

How can you make these reactions happen?

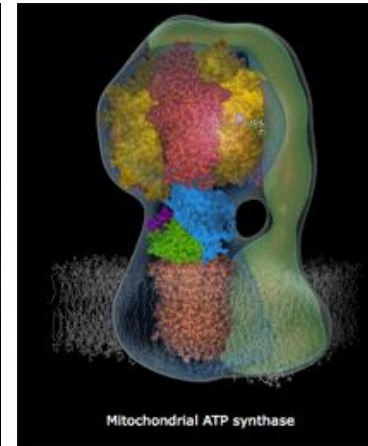
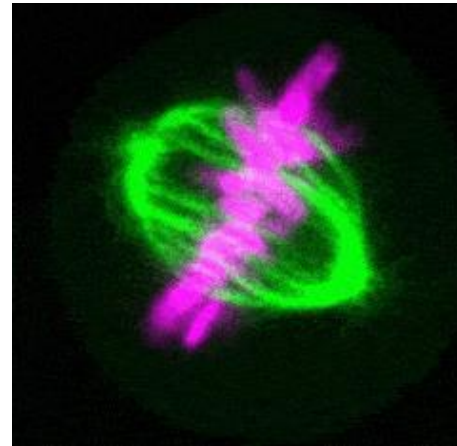
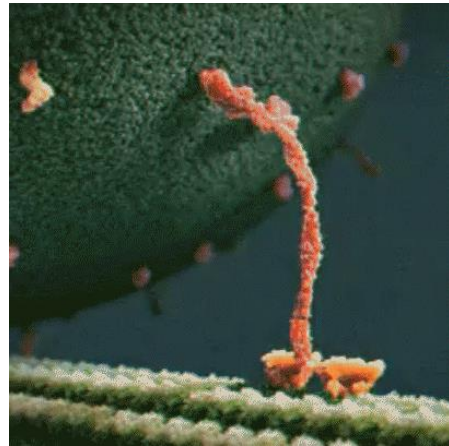
# Chemically-driven non-equilibrium systems

Transient systems  
(may NOT absorb energy)

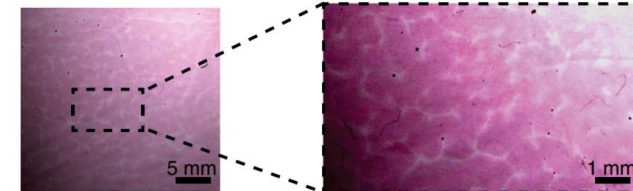
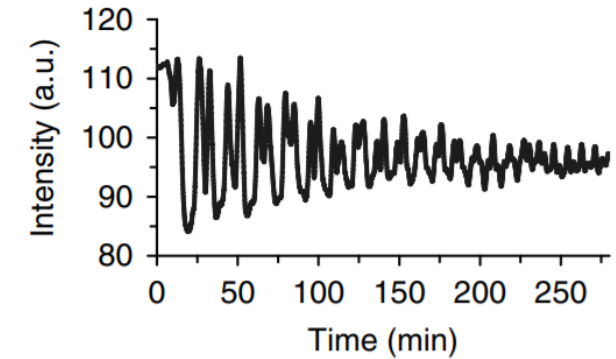


Kinetic  
asymmetry

Driven systems  
(DO absorb energy)



Oscillating systems  
(DO absorb energy & are synchronized)



Bifurcation

Do not forget the big picture: alternating conditions, light, spatial differentiation..

# Notation used to describe these phenomena

Often used as interchangeable in this context:

F = Fuel or S = Substrate

W = Waste or P = Product

M = Monomer/Machine or C = Catalyst (or E = Enzyme)

M' or C' = other conformation of Monomer/Machine and Catalyst

[in some cases: M = L, M' = H, M\* = L']

S•C or F•M or M\* or P•C

= Substrate-Catalyst complex, Fuel-Monomer/Fuel-Machine complex, activated Monomer, Product-Catalyst complex (sometimes indicated as «bound state»)

M<sub>2</sub> or A<sub>2</sub> = Dimer or Aggregate of M

M\*<sub>2</sub> or A\*<sub>2</sub> = Dimer or Aggregate of M\*

S + C



S•C



P + C

Standard enzymatic catalysis

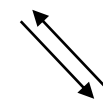
F + M



M\*



W + M



A\*<sub>2</sub>

Example of transient assembly

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W = Waste or P = Product

M = Monomer/Machine or C = Catalyst (or E = Enzyme)

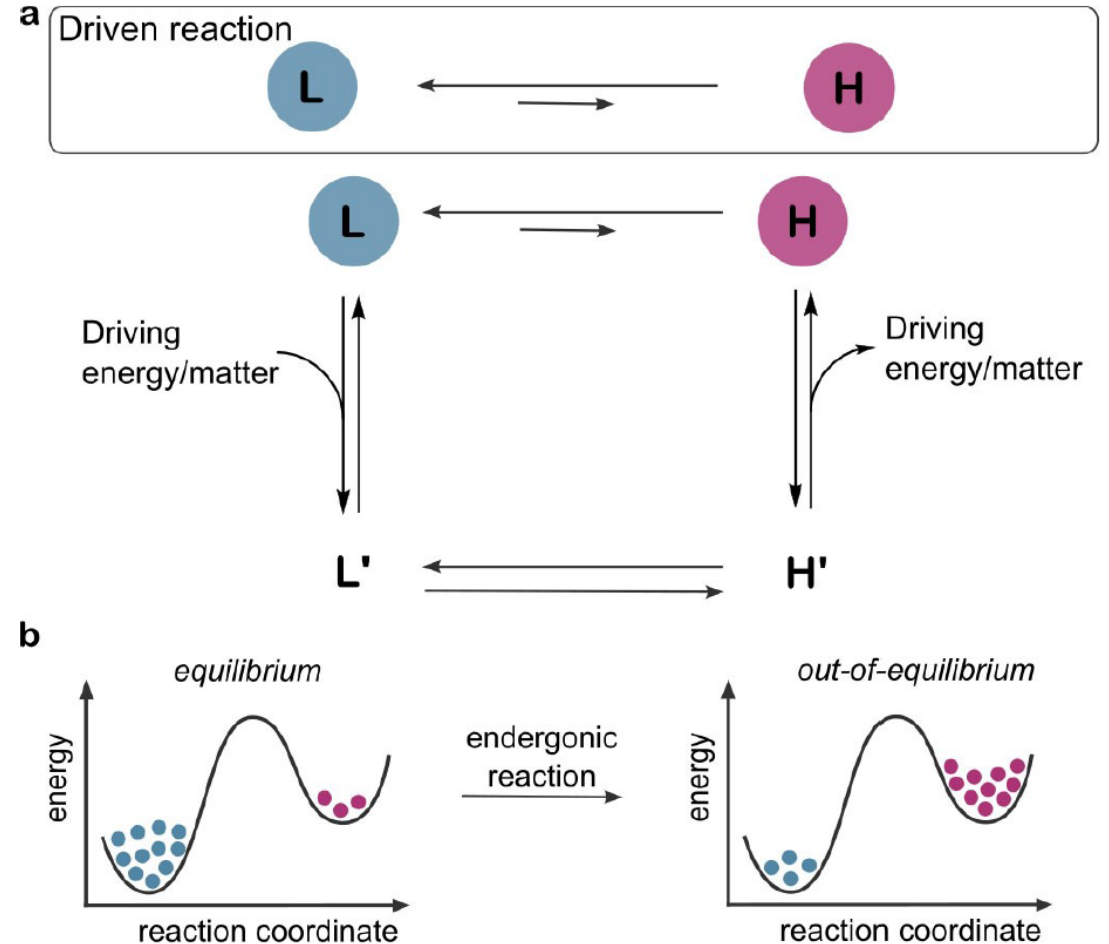
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[in some cases: M = L, M' = H, M\* = L']

S•C or F•M or M\* or P•C

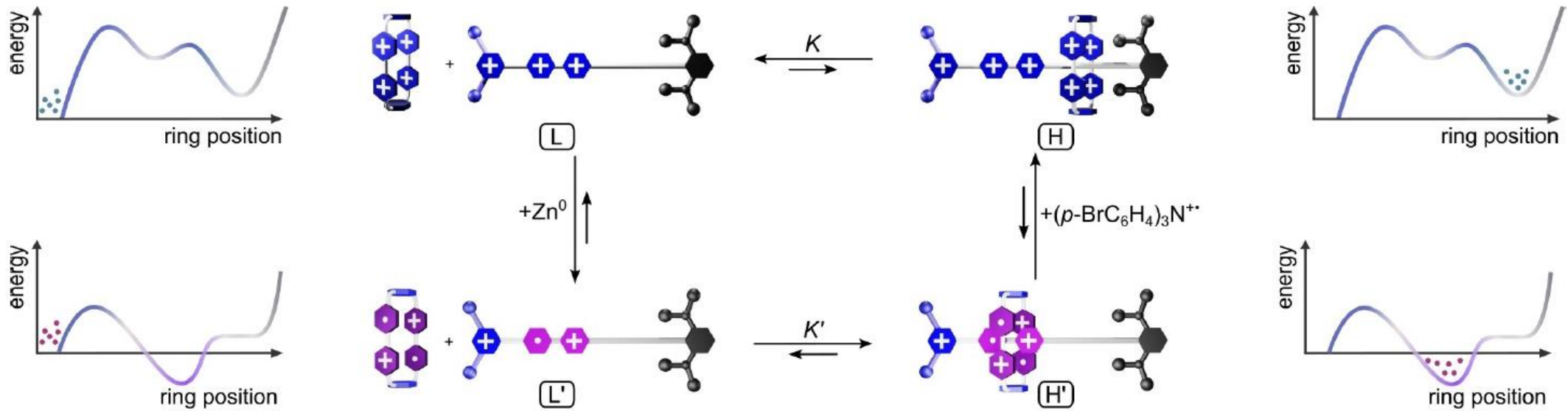
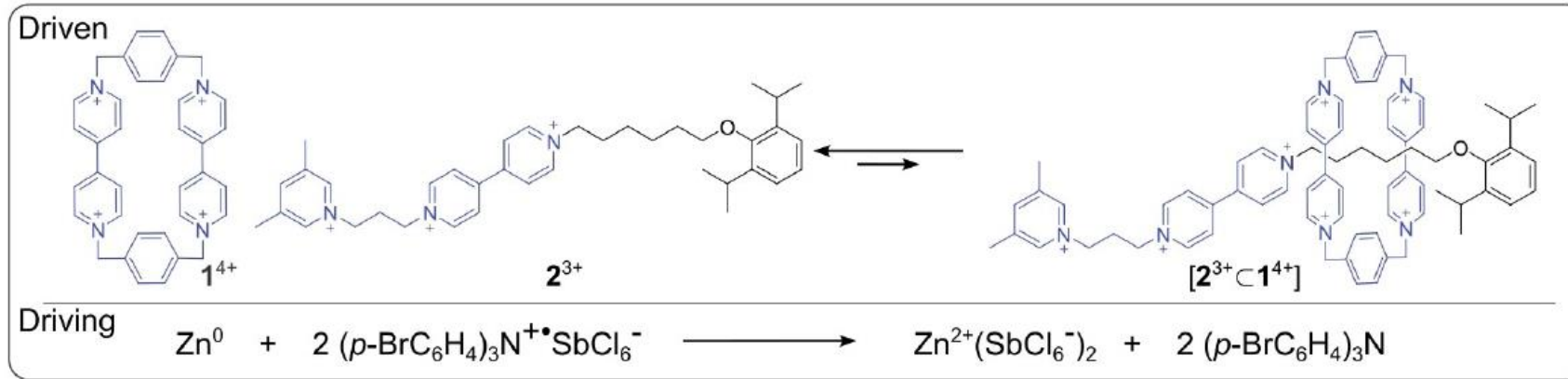
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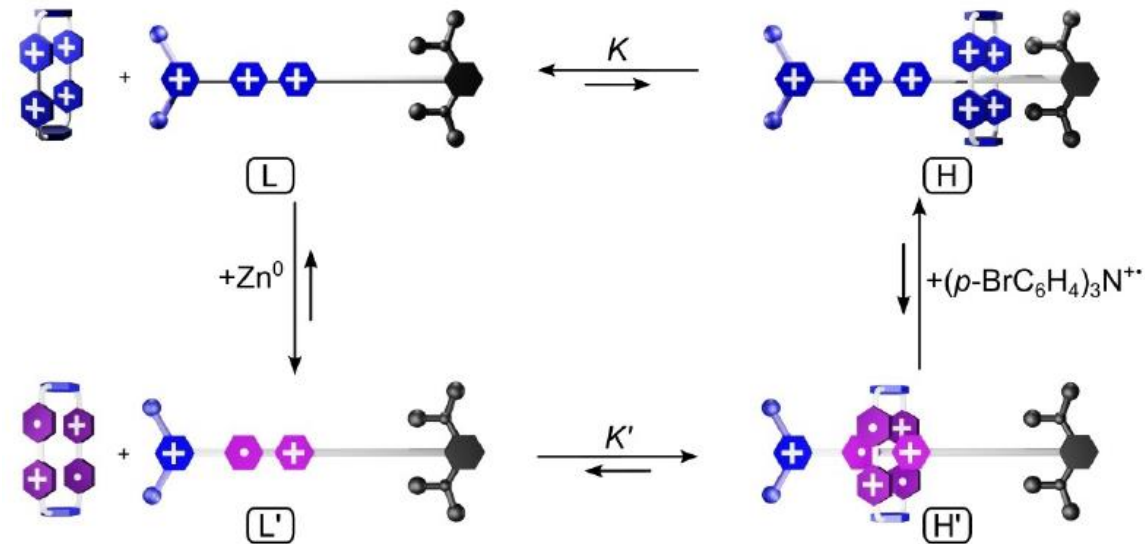


