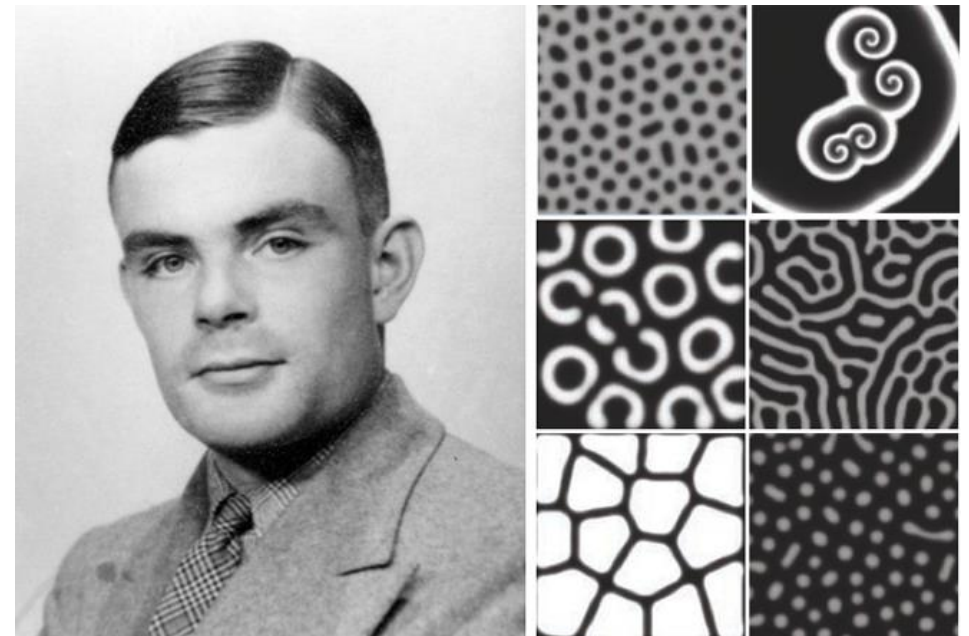
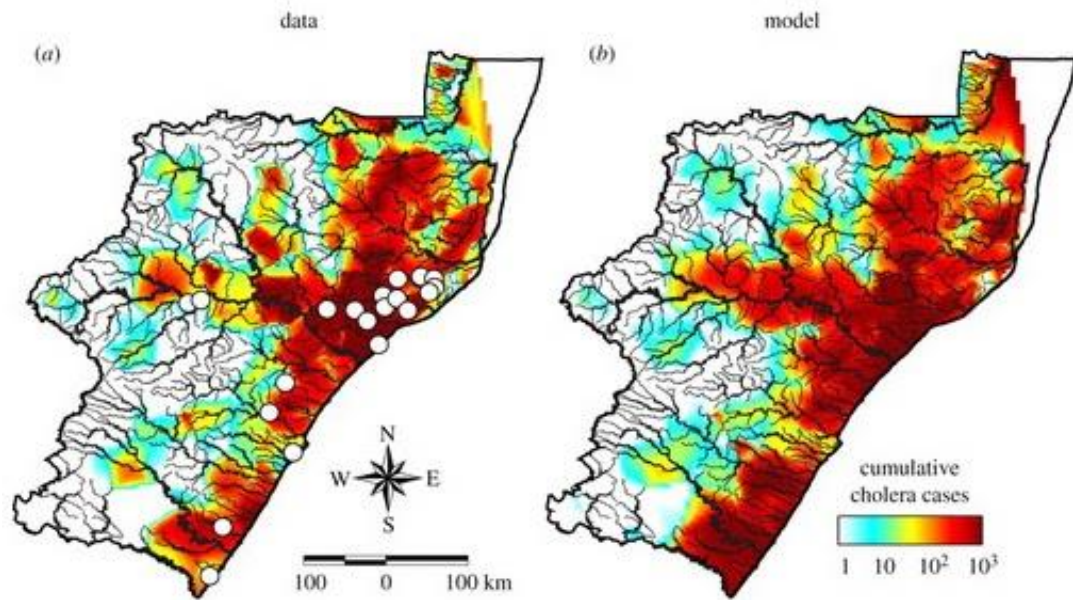
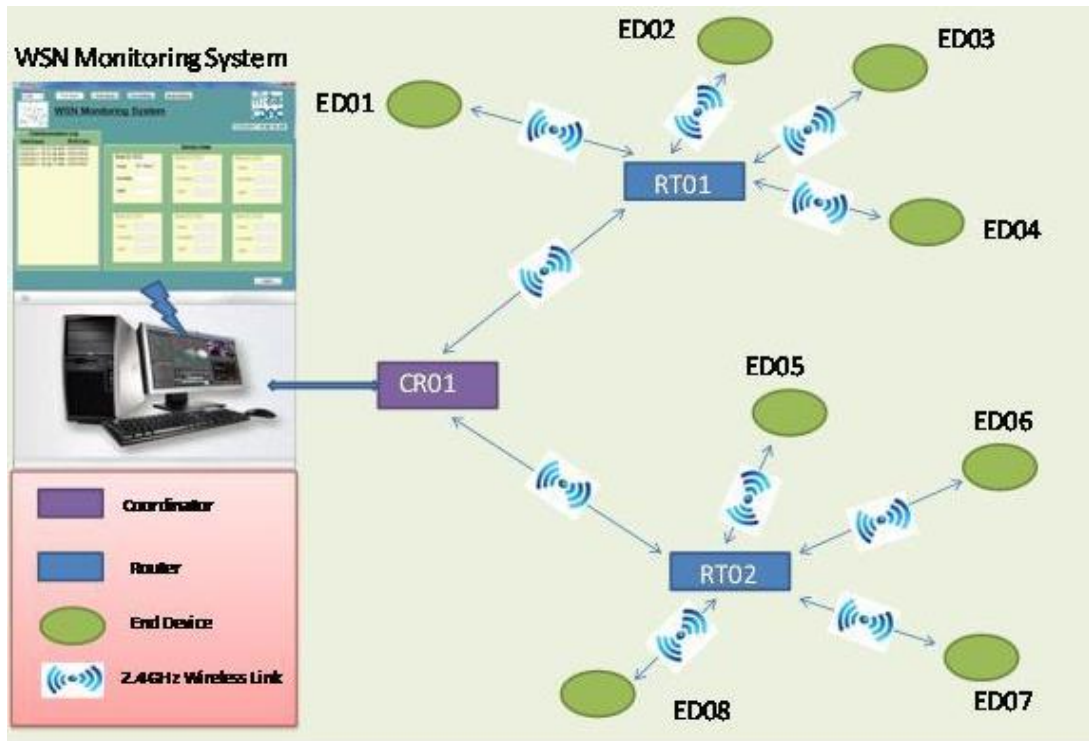


Cyber-Physical Systems

Laura Nenzi

Università degli Studi di Trieste
I Semestre 2024

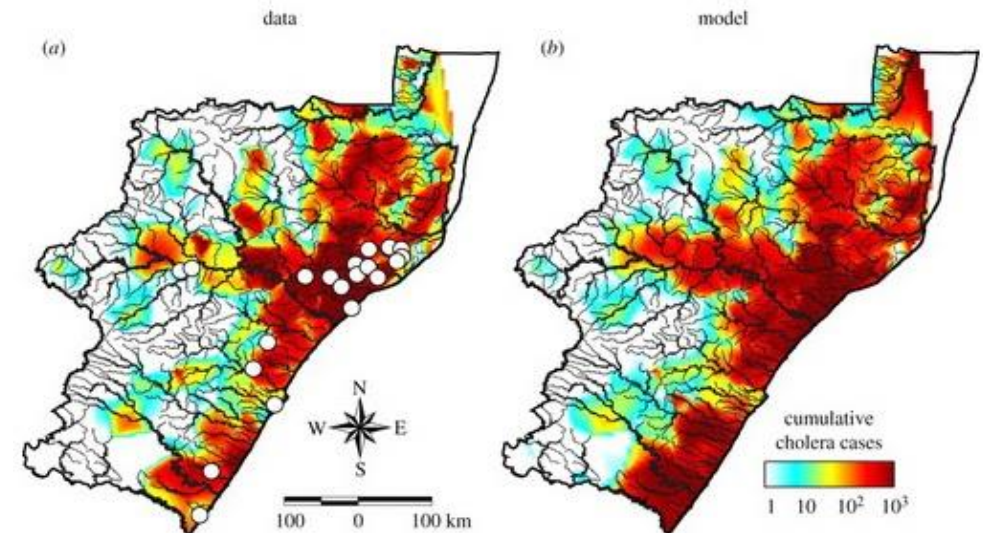
Lecture 15: Spatio-Temporal Reach and Escape Logic

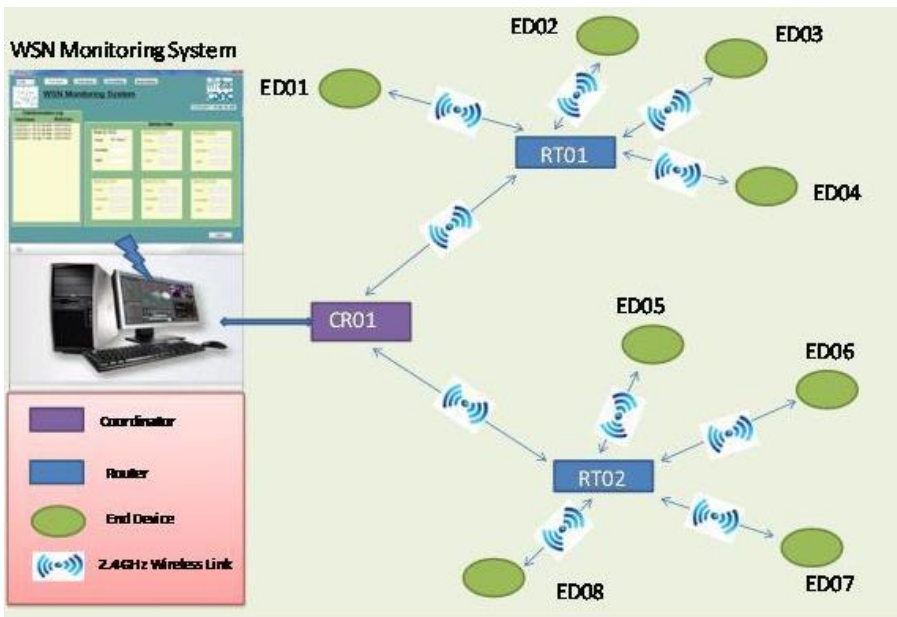




Availability: I can always find a station with at least one bike in a radius of 500 meters

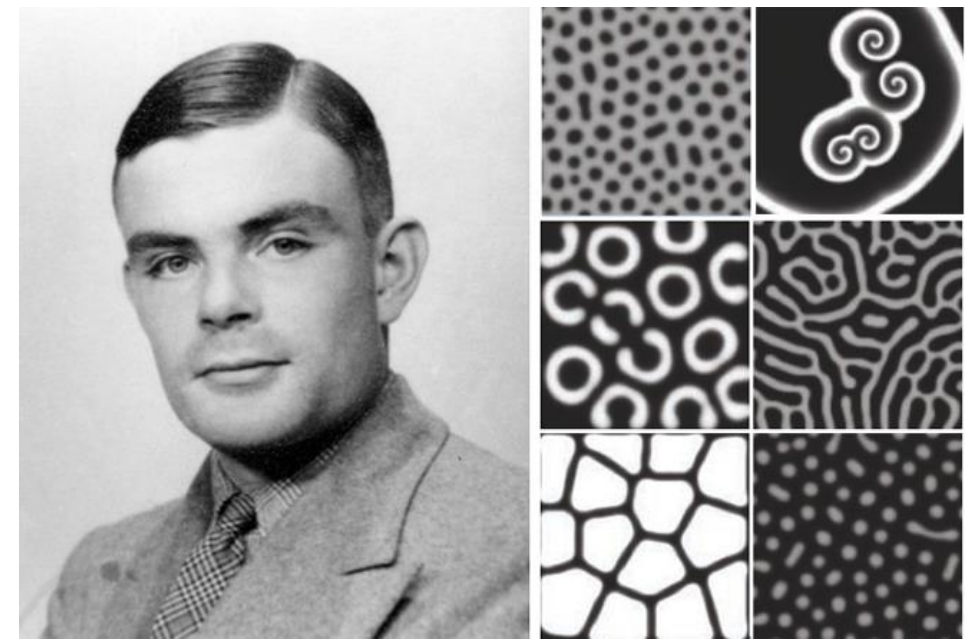
Spread: after 10 time units, there exists a location l' at a certain distance from location l where the number of infected individuals is more than 50





Reliability: we can always find a path of sensors such that all sensors have a battery level greater than 0.5

Spots: regions with low density of protein A are always surrounded by regions with high level of protein B



How to specify such spatio-temporal behaviours in a formal and human-understandable language ?

How to monitor their onset efficiently?

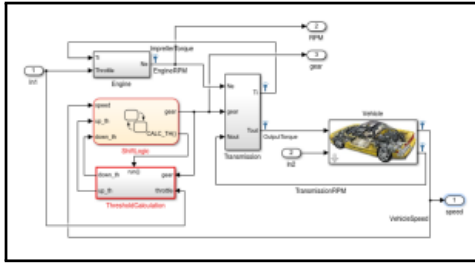
Part 1 :

- Space Model and traces
- Spatio- Temporal Reach and Escape Logic (STREL)

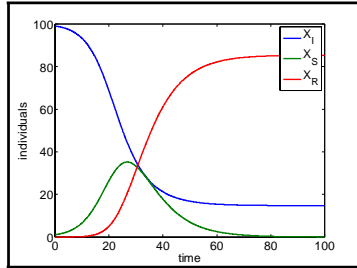
Part 2:

- Monitoring
- Applicability to different scenarios

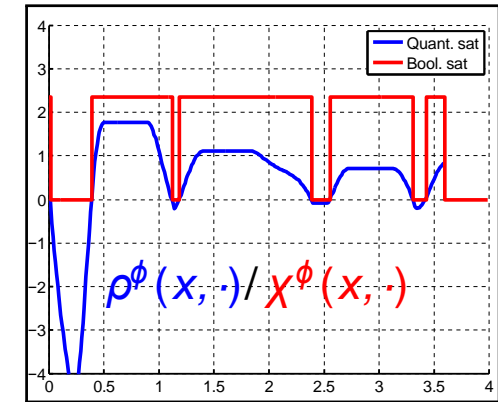
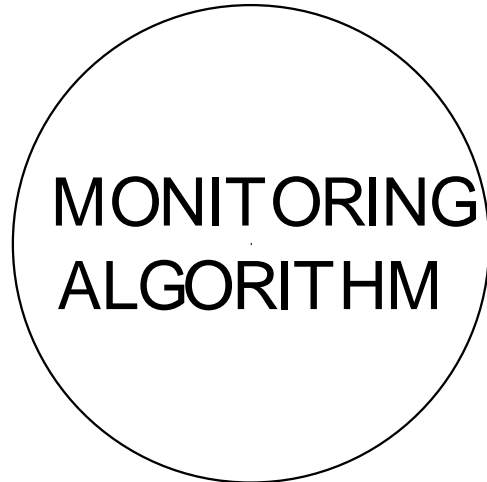
MODEL



