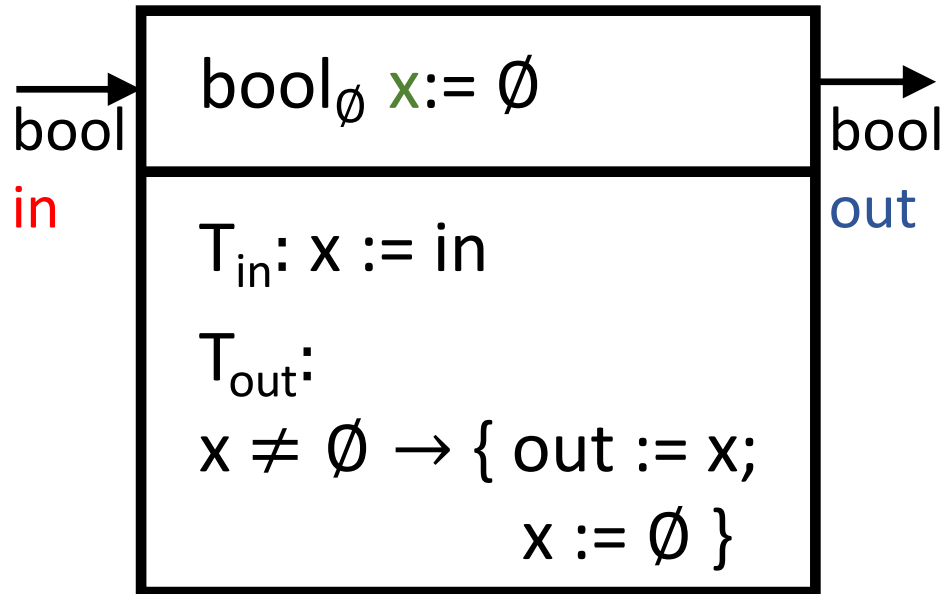
- ▶ ARC may have no inputs or outputs, just internal tasks
 - ▶ Update may have no guards
- ▶ In each step, execute T_x or T_y
- ▶ Sample execution:

$(0,0) \xrightarrow{T_y} (0,1) \xrightarrow{T_y} (0,2) \xrightarrow{T_x} (1,2) \xrightarrow{T_y} (1,3)$

- ▶ Interleaved model of concurrency



Asynchronous Process/Reactive Component



- ▶ Set of input channels: I
 - ▶ ESM representation: **in**?v, where v is the value to be received
- ▶ Set of output channels: O
 - ▶ ESM representation: **out**!v, where v is the value to be written
- ▶ Set of state variables X
- ▶ Initialization Init which maps state variables to initial values

Updates are different from SRCs!

Input Task defines updates of the form: $G \rightarrow x := E(X, in)$

- ▶ Guard condition G : some expression over *only* state variables X ; input task can be executed only if G is true
- ▶ For each in in I , we associate a read-set ($X \cup \{in\}$): variables that can appear in E for input task associated with in (rationale: can read value on in only if that task is enabled)
- ▶ Defines a set of input actions of the form: $q \xrightarrow{in?v} q'$
 - ▶ where q is value of state variables before update, and q satisfies G
 - ▶ value of state variables after update is $q' = E(X \mapsto q, in \mapsto v)$

Updates are different from SRCs!