# Alternating conditions: example

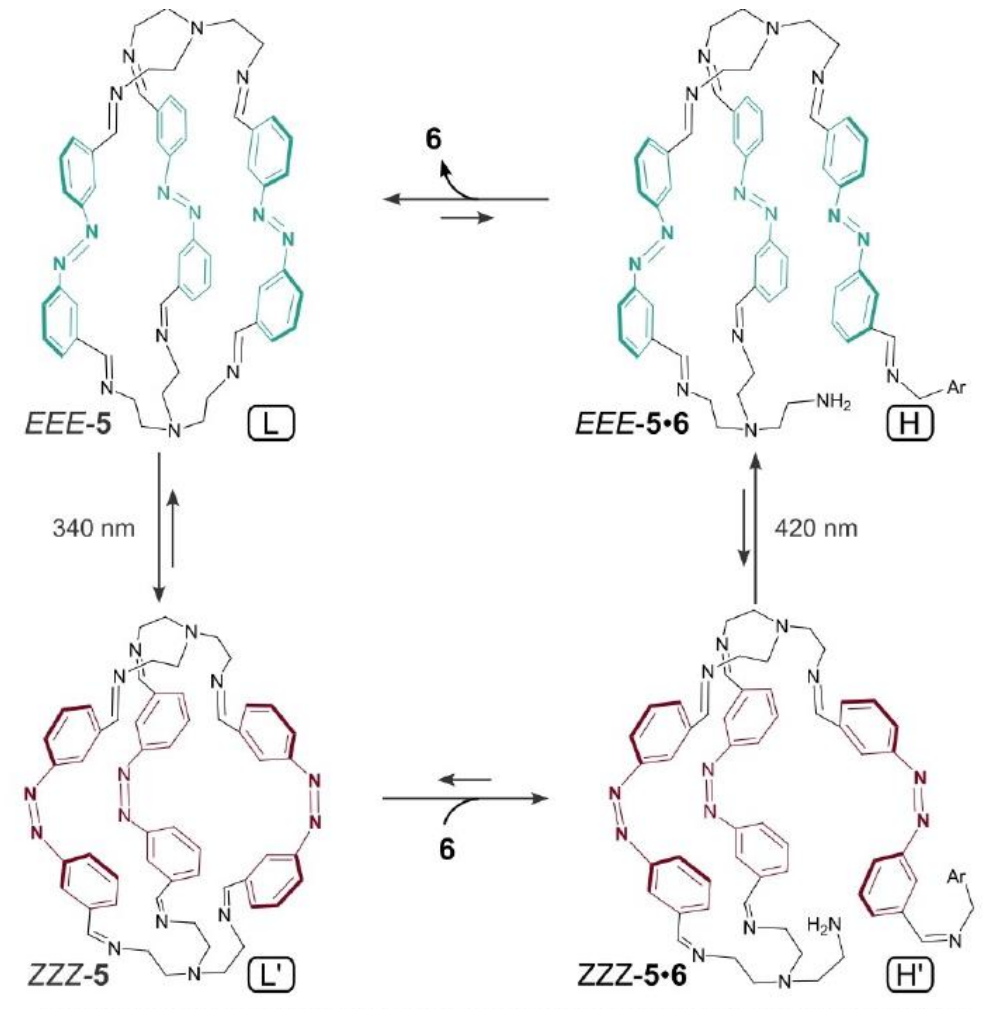
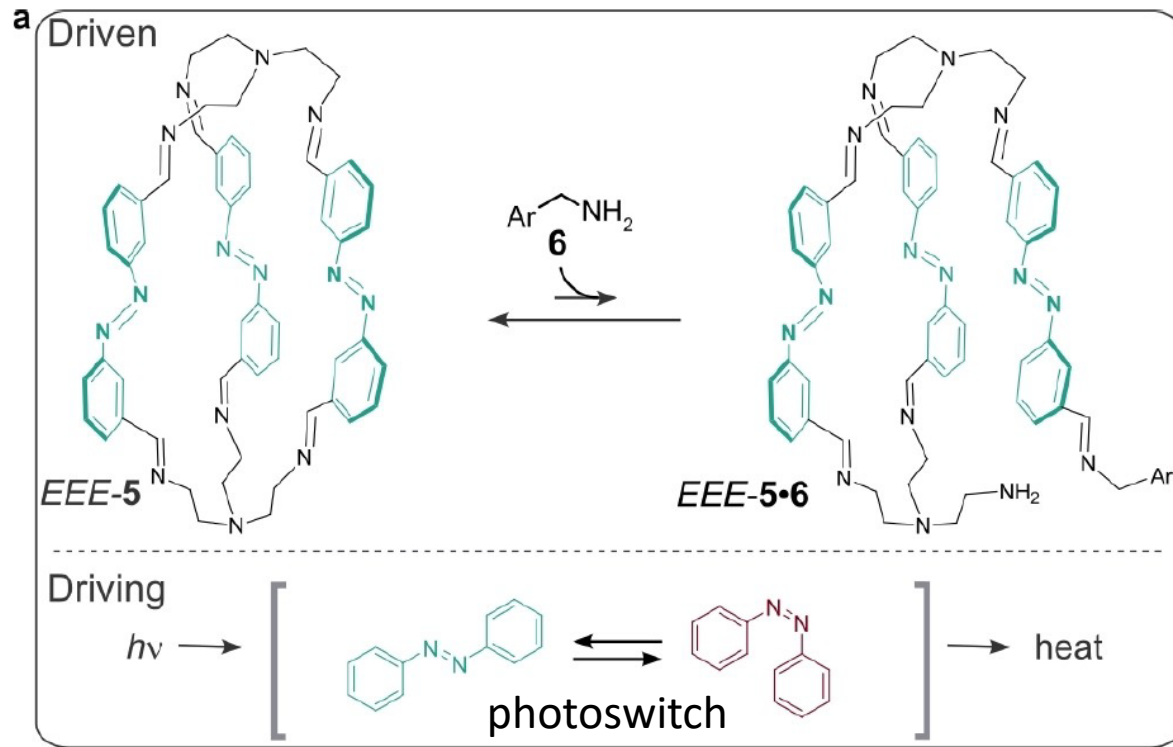


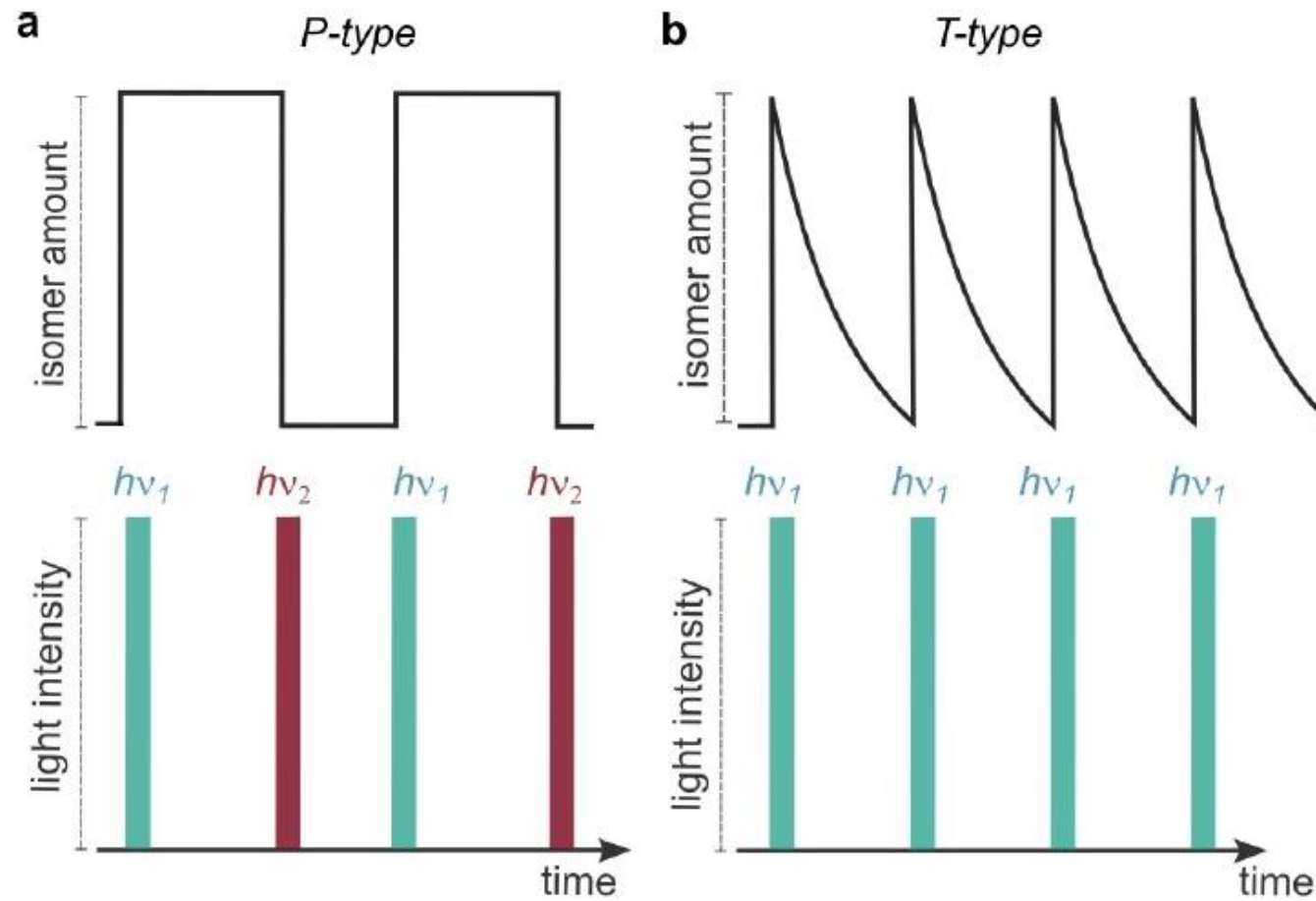
Under appropriate kinetic & thermodynamic conditions:

- A cyclic reaction sequence is performed
- Concentrations are different from equilibrium values
- Energy is stored in the system



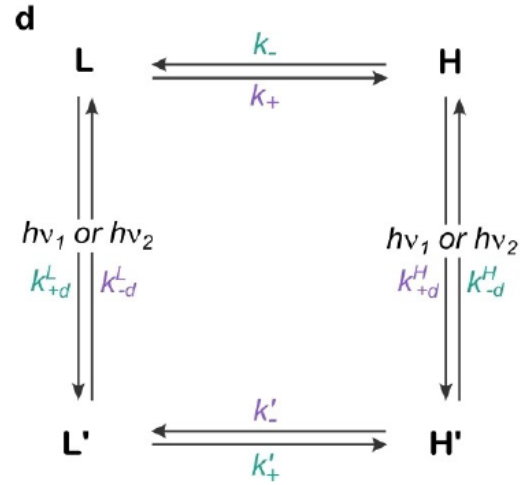
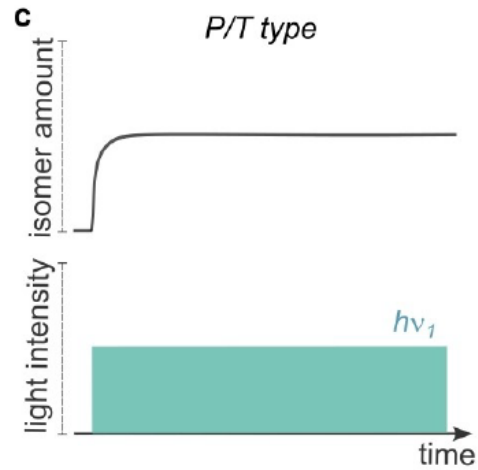
# Alternating conditions with light: example





What happens if we keep the light «on»?





$$K_r = \frac{k_{+d}^L \times k'_+ \times k_{-d}^H \times k_-}{k_{-d}^L \times k'_- \times k_{+d}^H \times k_+}$$

$$\frac{[L']_{PSS}}{[L]_{PSS}} = \frac{k_{+d}^L}{k_{-d}^L} = \frac{\epsilon_L \times QY_{L \rightarrow L'}}{\epsilon_{L'} \times QY_{L' \rightarrow L}} = K_{PSS}^L(\lambda)$$

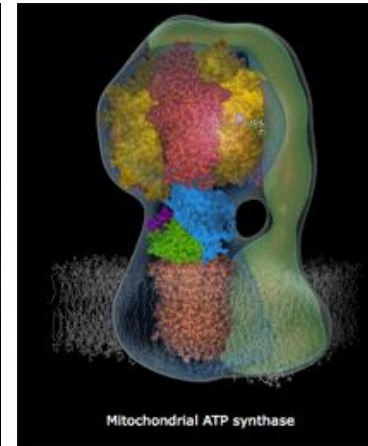
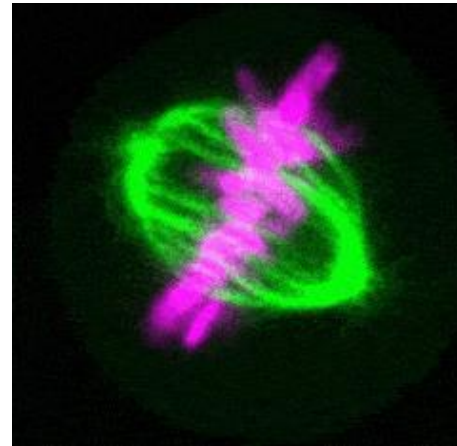
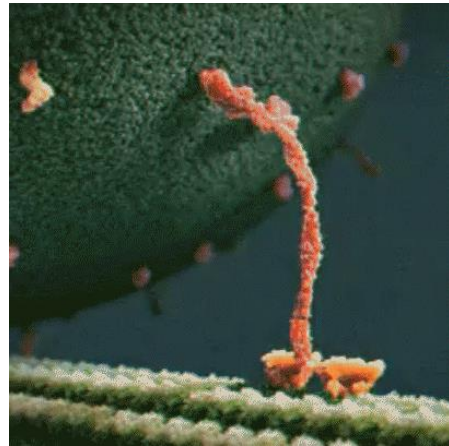
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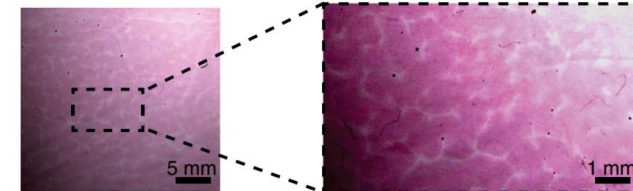
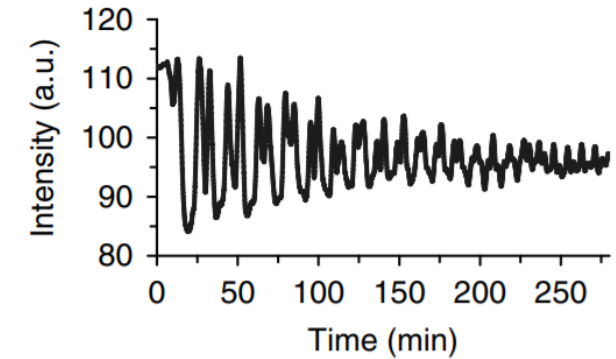


Kinetic  
asymmetry

Driven systems  
(DO absorb energy)



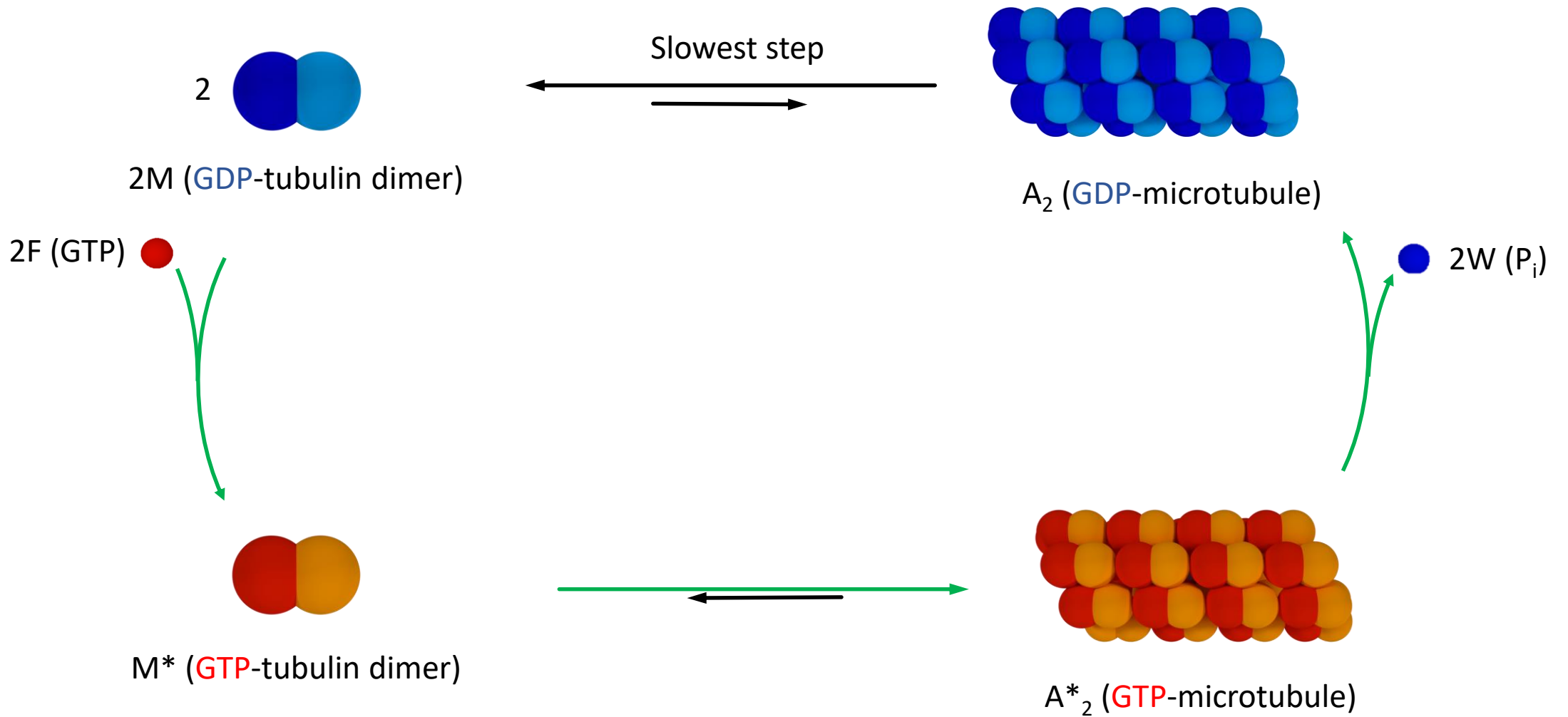
Oscillating systems  
(DO absorb energy & are synchronized)



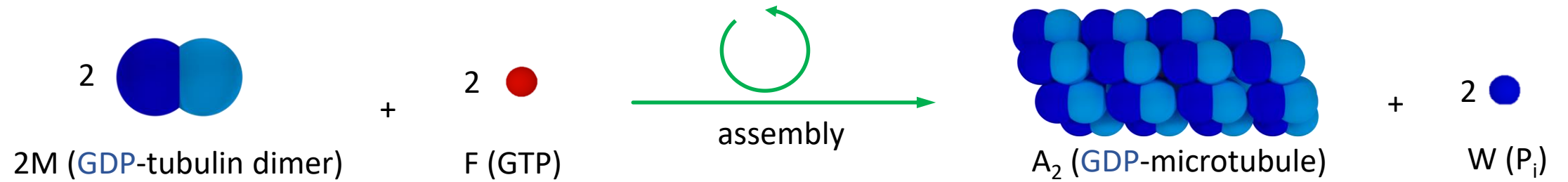
Bifurcation

Do not forget the big picture: alternating conditions, light, spatial differentiation..