SIMULATION



RESULTS



PROPERTIES

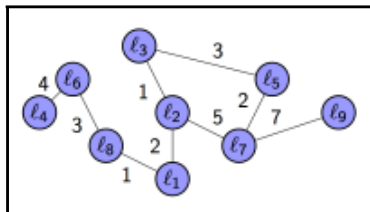


SPECIFICATION

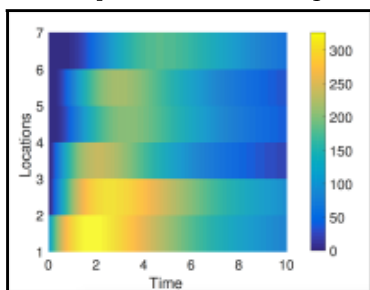
$$F^I G^{[0, \infty)} a$$

INPUTS

Spatial Configuration



Sp-Temporal Trajectory



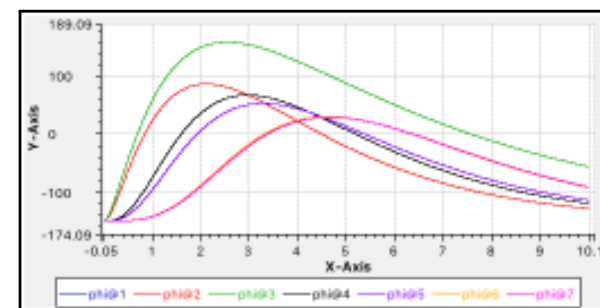
Specification

$$F_{[0, T]} \varphi_1 S_{[0, d]} \varphi_2$$

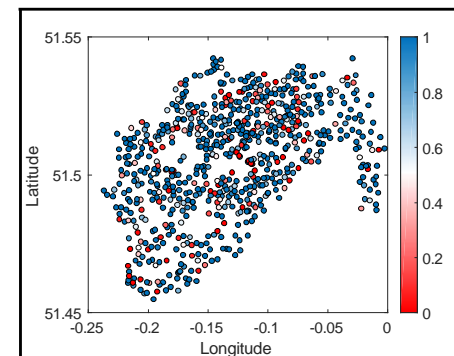
MONITORING
ALGORITHM

OUTPUTS

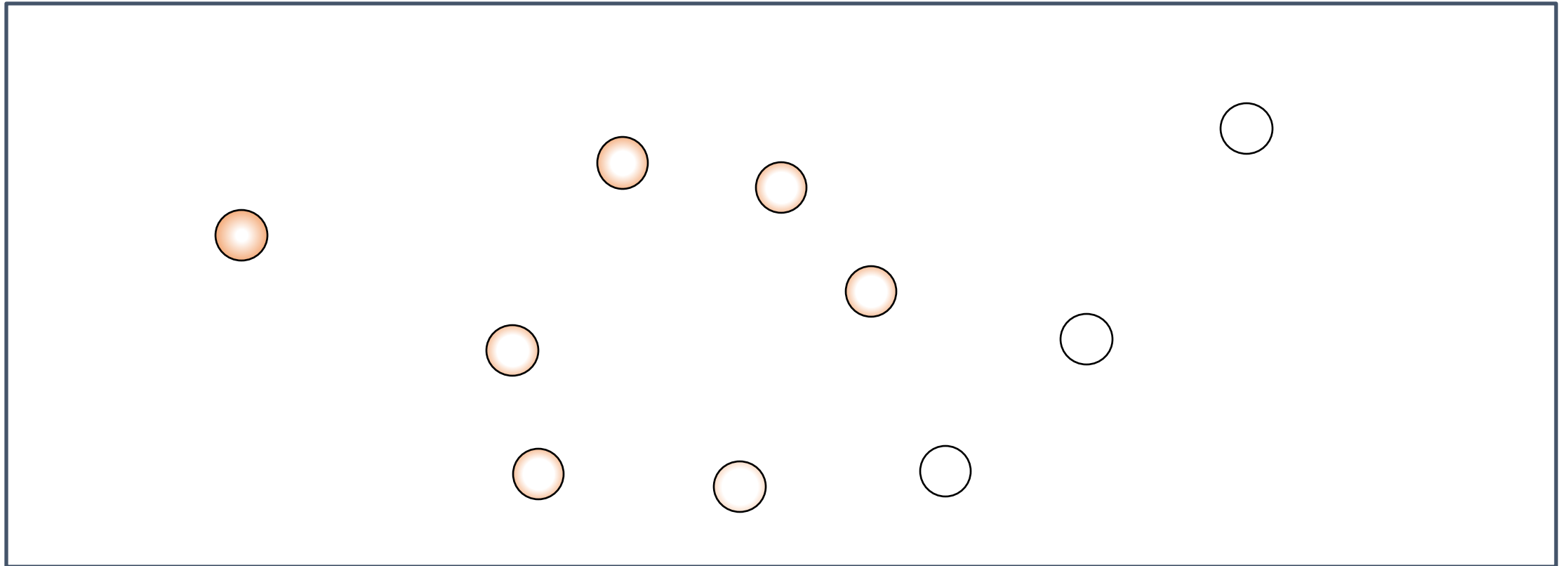
Sp-Temporal Satisfaction



Spatial Satisfaction



Running Example: Wireless Sensor Network



Space Model, Signal and Traces

Spatial Configuration

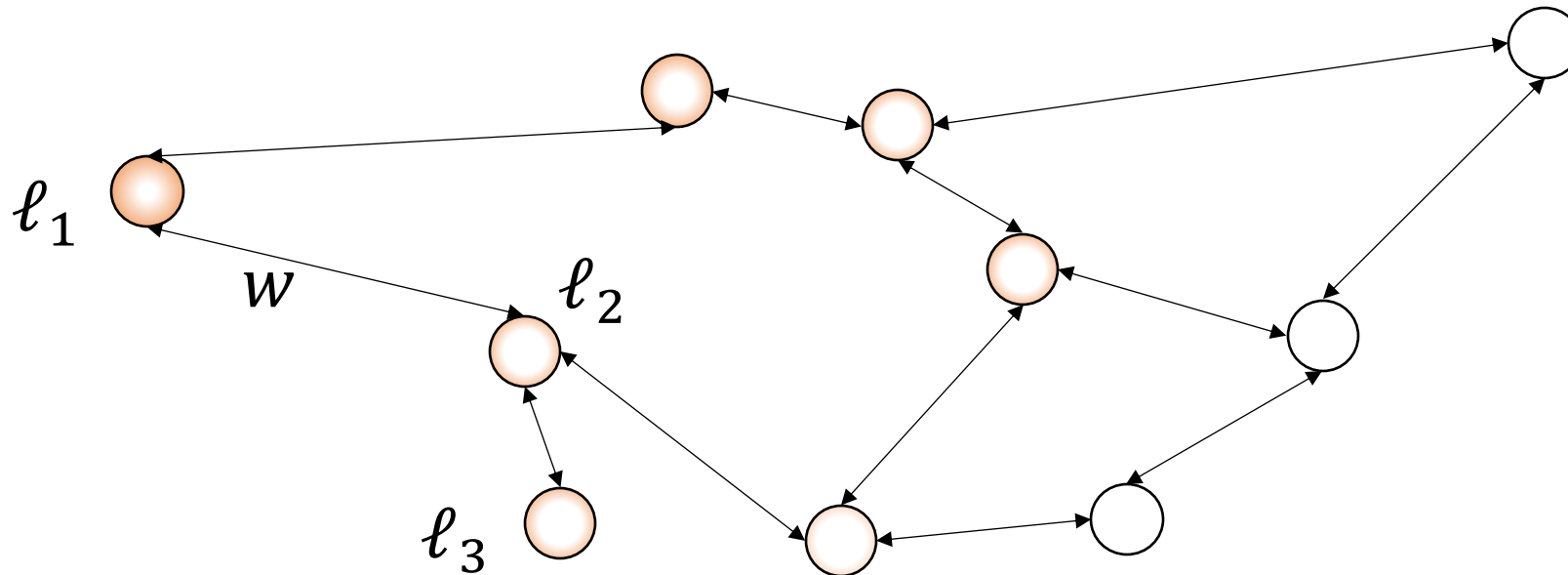
We consider a discrete space described as a weighted (direct) graph

Reasons:

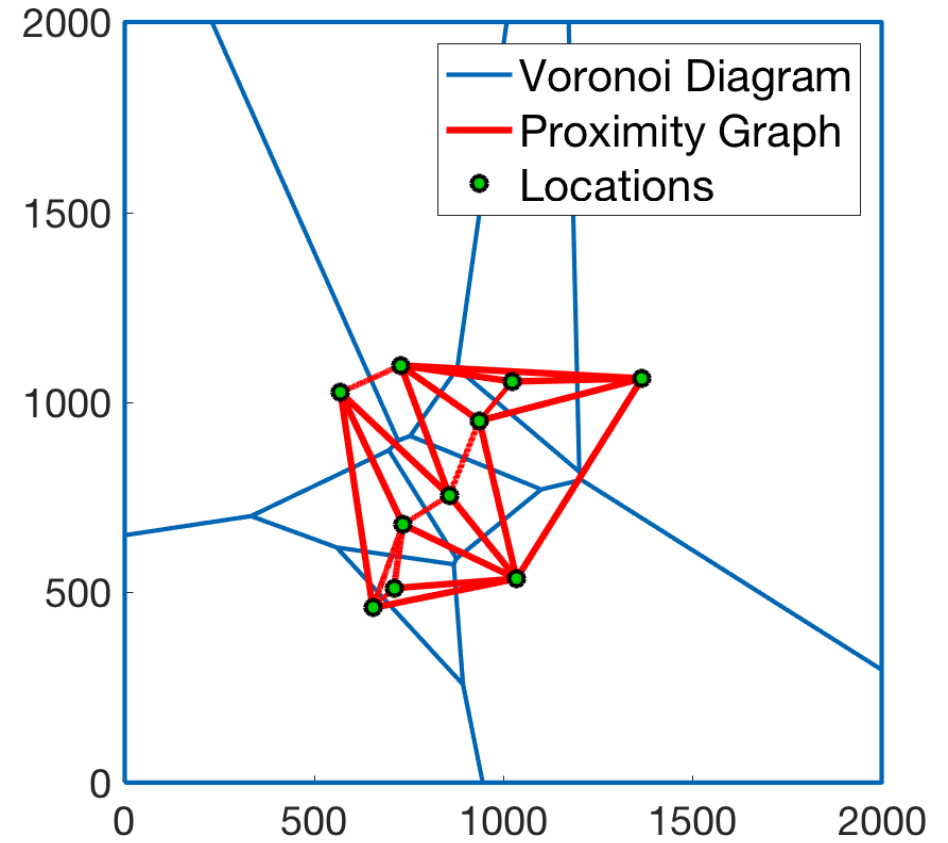
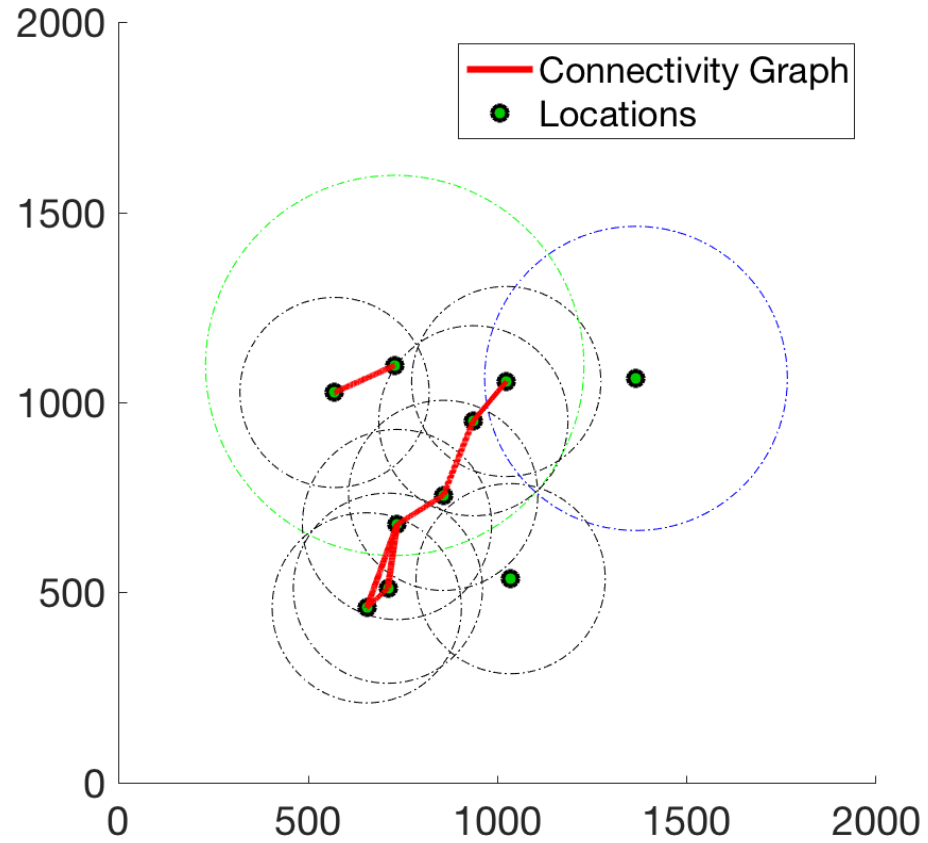
- many applications, like bike sharing systems, smart grid and sensor networks are naturally framed in a discrete spatial structure
- in many circumstances continuous space is abstracted as a grid or as a mesh, e.g. numerical integration of PDEs

Space Model $S = \langle L, W \rangle$

- L is a set of nodes that we call locations;
- $W \subseteq L \times \mathbb{R} \times L$ is a proximity function associating a label $w \in \mathbb{R}$ to distinct pair $\ell_1, \ell_2 \in L$. If $(\ell_1, w, \ell_2) \in W$, it means that there is an edge from ℓ_1 to ℓ_2 with weight $w \in \mathbb{R}$

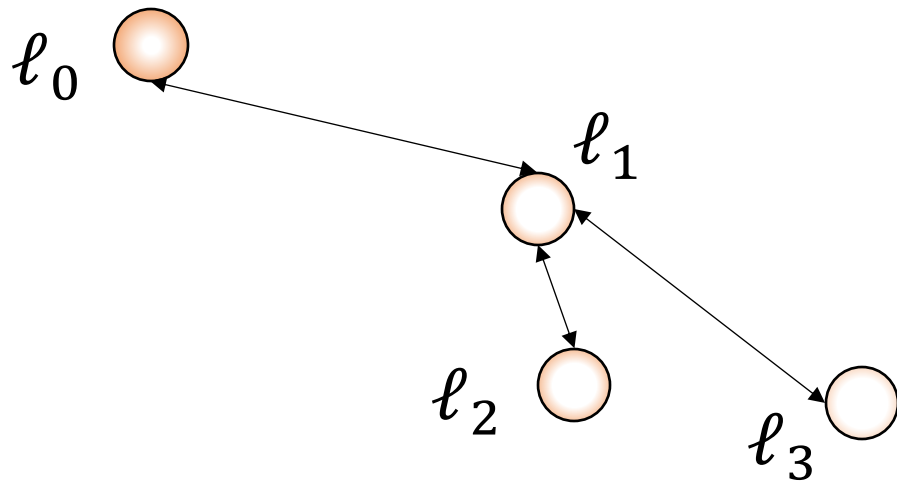


Example



Route $\tau = \ell_0 \ell_1 \ell_2 \dots$

It is a infinite sequence s.t. $\forall i \geq 0 \exists w$ s.t. $(\ell_i, w, \ell_{i+1}) \in W$



$\ell_0 \ell_1 \ell_2 \ell_1 \dots$ is a route

$\ell_0 \ell_1 \ell_2 \ell_3 \dots$ is a not route

$\tau[i]$ to denote the i - th node τ

$\tau(\ell)$ to denote the first occurrence of $\ell \in \tau$

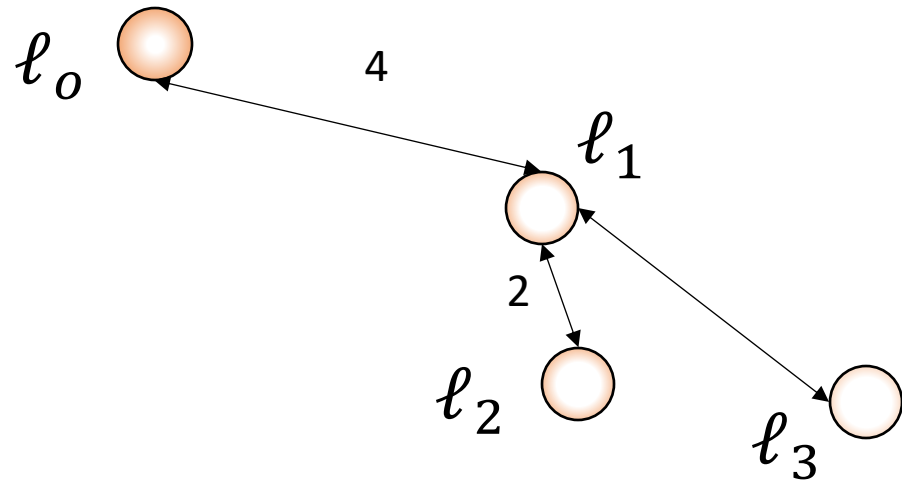
Route Distance $d_{\tau}^f [i]$

The distance $d_{\tau}^f [i]$ up to index i is:

$$d_{\tau}^f [i] = \begin{cases} 0 & i = 0 \\ f(d_{\tau[1..]}^f [i - 1], w) & (i > 0) \text{ and } \tau[0] \stackrel{w}{\mapsto} \tau[1] \end{cases}$$

$$d_{\tau}^f (\ell) = d_{\tau}^f [\tau(\ell)]$$

Route Distance $d_{\tau}^f [i]$



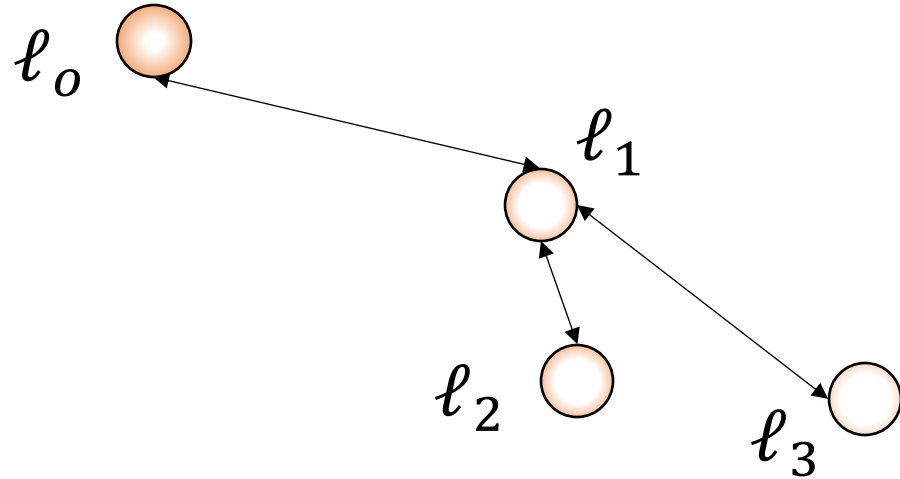
$$\text{weight}(x, y) = x + y$$

$$\text{hops}(x, y) = x + 1$$

$$\begin{aligned} d_{l_0 l_1 l_2 \dots}^{\text{weight}} [2] &= \text{weight}(d_{l_1 l_2 \dots}^{\text{weight}} [1], 4) = d_{l_1 l_2}^{\text{weight}} [1] + 4 = \dots \\ &= \text{weight}(d_{l_2 \dots}^{\text{weight}} [0], 2) + 4 = 6 \end{aligned}$$