Output Task: defines updates of the form: $G \rightarrow \text{out} := E(X)$

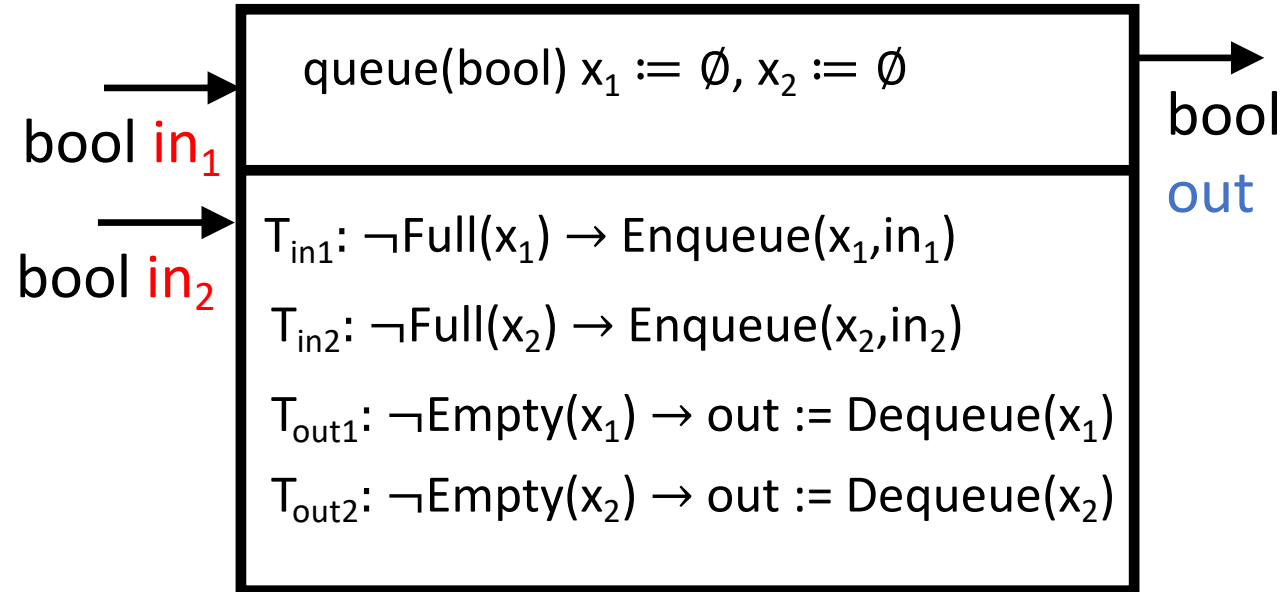
- ▶ Guard condition G : some expression over **only** variables in X ; output task can be executed only if G is true
- ▶ Any expression containing only state variables can appear in E
- ▶ Defines an output action of the form $q \xrightarrow{\text{out!}v} q'$
 - ▶ where q is value of state variables before update, and q satisfies G
 - ▶ value of state variables after update is q'
 - ▶ value v is output on channel **out**

Updates are different from SRCs!

Internal Task: defines updates of the form: $\mathbf{G} \rightarrow \mathbf{x} := \mathbf{E}(\mathbf{X})$

