





A radio receiver used to measure the average power coming from a radio telescope in a welldefined frequency range is called a radiometer.

Noise of a Radiometer

Visibility measurements are limited by several sources of noise: the atmosphere, the antenna itself, the ground and the receivers. The rms noise associated with a given baseline *ij* is given by:



This is the noise on the real and on the imaginary parts of the visibilities (measured independently). This is also the noise on the amplitude *S*.

It is more complex to define the error on the phase, scales as σ/S .



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It is more complex to define the error on the phase, of the order of σ/S .

$$T_{\text{sys}} = T_{\text{CMB}} + T_{\text{rsb}} + \Delta T_{\text{source}} + [1 - exp(-\tau_A)]T_{\text{atm}} + T_{\text{spill}} + T_r + \dots$$

where

 $T_{\rm rsb}$ radio source background

 $\Delta T_{\rm source}$ source brightness temperature

 $[1 - exp(-\tau_A)]T_{atm}$ brightness of atmospheric emission

 $T_{\rm spill}$ brightness temperature due to antenna spillovers

 $T_{\rm r}$ radiometer noise temperature

Visibility parameters as a function of time



Visibility parameters as a function of frequency



Noise of a Radiometer

For N identical antenna/receivers, i.e. N (N - 1)/2 baselines, the point-source sensitivity is

$$\delta S = \frac{2k}{A\eta_{\rm A}\eta_{\rm Q}\eta_{\rm P}} \cdot \frac{T_{\rm SYS}}{\sqrt{N(N-1) B T}}$$

For large N, scales as $\sim \frac{1}{N}$

The sensitivity for extended sources depends on the angular resolution

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Nearly all practical radiometers are heterodyne receivers

The reference frequency (RF) amplifier is followed by a mixer that multiplies the RF signal by a sine(cosine) wave of frequency ν_{LO} generated by a local oscillator (LO). The intermediate frequency (IF) is a result of a phase shift.



 $2\sin(2\pi\nu_{\rm LO}t)\sin(2\pi\nu_{\rm RF}t) = \cos[2\pi(\nu_{\rm LO} - \nu_{\rm RF})t] - \cos[2\pi(\nu_{\rm LO} + \nu_{\rm RF})t]$

The advantages of heterodyne receivers include

1. shifting the signals to lower frequencies $\nu_{IF} < \nu_{RF}$ which are easier to amplify, transmit over long distances, filter, and digitize;

- 2. tunability over a wide range of $u_{
 m RF}$
- 3. tuning by adjusting only the local oscillator frequency so that

4. the IF amplifier and back-end devices such as multichannel filter banks or digital spectrometers can all operate over fixed frequency ranges.

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4. the IF amplifier and back-end devices such as multichannel filter banks or digital spectrometers can all operate over fixed frequency ranges.



Heterodyne systems

- Down-convert the spectrum from Radio Frequency (50 < F_R < 500 GHz) to Intermediate Frequency (F_R < 20 GHz)
- Tuning the receiver = setting the FLO1 + optimizing some LO and Mixer parameters

LO = local oscillator



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Example of heterodyne receiver: NOEMA

IF Processing

- Adapt the output of the receiver to the input of the correlator
 - 1 NOEMA receiver band delivers 4 x 8 GHz sidebands [4-12 GHz IF1]
 - 1 NOEMA correlator unit accepts 1 x 4 GHz [0-4 GHz IF2] x 12 antennas
- IF processor splits each sideband into 2 x 4GHz **basebands**
 - Downconvertion to 0-4GHz IF2



(A receiver is sensitive to a single polarization, here example for H polarization)

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PDS456 z=0.185 (1"~3 kpc)

We aim to map the CO emission in the quasar host galaxy and detect the far-infrared continuum emission, due to dust heated by star formation

Let's start from what we already know...



Yun et al. 2004, Owens Valley Radio Observatory (OVRO) detection of CO(1-0). Source is unresolved, beam ~6"

Yun et al. 2004, known far-infrared/radio continuum SED

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Spectra	Line						
Baseba	nd-1						C E
Fractio	r Centre Freq (rest,Isrk)	Centre Freq (sky,bar)	Transition	Bandwidth, Resolution (smoothed)		Spec I Avg.	Representative Window
1(Full)	114.22176 GHz	96.38593 GHz	CO v=0 1-0	1875.000 MHz(5832 km/s), 976.563 kHz(3.037 km/s)	\sim	1	۲
				58.594 MHz(182 km/s), 30.518 kHz(0.095 km/s)			
				117.188 MHz(364 km/s), 61.035 kHz(0.190 km/s)			
				234.375 MHz(729 km/s), 122.070 kHz(0.380 km/s)			
				468.750 MHz(1458 km/s), 244.141 kHz(0.759 km/s)			
Add spectral window centred on a spectral line Add 937.500 MHz (2916 km/s), 488.281 kHz (1.519 km/s)						VS	
	-			1875.000 MHz(5832 km/s), 976.563 kHz(3.037 km/s)			
Baseba	nd-2			1875.000 MHz(5832 km/s), 31.250 MHz(97.198 km/s)			