Location Distance $d_S^f[\ell_i, \ell_j]$

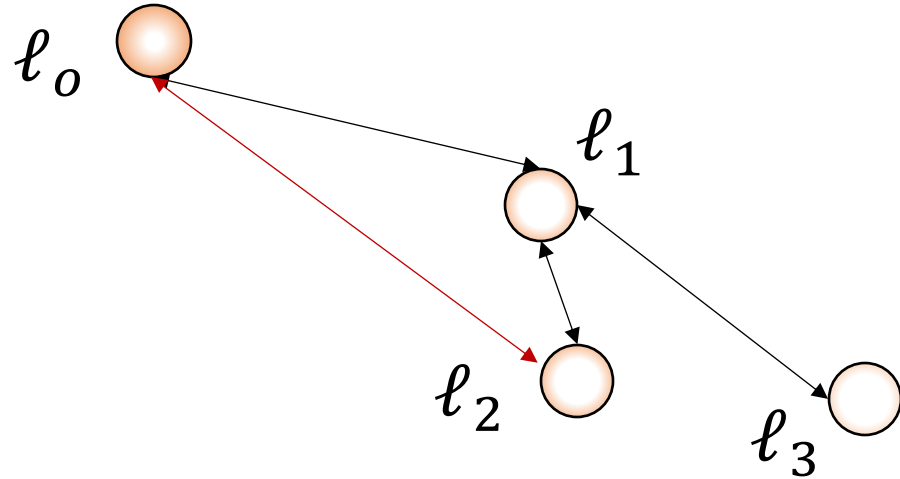
$$d_S^f[\ell_i, \ell_j] = \min\{d_\tau[\ell_j] \mid \tau \in \text{Routes}(S, \ell_i)\}$$



$$d_S^{\text{hops}}[\ell_0, \ell_2] = \mathbf{2}$$

Location Distance

$$d_S^f[l_i, l_j] = \min\{d_\tau[l_j] \mid \tau \in \text{Routes}(S, l_i)\}$$



$$d_S^{\text{hops}}[l_0, l_2] = \mathbf{1}$$

Signal and Trace

Spatio-Temporal Signals $\sigma: L \rightarrow \mathbb{T} \rightarrow D$

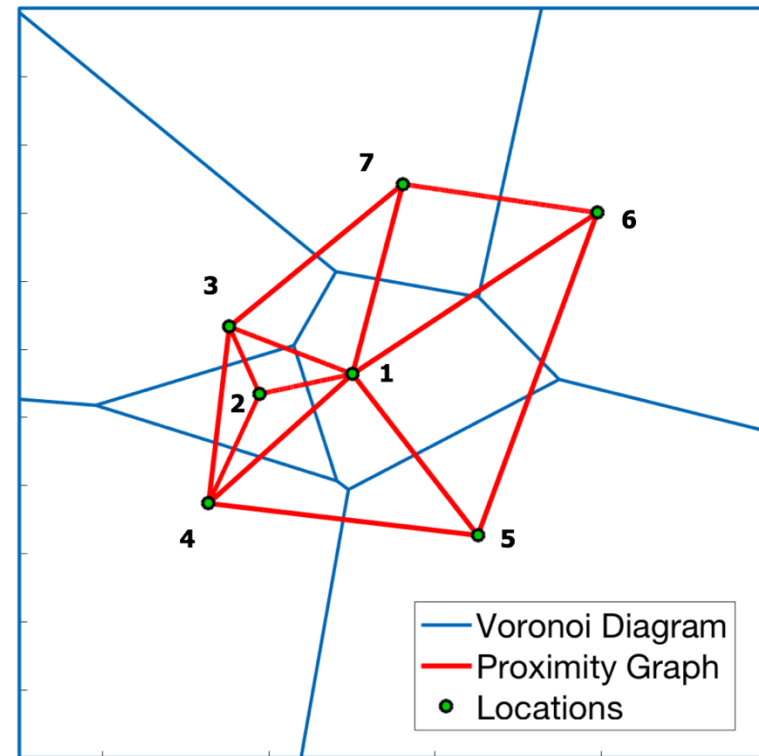
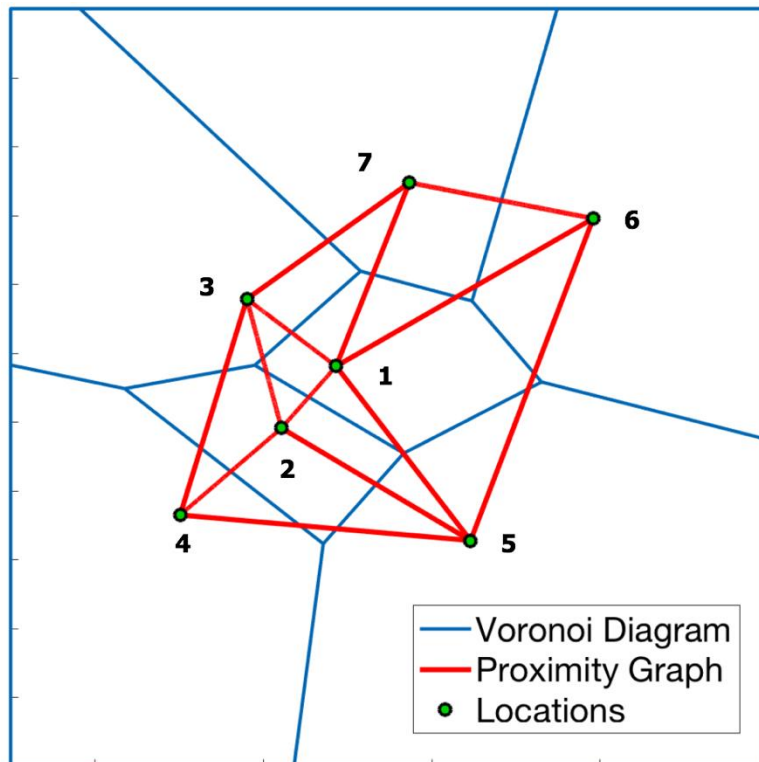
Spatio-Temporal Trace $\vec{x}: L \rightarrow \mathbb{T} \rightarrow D^n$

$$x(\ell) = (v_B, v_T)$$

$$x(\ell, t) = (v_B(t), v_T(t))$$

Dynamic Spatial Model

(t_i, S_i) for $i = 1, \dots, n$ and $S(t) = S_i \forall t \in [t_i, t_{i+1})$



STREL

Spatio- Temporal Reach and Escape Logic (STREL)

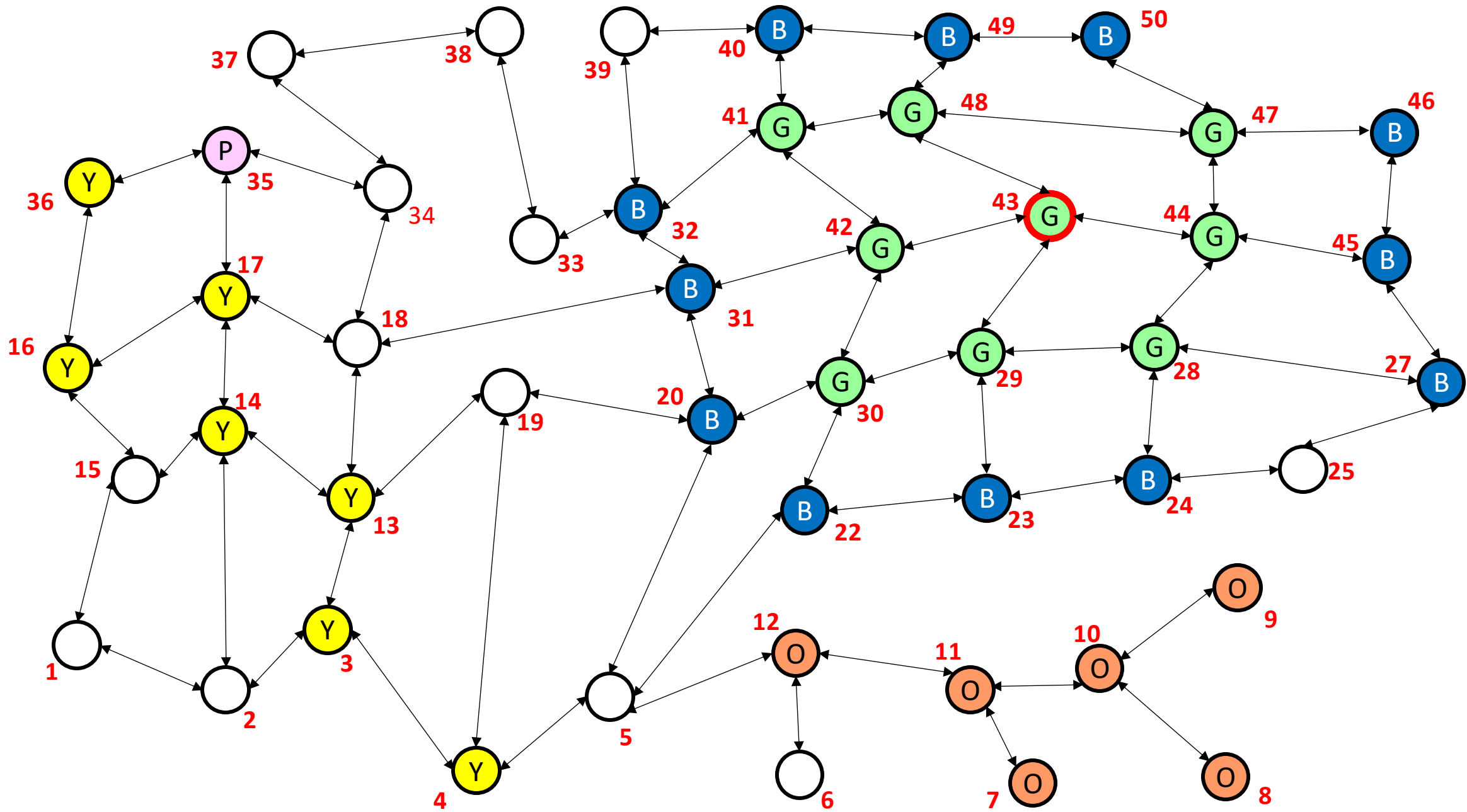
It is an extension of the Signal Temporal Logic with a number of spatial modal operators

STREL Syntax

$$\varphi := true \mid \mu \mid \neg\varphi \mid \varphi_1 \wedge \varphi_2 \mid \varphi_1 \mathbf{U}_I \varphi_2 \mid \varphi_1 \mathbf{S}_I \varphi_2 \mid \varphi_1 \mathcal{R}_d^f \varphi_2 \mid \mathcal{E}_d^f \varphi$$

In addition, we can derive:

- The disjunction operator: \vee
- the temporal operators: F_I, G_I, O_I, H_I
- the spatial operators: somewhere, everywhere and surround

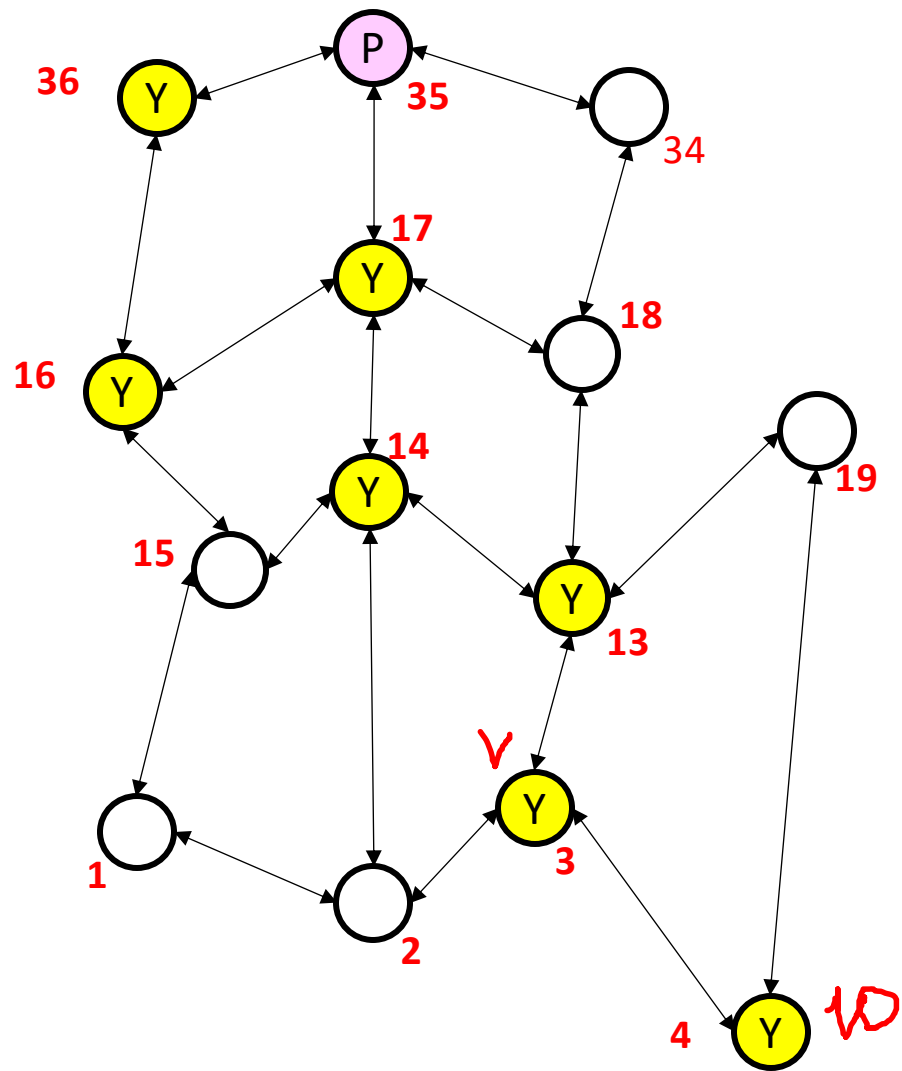


Reach: $'_1 \mathbf{R}_{[d_1, d_2]}^f ' _2$

(S, \vec{x}, ℓ, t) satisfies $'_1 \mathbf{R}_{[d_1, d_2]}^f ' _2$ iff it satisfies φ_2 in a location ℓ' reachable from ℓ through a route τ , with a length $d_\tau^f(\ell') \in [d_1, d_2]$ and such that $\tau[0] = \ell$ and all its elements with index less than $\tau(\ell')$ satisfy φ_1

Reach

yellow $\mathcal{R}_{[1,4]}^{hops}$ *pink*



$$\tau = l_3 l_{13} l_{14} l_{17} l_{35}$$

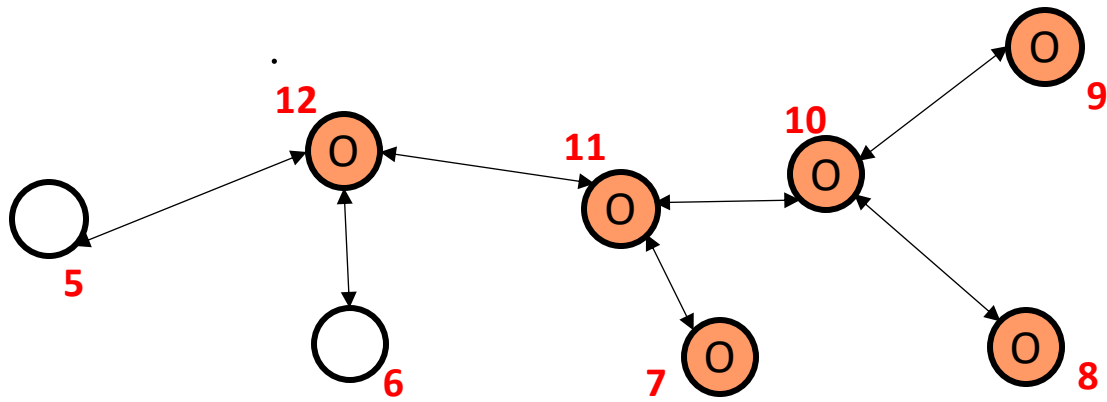
$$d_{\tau}^{hops}(l_{35}) = 4, \text{ where } \tau[0] = l_3$$

Escape: $\mathcal{E}_{[d_1, d_2]}^f \varphi$

(S, \vec{x}, ℓ, t) satisfies $\mathcal{E}_{[d_1, d_2]}^f \varphi$ if and only there exists a route τ and a location $\ell' \in \tau$ such that $\tau[0] = \ell$, $d_S^f[\ell, \ell'] \in [d_1, d_2]$ and all elements $\tau[0], \dots, \tau[k]$ (with $\tau(l') = k$) satisfy φ