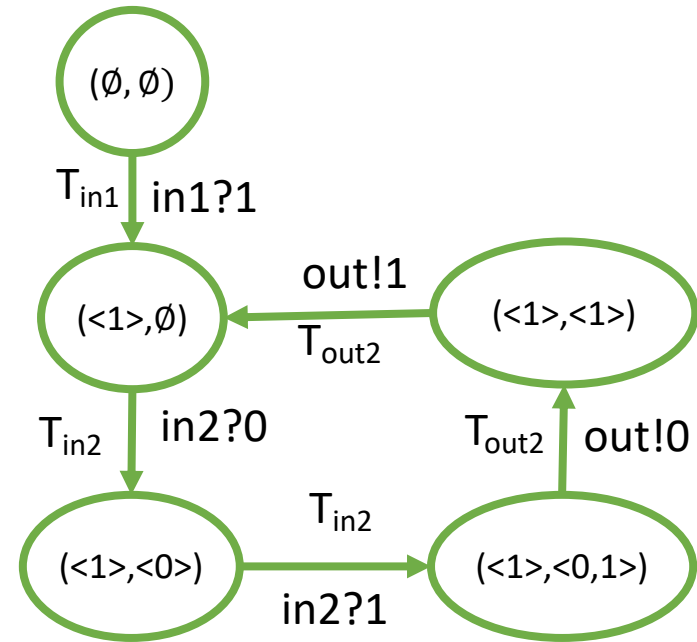
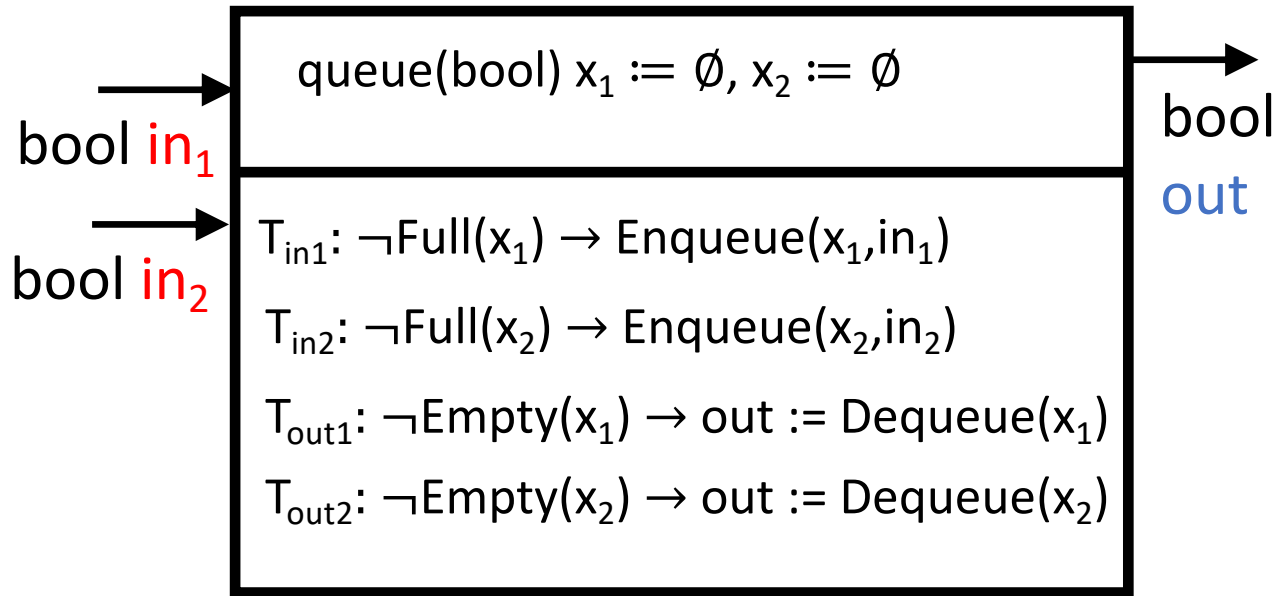
- ▶ Guard condition G : some expression over **only** variables in X ; internal task can be executed only if G is true
- ▶ Any expression containing only state variables can appear in E , only state variables appear on LHS
- ▶ Defines an internal action of the form $q \xrightarrow{\varepsilon} q'$
 - ▶ where q is value of state variables before update, and q satisfies G
 - ▶ value of state variables after update is q'
 - ▶ No input is read or output is produced!