Baseba	Baseband-1								
Fractio	Eraction Centre Freq Centre Freq Spec Representative								
, action	(rest,lsrk)	(sky,bar)	Transition	Bandwidth, Resolution (smoothed)	Avg.	Window			
1(Full)	114.22176 GHz	96.38593 GHz	CO v=0 1-0	1875.000 MHz(5832 km/s), 7.813 MHz(24.299 km/s)	16~	•			



Baseband-1								
Fraction	Centre Freq (rest,Isrk)	Centre Freq (sky,bar)	Transition	Bandwidth, Resolution (smoothed)	Spec Avg.	Representative Window		
1(Full)	114.22176 GHz	96.38593 GHz	CO v=0 1-0	1875.000 MHz(5832 km/s), 7.813 MHz(24.299 km/s)	\sim	•		

Baseband-2							
1(Full)	117.31955 GHz	99.00000 GHz	Continuum 1	1875.000 MHz(5678 km/s), 7.813 MHz(23.658 km/s)	16 🔘		
Baseba	and-3						
1(Full)	102.50648 GHz	86.50000 GHz	Continuum 2	58.594 MHz(203 km/s), 244.141 kHz(0.846 km/s)	\sim O		
Baseband-4							
1(Full)	100.72891 GHz	85.00000 GHz	Continuum 3	1875.000 MHz(6613 km/s), 7.813 MHz(27.554 km/s)	16 🔾		



PDS456 z=0.185 (1"~3 kpc) Detection SNR~5 of the frequency-integrated CO line

We have assumed a CO FWHM of 0.1 GHz (~300 km/s)

Note: The time in brackets is that required to reach the sensitivity. Operational requirements often mean that the actual observed time is longer, especially for mosaics. Please see the User Manual for more details.

Estimated Total time for Science Goal	20.12 min
Representative frequency (sky, first source)	97.271 GHz
Bandwidth used for sensitivity	0.100 GHz
Requested sensitivity	1.600 mJy
Input Parameters	

Cluster 1

Source Name		RA		Dec	Velocity	
		02:05:03.0000		-20:00:00.000	46803.042 km/s	
Possible Configuration Combinations						
12-m (1)	12-m (2)	7-m	ТР	Nominal Beam(")	Max expected axial ratio	
C-2	None	No	No	2.19 x 2.552	1.5	

Input Parameters

Precipitable water vapour (all sources) 5.186mm (7th Octile)

Time required for 12m (1) [C-2]	
Time on source per pointing (first source)	5.04 min [11.78 s]
Total number of pointings (all sources)	1
Number of tunings	1
Total time on source	5.04 min [11.78 s]
Total calibration time	13.17 min
Other overheads	1.92 min
Total time for 1 SB execution	20.12 min
Number of SB executions	1
Total time to complete SB	20.12 min

Calibration Breakdown per SB execution

2 x Pointing	4.00 min
I x Amplitude/bandpass	5.00 min

PDS456 z=0.185 (1"~3 kpc) Detection SNR~20 of the frequency-integrated CO line

We have assumed a CO FWHM of 0.1 GHz (~300 km/s)

Note: The time in brackets is that required to reach the sensitivity. Operational requirements often mean that the actual observed time is longer, especially for mosaics. Please see the User Manual for more details.

Input Parameters	funners and a second and a second as a
Requested sensitivity	0.4 mJy
Bandwidth used for sensitivity	0.100 GHz
Representative frequency (sky, first source)	97.271 GHz
Estimated Total time for Science Goal	20.12 min

Cluster 1

Source Name		RA		Dec	Velocity	
		02:05:03.0000	2:05:03.0000 -20:00:00.000		46803.042 km/s	
		Possible C	onfigurati	on Combinations		
12-m (1)	12-m (2)	7-m	TP	Nominal Beam(")	Max expected axial ratio	
C-2	None	No	No	2.19 x 2.552	1.5	

Input Parameters

Precipitable water vapour (all sources) 5.186mm (7th Octile)

Time required for 12m (1) [C-2]

Time on source per pointing (first source)	5.04 min [11.78 s]
Total number of pointings (all sources)	1
Number of tunings	1
Total time on source	5.04 min [11.78 s]
Total calibration time	13.17 min
Other overheads	1.92 min
Total time for 1 SB execution	20.12 min
Number of SB executions	phineses and the second s
Total time to complete SB	20.12 min