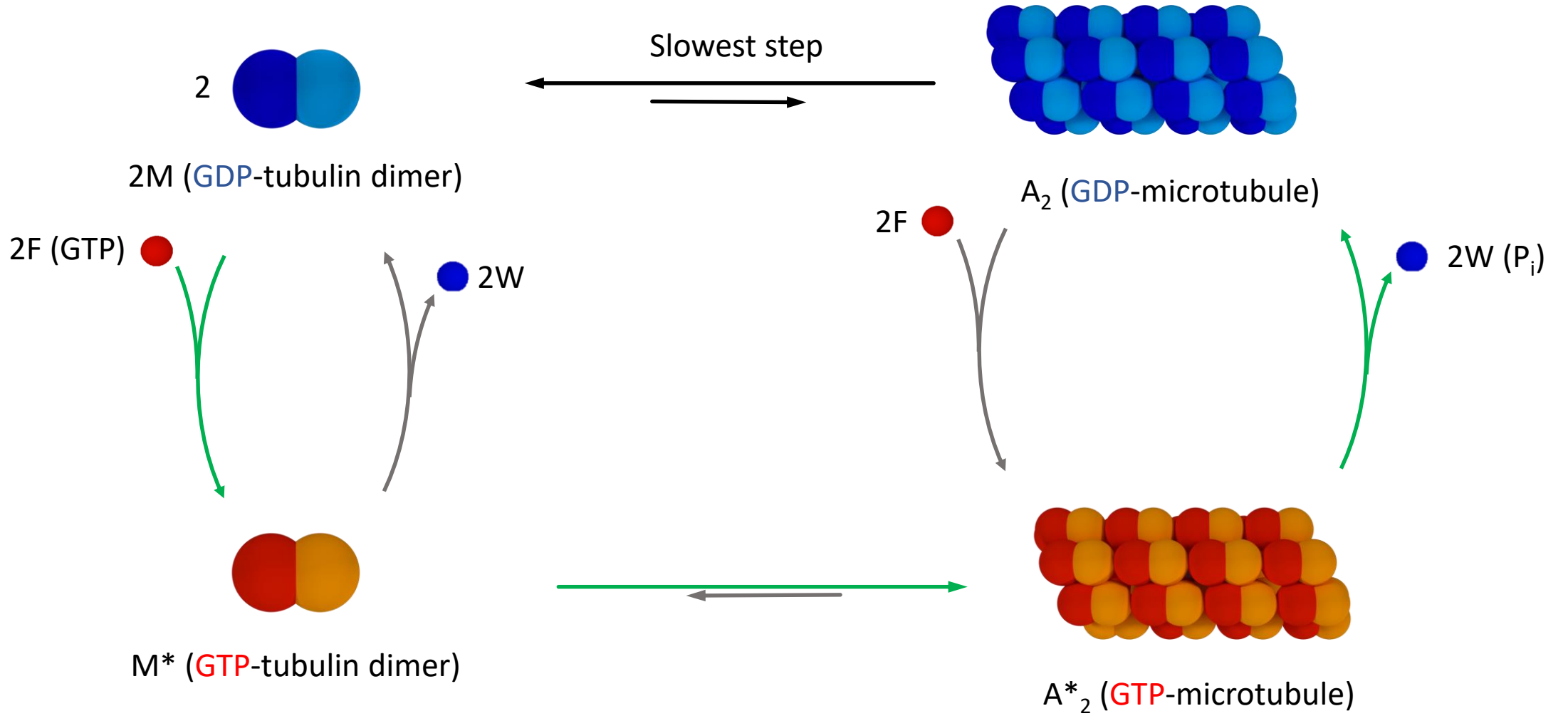
# Epitomic example: assembly of a dimer



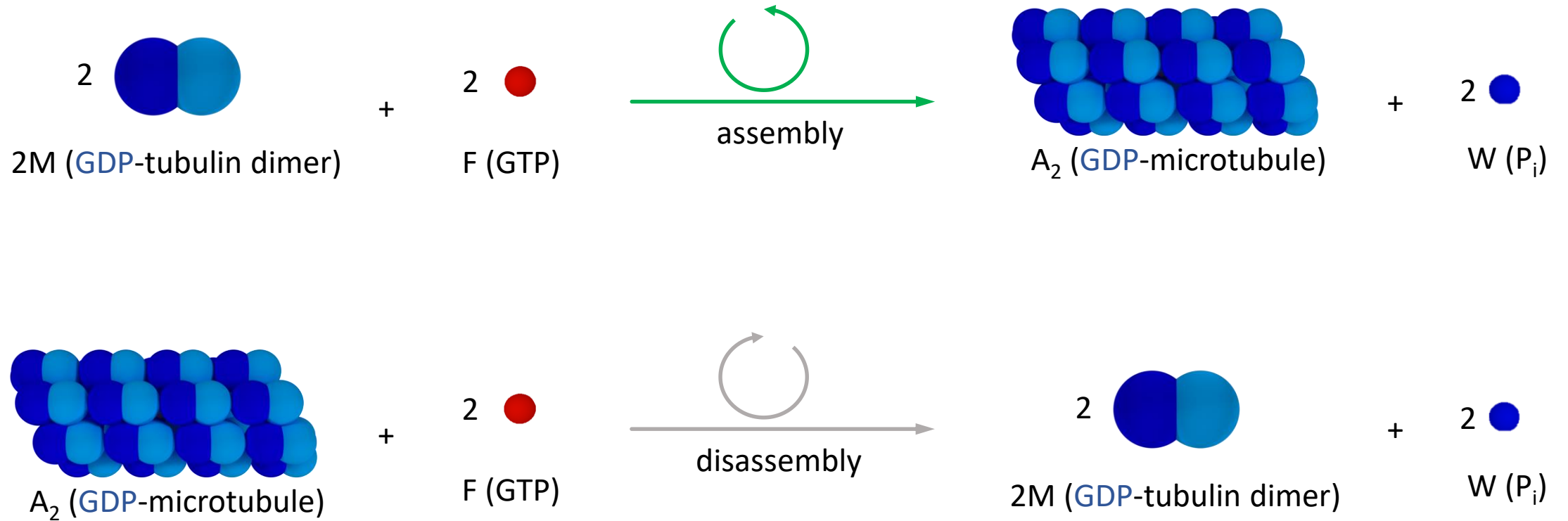
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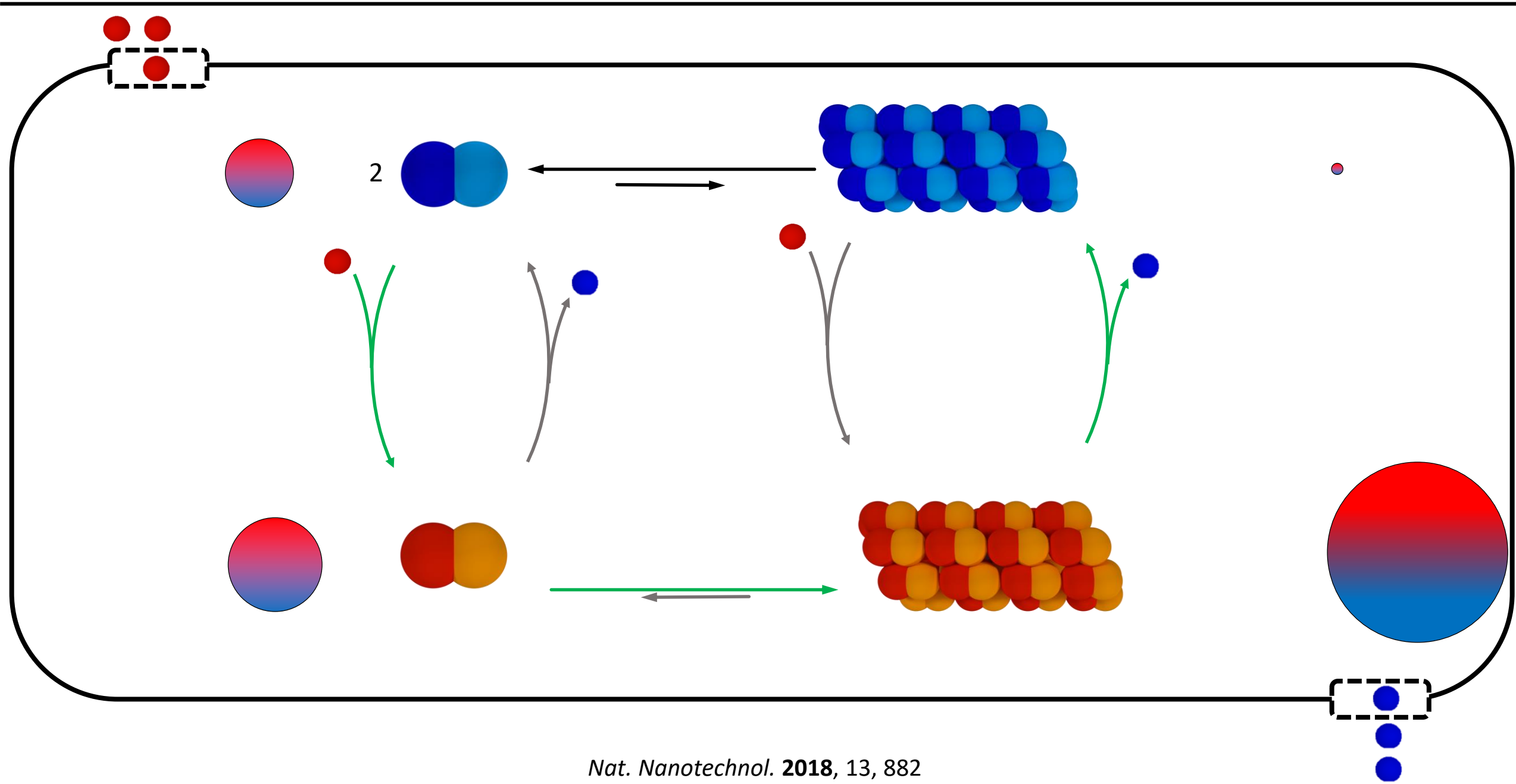
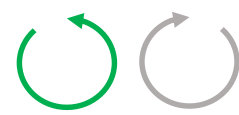
# Epitomic example: assembly of a dimer

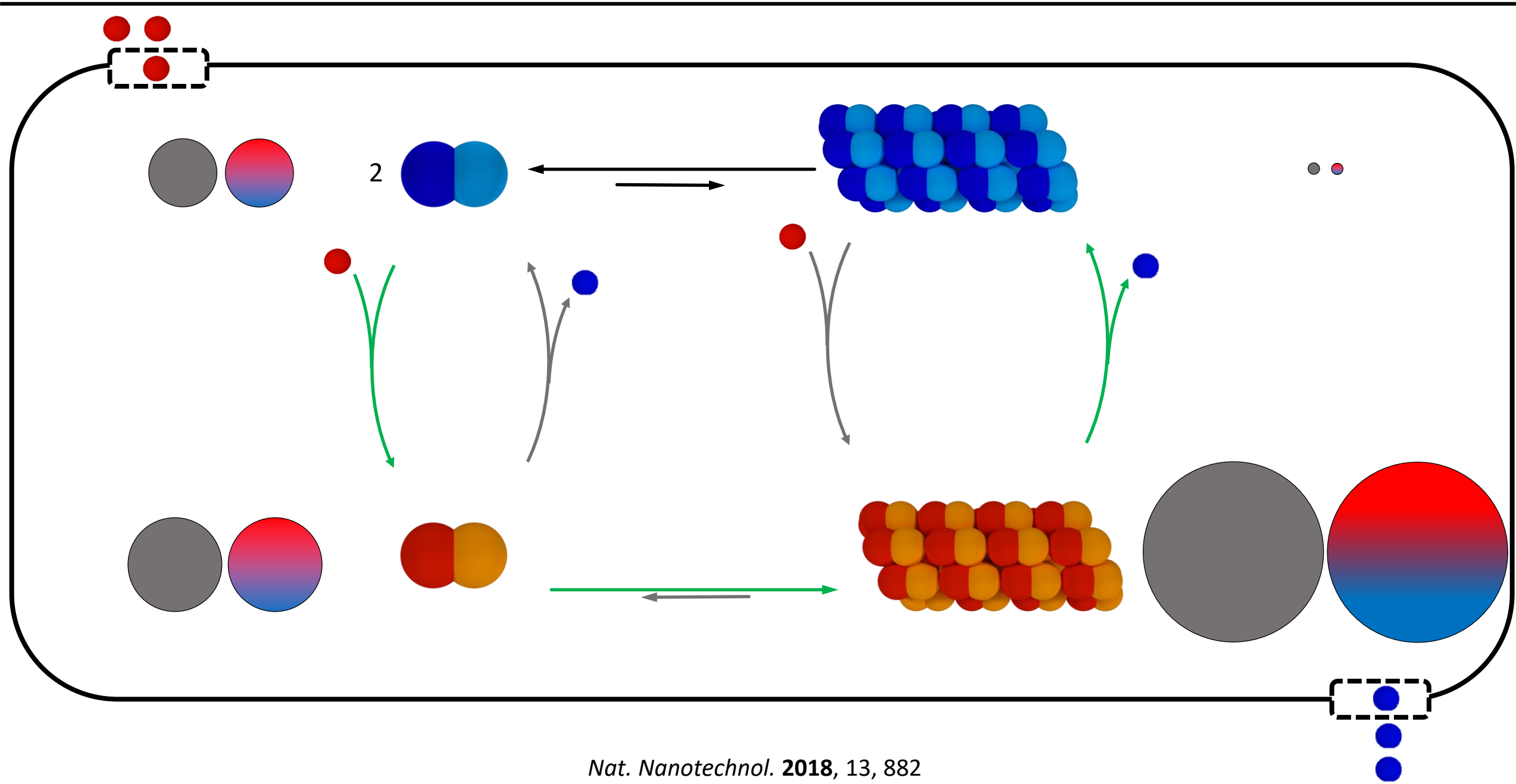
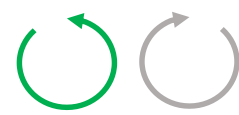