Asynchronous Example



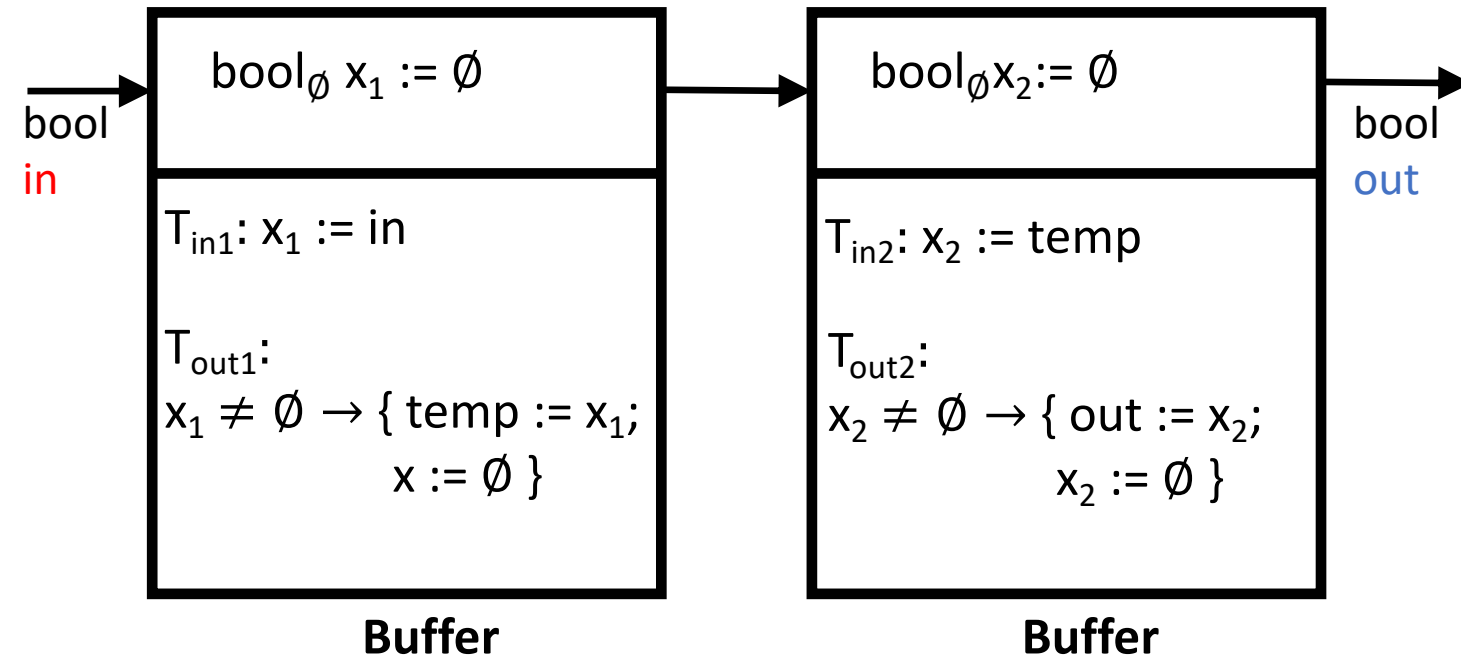
Asynchronous Processes can also be represented with extended state machines

Asynchronous Merge: Sequence of Actions



Asynchronous Processes can also be represented with extended state machines

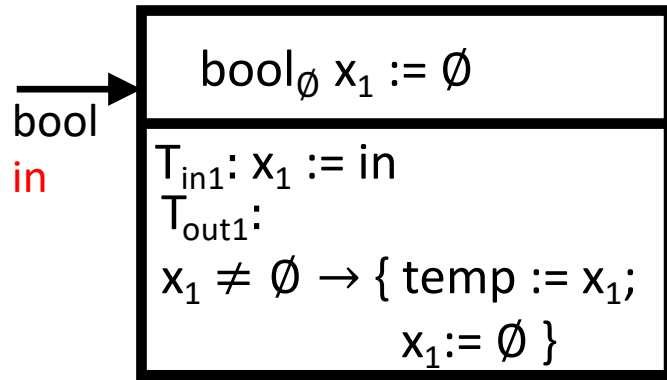
Composing Asynchronous Processes



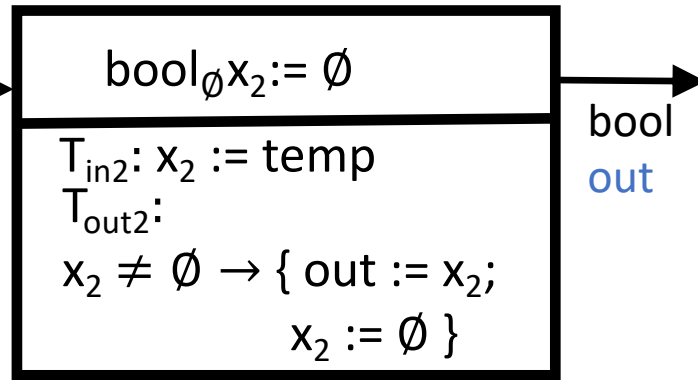
- ▶ Parallel composition: Inputs, Outputs, States and Initialization similar to the synchronous case
- ▶ Input consumption needs to be synchronized with output production for the 'temp' variable