Calibration Breakdown per SB execution

2 x Pointing	4.00 mir
x Amplitude/bandpass	5.00 mir

PDS456 z=0.185 (1"~3 kpc) CO mapping at ~600 pc resolution

Desired Performance								
Desired Angular Resolution (Synthesized Beam) Single Range Any Standalone ACA 								
	0.20000	arcsec	~					
Largest Angular Structure in source	1.0	arcsec	\sim					
Desired sensitivity per pointing		0.1	mJy	\checkmark equivalent to	323.06 mK			
Bandwidth used for Sensitivity	User		~	Frequency Width	0.10000	GHz		

SNR/beam~5

Input ParametersRequested sensitivity0.1000 mJyBandwidth used for sensitivity0.100 GHzRepresentative frequency (sky, first source)97.271 GHzEstimated Total time for Science Goal2.25 h

Cluster 1

C-7

?

I	Source	Name	RA		Dec	Velocity		
02:05:03.0000 -				-20:00:00.000 46803.042 km/s				
ľ	Possible Configuration Combinations							
ł				-		Mary average at a d		
	12-m (1)	12-m (2)	7-m	TP	Nominal Beam(")	axial ratio		

0.2 x 0.238

1.5

No

We have assumed a CO size of ~0.65" (~2kpc) and a CO FWHM of 0.1 GHz (~300 km/s)

Input Parameters Precipitable water vapour (all sources)	5.186mm (7th Octile)
Time required for 12m (1) [C-7]	
Time on source per pointing (first source)	50.80 min [50.26 min]
Total number of pointings (all sources)	1
Number of tunings	1
Total time on source	50.80 min [50.26 min]
Total calibration time	1.27 h
Other overheads	7.53 min
Total time for 1 SB execution	1.12 h
Number of SB executions	2
Total time to complete SB	2.25 h

Calibration Breakdown per SB execution

2 x Pointing	4.00 min
x Amplitude/bandpass	5.00 min

No

None

Input Parameters PDS456 z=0.185 (1"~3 kpc) 0.1000 mJy Requested sensitivity CO mapping at ~600 pc resolution 0.100 GHz Bandwidth used for sensitivity Representative frequency (sky, first source) 97.271 GHz Estimated Total time for Science Goal 2.76 h **Desired Performance** Cluster 1 2 Single Range Any Standalone ACA Desired Angular Resolution (Synthesized Beam) **Possible Configuration Combinations** 0.20000 arcsec Max expected Largest Angular Structure in source 3.00000 arcsec \sim TP Nominal Beam(") 12-m (1) 12-m (2) 7-m axial ratio ✓ equivalent to 323.06 mK 0.10000 Desired sensitivity per pointing mJy C-7 C-4 No 1.5 No 0.2 x 0.238 GHz User Frequency Width 0.10000 Bandwidth used for Sensitivity \sim \sim SNR/beam~5 Input Parameters Precipitable water vapour (all sources) 5.186mm (7th Octile) We have assumed a CO size of ~0.65" (~2kpc) Time required for 12m (1) [C-7] and a CO FWHM of 0.1 GHz (~300 km/s) Time on source per pointing (first source) 50.80 min [50.26 min] Total number of pointings (all sources) 1 Number of tunings 1 Total time on source 50.80 min [50.26 min] Plus an extended CO component 1.27 h Total calibration time Other overheads 7.53 min Total time for 1 SB execution 1.12 h 2 Number of SB executions Total time to complete SB 2.25 h Calibration Breakdown per SB execution 4.00 min 2 x Pointing 1 x Amplitude/bandpass 5.00 min 29 x Phase 8.70 min 3 x CheckSource 3.00 min 4 x Atmospheric 2.67 min Calibration overheads 14.83 min Additional Arrays 30.99 min Time required for additional 12-m

Estimated total time for cluster 1 2.76 h

Input Parameters PDS456 z=0.185 (1"~3 kpc) Requested sensitivity 0.1000 mJy CO mapping at ~600 pc resolution Bandwidth used for sensitivity 0.100 GHz Representative frequency (sky, first source) 97.271 GHz Estimated Total time for Science Goal 2.76 h **Desired Performance** Cluster 1 2 Single Range Any Standalone ACA Desired Angular Resolution (Synthesized Beam) **Possible Configuration Combinations** 0.20000 arcsec Max expected Largest Angular Structure in source 3.00000 arcsec \sim TP Nominal Beam(") 12-m (1) 12-m (2) 7-m axial ratio 0.10000 equivalent to 323.06 mK Desired sensitivity per pointing mJy C-7 C-4 No 1.5 No 0.2 x 0.238 Frequency Width 0.10000 GHz Bandwidth used for Sensitivity User \sim \sim SNR/beam~5 Input Parameters Precipitable water vapour (all sources) 5.186mm (7th Octile) PDS456-coremap-300kms Time required for 12m (1) [C-7] -30 km/s Time on source per pointing (first source) 50.80 min [50.26 min] Total number of pointings (all sources) 1 54'' Number of tunings 1 Total time on source 50.80 min [50.26 min] 1.27 h Total calibration time 55' 3 kpc Other overheads 7.53 min Declination Total time for 1 SB execution 1.12 h 2 Number of SB executions Total time to complete SB 2.25 h 56'' ICRS **Calibration Breakdown per SB execution** 4.00 min 2 x Pointing 57' 1 x Amplitude/bandpass 5.00 min 29 x Phase 8.70 min 3 x CheckSource 3.00 min 4 x Atmospheric 2.67 min -14°15'58" Calibration overheads 14.83 min Additional Arrays 19^{\$}.75 17^h28^m19^s.95 19^s.85 19^s.65 Time required for additional 12-m 30.99 min ICRS Right Ascension