# Epitomic example: assembly of a dimer

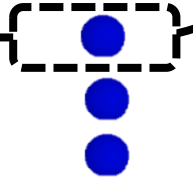
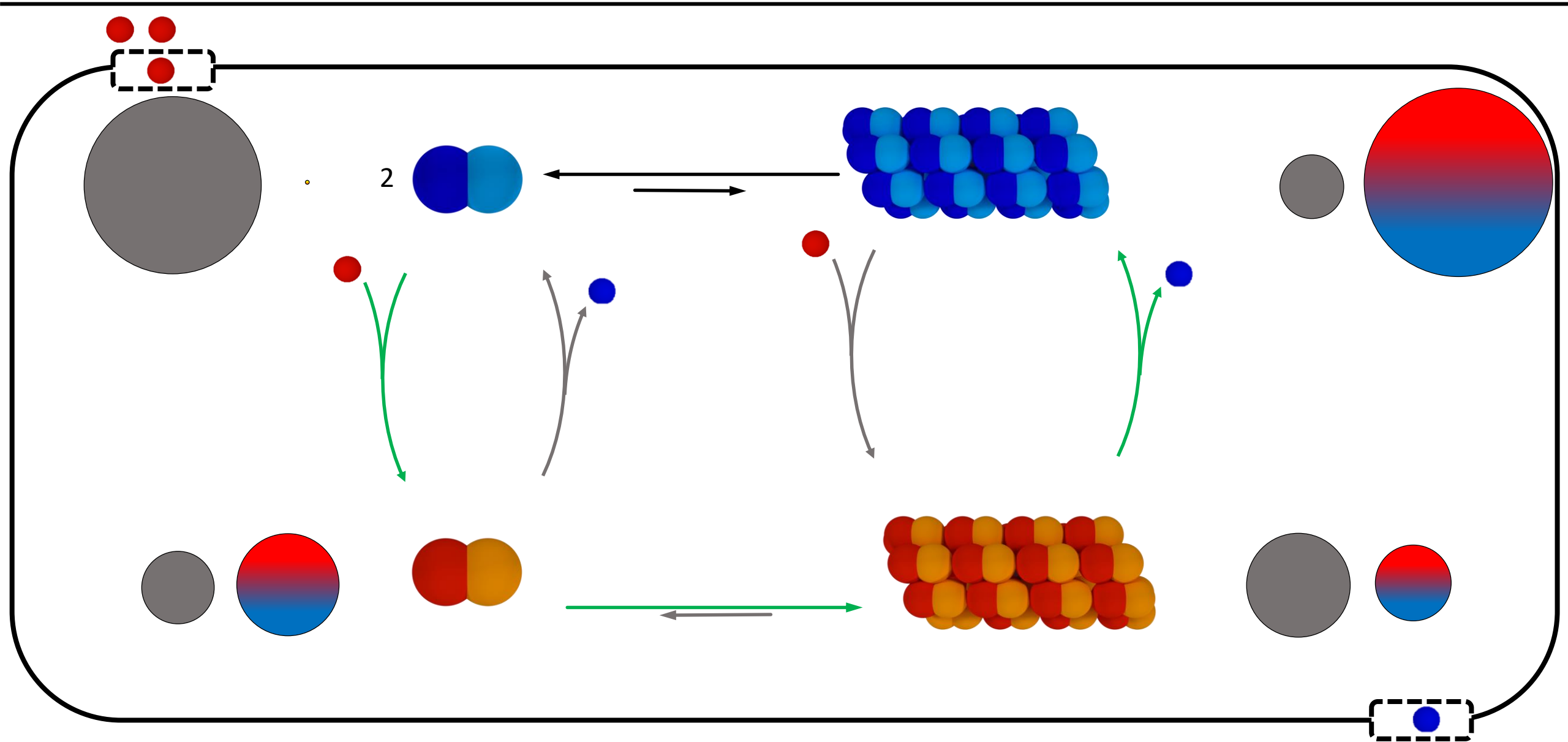
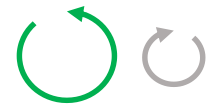


Both paths are thermodynamically allowed, kinetics dictates which one will prevail









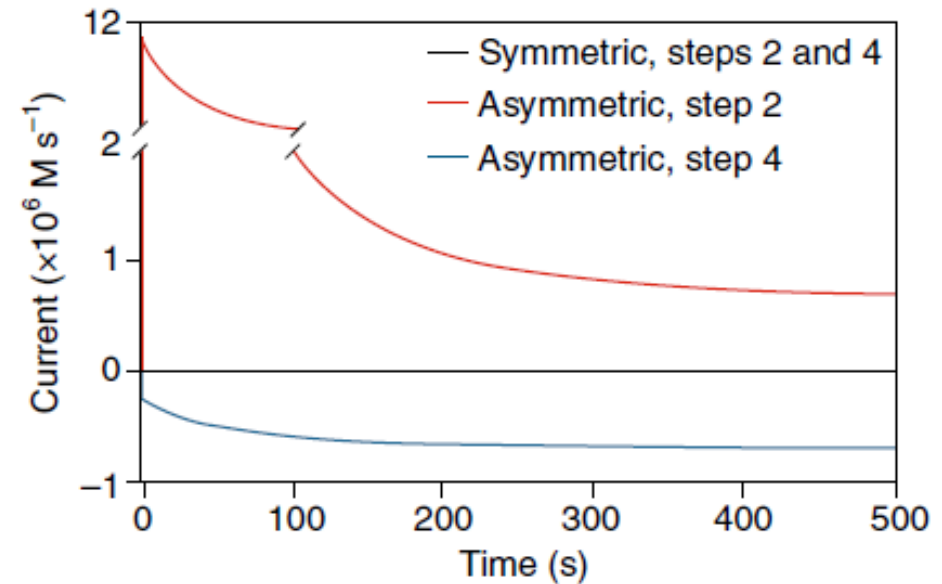
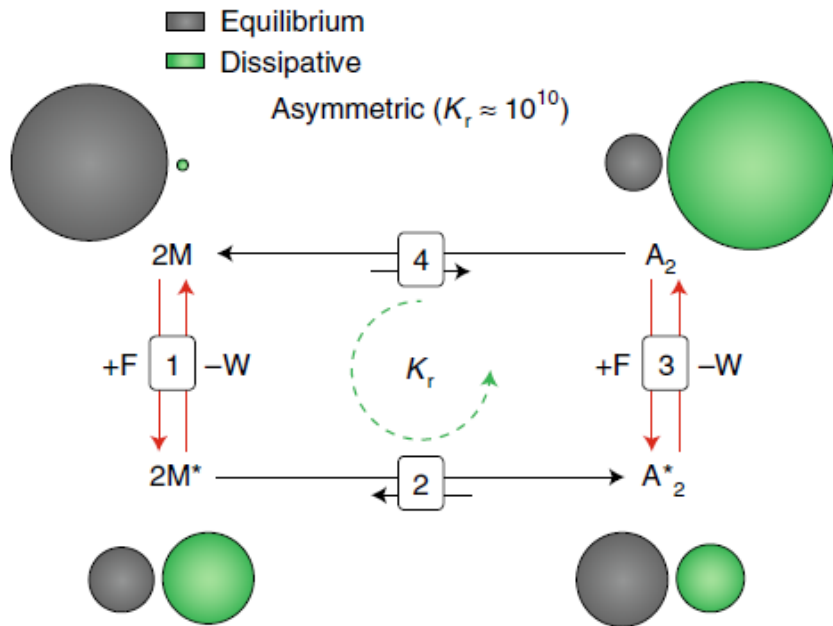
A cyclic current arises

Concentrations are stationary, but differ from equilibrium values

Energy is stored in the system

Expression for step 2 net chemical current:

$$v_2 = k_{2f} \times [M]^2 - k_{2b} \times [A^*_2]$$



Key underlying phenomenon: different transition state depending on network position  
i.e. chemical reactivity depends on target/mechanical state: *information*