Composed DoubleBuffer

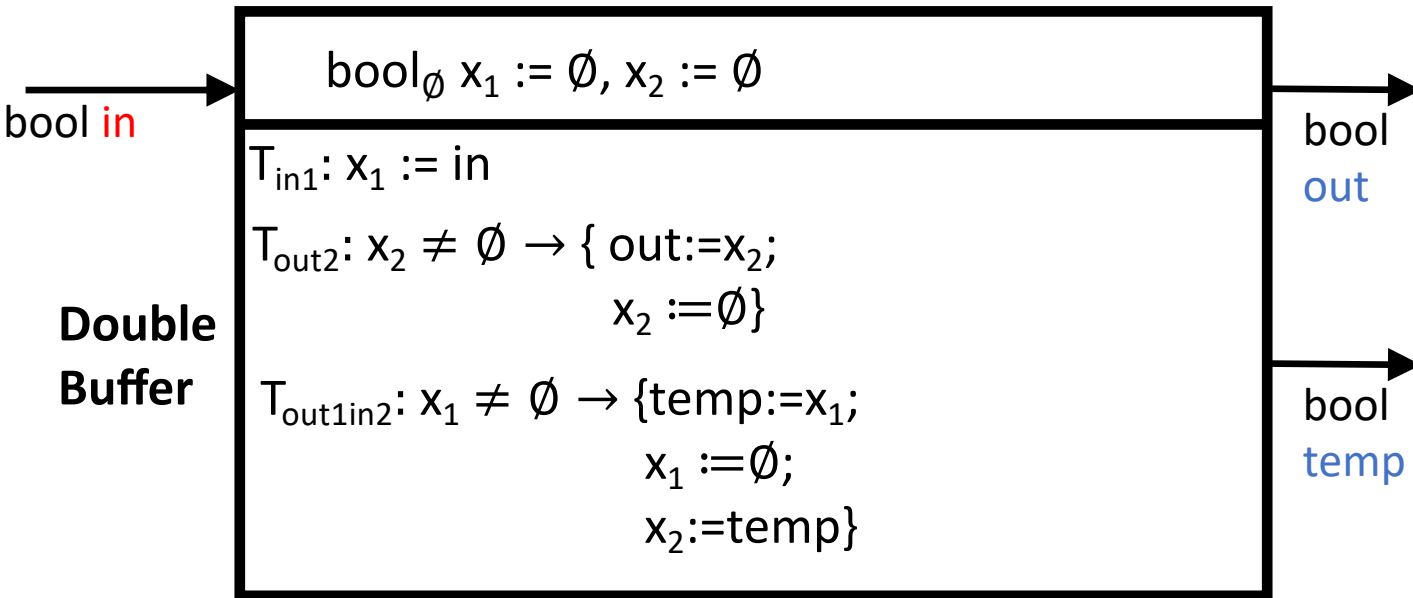
Buffer



Buffer



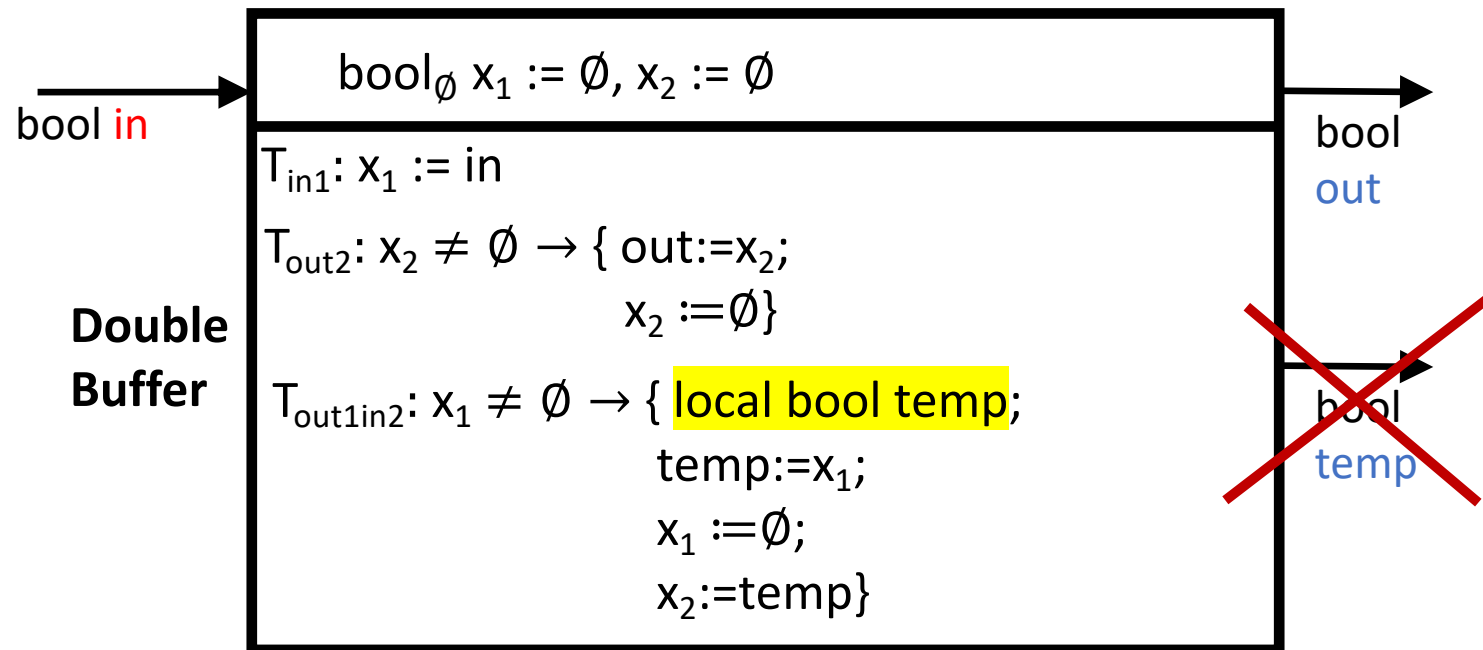
Double Buffer



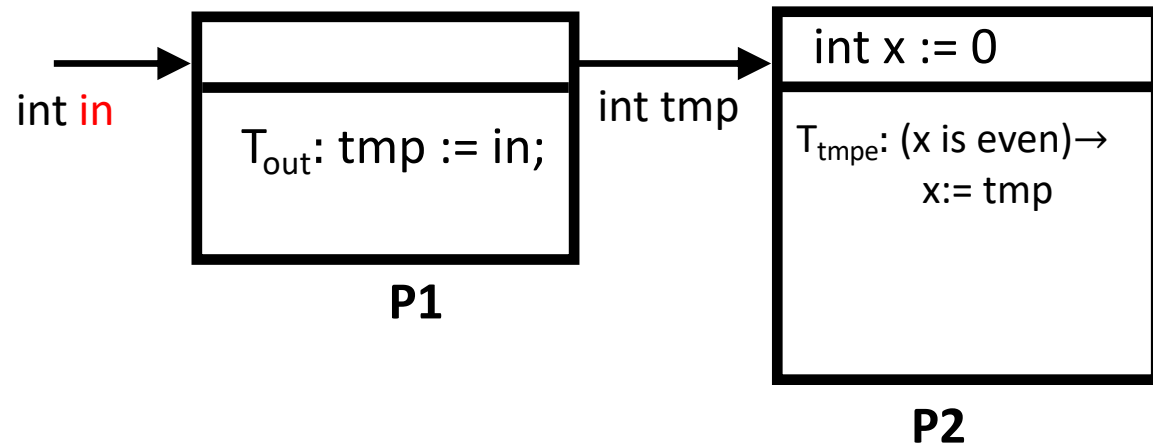
- ▶ Defining $P_1 \mid P_2$
- ▶ In each step only 1 task executes
- ▶ If y is an output channel of P_1 and input channel of P_2 :
- ▶ Output task for $P_1: G_1 \rightarrow U_1$
- ▶ Input task for $P_2: G_2 \rightarrow U_2$
- ▶ Composition has output task for y with code: $G_1 \wedge G_2 \rightarrow U_1; U_2$

Output Hiding

Hiding output y : achieved by removing y from the set of output channels and turning each output task associated with the channel y into an internal task by declaring y to be a local variable