Escape:

$\mathcal{E}^{hops}_{[3, \infty]}$ *orange*



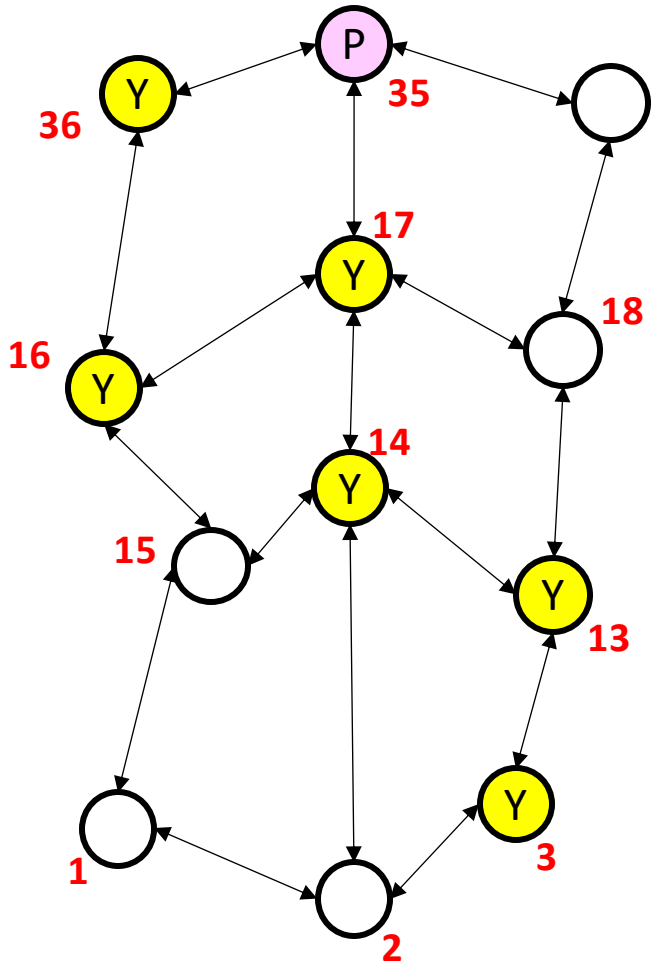
$$\tau = l_9 l_{10} l_{11} l_{12}$$

$$\tau[0] = l_9, \tau[3] = l_{12}$$

$$d_S^{hops}[l_9, l_{12}] = 3$$

Somewhere:

$$\diamond_{[d_1, d_2]}^f \varphi$$



(S, \vec{x}, ℓ, t) satisfies $\diamond_{[d_1, d_2]}^f \varphi$ iff there exists a location ℓ' reachable from ℓ , and a s.t. $d_S^f[\ell, \ell'] \in [d_1, d_2]$, that satisfies φ

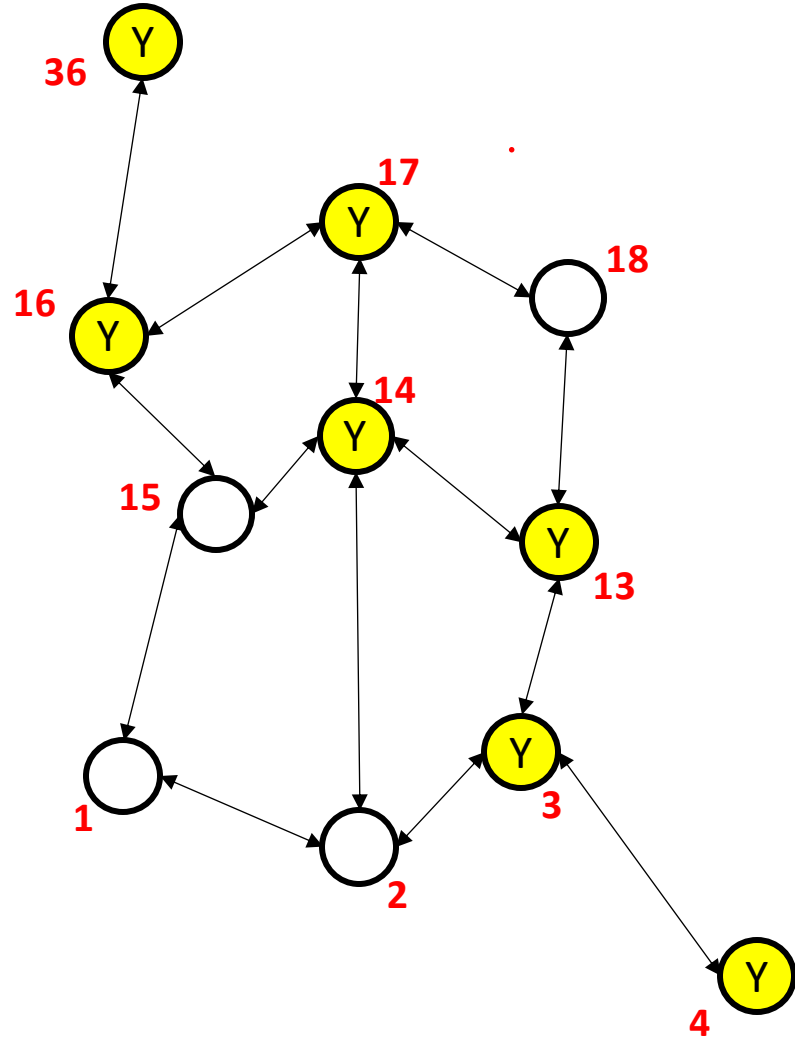
$$\diamond_{[3, 5]}^{hops} \textit{pink}$$

$$\tau[0] = \ell_1, \tau[k] = \ell_{35}$$

$$\tau = \ell_1 \dots \ell_{35}$$

$$d_{\tau}^{hops}(k) \in [3, 5]$$

Everywhere: $\square_{[d_1, d_2]}^f \varphi$



(S, \vec{x}, ℓ, t) satisfies $\square_{[d_1, d_2]}^f \varphi$ iff all the locations ℓ' reachable from ℓ via a path s.t. $d_S^f[\ell, \ell'] \in [d_1, d_2]$, satisfy φ

$\square_{[2, 3]}^{hops} yellow$

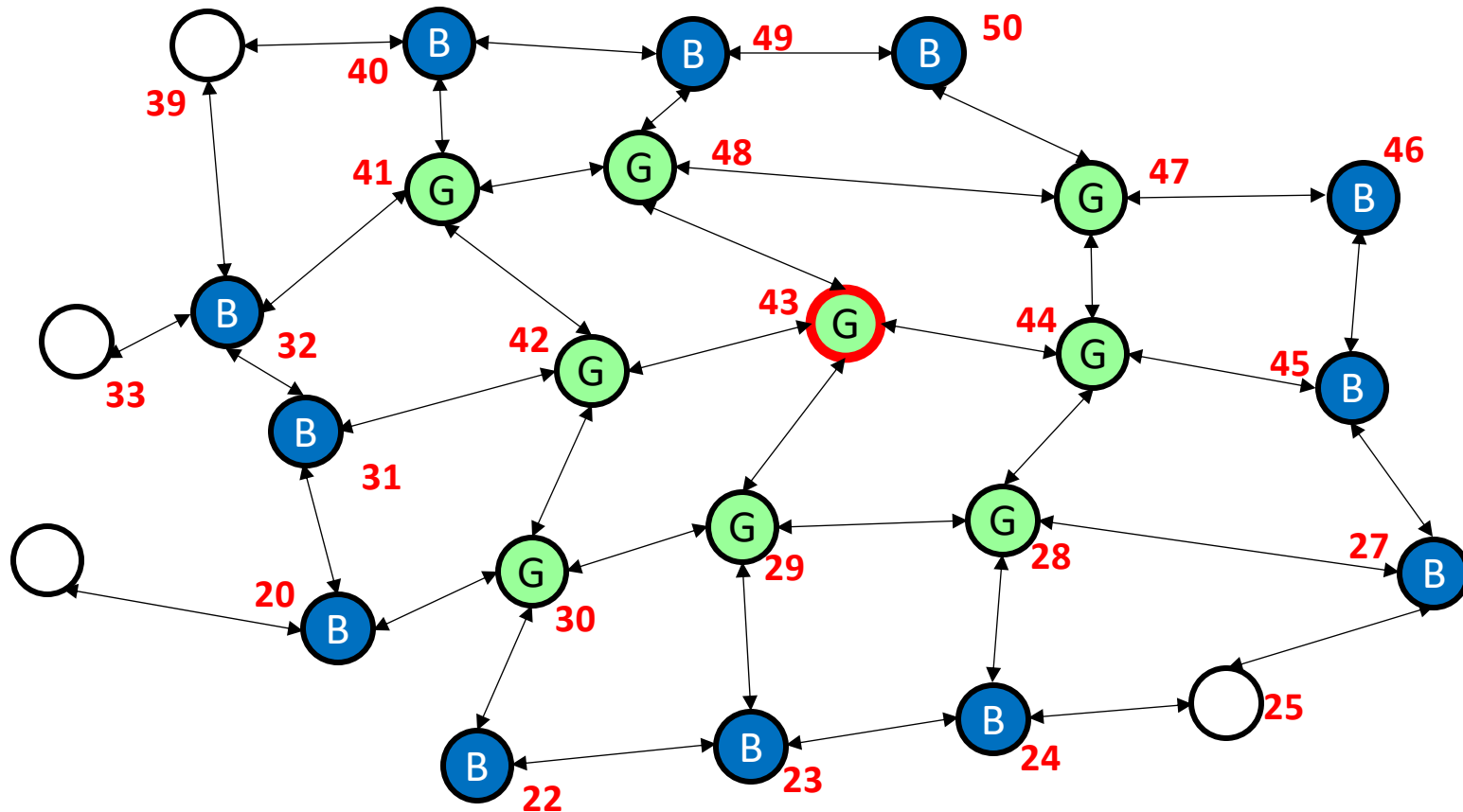
Surround:

$$\varphi_1 \odot_{[d_1, d_2]}^f \varphi_2$$

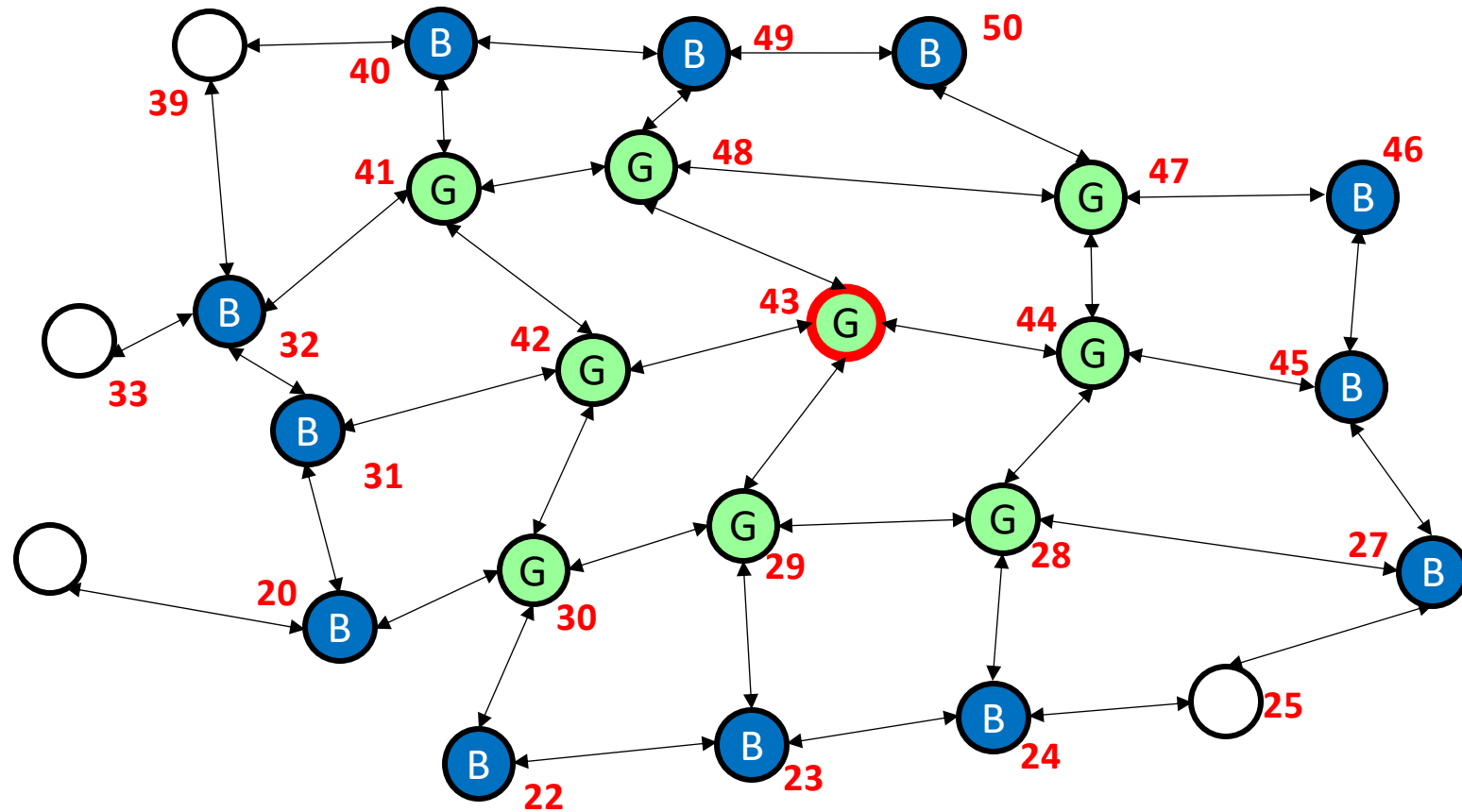
(S, \vec{x}, ℓ, t) iff there exists a φ_1 -region that contains ℓ , all locations in that region satisfies φ_1 and are reachable from ℓ via a path with length less than d_2 .

All the locations that do not belong to the φ_1 -region but are directly connected to a location of that region must satisfy φ_2 and be reached from ℓ via a path with length in the interval $[d_1, d_2]$.

Surround: *green* \odot ^{hops} $[0,100]$ *blue*



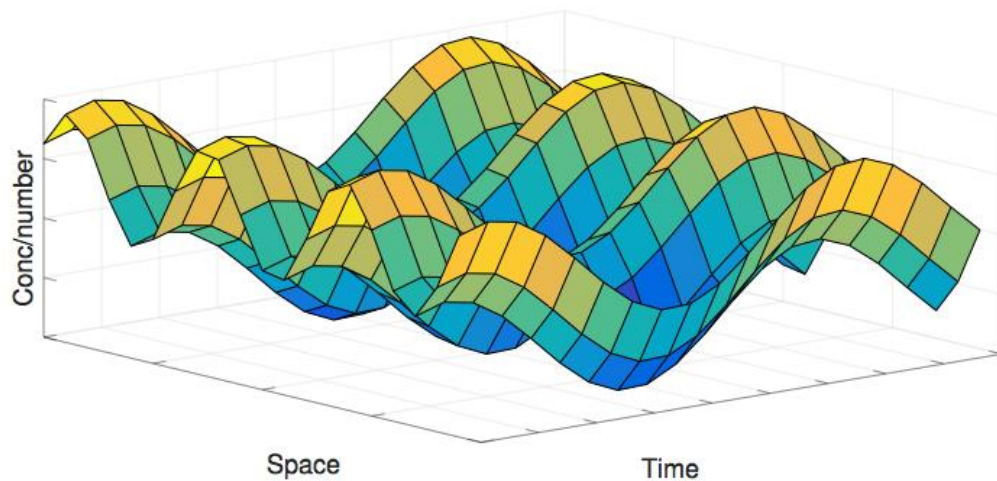
Surround: *green* \odot ^{hops} *blue*
[2,3]



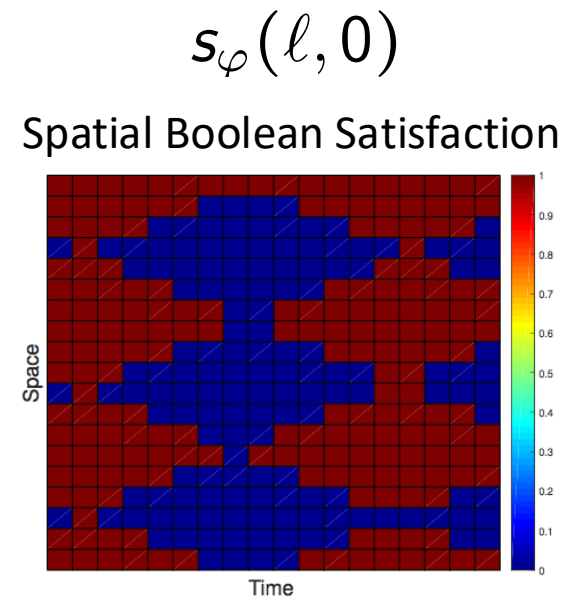
Offline Monitoring Algorithm

Spatial Boolean Signal

$s_\varphi : L \rightarrow [0, T] \rightarrow \{0, 1\}$ such that $s_\varphi(l, t) = 1 \Leftrightarrow (\mathcal{S}, \vec{x}, l, t) \models \varphi$