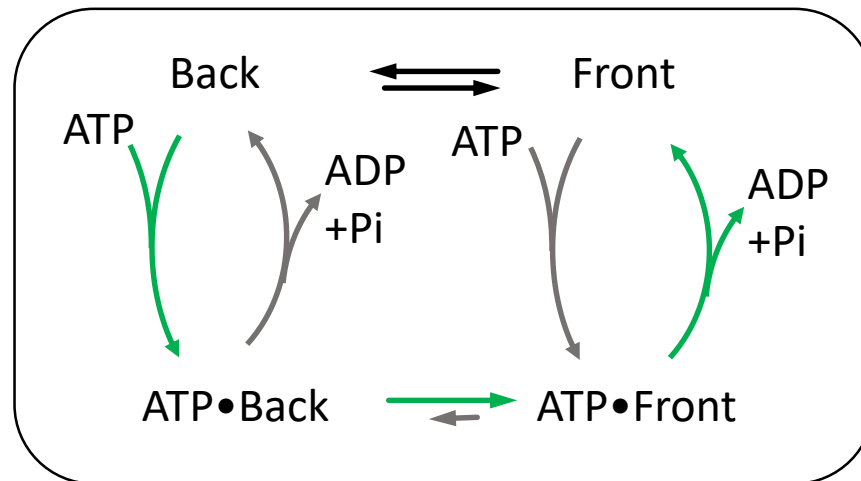
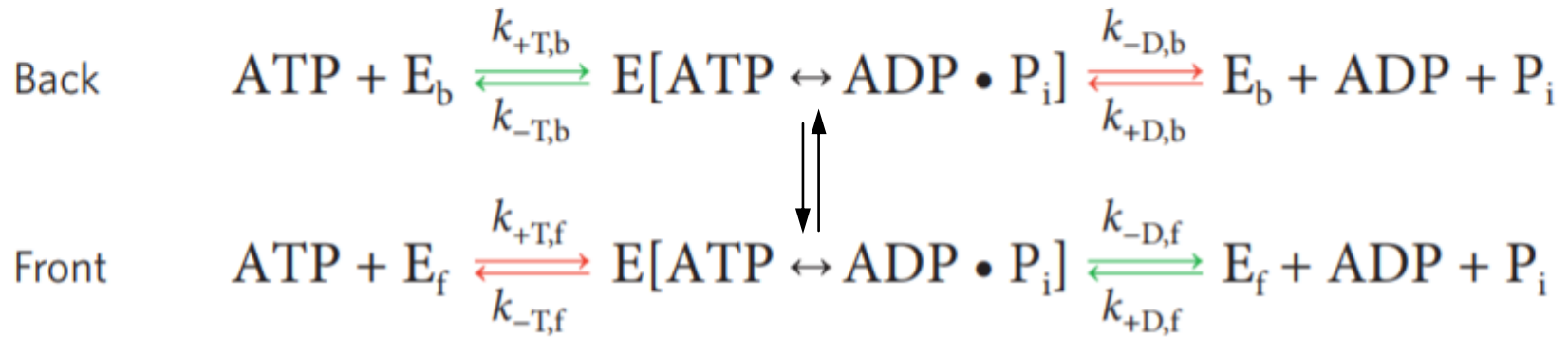
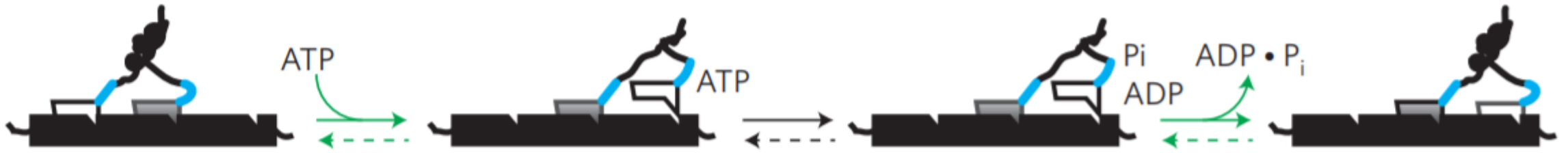
Identify a self-standing reaction (mass/redox balance should be ok)

The self-standing reaction should take part in a cyclic reaction path

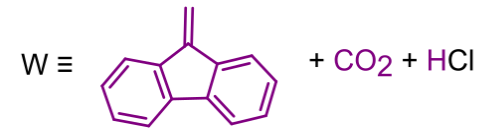
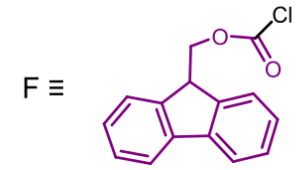
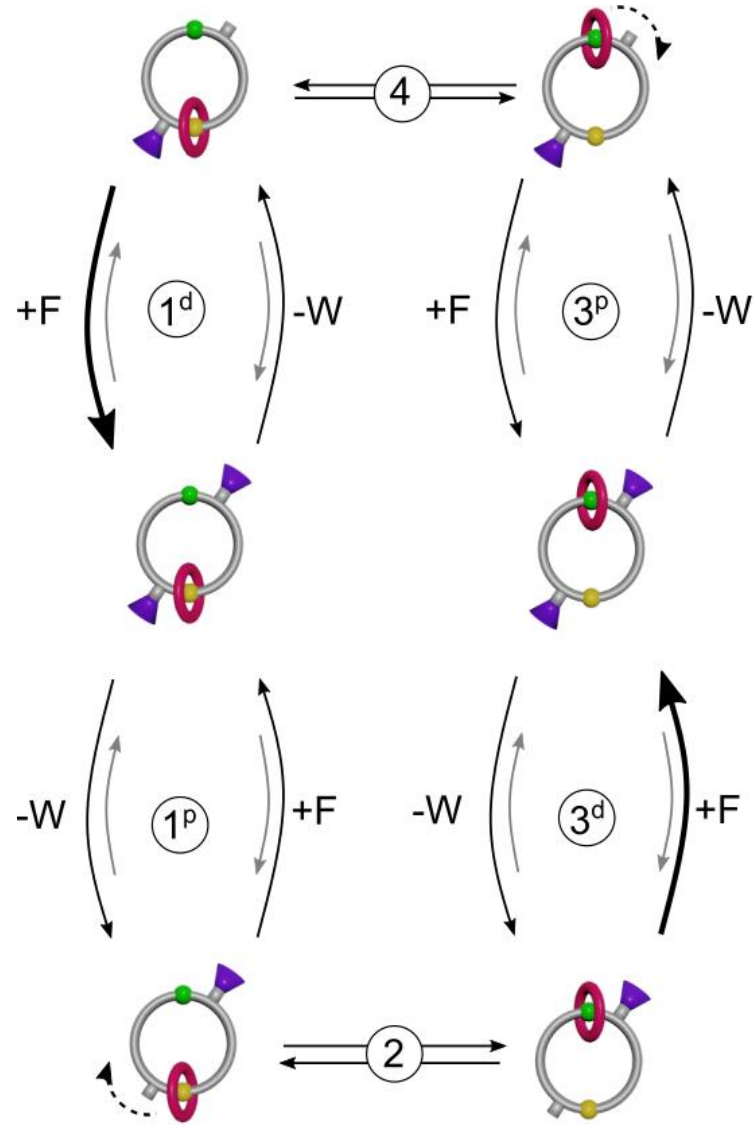
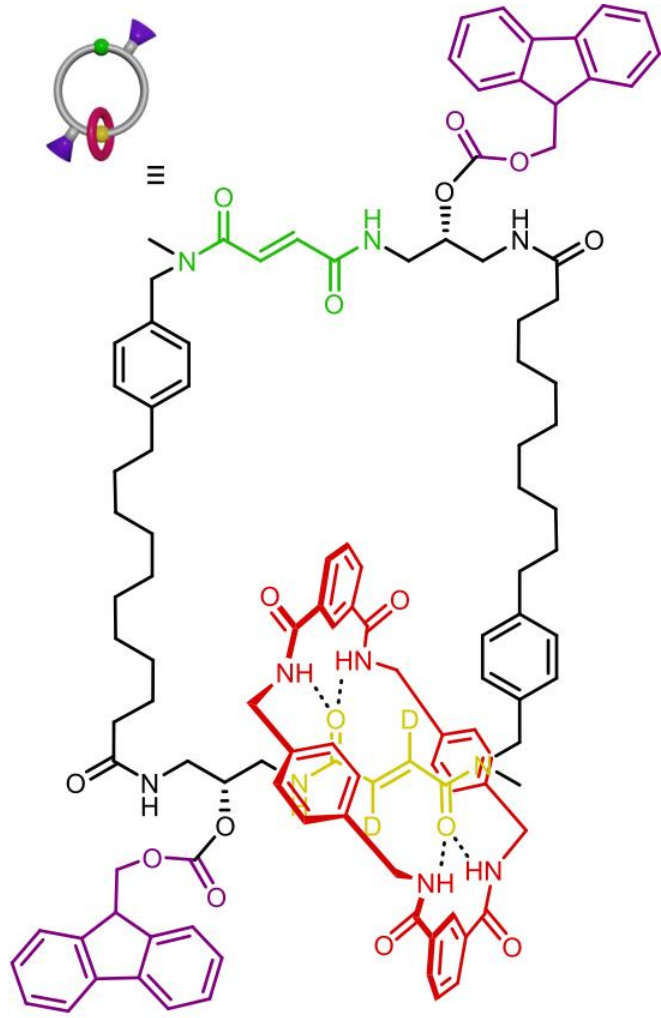
A branch of the cycle should afford the conversion of Substrate into Product

Design/evaluate kinetic asymmetry

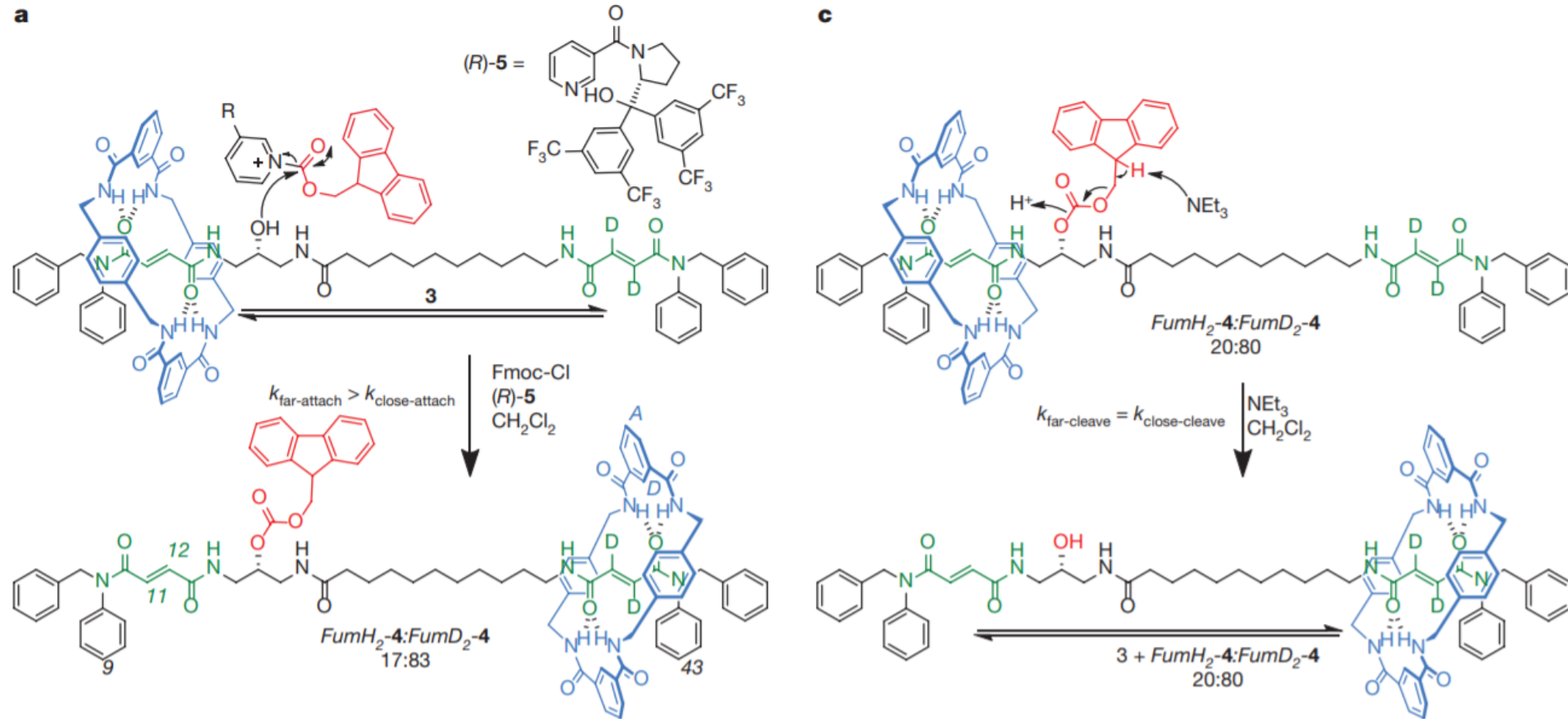
# Example 1: kinesin directional stepping