Estimated total time for cluster 1 2.76 h

PDS456 z=0.185 (1"~3 kpc) CO mapping at ~600 pc resolution Information about CO kinematics

Desired Performance					?						
Desired Angular Resolution (Synthesized Beam)	Single Range O.20000 arcs	Any O Standal	one ACA		in Ri	equested sensi	rs tivity				0.1000 mJy
Largest Angular Structure in source	1.0 arcs	ec 🗸			B	epresentative fr	requency (sky, fi	rst source)			97.271 GHz
Desired sensitivity per pointing	0.10000	mJy	✓ equivalent to	323.06 mK	E	stimated To	otal time for s	Science G	oal		20.14 h
Bandwidth used for Sensitivity	User	~	Frequency Width	30	km/s V Venaster 1						
					Sourc	e Name	RA		Dec		Velocity
					pds		02:05:03.0000		-20:00:00.000	46803	3.042 km/s
							Possible (Configuratio	n Combinations		
					12-m (1)	12-m (2)	7-m	TP	Nominal Beam	(")	Max expected axial ratio
					C-7	None	No	No	0.2 x 0.238	1.	.5

Precipitable water vapour (all sources

Input Parameters

Time required for 12m (1) [C-7] Time on source per pointing (first source) 8.65 h [8.61 h] Total number of pointings (all sources) 1 Number of tunings 1 Total time on source 8.65 h [8.61 h] Total calibration time 10.47 h Other overheads 1.02 h Total time for 1 SB execution 1.83 h Number of SB executions 11 Total time to complete SB 20.14 h

5.186mm (7th Octile)

PDS456 z=0.185 (1"~3 kpc) CO mapping at ~600 pc resolution Information about CO kinematics





	Requested sensitivity Bandwidth used for sensitivity Representative frequency (sky, first source)									0.1000 mJy 100.000 km/s 97.271 GHz	
(m/	m/s Estimated Total time for Scie				Scienc	e Goa	al			6.25 h	
	Cluster 1										
	Sou	urce N	lame	RA			Dec			Velocity	
pds 02:05:03.0000						-20	0:00:00.000		468	03.042 km/s	
				Possible (Configur	ation	Combinations				
	12-m (1)	12-m (2)	7-m	т	P	Nominal	Beam(")		Max expected axial ratio	
(C-7	I	None	No	No		0.2 x 0.238			1.5	
	Input Parameters										
	Precipitable water vapour (all sources)					186mn	n (7th Octile)				
	Time	requ	ired for 12n	n (1) [C-7]							
	Time	on so	ource per poi	nting (first sou	rce) 2.6	60 h [2	2.58 h]	16			
	Total number of pointings (all sources)				\ 1	1					

Input Parameters

Time required for 12m (1) [C-7]		
Time on source per pointing (first source)	2.60 h [2.58 h]	16
Total number of pointings (all sources)	1	
Number of tunings	1	
Total time on source	2.60 h [2.58 h]	
Total calibration time	3.32 h	
Other overheads	19.57 min	
Total time for 1 SB execution	1.56 h	
Number of SB executions	4	
Total time to complete SB	6.25 h	

PDS456 z=0.185 (1"~3 kpc) Continuum detection

Sensitivity		?					
Requested RMS over 100.000 km/s is 100.00 uJy	For a peak flux density of 550.00 uJy , the S/N is 5.5						
Achieved RMS over the total 5.537 GHz bandwidth is 7.63 uJy	For a continuum flux density of 100.00 uJy , the achieved S/N is	13.1					
For a peak line flux of 550.00 uJy , the achieved S/N over 1/3 of the source line width (300.00 km/s / 3 = 100.00 km/s) is 5.5							
Line width / bandwidth used for sensitivity (300.00 km/s / 100.00 km/s)	= 3.00						



PDS456 z=0.185 (1"~3 kpc) Continuum detection