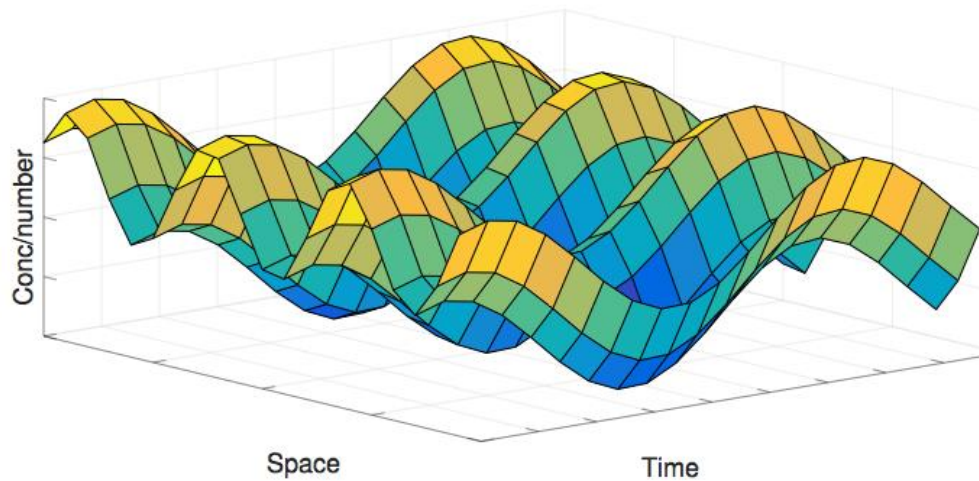
SSTL Monitor
Formula ϕ



Offline Monitoring Algorithm

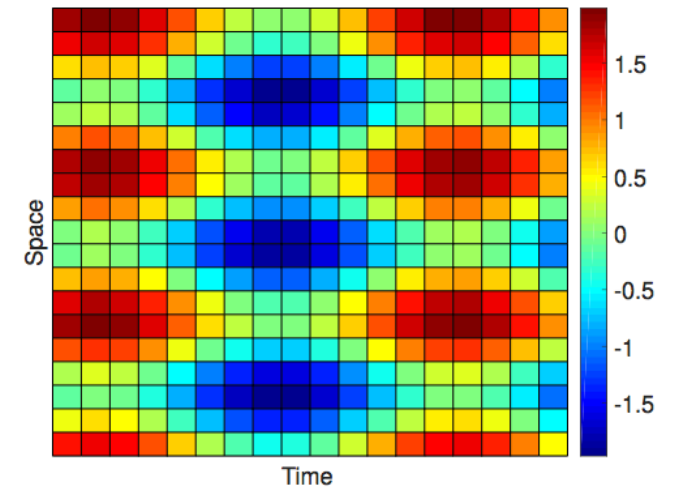
Spatial Quantitative Signal

$$\rho_\varphi : L \rightarrow [0, T] \rightarrow \mathbb{R} \cup \pm\infty \quad \text{such that} \quad \rho_\varphi(l, t) = \rho(\mathcal{S}, \vec{x}, l, t)$$



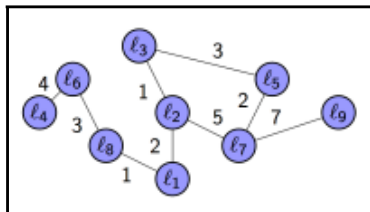
SSTL Monitor
Formula ϕ

$\rho_\varphi(l, 0)$
Spatial Quantitative Satisfaction

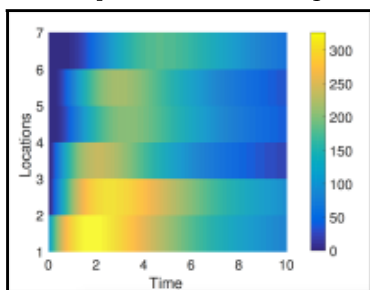


INPUTS

Spatial Configuration



Sp-Temporal Trajectory



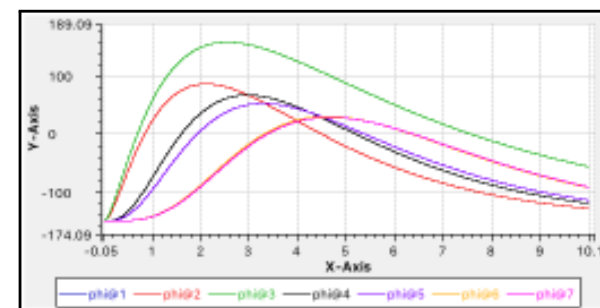
Specification

$$F_{[0, T]} \varphi_1 S_{[0, d]} \varphi_2$$

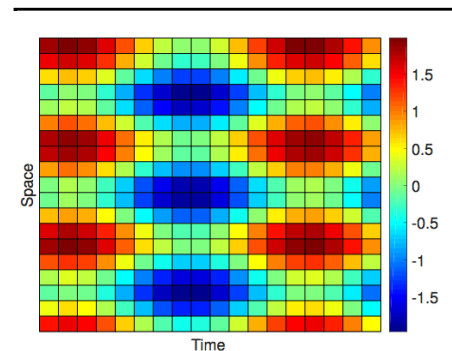
MONITORING
ALGORITHM

OUTPUTS

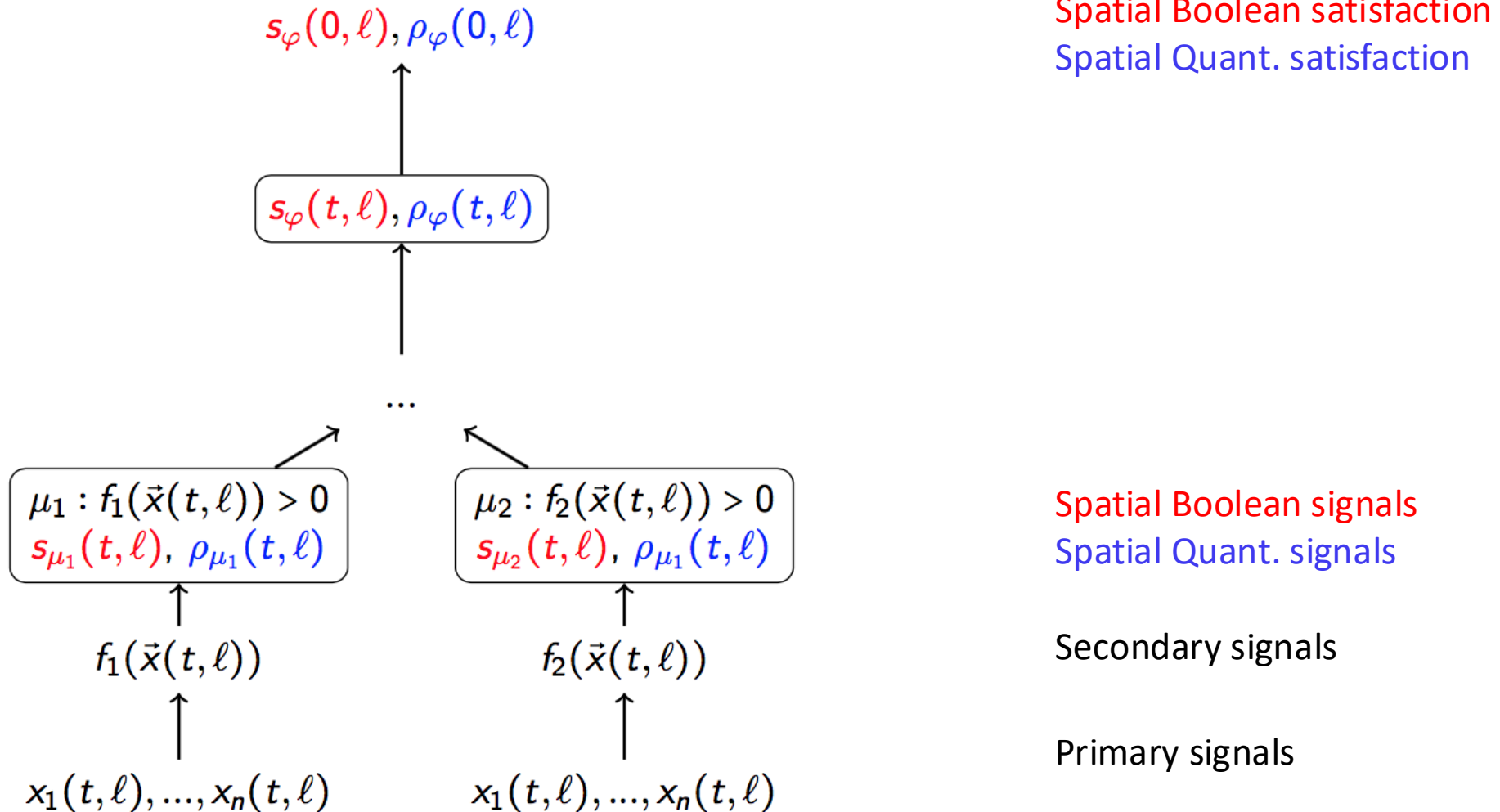
Sp-Temporal Satisfaction



Spatial Satisfaction



Offline Monitoring Algorithm



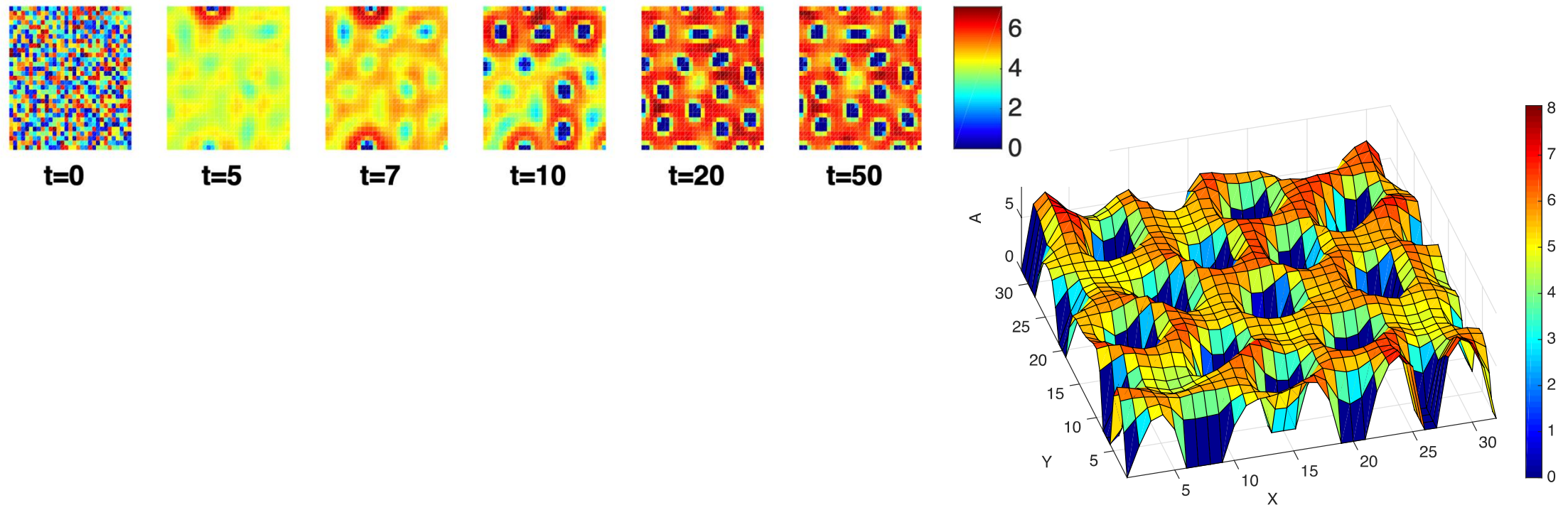
Computational consideration

- Temporal operators: like in STL monitoring [1] is **linear** in the length of the signal times the number of locations in the spatial model.
- Spatial properties are more expensive, they are based on a variations of the classical Floyd-Warshall algorithm.
The number of operations to perform is **quadratic** for the reach operator and **cubic** for the escape

Static Space and Regular Grid

The formation of Patterns

The production of skin pigments that generate spots in animal furs:

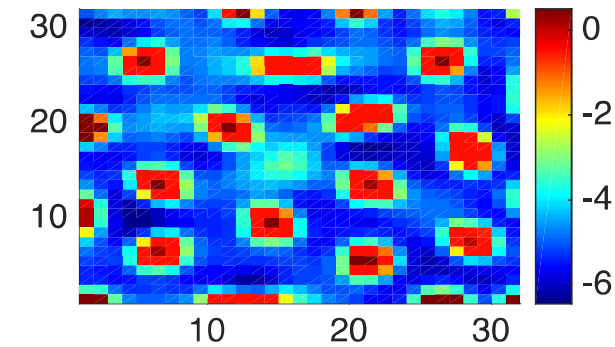
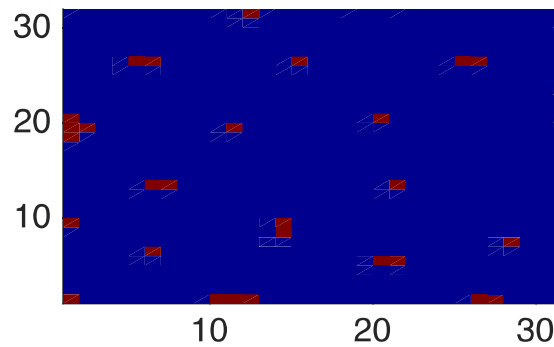
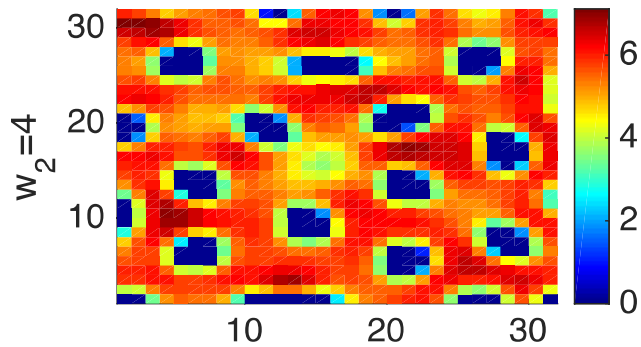
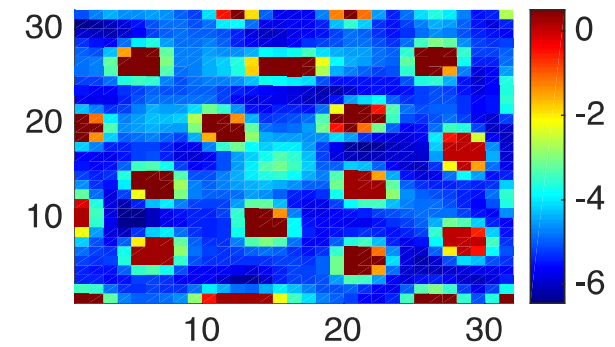
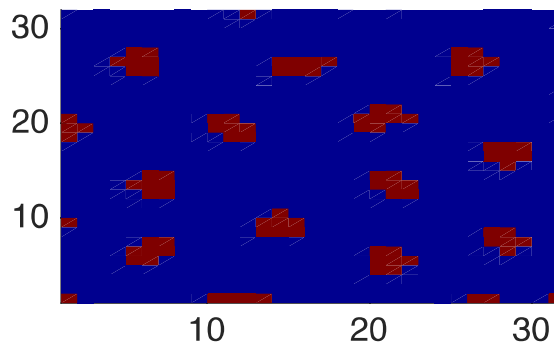
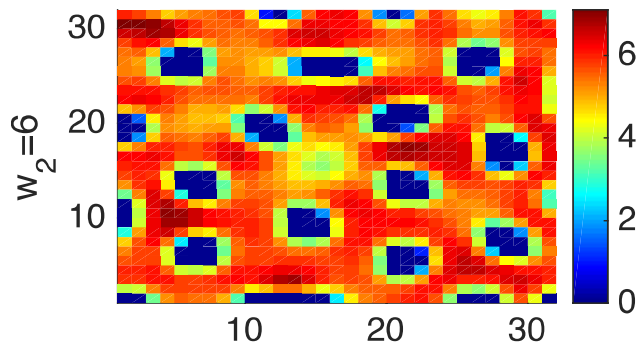


Space model: a $K \times K$ grid treated as a graph, $\text{cell}(i, j) \in L = \{1, \dots, K\} \times \{1, \dots, K\}$

Spatio-Temporal Trajectory: $x: L \rightarrow \mathbb{T} \rightarrow \mathbb{R}^2$ s.t. $x(\ell) = (x_A, x_B)$

Spot formation property

$$\phi_{spot_{form}} = F_{[19,20]} G((A \leq 0.5) \odot_{[1,w_2]}^{hops} (A > 0.5))$$