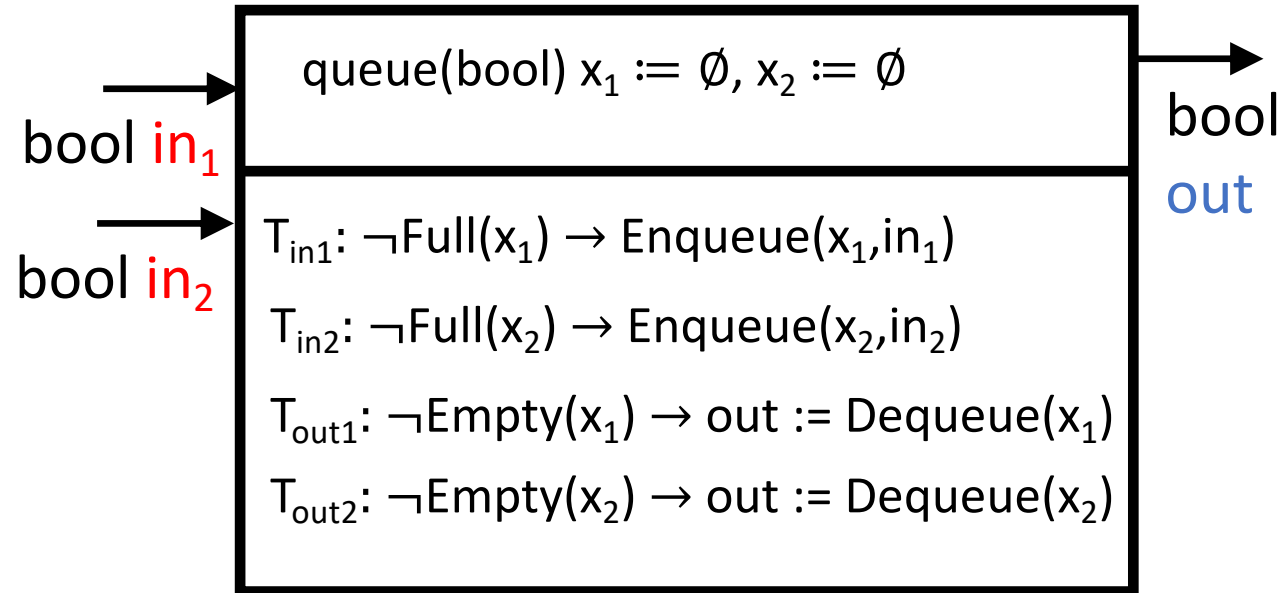
Blocking vs. Non-blocking Synchronization



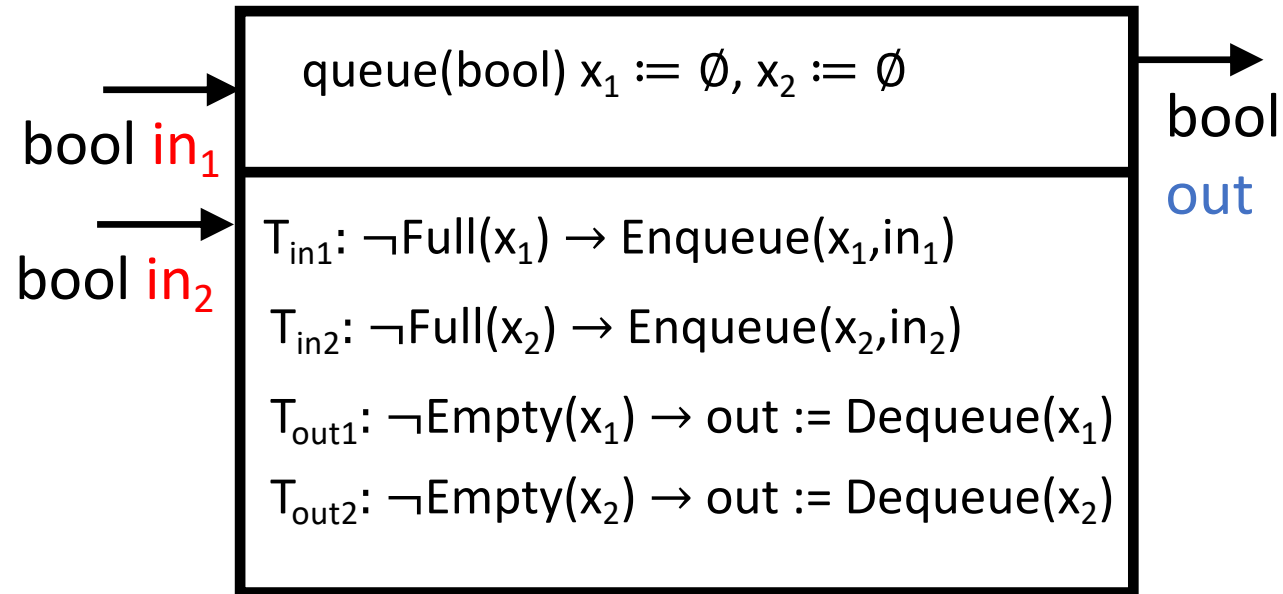
How do you make P2 non-blocking?