# Example 2: catenane rotary motor

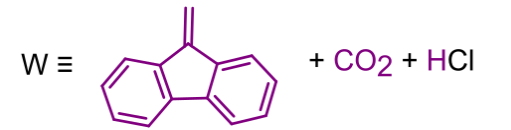
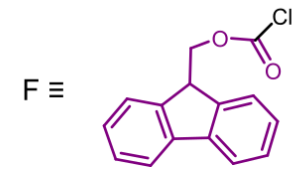
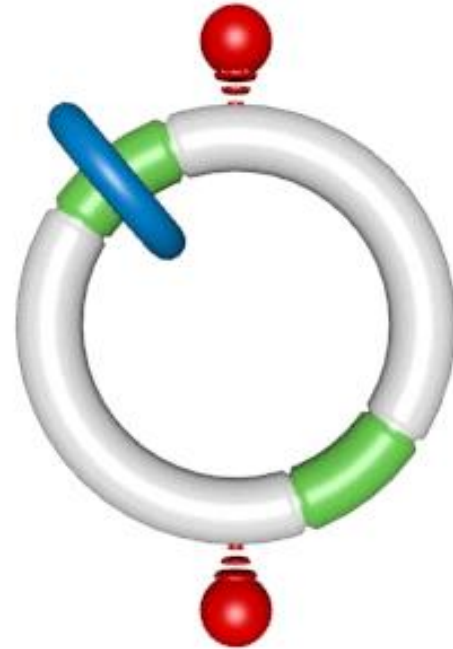
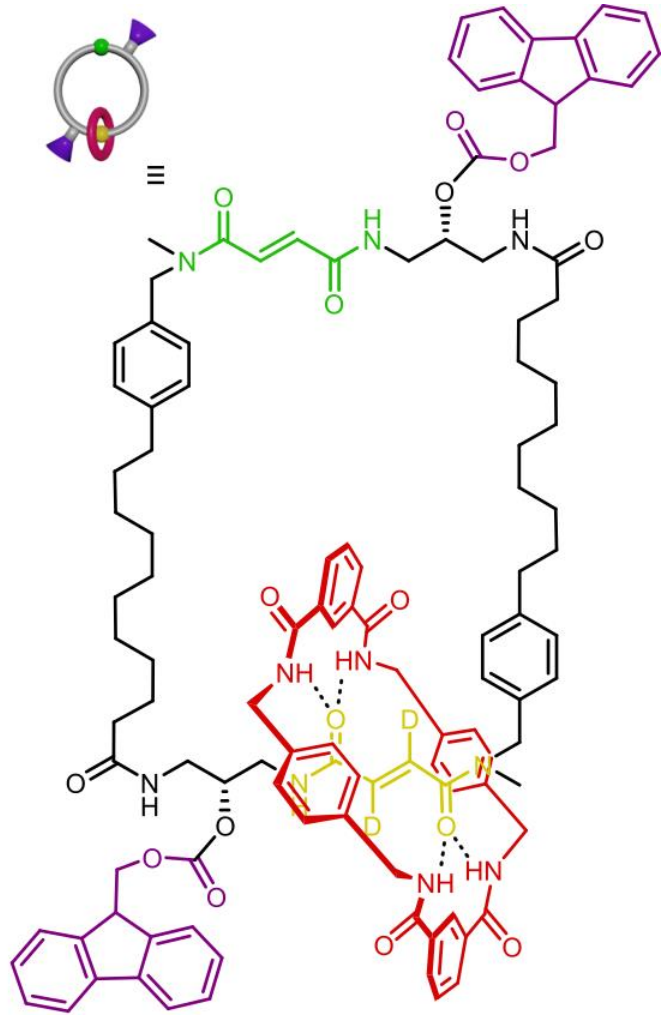


# Example 2: catenane rotary motor



The molecular origin of kinetic asymmetry lies in the different mechanisms for attachment and detachment

# Example 2: catenane rotary motor



A cyclic current arises – kinesin, catenane rotor

Concentrations are stationary, but differ from equilibrium values – microtubules, molecular pump

Energy is stored in the system



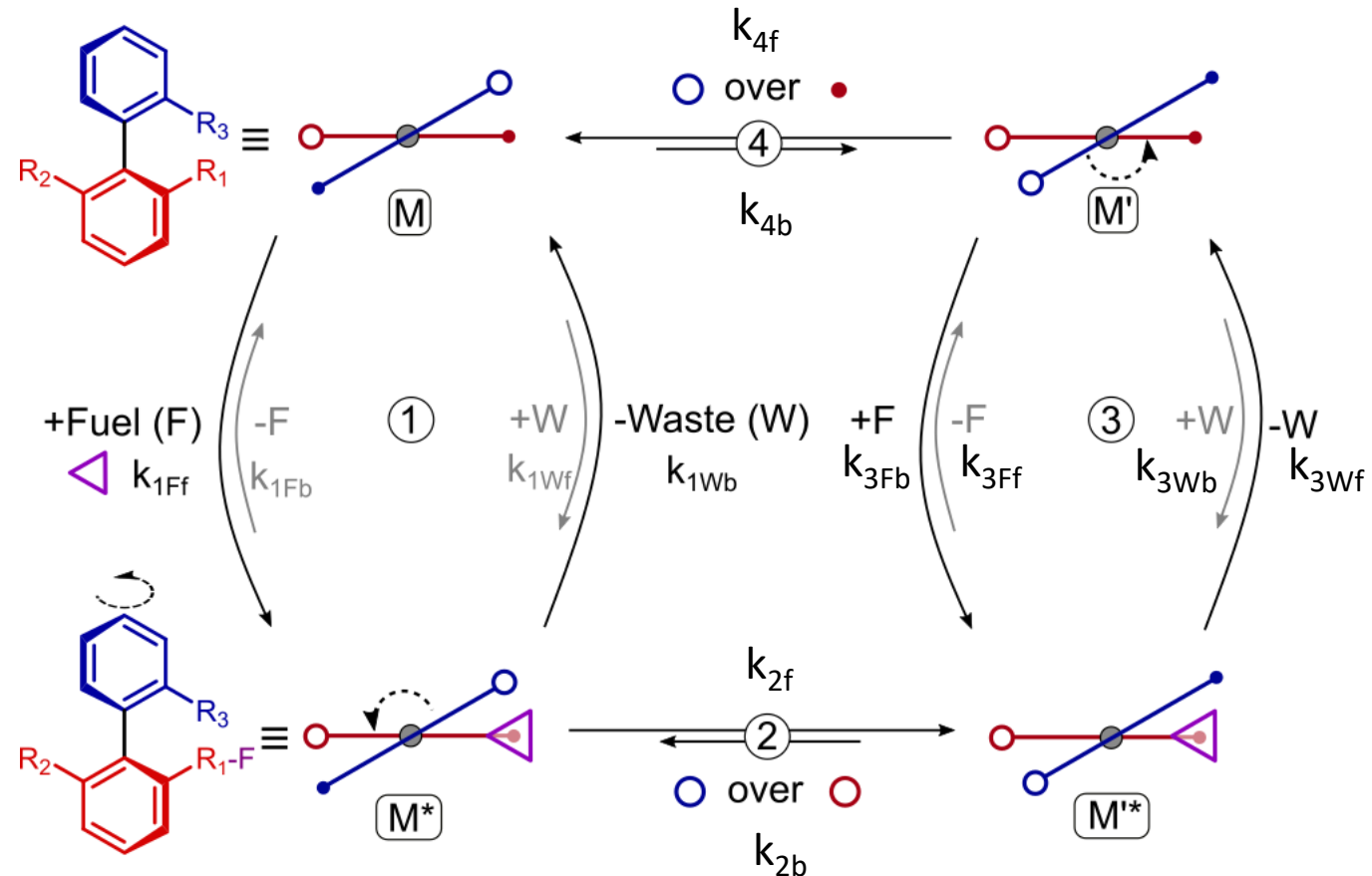
# Exercise: kinetic asymmetry and energy

Consider the following scheme, which depicts a hypothetical chemically-driven rotary motor.

Is the motor rotating under the stationary condition  $[F] = 2 \text{ M}$ ,  $[W] = 0.02 \text{ M}$ .

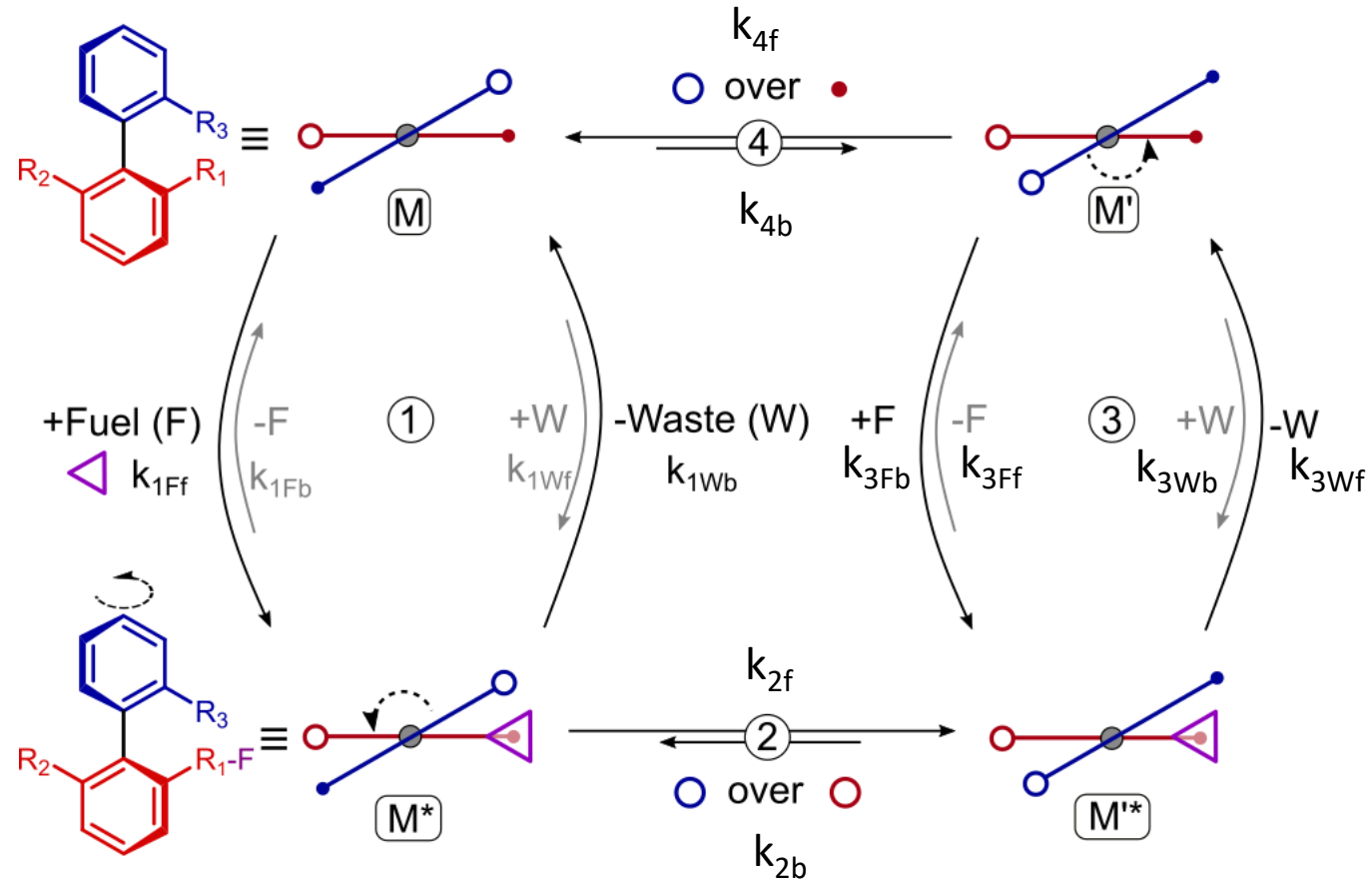
What is the upper bound for the work that the motor can do at room temperature (298 K)?