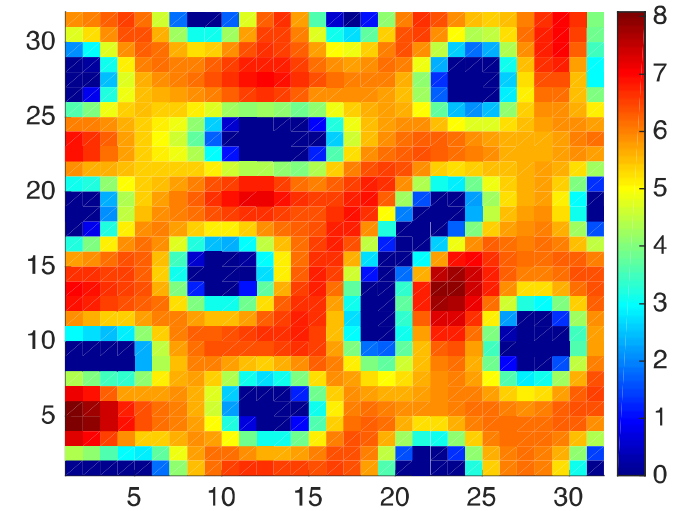
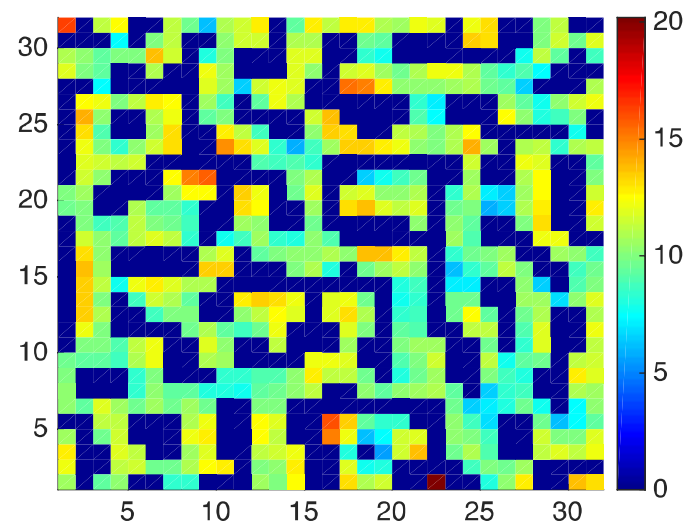
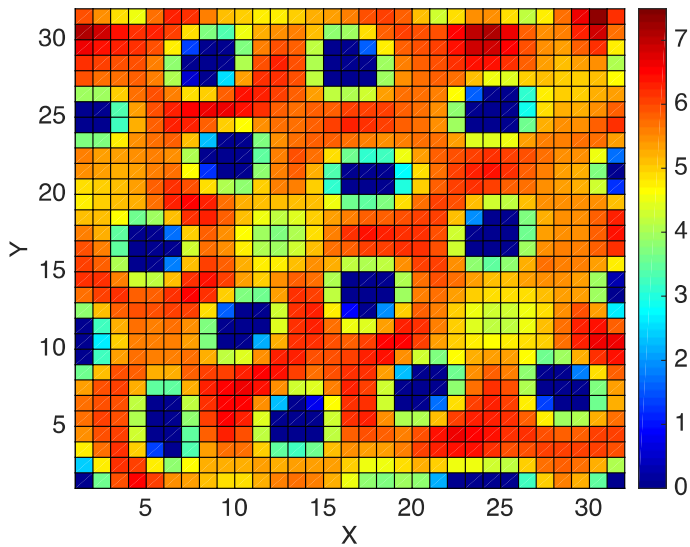
$x_A(50, l)$

Boolean sat.

Quantitative sat.

The formation of Patterns

$$\phi_{pattern} := \square^{hops} \diamond_{[0,15]}^{hops} \phi_{spot_{form}}$$

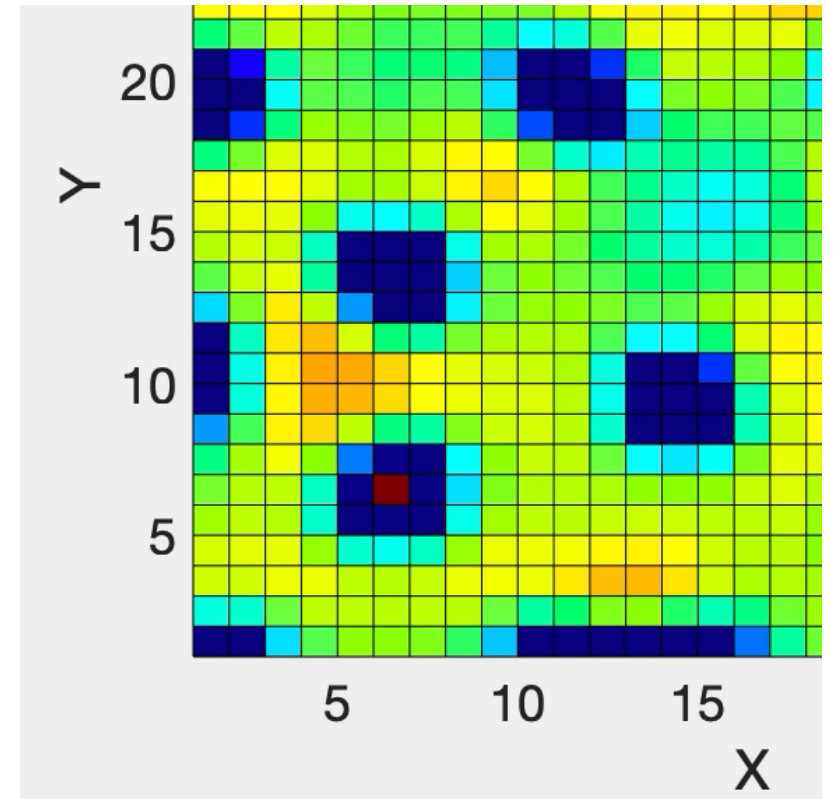


Perturbation Property

$$\phi_{\text{pert}} := (x_A \geq 10) \wedge (\phi_{\text{absorb}} \odot_{[1,2]}^{\text{hops}} \phi_{\text{no_effect}})$$

▶ $\phi_{\text{absorb}} = F_{[0,1]} G_{[0,10]} (x_A < 3)$;

▶ $\phi_{\text{noeffect}} := G_{[0,20]} (x_A < 3)$



Static Space and Stochastic Systems

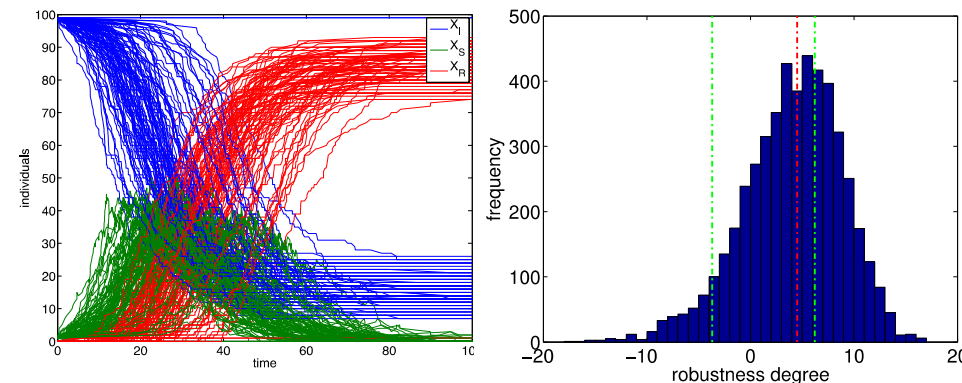
Application to Stochastic Systems

STREL can be applied on stochastic systems considering methodologies as Statistical Model Checking (SMC)

Stochastic process $\mathcal{M} = (\mathcal{T}, \mathcal{A}, \mu)$ where \mathcal{T} is a trajectory space and μ is a probability measure on a σ -algebra of \mathcal{T}

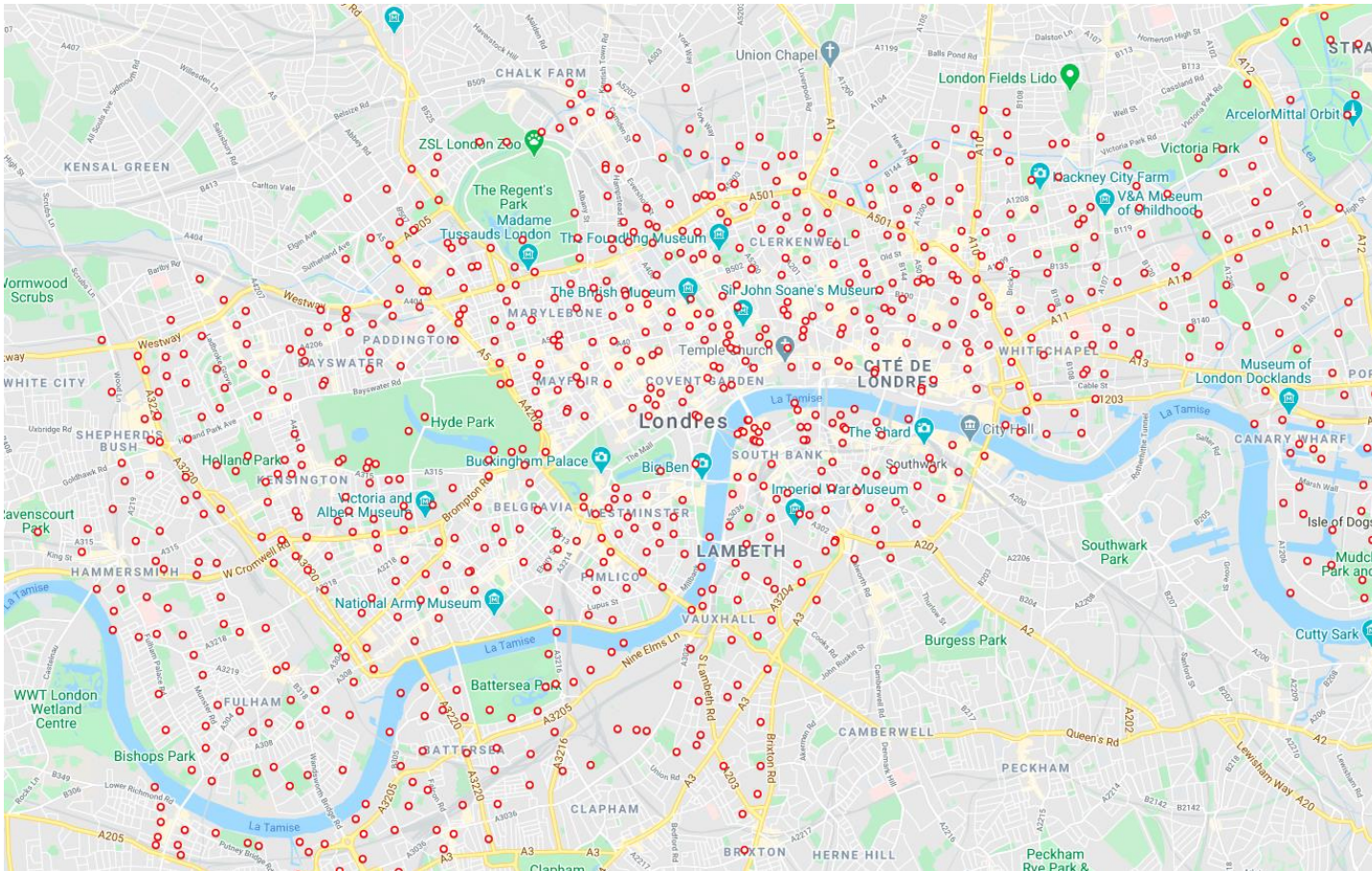
We approximate the satisfaction probability $S(\varphi, t)$, i.e. the probability that a trajectory generated by the stochastic process \mathcal{M} satisfies the formula φ .

We can do something similar with the quantitative semantics computing the robustness distribution



Bike Sharing Systems (BSS)

London Santander Cycles Hire network



- 733 bike stations (each with 20-40 slots)
- a total population of 57,713 agents (users) picking up and returning bikes

We model it as a Population Continuous Time Markov Chain (PCTMC) with time-dependent rates, using historic journey and bike availability data.

Prediction for 40 minutes.

Bike Sharing Systems (BSS)

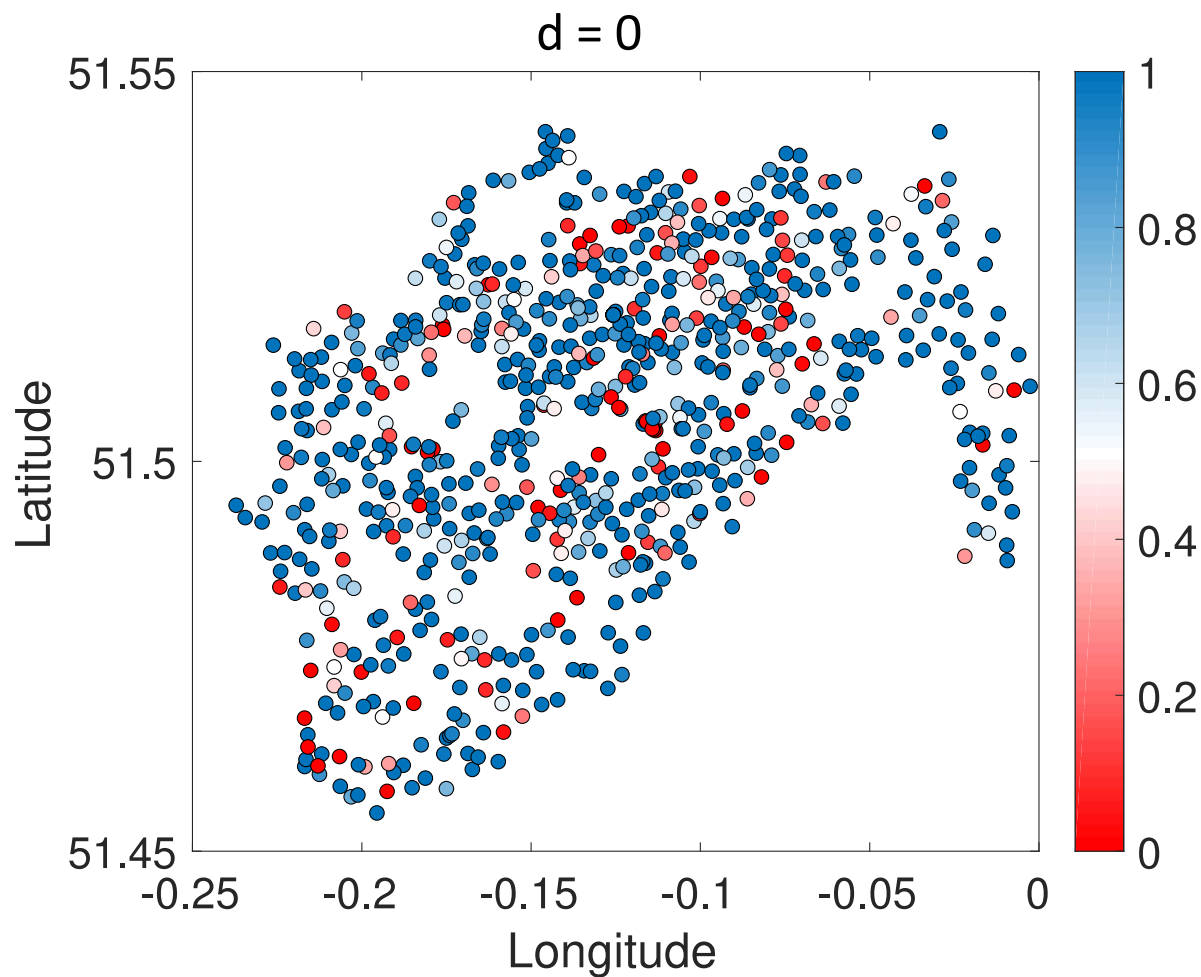
Spatio-Temporal Trajectory: $x: L \times \mathbb{T} \rightarrow \mathbb{Z}^2$ s.t. $x(i, t) = (B_i(t), S_i(t))$

