

PROGRAMMING FOR COMPUTATIONAL CHEMISTRY

Data

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- Abstraction of computation modules

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- Procedural programming

Practical example

Given two integers `n1` and `n2`, both read from `standard input`, we want to sum them into a variable `total`, then printed on the screen (`standard output`) (`add.f90`)

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- KB, MB, GB, TB etc.

Data types

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- **character*p**: string of alphanumeric character, with length p

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Data types

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 - 1 set of values (**domain**)
 - 2 set of **operations**

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- **Scientific notation in base 2**

Floating point arithmetics

- **Single precision** (real*4): **32 bits**, from $\sim 1.175 * 10^{-38}$ to $\sim 3.403 * 10^{+38}$
- **Double precision** (real*8): **64 bits**, from $\sim 2.225 * 10^{-308}$ to $\sim 1.798 * 10^{+308}$

$$\text{floating point} = (-1)^s * f * 2^e$$

Single precision



Double precision



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- **Finite** range
- Systematic error in representing real numbers (**round-off error**)

$$101.01 = 1 \times 2^2 + 0 \times 2^1 + 1 \times 2^0 + 0 \times 2^{-1} + 1 \times 2^{-2} = 5.25$$

$$\begin{aligned}101.01 &= 1 \times 2^2 + 0 \times 2^1 + 1 \times 2^0 + 0 \times 2^{-1} + 1 \times 2^{-2} = 5.25 \\0.0101 &= 0 \times 2^0 + 0 \times 2^{-1} + 1 \times 2^{-2} + 0 \times 2^{-3} + 1 \times 2^{-4} \\&= 1./4. + 1./16. = 0.3125\end{aligned}$$

Practical examples

- Rewrite `add.f90` with `real` and `double precision` numbers