# 2024/2025 FLUIDODINAMICA GEOFISICA

FISICA [SM23] Laurea Magistrale - Fisica dei sistemi complessi, clima e finanza SSD: ICAR/01, GEO/12 24 hours, 6 CFU

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Aims: To introduce students to fluid dynamics basic principles and to the main topics of geophysical fluid dynamics

## **Syllabus**

#### Part I Fluid Mechanics

Lecture 1 Introduction to Fluid Mechanics: Properties and definition; Viscosity; Statics; Pressure and Buoyancy force

Lecture 2 Tensors; Gradient, Divergence, Curl; Stokes and Gauss Theorems; Lagrangian Derivative and Streamlines

 $Lecture\ 3\ Kinematics:\ Strain\ rates;\ Vorticity\ and\ Circulation;\ Streamfunctions;\ Relative\ motion\ near\ a\ point$ 

Lecture 4 Conservation of Mass: Reynolds Transport Theorem; Continuity, Advection-Diffusion Equation

Lecture 5 Conservation of Momentum: Cauchy's Equation; Constitutive equation for Newtonian fluids

Lecture 6 Conservation of Momentum: Navier-Stokes Equations

Lecture 7 Conservation of Momentum: Rotating frame of reference and Coriolis

Lecture 8 Conservation of Energy: Mechanical energy; Thermal energy equation

Lecture 9 Conservation of Energy: Bernoulli equation

Lecture 10 Vorticity dynamics

### **Part II Geophysical Fluid Dynamics**

Lecture 10 Introduction to Geophysical FD: scales of motion, rotation/stratification in atmosphere and ocean

Lecture 11 Rotating frame of reference: Coriolis force, inertial oscillations, acceleration on a 3-D rotating planet

Lecture 12 Governing equations of GFD: momentum, mass conservation, energy, equation of state

Lecture 13 Boussinesq approximation; scale analysis and further simplifications of governing equations; Rossby, Ekman, Reynolds numbers

Lecture 14 Geostrophy: geostrophic flows; Taylor-Proudman theorem; non-geostrophic flows; vorticity dynamics

Lecture 15 Friction and rotation 1: Prandtl hypothesis, Bottom Ekman layers

Lecture 16 Friction and rotation 2: Surface Ekman layer, Ekman pumping, Ekman layers in real geophysical flows

Lecture 17 Barotropic waves 1: hypotheses, Kelvin waves, Poincarè waves

Lecture 18 Barotropic waves 2: Rossby waves, topographic waves and their analogies

Lecture 19 Stratification: static stability, Froude number, combination of rotation and stratification

Lecture 20 Mixing 1: mixing of stratified fluids, Kelvin-Helmoltz instability – Instability of a stratified shear flow

Lecture 21 Mixing 2: Taylor-Goldstein equation, Richardson number; turbulence in a stratified shear flow

### **Books:** any textbook on Fluid Mechanics / GFD, but particularly:

- `Introduction to Geophysical Fluid Dynamics Physical and Numerical Aspects' by B. Cushman-Roisin J.-M. Beckers (<a href="https://www.elsevier.com/books/introduction-to-geophysical-fluid-dynamics/cushman-roisin/978-0-12-088759-0">https://www.elsevier.com/books/introduction-to-geophysical-fluid-dynamics/cushman-roisin/978-0-12-088759-0</a>) (<a href="https://www.ccpo.odu.edu/~klinck/Reprints/PDF/roisinGFD2010.pdf">https://www.ccpo.odu.edu/~klinck/Reprints/PDF/roisinGFD2010.pdf</a>)
- 'Physical Fluid Dynamics' by D. J. Tritton
- `Fluid Mechanics' by P. K. Kundu (available online)
- `Atmospheric and Oceanic Fluid Dynamics' by G.K. Vallis
- `Essentials of Atmospheric and Oceanic Dynamics', by G.K. Vallis