Space model

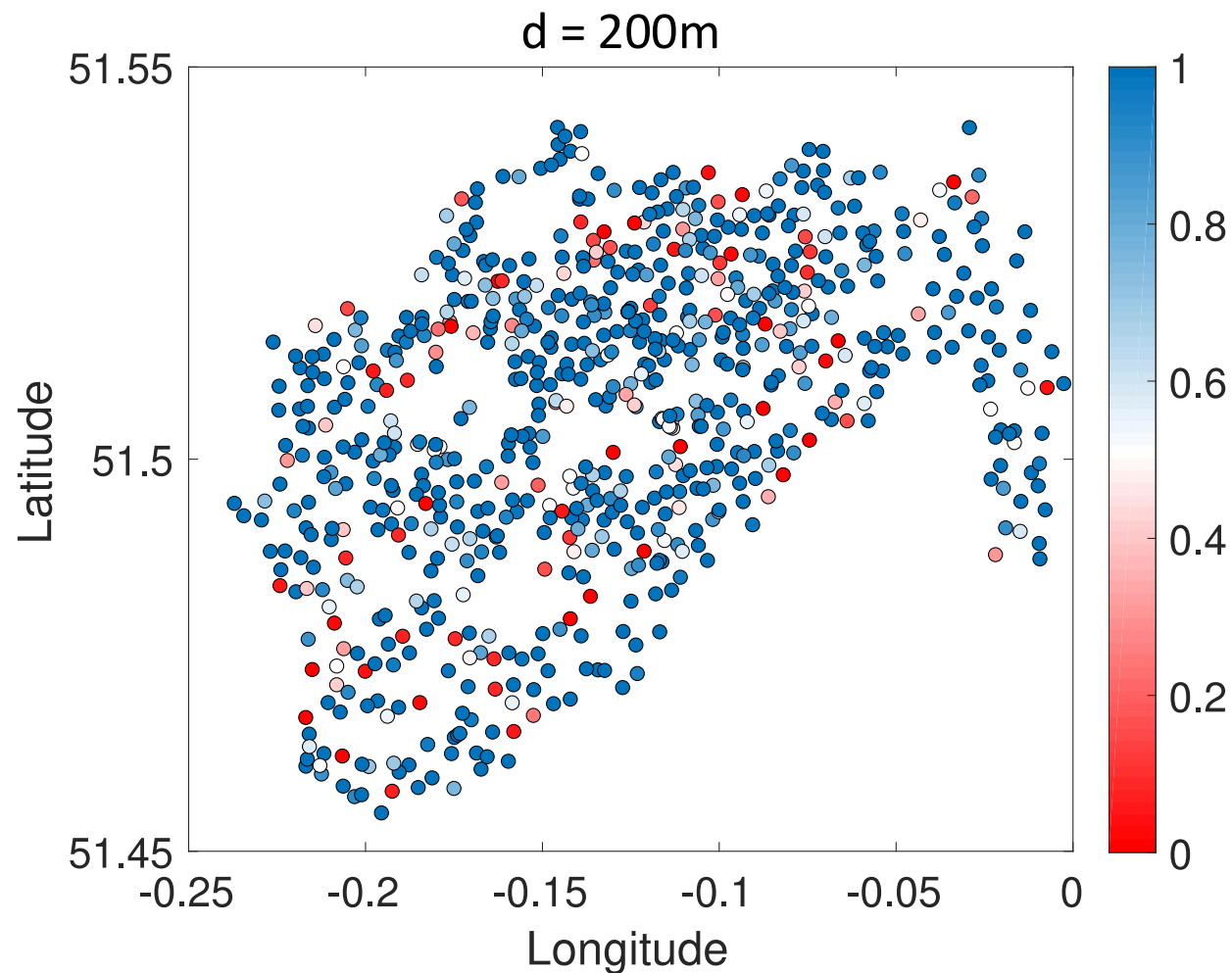
- Locations: $L = \{\text{bike stations}\}$,
- Edges: $(\ell_i, w, \ell_j) \in W$ iff $w = \|\ell_i - \ell_j\| < 1 \text{ kilometer}$

Availability of Bikes

$$\phi_1 = G \{ \diamond_{[0,d]}^{weight} (B > 0) \wedge \diamond_{[0,d]}^{weight} (S > 0) \}$$



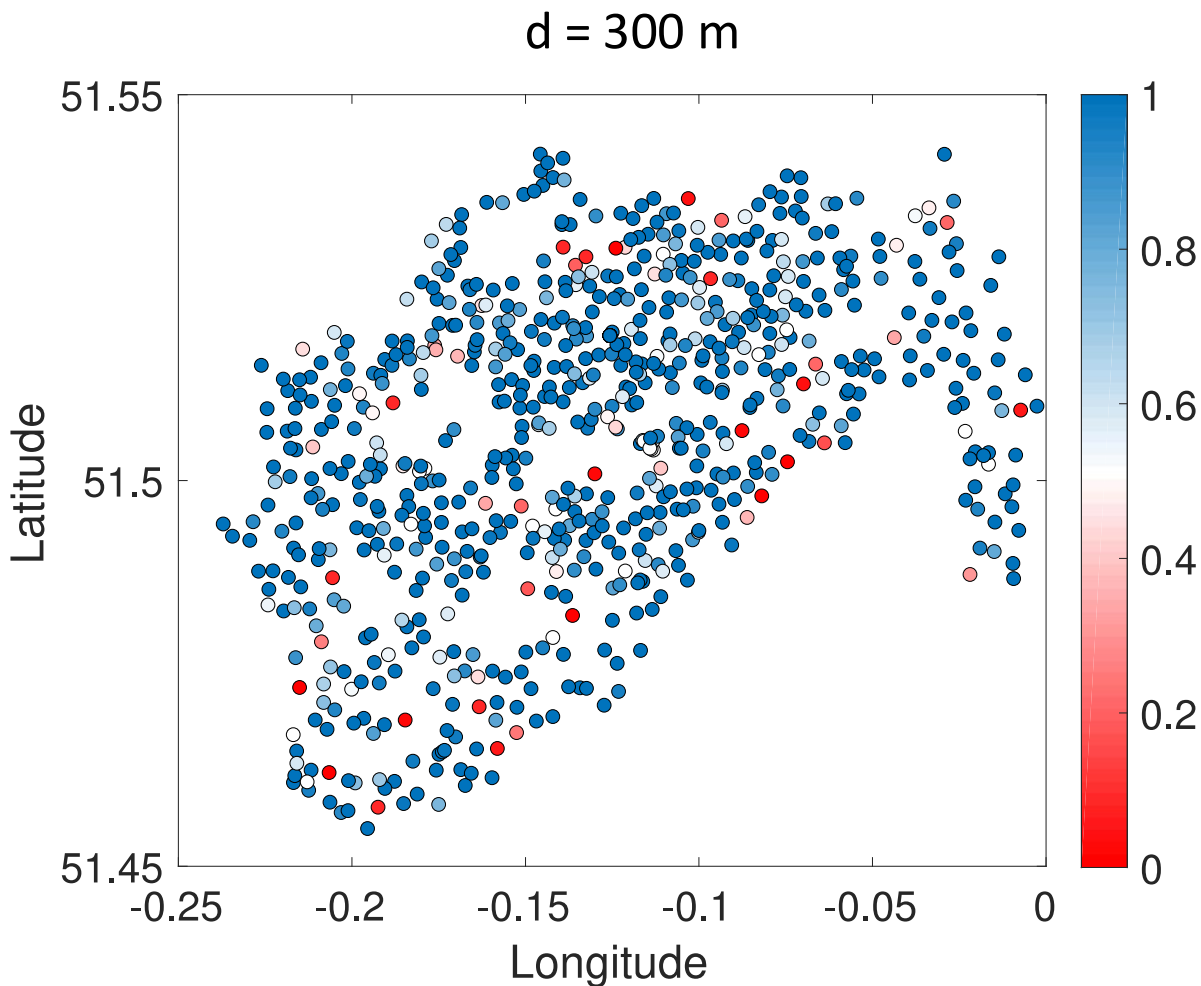
std in $[0, 0.0158]$, mean std = 0.0053.



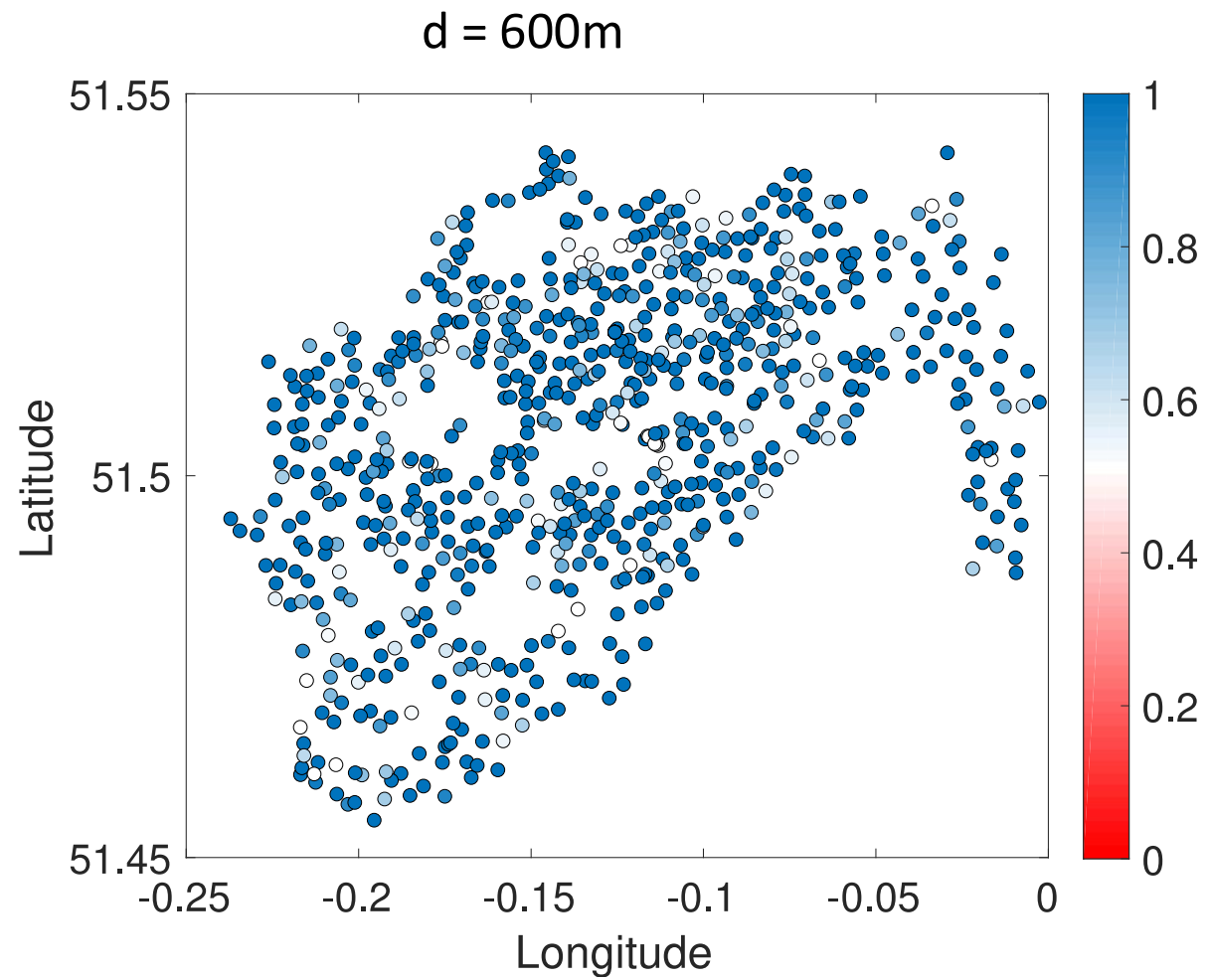
std in $[0, 0.0158]$, mean std = 0.0039.

Availability of Bikes

$$\phi_1 = G \{ \diamond_{[0,d]}^{weight} (B > 0) \wedge \diamond_{[0,d]}^{weight} (S > 0) \}$$



std in $[0, 0.0151]$, mean std = 0.0015.



std in $[0, 0.0142]$, mean std = 0.0002.

Bike Sharing Systems (BSS)

$$\psi_1 = G \left\{ \diamond_{[0,d]}^{weight} \left(F_{[t_w,t_w]} B > 0 \right) \wedge \diamond_{[0,d]}^{weight} \left(F_{[t_w,t_w]} S > 0 \right) \right\}$$

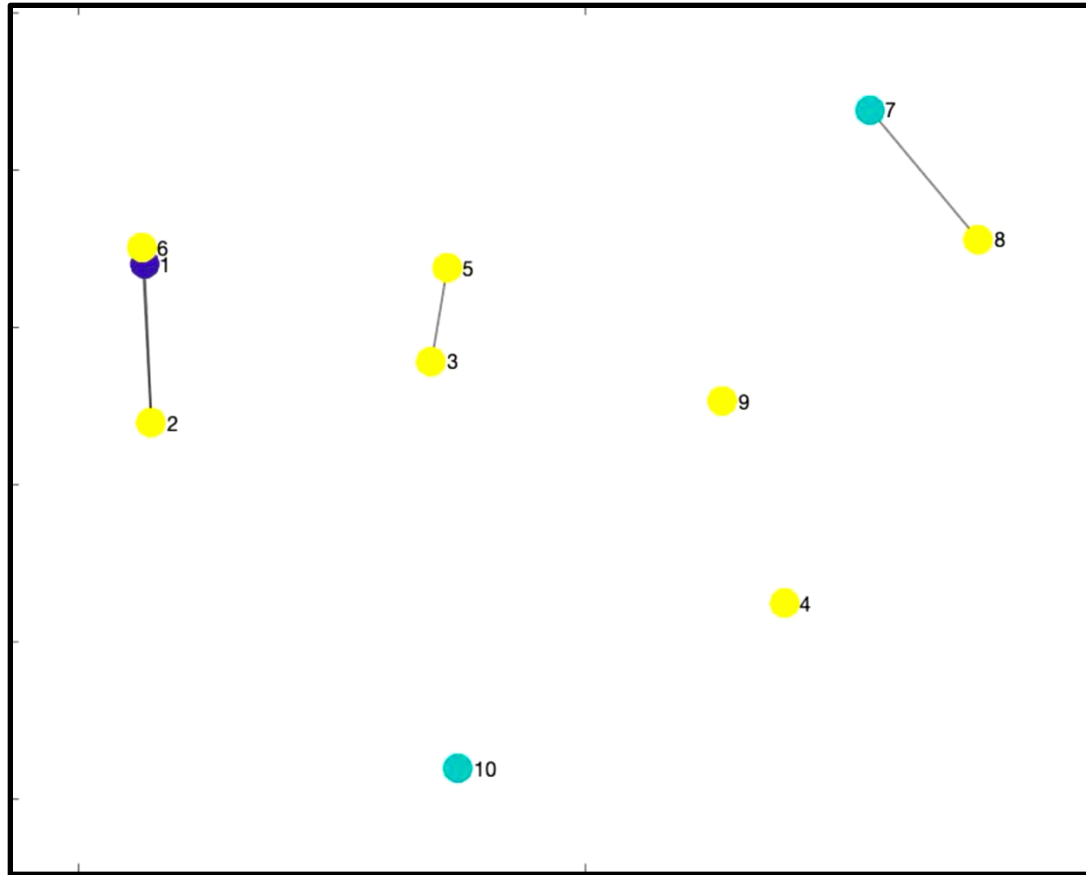
Average walking speed of 6.0 km/h, e.g. $d = 0.5$ km $\rightarrow t_w = 6$ minutes

The results similar to the results of previous property

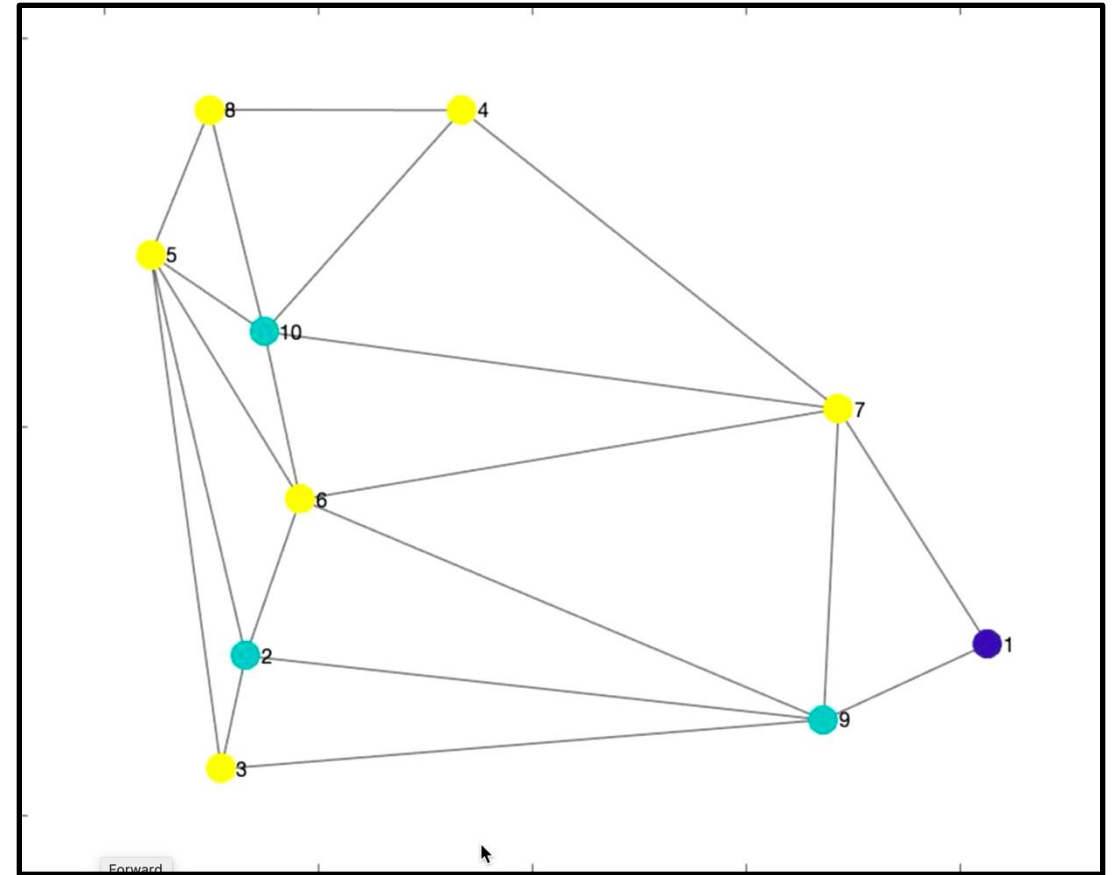
Dynamic Space

Mobile Ad-hoc sensor NETWORK (MANET)