- ▶ Task T_{out} of P1 can *produce* a value on the output only if P2 has an input task that is enabled to *consume* the value with some input task
- ▶ In this example, once x becomes odd, P2 cannot consume (no enabled input task) and it **blocks** communication
- ▶ Process is **non-blocking** on channel **in** for a state s if at least one guarded update corresponding to input task for **in** is enabled in the state s
- ▶ Process is **non-blocking** if it is non-blocking in every channel and for every states.

Blocking vs. Non-blocking Synchronization in Merge



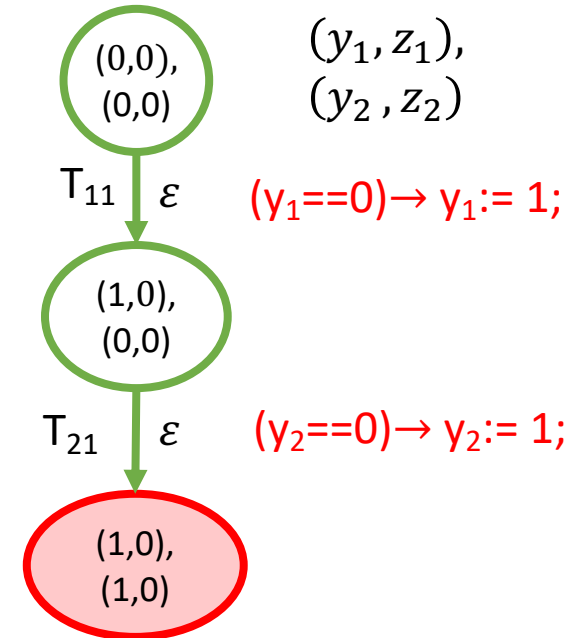
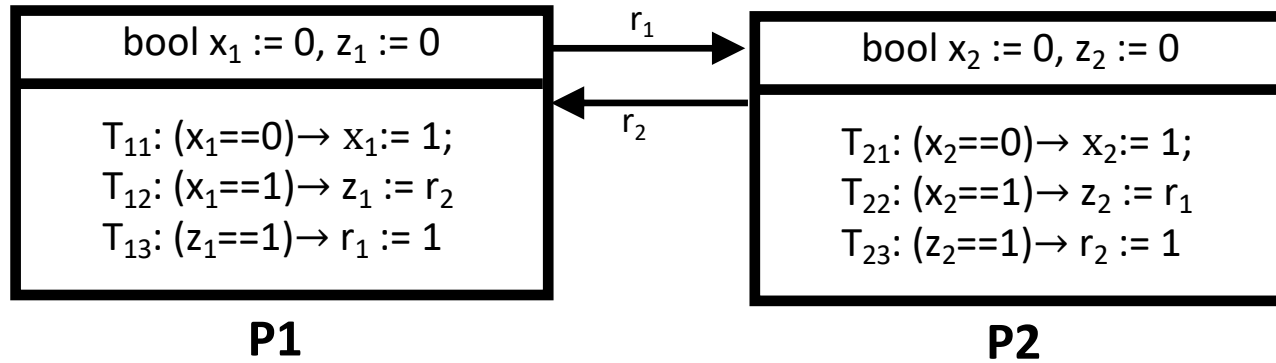
Blocking vs. Non-blocking Synchronization in Merge



An input on the channel in_1 cannot be processed if the queue x_1 is full, and thus the producer of outputs on the channel in_1 has to wait until this queue becomes non-full

Deadlocks

- ▶ Common error in asynchronous designs
- ▶ Caused by each process waiting for another process to execute a task, but no task is enabled



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