Use the available rate constants to answer these questions (see excel, with  $k_{1Ff} = k_{0\_1Ff} \cdot [S]$ )



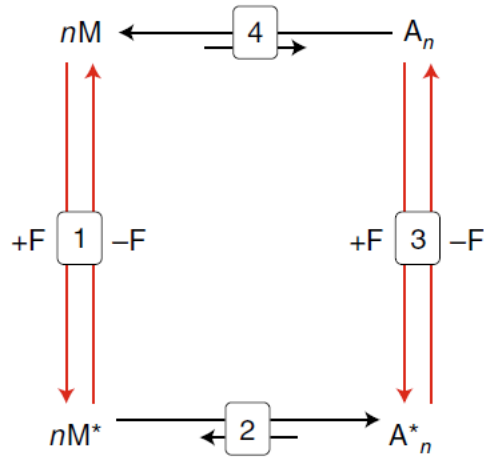
# Exercise: kinetic asymmetry and energy

Thermodynamic relations remain valid, for any thermodynamic cycle:  $\prod k_f / \prod k_b = 1$

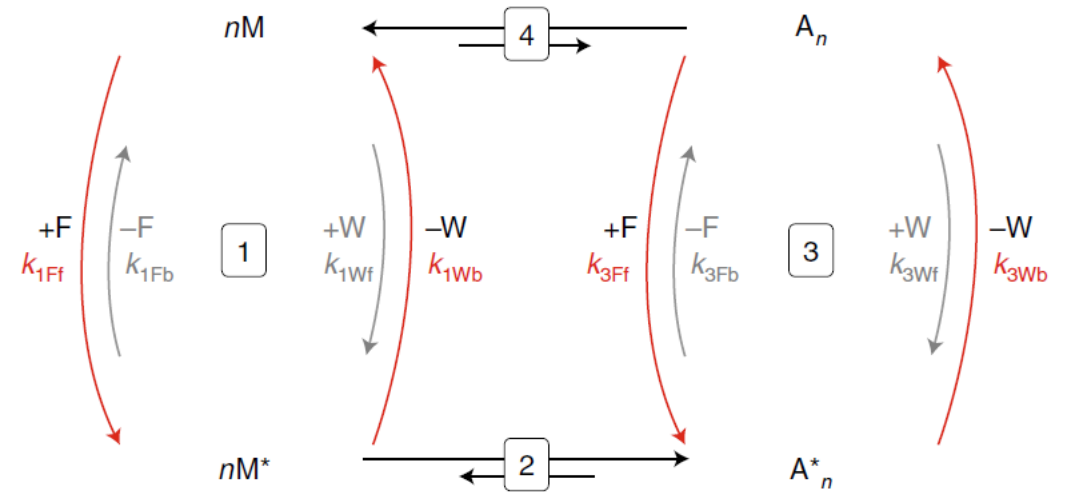


Forward reactions defined according to counterclockwise cycle

# Energy storage: the ratcheting constant, $K_r$



$$K_1^n K_2 K_3^{-1} K_4^{-1} = 1$$



$$\left( \frac{k_{1Ff} + k_{1Wf}}{k_{1Wb} + k_{1Fb}} \right)^n K_2 \left( \frac{k_{3Ff} + k_{3Wf}}{k_{3Wb} + k_{3Fb}} \right)^{-1} K_4^{-1} = K_r$$

with:

$$k_{1Ff} = [F] \times k_{1Ff}^0 \quad k_{3Ff} = [F]^n \times k_{3Ff}^0$$

$$k_{1Wf} = [W] \times k_{1Wf}^0 \quad k_{3Wf} = [W]^n \times k_{3Wf}^0$$

because:  $v_{1Ff} = k_{1Ff}^0 \times [F] \times [M]$

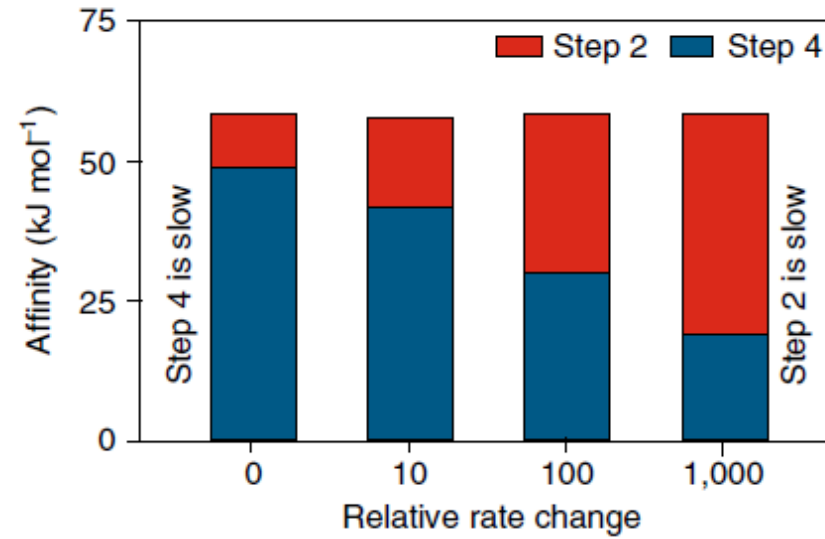
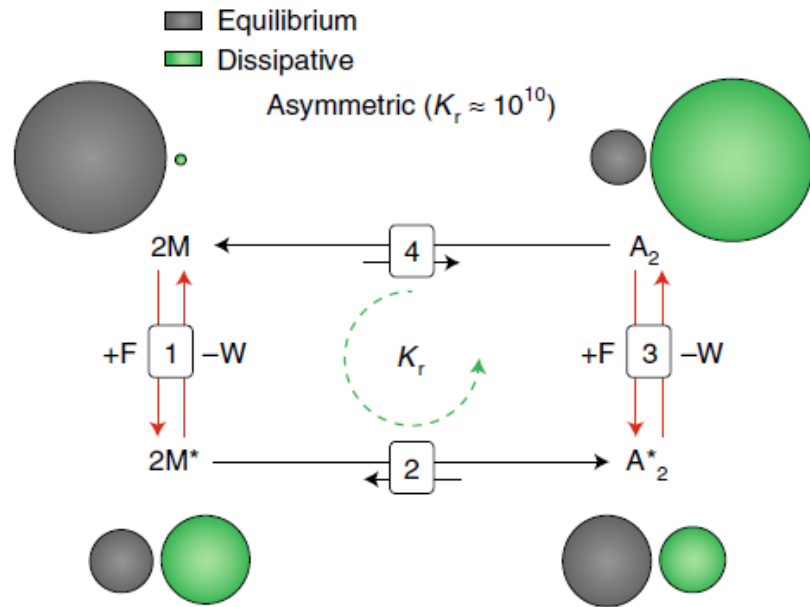
Probability of cycling counter clockwise / probability of cycling clockwise

[Why brownian directionality emerges: because F to W conversion liberates energy, that is not any more available]

Origin of the name: brownian ratchets, popularized by Feynman <https://www.youtube.com/watch?v=M3fYbCatKbA>

Further readings: «Life's Ratchet: How Molecular Machines Extract Order from Chaos» by P. M. Hoffmann

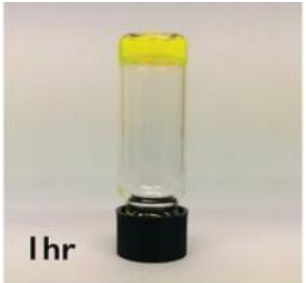
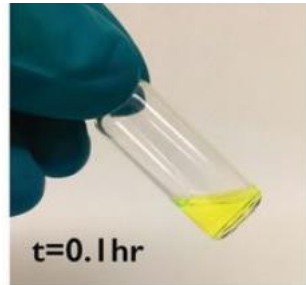
# Energy storage: the ratcheting constant, $K_r$



$\Delta = RT \ln (K_r)$  is an upper bound for the energy stored in the system

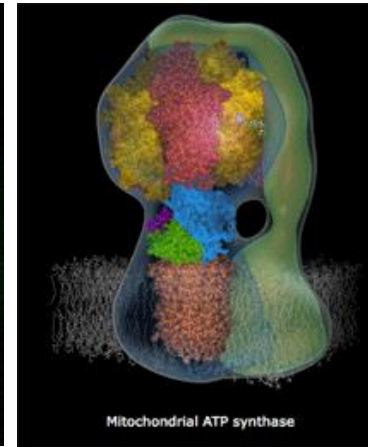
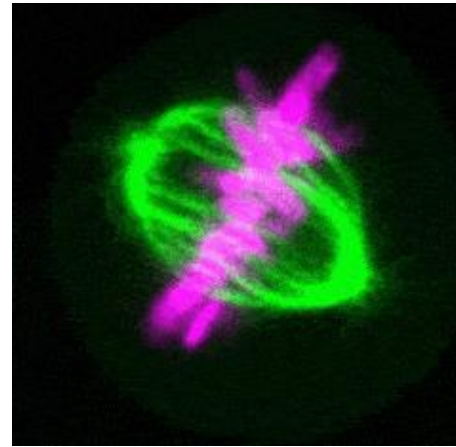
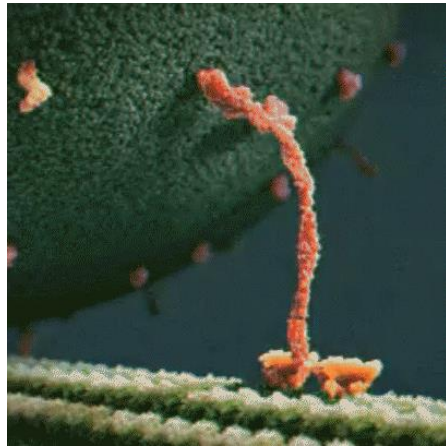
Originates from affinity values: e.g. for step 2,  $A = -RT \ln ([A^*_2]/[M]^2) + RT \ln [K_2]$

Transient systems  
(do NOT absorb energy)



Kinetic  
asymmetry

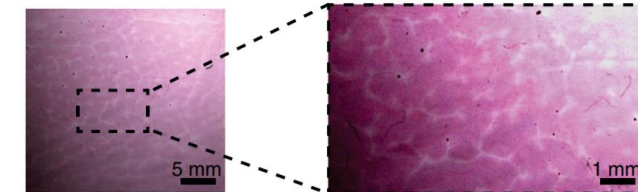
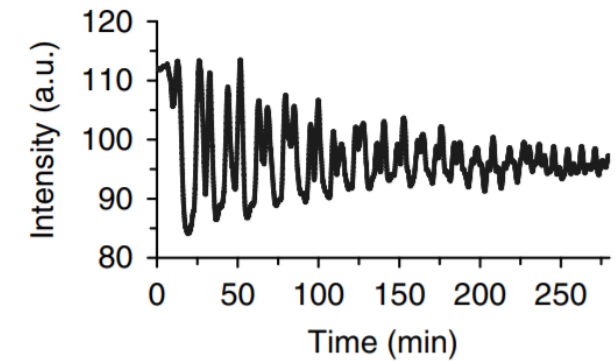
Driven systems  
(DO absorb energy)



Learning points: alternating conditions or light to drive endergonic reactions; what is kinetic asymmetry; how it underlies molecular machines & assembly of high-energy structures; how it's related to energy storage and energy transduction; how to calculate it

Topics & techniques: chemical reaction networks, non-equilibrium thermodynamics, organic chemistry, NMR & optical spectroscopies, kinetic modeling, microscopy, compartmentalization...

Oscillating systems  
(DO absorb energy & are synchronized )



Bifurcation