Coordinator ● Router ● End-devices ●



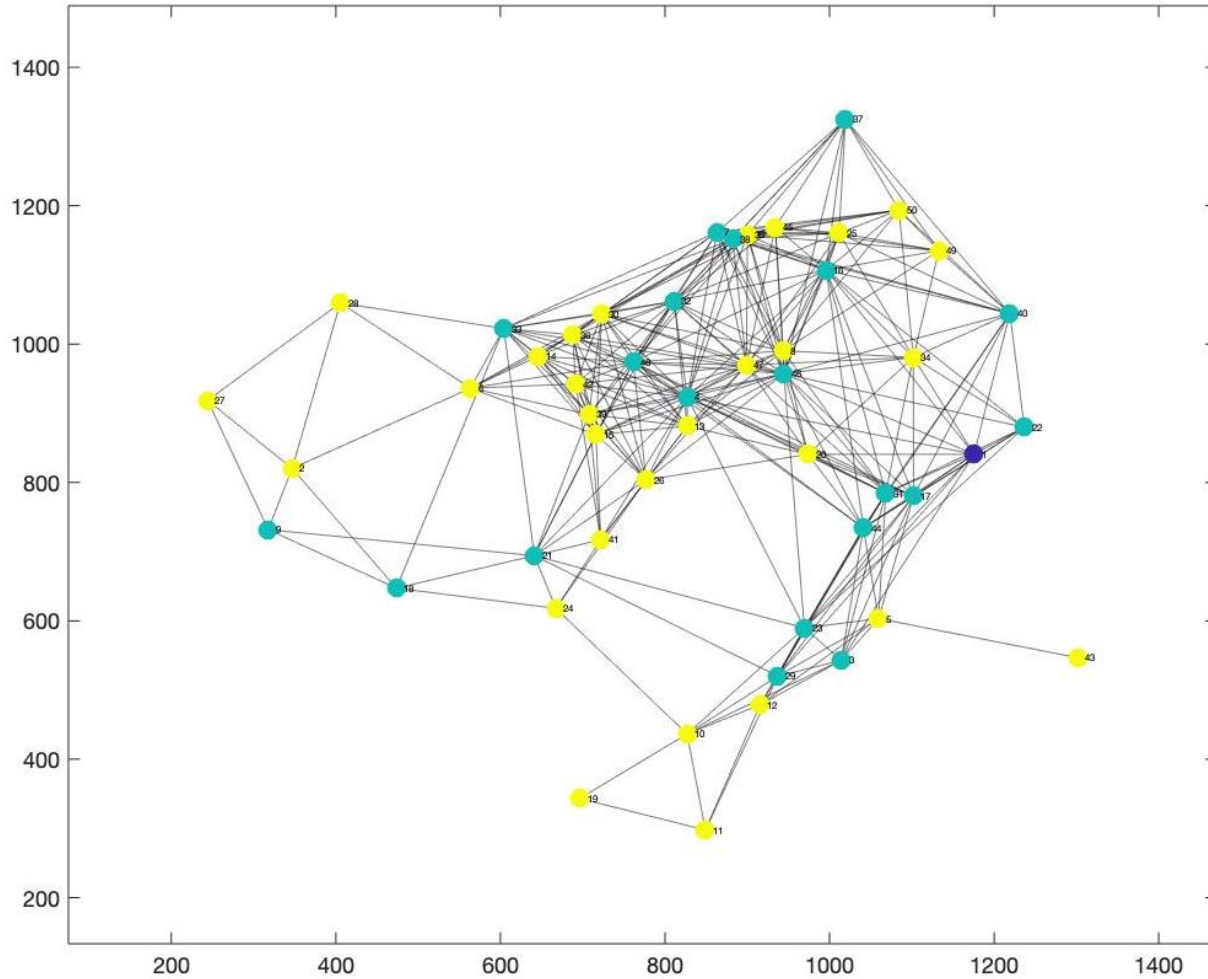
Connectivity Graph



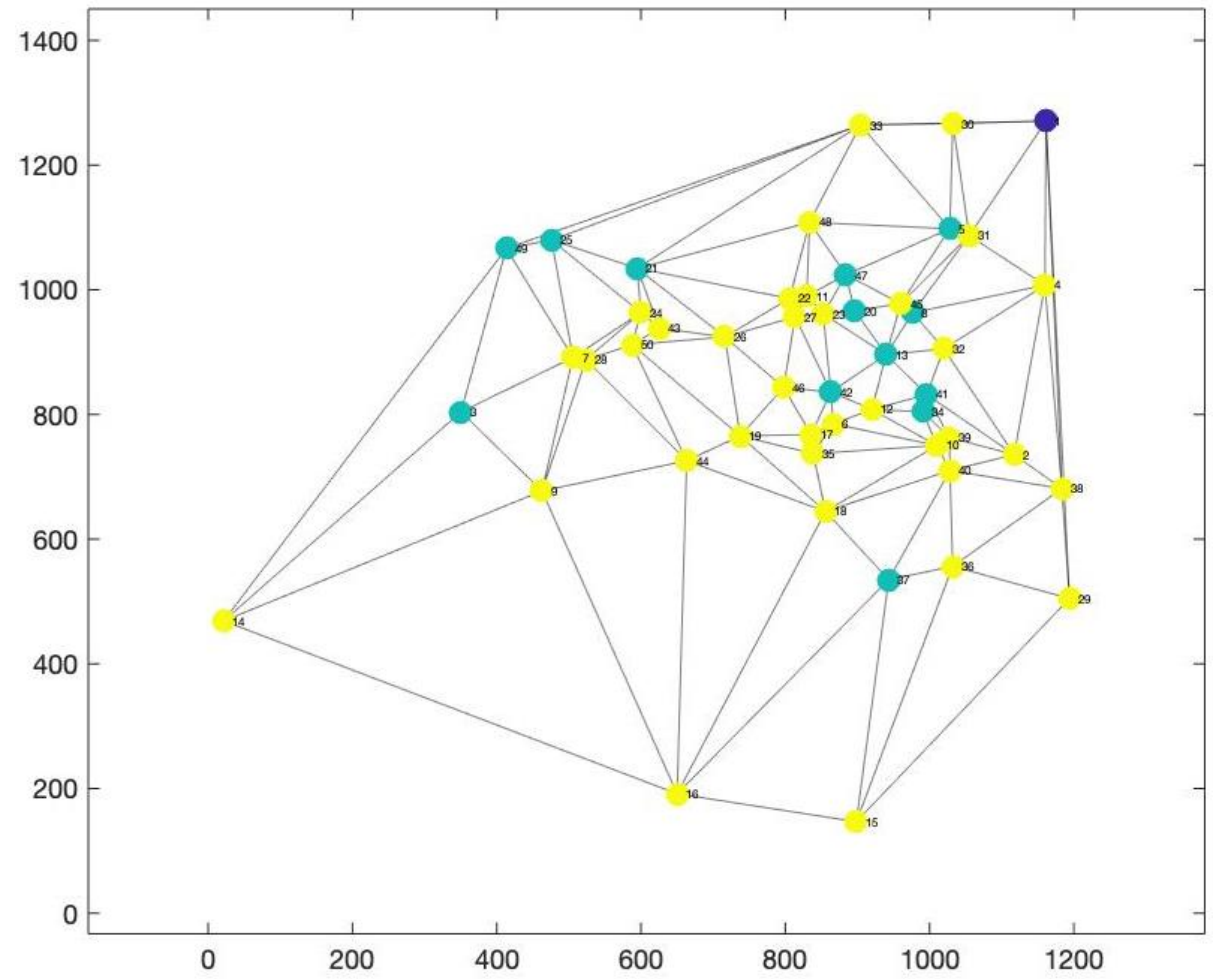
Proximity Graph

Mobile Ad-hoc sensor NETWORK (MANET)

Coordinator ● Router ● End-devices ●



Connectivity Graph



Proximity Graph

Mobile Ad-hoc sensor NETWORK (MANET)

Space model $S(t)$

- Locations: $L = \{devices\}$,
- Edges: $(\ell_i, w, \ell_j) \in W$ iff $w = \|\ell_i - \ell_j\| < \min(r_i, r_j)$

Spatio-Temporal Trajectory: $x: L \times \mathbb{T} \rightarrow \mathbb{Z} \times \mathbb{R}^2$ s.t.

$x(i, t) = (nodeType, battery, temperature)$

$nodeType = 1, 2, 3$ for coordinator, router, and end_device

Connectivity in a MANET

“an end device is either connected to the coordinator or can reach it via a chain of routers”

“broken connection is restored within h time units”

Connectivity in a MANET

“an end device is either connected to the coordinator or can reach it via a chain of routers”

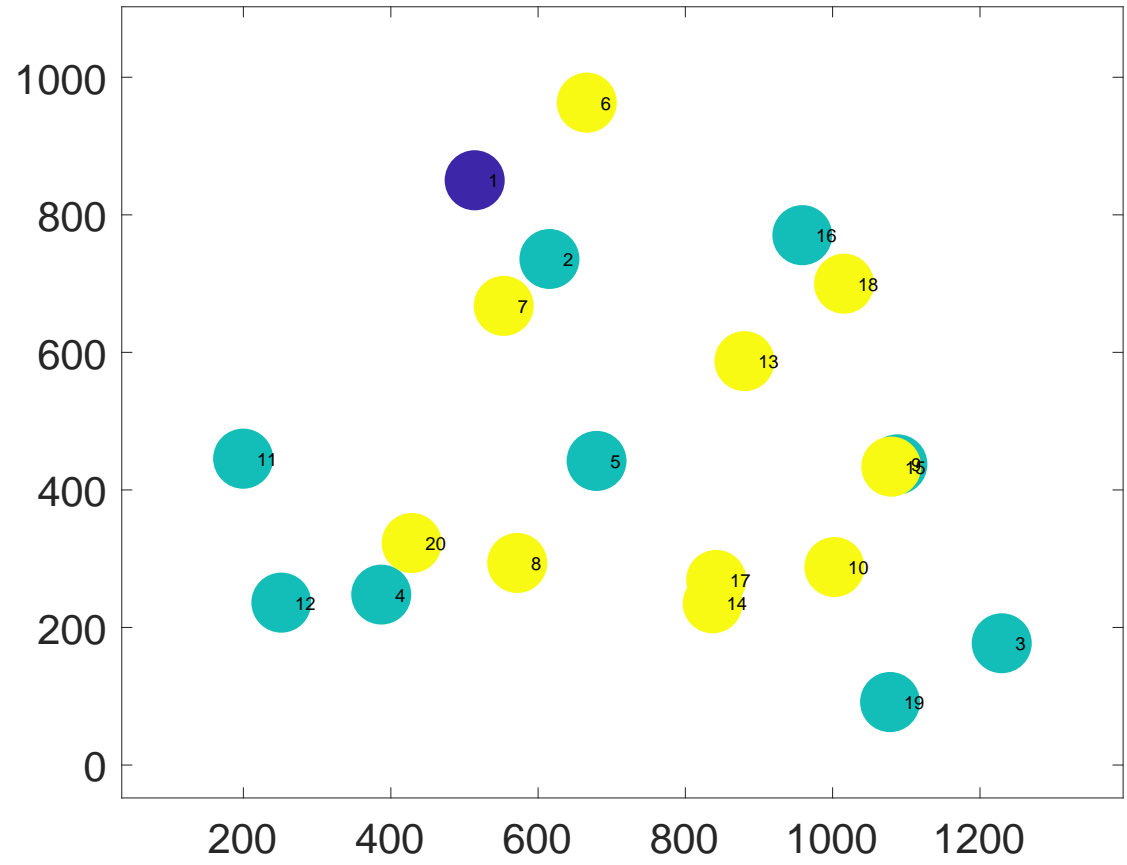
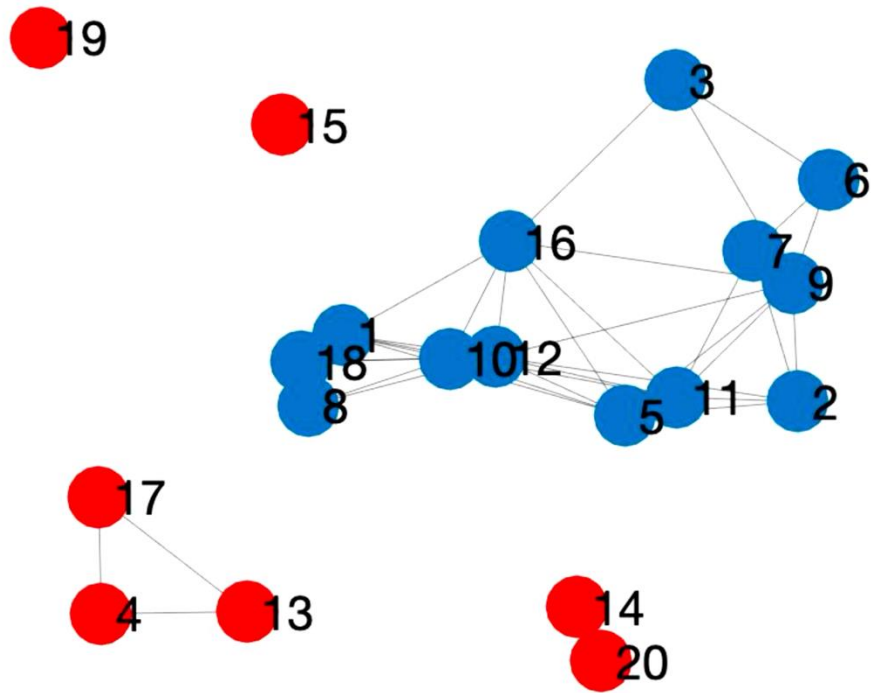
$$\phi_{connect} = device \mathcal{R}_{[0,1]}^{hop} (router \mathcal{R}^{hop} coord)$$

“broken connection is restored within h time units”

$$\phi_{connect_restore} = G(\neg \phi_{connect} \rightarrow F_{[0,h]} \phi_{connect})$$

Boolean Satisfaction at each time step

$$\phi_{connect} = device \mathcal{R}_{[0,1]}^{hop} (router \mathcal{R}^{hop} coord)$$



Delivery in a MANET

“from a given location, we can find a path of (hops) length at least 5 such that all nodes along the path have a battery level greater than 0.5”

$$\psi_3 = \mathcal{E}_{[5, \infty]}^{hops} (battery > 0.5)$$

Reliability in a MANET

“reliability in terms of battery levels, e.g. battery level above 0.5

$$\phi_{\text{reliable_router}} = ((\text{battery} > 0.5) \wedge \text{router}) \mathcal{R}^{\text{hop}} \text{coord}$$

$$\phi_{\text{reliable_connect}} = \text{device} \mathcal{R}_{[0,1]}^{\text{hop}} (\phi_{\text{reliable_router}})$$

Moonlight: <https://github.com/MoonLightSuite/MoonLight/wiki>

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Home

Simone edited this page on 1 Jul · 30 revisions

MoonLight build passing codecov 39%

MoonLight is a light-weight Java-tool for monitoring temporal, spatial and spatio-temporal properties of distributed complex systems, as *Cyber-Physical Systems* and *Collective Adaptive Systems*.

It supports the specification of properties written with the *Reach and Escape Logic* (STREL). STREL is a linear-time temporal logic, in particular, it extends the *Signal Temporal Logic* (STL) with a number of spatial operators that permit to described complex spatial behaviors as being surround, reaching target locations, and escaping from specific regions.

MoonLight is implemented in Java, but it features also a [MATLAB](#) interface that allows the monitoring of spatio-temporal signals generated within the MATLAB framework. A [Python](#) Interface is under development.

Getting Started

First, you need to download JAVA (version 8) and set the environmental variable

```
JAVA_HOME= path to JAVA home directory
```

Then you need to get or generate the executable for Python or MATLAB.

First, you need to clone our repository

```
$ git clone https://github.com/MoonLightSuite/MoonLight.git
```

or download it ([link](#)).

Then you need to compile it by executing the following Gradle tasks in the console

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- [Script Syntax](#)
- [Matlab](#)
 - [Installation](#)
 - [Getting Started](#)
- [Python](#)
- [License](#)

Clone this wiki locally

<https://github.com/MoonLightSuite/MoonLight/wiki>

```
1      (atomicExpression)
2      | ! Formula
3      | Formula & Formula
4      | Formula | Formula
5      | Formula -> Formula
6      | Formula until [a b] Formula
7      | Formula since [a b] Formula
8      | eventually [a b] Formula
9      | globally [a b] Formula
10     | once [a b] Formula
11     | historically [a b] Formula
12     | escape(distanceExpression)[a b] Formula
13     | Formula reach (distanceExpression)[a b] Formula
14     | somewhere(distanceExpression) [a b] Formula
15     | everywhere (distanceExpression) [a b] Formula
16     | {Formula}
```

Bibliography

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- ▶ Jin, Deshmukh et al. Mining Requirements from Closed-loop Control Models (HSCC '13, IEEE Trans. On Computer Aided Design '15)
- ▶ Bartocci, E., Bortolussi, L., Sanguinetti, G.: Data-driven statistical learning of temporal logic properties, *FORMATS*, 2014
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